# TRINITY COLLEGE DUBLIN THE UNIVERSITY OF DUBLIN

# Faculty of Engineering, Mathematics and Science

# **School of Computer Science & Statistics**

Integrated Computer Science Programme B.A. (Mod.) MSISS B.A. (Mod.) Computer Science & Business Junior Sophister Annual Examination

Trinity Term 2015

# **Introduction to Functional Programming**

Thursday 14th May 2015

**Goldsmith Hall** 

09:30-11:30

#### Mr Andrew Anderson

## Instructions to Candidates:

Attempt **three** questions. All questions carry equal marks. Each question is scored out of a total of 33 marks.

There is a reference section at the end of the paper (pp6-8).

You may not start this examination until you are instructed to do so by the Invigilator.

Materials permitted for this examination:

None

 The Haskell module Prelude is imported by default in every Haskell program. The Prelude defines a large number of useful list functions.

Give a complete implementation of the Prelude functions described below, **including** the implementations of any functions used as helpers, unless stated otherwise.

(a) repeat generates an infinite list of copies of x. For example, repeat 5 generates the list [5,5,5,5,5...].

repeat

:: a -> [a]

[4 marks]

(b) replicate generates a finite list of exactly n copies of x. For example, replicate 3 'A' generates the list ['A', 'A', 'A'].

replicate

:: Int -> a -> [a]

[5 marks]

(c) concat joins a list of lists together into a single list. For example, concat [[1, 2], [3]] creates the list [1, 2, 3].

concat

:: [[a]] -> [a]

[5 marks]

(d) zip creates a new list by joining elements at the same index in two input lists into pairs. zip [1,2] ['a', 'b'] creates the list [(1, 'a'), (2, 'b')].

zip

[6 marks]

(e) unzip converts a list of pairs into a pair of lists by sending the first element of each input pair to one list, and the second element to another. For example, unzip [(1,4), (2,5), (3,6)] creates the pair ([1,2,3], [4,5,6]). Unzipping the empty list should result in a pair of empty lists.

unzip

[6 marks]

(f) minimum finds the least value in a non-empty list. The class constraint (Ord a) ensures that the operations of the typeclass Ord work on items in the list. The operations of the typeclass Ord are listed in the reference — you need not implement them.

minimum

[7 marks]

2. Consider the following function definitions:

```
f1 [] _ = []
f1 _ [] = []
f1 (x:xs) (y:ys) = (x * y) : f1 xs ys

f2 [] _ = []
f2 _ [] = []
f2 (x:xs) (y:ys) = (x + y) : f2 xs ys

f3 [] _ = []
f3 _ [] = []
f3 (x:xs) (y:ys) = (x y) : f3 xs ys

f4 [] _ = []
f4 _ [] = []
f4 (x:xs) (y:ys) = (y, x) : f4 xs ys

f5 [] _ = []
f5 _ [] = []
f5 (x:xs) (y:ys) = x : f5 xs ys
```

They all have a common pattern of behaviour.

(a) Write a higher-order function hof that captures this common behaviour without using any function from the reference.

[6 marks]

(b) Write the type signature that Haskell will infer for hof.

[2 marks]

(c) Rewrite each of £1, £2, ... above to be a call to hof with appropriate arguments. You may use any Prelude function from the reference as a helper.

[20 marks]

(d) Is hof provided by the Haskell Prelude (under another name)?

If so, what is it called?

[5 marks]

3. A hash table is a very common data structure which maps keys to values (a dictionary). To speed up the search for the value associated with some key, a hash table organises (key, value) pairs into buckets. In each bucket, all the keys have the same value under some hash function. To look up the value associated with some key, we first compute the hash of the key, then we search only the bucket associated with that hash, and not the full table. An example hash function hash is given below.

```
type Bucket k v = [(k, v)]
type HashTable k v = [(Int, Bucket k v)]
hash :: String -> Int
hash str = (sum (map ord str)) 'mod' 255
```

Given a key, to extract the corresponding value from a hash table, we must first decide what *bucket* it would be in. To do this, we run the **hash function** on the key, which generates the number of the bucket. Once we've found this bucket, we then need to look up the value which corresponds to our key in the bucket.

```
lookup :: String -> (HashTable String String) -> String
lookup str table =
  let hashValue = hash str
        (_, bucket) = head (filter ((== hashValue) . fst) table)
        (_, value) = head (filter ((== str) . fst) bucket)
  in value
```

- (a) Explain the ways in which function lookup can fail, with Haskell runtime errors.

  Don't worry about precise error messages, but do state what causes the errors.

  [5 marks]
- (b) Add in error handling for function lookup above, using the Maybe type, to ensure this function is now total. Note that this will require changing the type of this function. You may assume the existence of a list function find :: (a -> Bool) -> [a] -> Maybe a. [14 marks]
- (c) Add in error handling for the lookup function above, using the Either type, ensuring it is now total, and giving back a useful error message. Note that this will also require changing the type of the function. You may assume the existence of a list function find :: (a -> Bool) -> [a] -> Maybe a. The convention when using Either is to represent failure with the (Left errMsg) constructor, and success with the (Right someValue) constructor. [14 marks]

4. (a) Consider the following function definition:

```
diffsq [] = 0
diffsq (x:xs) = x * x - diffsq xs
```

Use the shorthand AST notation to show how the application diffsq [2,3] is evaluated, indicating clearly where copying takes place. You need not draw the full AST (with cons-nodes) for the lists but just show any list instead as a single node, [], [6], etc, as appropriate. [10 marks]

(b) Consider the following function definitions:

```
zig n = n : zag (n-1)
zag n = n : zig (n-1)
take 0 xs = []
take n (x:xs) = x : take (n-1) xs
```

Show the evaluation of take 2 (zig 20) using both *Strict* Evaluation and *Lazy* Evaluation. Show enough evaluation steps to either indicate the final result, or to illustrate why no such result will emerge. [8 marks]

- (c) Using explicit numbers, lists and either or both functions take, zig, and zag above, and no others, write expressions, if possible, that:
  - i. terminate when evaluated both strictly and lazily
  - ii. terminate when evaluated strictly but not when evaluated lazily
  - iii. terminate when evaluated lazily but not when evaluated strictly
  - iv. fail to terminate when evaluated either strictly or lazily

[4 marks]

(d) Write a program that prompts the user for a filename of the form \( \frac{root} \). in (where \( \frac{root} \) is the filename less its extension) opens that file, reads its contents, uses the function hash :: String -> Int from Question 3 to compute the hash of the entire file contents and outputs the result to file \( \frac{root} \). chk (See the Reference, p8 for file input/output functions). [11 marks]

#### Reference

#### **Prelude List Functions**

```
:: (a -> b) -> [a] -> [b]
map
(++)
                  :: [a] -> [a] -> [a]
filter
                  :: (a -> Bool) -> [a] -> [a]
                  :: [[a]] -> [a]
concat
head
                  :: [a] -> a
                  :: [a] -> [a]
tail
last
                  :: [a] -> a
init
                  :: [a] -> [a]
null
                  :: [a] -> Bool
                  :: [a] -> Int
length
(!!)
                  :: [a] -> Int -> a
                  :: (a \rightarrow b \rightarrow a) \rightarrow a \rightarrow [b] \rightarrow a
foldl
foldl1
                  :: (a -> a -> a) -> [a] -> a
scanl
                  :: (a -> b -> a) -> a -> [b] -> [a]
scanl1
                  :: (a -> a -> a) -> [a] -> [a]
foldr
                  :: (a -> b -> b) -> b -> [a] -> b
foldr1
                  :: (a -> a -> a) -> [a] -> a
scanr
                  :: (a -> b -> b) -> b -> [a] -> [b]
scanr1
                  :: (a -> a -> a) -> [a] -> [a]
iterate
                  :: (a -> a) -> a -> [a]
                  :: a -> [a]
repeat
replicate
                  :: Int -> a -> [a]
cycle
                  :: [a] -> [a]
take
                  :: Int -> [a] -> [a]
                  :: Int -> [a] -> [a]
drop
                  :: Int -> [a] -> ([a],[a])
splitAt
takeWhile
                  :: (a -> Bool) -> [a] -> [a]
dropWhile
                  :: (a -> Bool) -> [a] -> [a]
span, break
                  :: (a \rightarrow Bool) \rightarrow [a] \rightarrow ([a],[a])
                  :: [a] -> [b] -> [(a,b)]
zip
                  :: [(a,b)] -> ([a], [b])
unzip
                  :: (a -> b -> c) -> [a] -> [b] -> [c]
zipWith
minimum
                  :: (Ord a) => [a] -> a
```

#### **Other Prelude Functions**

## **Prelude Typeclasses**

class Eq a => Ord a where

compare :: a -> a -> Ordering

(<) :: a -> a -> Bool (>=) :: a -> a -> Bool

(>) :: a -> a -> Bool

(<=) :: a -> a -> Bool

max :: a -> a -> a

min :: a -> a -> a

#### **Prelude IO Functions**

type FilePath = String

putChar :: Char -> IO ()
putStr :: String -> IO ()
putStrLn :: String -> IO ()

print :: Show a => a -> IO ()

getChar :: IO Char getLine :: IO String getContents :: IO String

readFile :: FilePath -> IO String

writeFile :: FilePath -> String -> IO ()

#### **Data.Char Functions**

isControl :: Char -> Bool :: Char -> Bool isSpace isLower :: Char -> Bool isUpper :: Char -> Bool isAlpha :: Char -> Bool isAlphaNum :: Char -> Bool isPrint :: Char -> Bool isDigit :: Char -> Bool toUpper :: Char -> Char toLower :: Char -> Char :: Char -> Char toTitle digitToInt :: Char -> Int intToDigit :: Int -> Char ord :: Char -> Int :: Int -> Char chr