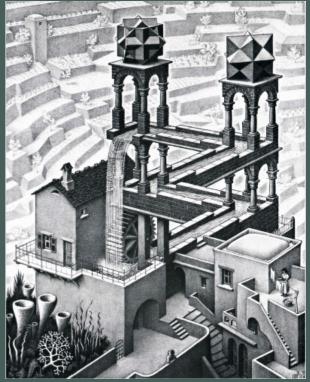
2.1 - Forest water and energy balance (theory)

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Ecosystem Modelling Facility

2022-06-14







Outline

- 1. Preliminary concepts
- 2. Forest water balance in medfate
- 3. Transpiration and photosynthesis under the basic model
- 4. Transpiration and photosynthesis under the advanced model
 - 5. Plant drought stress and cavitation
 - 6. Basic vs. advanced models: a summary of differences



Water potential

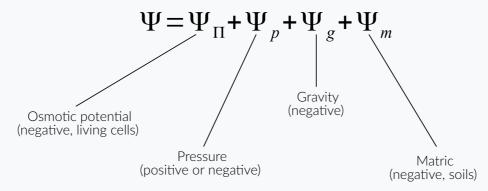
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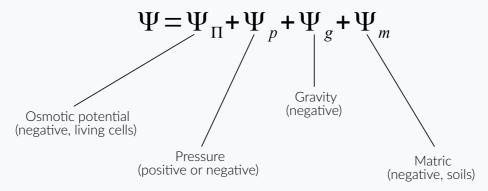




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But not all components are equally relevant in all contexts



Soil water retention curves

The water retention curve of a soil (or soil moisture characteristic curve) is the relationship between volumetric soil moisture content (θ in $m^3 \cdot m^{-3}$ of soil excluding rock fragments) and the corresponding soil water potential (Ψ , in MPa)



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Two water retention curve models are available in **medfate**:

1. Saxton model:

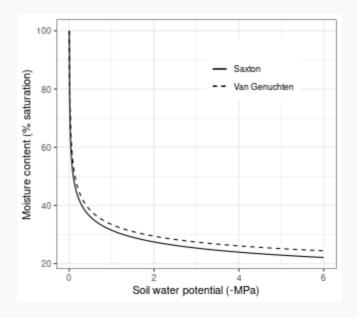
$$heta(\Psi) = (\Psi/A)^{(1/B)}$$

where A and B depend on the texture and, if available, organic matter in the soil.

2. Van Genuchten model:

$$heta(\Psi) = heta_{res} + rac{ heta_{sat} - heta_{res}}{\left[1 + (lpha \cdot \Psi)^n
ight]^{1 - 1/n}}$$

where $\theta(\psi)$ is the water retention, θ_{sat} is the saturated water content, θ_{res} is the residual water content, α is related to the inverse of the air entry pressure, and n is a measure of the pore-size distribution.





Water potential drop in plants

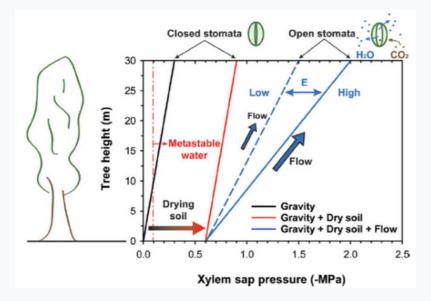
When stomata are closed (e.g. pre-down), plant leaf water potential is assumed to be in equilibrium with the water potential in the rhizosphere (neglecting gravity effects).



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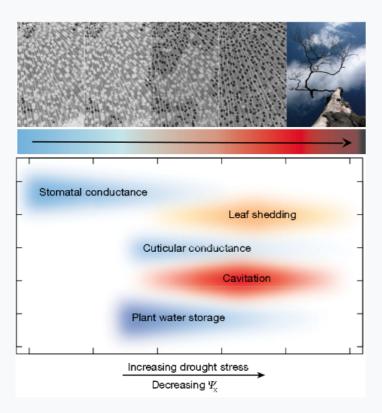
When stomata are open, a larger transpiration flow (*E*) implies (in steady state) a larger drop in water potential along the transpiration pathway:





Drought impacts on plants

The decrease in soil water potential caused by drought has multiple effects on plants, with some processes ceasing to occur and others becoming important or being promoted, depending on the plant response strategy.

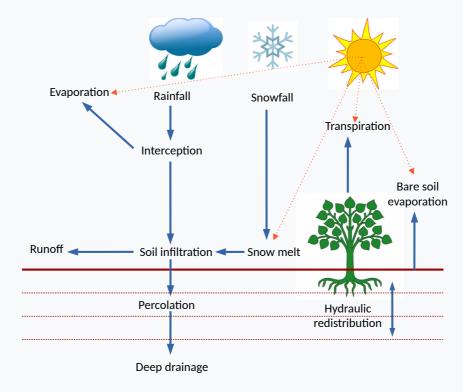


Process or variables affected	Reduction in tissue water potential ψ and turgor P 0 ——————————————————————————————————
Cell growth	
Growth respiration	
ABA release	
Stomatal conductance /transpiration	
Leaf energy budget	
Photosynthesis	
Xylem cavitation	
Root disconnection from soil	
Maintenance respiration	
NSC transport	
Leaf turgor loss	
Leaf shedding	
Plant mortality	



Water balance components

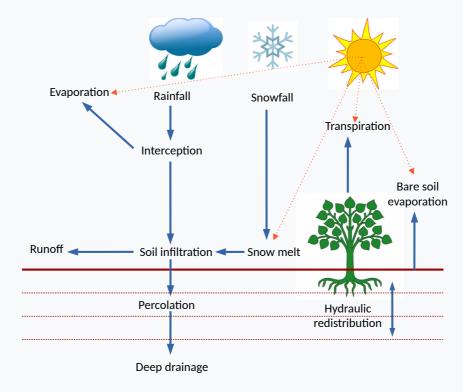
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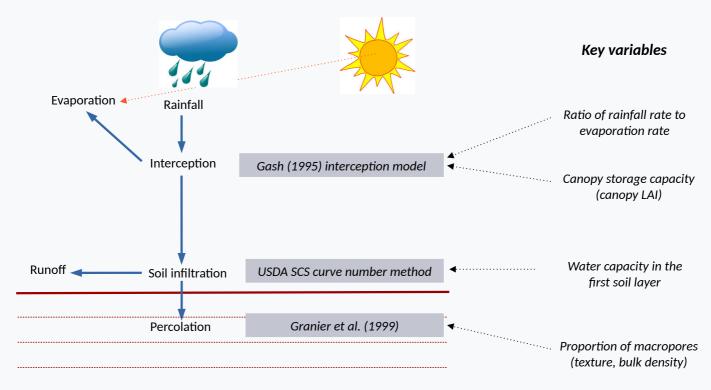
Variations in soil water content can be summarized as:

$$\Delta V_{soil} = Pr + Sm - In - Ru - Dd - Es - Ex$$



Soil water inputs

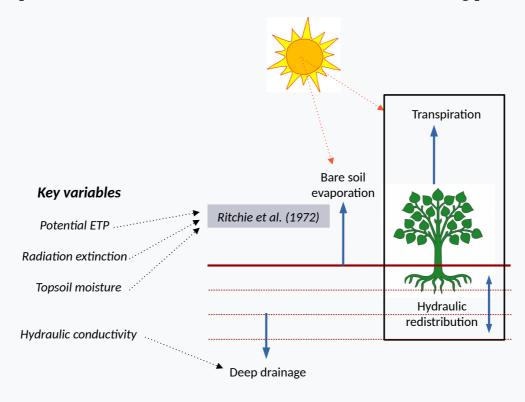
If rainfall occurs during a given day, three processes are simulated to update the water content in soil layers:





Soil water outputs

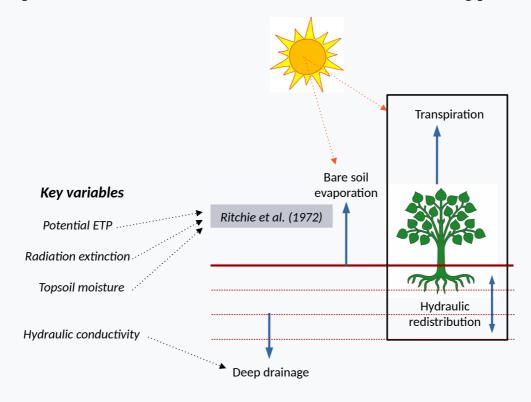
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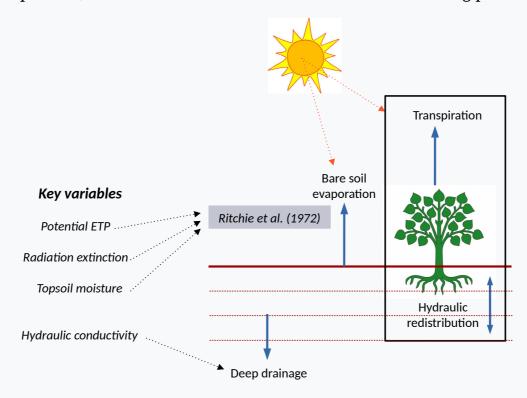


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Soil water outputs

Regardless of precipitation, soil moisture can be modified due to the following processes:



Soil water uptake by plants and transpiration are modelled differently depending on the water balance model: **basic** vs **advanced**.

Hydraulic redistribution is only simulated in the advanced water balance model.



Maximum transpiration

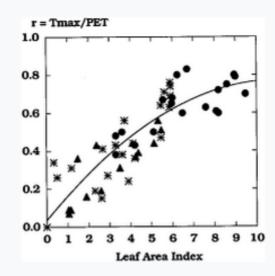
Maximum canopy transpiration

Maximum canopy transpiration Tr_{\max} depends on potential evapotranspiration, PET, and the amount of transpirating surface, i.e. the stand leaf area index, thanks to:

$$rac{Tr_{ ext{max}}}{PET} = -0.006 \cdot (LAI_{stand}^{\phi})^2 + 0.134 \cdot LAI_{stand}^{\phi}$$

and therefore:

$$Tr_{ ext{max}} = PET \cdot \left(-0.006 \cdot (LAI_{stand}^{\phi})^2 + 0.134 \cdot LAI_{stand}^{\phi}
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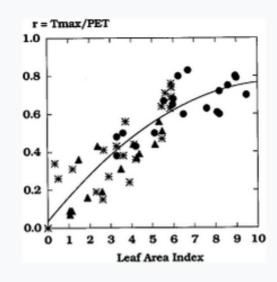
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Maximum plant transpiration

Maximum canopy transpiration is divided among plant cohorts according to the amount of light absorbed by each one:

$$Tr_{ ext{max},i} = Tr_{ ext{max}} \cdot rac{f_i^{0.75}}{\sum_j f_j^{0.75}}$$



where f_i is the fraction of total absorbed short-wave radiation that is due to cohort i.



Actual plant transpiration

Actual plant transpiration depends on soil moisture and is calculated for each soil layer s separately.



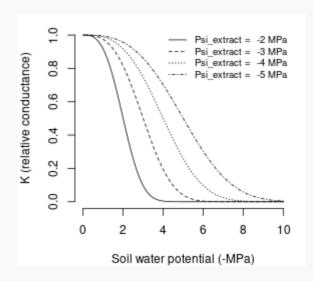
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A relative whole-plant water conductance, K is defined for any given soil layer s using:

$$K(\Psi_s) = \exp iggl\{ \ln{(0.5)} \cdot \left[rac{\Psi_s}{\Psi_{extract}}
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where $\Psi_{extract}$ is the water potential at which transpiration is 50% of maximum, and Ψ_s , the water potential in layer s.





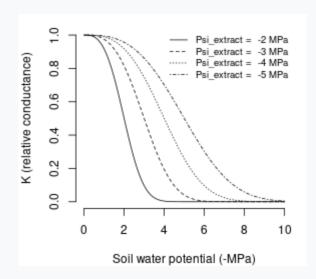
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The water extracted by a plant cohort from soil layer s and transpired, Tr_s , is the product:

$$Tr_s = Tr_{ ext{max}} \cdot K(\Psi_s) \cdot FRP_s$$

where FRP_s is the proportion of plant fine roots in layer s.



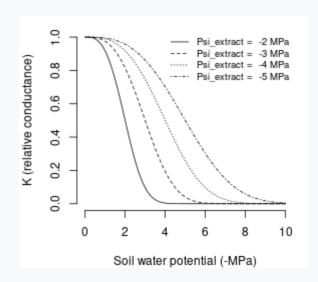
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The transpiration summed across soil layers is:

$$Tr = \sum Tr_s$$



Plant photosynthesis

Gross photosynthesis for a plant cohort, A_g , is estimated as a function of transpiration, Tr, using:

$$A_q = Tr \cdot WUE_{ ext{max}} \cdot (L^{PAR})^{WUE_{decay}}$$

where WUE_{\max} is the maximum water use efficiency of the cohort under maximum light availability, L^{PAR} is the proportion of PAR available and WUE_{decay} is an exponent.

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Despite its simplicity, a gross surrogate of 'plant' water potential, Ψ_{plant} , may be obtained using:

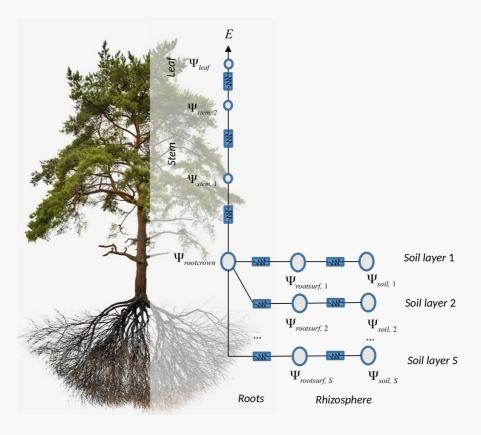
$$\Psi_{plant} = K^{-1} \left(\sum_s K(\Psi_s) \cdot FRP_s
ight)$$

which can be intuitively understood as an *average of soil water potential* taking into account fine root distribution.



Hydraulic network

The analogy of a set of resistances in an electric circuit is often used to represent the resistance to water flow in an hydraulic network:





Vulnerability curves

The concept of vulnerability curve can be used to specify the relationship between water potential, Ψ , and hydraulic conductance, k, in any portion along the flow path.



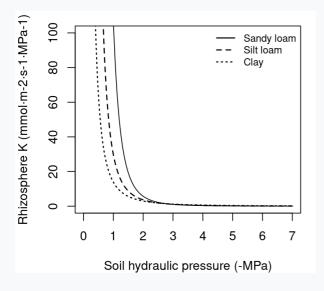
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Rhizosphere

Conductance is modelled as a van Genuchten (1980) function:

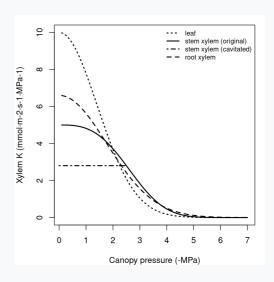
$$k(\Psi) = k_{max} \cdot v^{(n-1)/(2 \cdot n)} \cdot ((1-v)^{(n-1)/n} - 1)^2$$



Xylem

Conductance is modelled using a two-parameter Weibull function:

$$k(\Psi) = k_{max} \cdot e^{-((\Psi/d)^c)}$$





Hydraulic supply function

The supply function describes the **steady-state** rate of water flow, E, as a function of water potential drop.



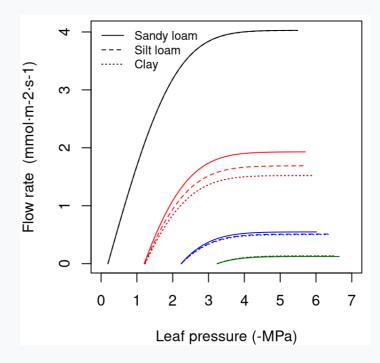
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The steady-state flow rate E_i through any element i is related to the flow-induced drop in water potential across that element, $\Delta \Psi_i = \Psi_{down} - \Psi_{up}$, by the integral of the vulnerability curve $k_i(\Psi)$:

$$E_i = \int_{\Psi_{up}}^{\Psi_{down}} k_i(\Psi) d\Psi$$

where Ψ_{up} and Ψ_{down} are the upstream and downstream water potential values.





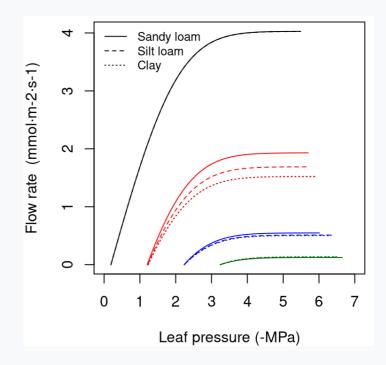
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The supply function can be integrated across the **whole hydraulic network**.

$$E(\Psi_{leaf}) = \int_{\Psi_{soil}}^{\Psi_{leaf}} k(\Psi) d\Psi$$



Leaf energy balance, gas exchange and photosynthesis

If we know air temperature, wind conditions, radiative balance and water vapor pressure in which leaves are, we can translate the supply function into several functions:

- Leaf temperature: $T_{leaf}(\Psi_{leaf})$
- Leaf vapor pressure deficit: $VPD_{leaf}(\Psi_{leaf})$
- Leaf diffusive conductance: $g_w(\Psi_{leaf})$

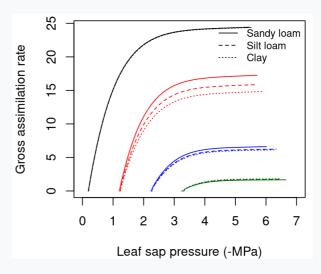


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If we know the absorbed PAR and $[CO_2]$ in the air, gross and net photosynthesis can be estimated using Farquhar's (1980) model as a function of Ψ_{leaf} , i.e. $A_g(\Psi_{leaf})$ and $A_n(\Psi_{leaf})$.



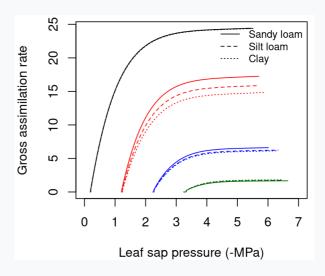


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Important parameters of Farquhar's model are the maximum rate of Rubisco carboxylation, V_{max} , and the maximum rate of electron transfer, J_{max} .



Stomatal regulation

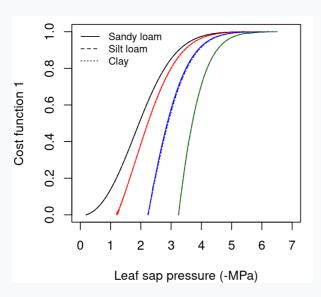
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The hydraulic supply function is used to derive a **cost function** $\theta(\Psi_{leaf})$ reflecting the increasing damage from cavitation.

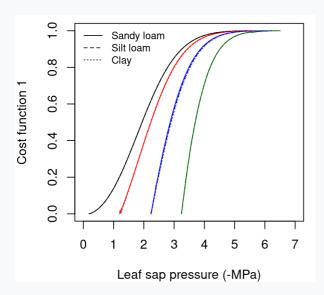




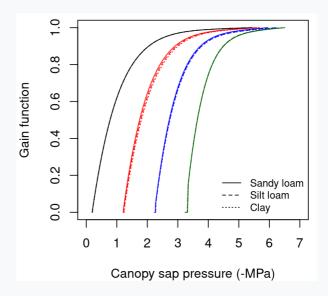
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The normalized photosynthetic gain function $\beta(\Psi_{leaf})$ reflects the increase in assimilation rate, with respect to the maximum.

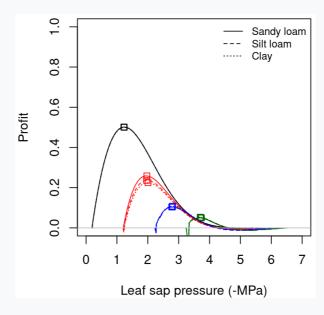




Stomatal regulation

Sperry et al (2017) suggested that stomatal regulation can be effectively estimated by determining the maximum of the *profit function*:

$$Profit(\Psi_{leaf}) = eta(\Psi_{leaf}) - heta(\Psi_{leaf})$$

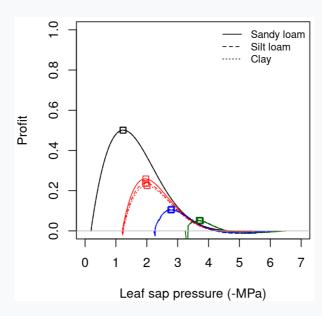




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The maximization is achieved when the slopes of the gain and cost functions are equal:

$$rac{\deltaeta(\Psi_{leaf})}{\delta\Psi_{leaf}} = rac{\delta heta(\Psi_{leaf})}{\delta\Psi_{leaf}}$$



From leaf to the canopy

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1. Building the supply function for each plant cohort



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Corollaries

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Hydraulic redistribution is an emergent output of the model when soil layers have *different degree of moisture* and *stomata are closed* (at night).



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Daily drought stress, DDS, is defined using ϕ , the phenological status, and the *one-complement* of relative whole-plant conductance:

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Advanced model

Since the derivative of the supply function, i.e. $dE/d\Psi_{leaf}$, is the *absolute* whole-plant conductance:

$$DDS = \phi \cdot \left[1 - rac{dE/d\Psi_{leaf}}{k_{max,plant}}
ight]$$

Cavitation

If cavitation has occurred in previous steps then the capacity of the plant to transport water is impaired.

Basic model

Estimation of PLC:

$$PLC_{stem} = 1 - \expiggl\{ \ln{(0.5)} \cdot \left[rac{\Psi_{plant}}{\Psi_{critic}}
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Effect on plant transpiration:

$$K_s^{PLC} = \min\{K_s, 1.0 - PLC_{stem}\}$$



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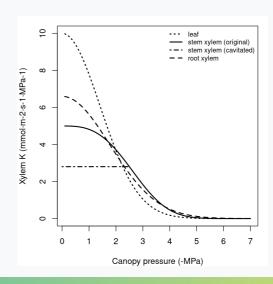
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Advanced model

Estimation of PLC:

$$PLC_{stem} = 1 - rac{k_{stem}(\Psi_{stem})}{k_{max,stem}}$$

Effect on the stem vulnerability curve:





6. Basic vs. advanced models: a summary of differences

Comparison of processes

Group	Process	Basic	Advanced
Forest hydrology	Rainfall interception	*	*
	Infiltration/percolation	*	*
	Bare soil evaporation	*	*
	Snow dynamics	*	*
	Transpiration	*	*
	Hydraulic redistribution		*
Radiation balance	Radiation extinction	*	*
	Diffuse/direct separation		*
	Longwave/shortwave separation		*
Plant physiology	Photosynthesis	[*]	*
	Stomatal regulation		*
	Plant hydraulics		*
	Stem cavitation	*	*
Energy balance	Leaf energy balance		*
	Canopy energy balance		*
	Soil energy balance		*



6. Basic vs. advanced models: a summary of differences

Comparison of state variables

State variable	Basic	Advanced
Soil moisture gradients	*	*
Soil temperature gradients		*
Canopy temperature gradients		*
Canopy moisture gradients		*
Canopy CO_2 gradients		*
Leaf phenology status	*	*
Plant water status	*	*
Water potential gradients		*
Stem cavitation level	*	*
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M.C. Escher - Waterfall, 1961

