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Performance Evaluation: Ball-Tree and KD-Tree in the context of MST

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Abstract. Now a day's many algorithms are invented / being inventing to find the solution for Euclidean Minimum Spanning Tree (*EMST*) problem, as its applicability is increasing in much wide range of fields containing spatial / spatio – temporal data viz. astronomy which consists of millions of spatial data. To solve this problem, we are presenting a technique by adopting the dual tree algorithm for finding efficient EMST and experimented on a variety of real time and synthetic datasets. This paper presents the observed experimental observations and the efficiency of the dual tree framework, in the context of kd-tree and ball-tree on spatial datasets of different dimensions.

Keywords: Euclidean Minimum Spanning Tree (EMST), dual Tree, kd-tree, ball-tree

1 Introduction

Minimum Spanning Tree (hereinafter, MST) is the one of the oldest and most thoroughly studied problem in computational geometry [1]. The Minimum-weight Spanning Tree or simply MST problem is one of the well-known optimization problems for finding minimum weighted spanning tree for both undirected and directed graphs. MST have many applications in computer design, communication, transportation and some other problems that can apply directly/indirectly are wireless network connectivity, clustering and classification of different data namely spatial data. In literature, several authors proposed a variety of greedy algorithms [2, 3, 4]. The general drawback with these greedy algorithms is that these cannot handle large amount of data and performance bottleneck will happened and later some more advanced algorithms are developed to solve this problem [5]. In this paper, authors evaluated the performance of dual tree algorithmic framework [6] using single linkage clustering [7] and compared the performance of the dual tree framework in the context of kd-tree and ball-tree. As per the Ref. [8] theoretically single-linkage clustering provides optimal clusters.

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2 Related Work

Many of the MST Algorithms are utilized Tarjan's Blue rule [10] to find the minimum weight edge. Using this rule many of the greedy algorithms are developed viz. Prims with O(m+nlogn) and Krushkal with O(mlogn) time complexity's respectively. In Dual-Tree Boruvka's Algorithm, the efficiency of the Boruvka's algorithm mainly depends on the adopted nearest neighbor technique. If we find nearest neighbors efficiently by using some intelligent data structure like spatial trees, kd-tree, ball tree or any spatial tree, the performance of the Boruvka's algorithm can be enhanced. For example, for the query set Q and reference set R, then for each point $q \square Q$ and $r \square R$ such that d(q, r) must be minimized and call it as nearest neighbor pair. Native approach will take $O(n^2)$ run time for finding nearest neighbor pair for n number of components[11]. Hence, in this paper, authors adopted the algorithms proposed by [7] to evaluate the performance of Dual Tree Boruvka and compared with kd-tree and ball-tree.

KD-tree [12] is one of the space partitioning tree for organizing k-dimensional data points. For building this kd-tree of n points it takes $O(n \log n)$ if we use the linear median finding algorithm described by [13] and for adding new point to the balanced tree it takes $O(\log n)$ and for removing a point from tree takes $O(\log n)$, because of removing a point from tree the balance of the tree will change then we need to rebalance the tree so for both adding and removing point from tree will take same time complexity of $O(\log n)$.

Ball Tree [14] is also binary tree data structure for maintaining spatial data hierarchically like kd-tree and oct-tree [15]. Each node in the ball-tree referred as ball contains a region of Euclidean points bounded by a hyper-sphere and interior balls are small containing their children balls. One can specify the ball n+1 float values as coordinates and r radius as its center. Like kd-tree the ball tree also uses top down approach for building the tree recursively from top to down by choosing the split dimension and splitting value to find these values, balls are sorted along each dimension and store the cost in an array. Best dimension and split location can be found in O(nlog(n)), so, time complexity to construct the ball-tree is $O(n(log n)^2)$.

3 Implementation

In this paper, authors adopted Dual-tree Boruvka in the context of kd-tree and ball-tree for finding the EMST. Experiments are performed on synthetic datasets and real time datasets [9]. Both algorithms are implemented and incorporated in weka3.6.4 [16] and compiled with the jdk1.6. Following Table and Fig. 1 shows the observations.

Table-1 Performance of kd-tree and ball-tree for 50 dimensions

<u>Operati</u>	Build		Insertion		Deletion		N-NN Search	
on Instanc es	kd-tree	ball-tree	kd-tree	ball-tree	kd-tree	ball-tree	kd-tree	ball-tree
10000	187	1203	188	1187	218	1172	31	47
25000	547	3469	531	3468	516	3454	96	110
50000	1344	7906	1172	8094	1156	8093	118	219
100000	2578	16547	2750	16437	2812	16485	391	422
200000	5937	36672	5688	36703	5640	36375	875	907

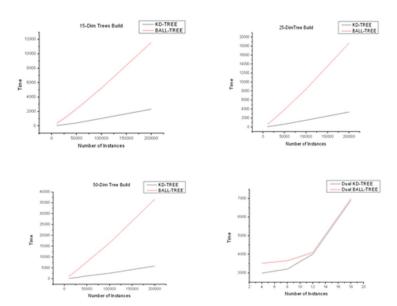


Fig-1: (a) time taken for building kd-tree and ball-tree for 15-dimensions (b) time taken for building kd-tree and ball-tree for For 25-dimensions (c) time taken for building kd-tree and ball-tree for 50-dimensions of data; (d) Comparison of dual tree algorithm using both kd-tree and ball-tree

From the above results, one can easily observe that the computational time for constructing ball-tree takes more time than the kd-tree, and as the dimensionality increases the performance of kd-tree is also increases when compared with ball-tree. Figure-1(d) shows the performance of DualTree Boruvka using kd-tree as well as ball-tree for varying dimensions on real-time datasets obtained from SDSS. Both algorithmic performance is nearly equal but overall performance differs with creation of tree structure, i.e., kd-tree takes $O(n \log n)$ and ball-tree takes $O(N(\log N)^2)$ for n points in Euclidean space. Finally, from the experimental results, authors conclude that DualTree Boruvka on kd-tree performs faster than the DualTree Boruvka on ball-tree for finding Euclidean MST.

4 Conclusion

In this paper, authors compared kd-tree and ball-tree based dual tree Boruvka algorithm for finding Euclidean Minimum Spanning Tree (*EMST*). For finding efficient EMST, authors adopted dual tree algorithm and experimented on a variety of real time and synthetic datasets of various dimensions. From the experimental observation, authors conclude that the *kd-tree performs faster than the ball-tree for not only constructing the tree and also for solving the EMST problem. Moreover, the kd-tree based dual tree Boruvka is giving good results than the ball-tree based dual-tree Boruvka.*

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