# Forest growth and dynamics (theory)

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### Outline

- 1. Simulation models and processes
- 2. Carbon pools and carbon balance
- 3. Growth and senescence
- 4. Mortality and recruitment
- 5. Biomass balance
- 6. Fire effects

M.C. Escher - Three worlds, 1955







1. Simulation models and processes



## About growth() and fordyn() models

- 1. Simulation functions in **medfate** have been designed and implemented in a **nested** manner.
- 2. The two water balance models (basic and advanced) are available for simulations with growth() and fordyn().
- 3. The growth() model implements several daily processes:
  - i. Carbon balance processes resulting from the interplay of sources (photosynthesis) and sinks (maintenance respiration, growth respiration, root exudation, etc.).
  - ii. Growth and senescence processes that modulate changes in *leaf area*, *sapwood area* and *fine root area* of woody plant cohorts.
  - iii. Structural changes (diameter and height for trees; cover and height for shrubs) derived from growth and senescence processes.
  - iv. Tree mortality, which reduces cohort density.
- 4. For applications spanning more than a few years, users will use the growth() model indirectly, via calls to fordyn(), which includes other processes implemented at **annual** steps:
  - i. Natural regeneration (recruitment)
  - ii. The effect of disturbances (at present, only forest management and fire effects).

#### fordyn()

Recruitment
Management prescription & effects

#### growth()

Carbon balance Tissue growth & senescence Mortality

#### spwb()

Soil/plant water balance Radiation balance Soil/canopy energy balance Turbulent mass transfer Leaf energy balance Stomatal regulation Plant hydraulics Photosynthesis



2. Carbon compartments, pools and carbon balance



## **Carbon compartments and pools**

### Carbon pool types

Structural carbon - Cell membranes, cell walls & cytosolic machinery.

Metabolic carbon - Labile carbon (sugar) concentration used to sustain cell functioning.

Storage carbon - Labile carbon (starch) concentration used as long-term carbon source.

### **Pools**

Compartment	Structural	Metabolic	Storage
Leaves	Leaf dry biomass $oldsymbol{B}_{leaf}$	Leaf sugar $SS_{leaf}$	Leaf starch $ST_{leaf}$
Sapwood	Sapwood dry biomass $m{B}_{sapwood}$	Sapwood sugar $SS_{sapwood}$	Sapwood starch $ST_{sapwood}$
Fine roots	Fine root dry biomass $m{B}_{fineroot}$		

**Important** 

Sapwood carbon includes branches, stem and coarse roots



### Labile carbon balance equations

A. Changes in **leaf metabolic** carbon result from considering gross photosynthesis ( $A_g$ ), leaf maintenance respiration ( $M_{leaf}$ ), phloem transport ( $F_{phloem}$ ) and sugar-starch dynamics ( $SC_{leaf}$ ) and translocation to sapwood storage ( $TS_{leaf}$ ):

$$\Delta SS_{leaf} \cdot V_{storage,leaf} = A_g - M_{leaf} - F_{phloem} - SC_{leaf} - TS_{leaf}$$

B. Changes in **leaf storage** carbon result from sugar-starch dynamics and translocation to sapwood storage ( $TT_{leaf}$ ):

$$\Delta ST_{leaf} \cdot V_{storage,leaf} = SC_{leaf} - TT_{leaf}$$

C. Changes in **stem metabolic** carbon result from considering phloem transport, maintenance respiration of sapwood ( $M_{sapwood}$ ) and fineroot ( $M_{fineroot}$ ) tissues, sugar-starch dynamics and translocation to sapwood storage ( $TS_{sapwood}$ ):

Atmosphere

Photosynthesis

Metabolic

Storage

Structural

Leaf senescence

Photosynthesis

Storage

Structural

$$SS_{leaf}$$

ST\_{leaf}

Photosynthesis

Storage

Structural

Sapwood senescence

Sapwood senescence

Sapwood growth

Fine root senescence

Soil/mycorrhizae

$$\Delta SS_{sapwood} \cdot V_{storage, sapwood} = F_{phloem} - M_{sapwood} - M_{fineroot} - SC_{sapwood} - TS_{sapwood}$$

D. Changes in **stem storage** carbon result from considering sugar-starch dynamics, translocation from other pools, growth respiration and root exudation:

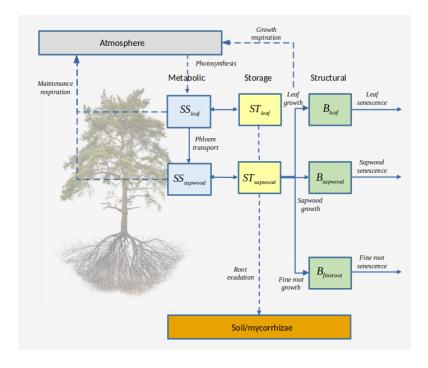
$$\Delta ST_{sapwood} \cdot V_{storage, sapwood} = SC_{sapwood} + TS_{leaf} + TT_{leaf} + TS_{sapwood} - G_{sapwood} - G_{leaf} - G_{fineroot} - RE_{sapwood}$$



## Labile carbon balance equations

E. Changes in **labile carbon pools** can be reduced to the balance between gross photosynthesis (  $A_g$  ), maintenance respiration ( M ), growth respiration ( G ) and root exudation ( RE ):

$$\Delta S_{labile} = A_g - (M + G + RE)$$





### Design of labile carbon processes

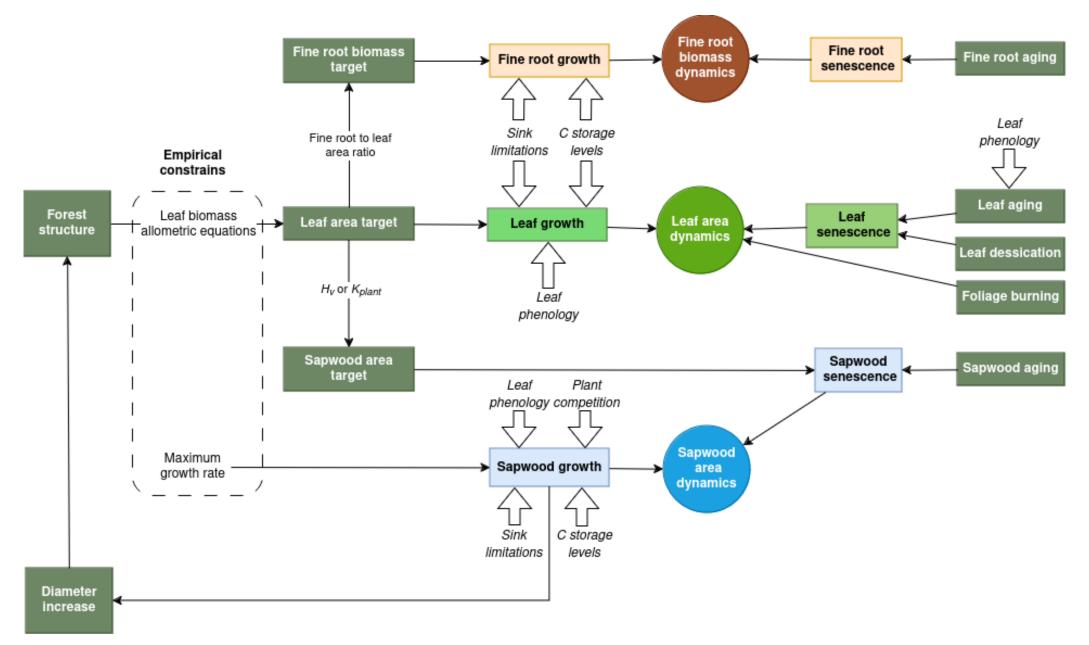
- Phloem transport is only explicitly modelled when using the advanced water submodel, following Hölttä et al. (2017)<sup>1</sup>.
- Sugar/starch dynamics are meant to keep sugar levels at a prescribed equilibrium value.
- The usual separation between **maintenance** and **growth** respiration is followed, with maintenance costs depending on temperature and phenology.
- **Translocation** of labile carbon towards sapwood storage occurs whenever there is senescence in a given tissue (leaves, branches).
- Root exudation is not a process competing for metabolic carbon, but a consequence of plant storage capacity being surpassed <sup>2</sup>.



# 3. Growth and senescence



# Drivers of growth and senescence





## Tissue growth

Daily leaf area increment  $\Delta LA$ , sapwood area increment  $\Delta SA$  and fine root biomass increment  $\Delta B_{fineroot}$  are defined as the minimum of three constraints:

$$\Delta LA = \min(\Delta LA_{alloc}, \Delta LA_{source}, \Delta LA_{sink})$$

$$\Delta SA = \min(\Delta SA_{source}, \Delta SA_{sink})$$

$$\Delta B_{fineroot} = \min(\Delta B_{fineroot,alloc}, \Delta B_{fineroot,source}, \Delta B_{fineroot,sink})$$

- $\Delta LA_{alloc}$  and  $\Delta B_{fineroot,alloc}$  are the increments allowed according to the targets set by **allocation** rules.
- $\Delta LA_{source}$ ,  $\Delta SA_{source}$  and  $\Delta B_{fineroot, source}$  are the maximum increments allowed by current starch availability.
- $\Delta LA_{sink}$ ,  $\Delta SA_{sink}$  and  $\Delta B_{fineroot,sink}$  are the increments expected due to **growth rates**, which are affected by temperature and turgor limitations <sup>1</sup>.

#### **Important**

- Sapwood area growth is **not limited** by allocation rules, effectively determining overall plant growth.
- Carbon is **preferentially** allocated to leaves and fine roots whenever storage levels are low because  $\Delta SA_{source}$  is more restrictive than  $\Delta LA_{source}$  or  $\Delta B_{fineroot,source}$ .



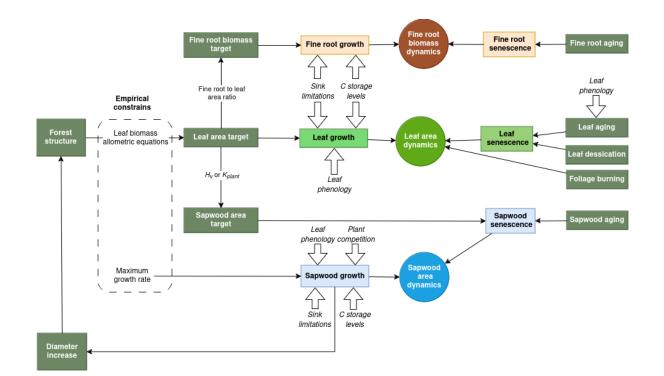
# Tissue growth

### **Key growth parameters**

Parameter	R	Definition	Explanation
$a_{fbt}, b_{fbt}, c_{fbt}$	Afbt,Bfbt, Cfbt	Allometric coefficients for tree leaf biomass, including competition	Determine allocation target for <b>tree leaf area</b> and influence sapwood area growth rates
$RGR_{cambium,max}$	RGRcambiummax	Maximum daily <b>tree</b> sapwood growth rate relative to cambium perimeter length	Determines overall maximum growth rates for tree species
$RGR_{sapwood,max}$	RGRsapwoodmax	Maximum daily <b>shrub</b> sapwood growth rate relative to cambium perimeter length	Determines overall maximum growth rates for shrub species
$1/H_v$	Al2As	Leaf area to sapwood area ratio	Determines allocation target for <b>sapwood</b> and, hence, sapwood senescence rates.
RGR	Ar2Al	Root area to leaf area ratio	Determines allocation target for <b>fine roots</b> and influences root maintenance costs
RSSG	RSSG	Minimum relative starch for sapwood growth to occur	Determines preference for maintenance over growth under low carbon availability (e.g. shade-tolerant species)



### Tissue senescence



- Leaf senescence rates are determined by:
  - Aging (leaf lifespan)
  - Phenology (winter deciduous)
  - Dessication (via stem cavitation)
- Sapwood senescence rates are determined by:
  - Aging (depending on temperature)
  - Sapwood area target (only if  $SA > SA_{target}$ )
- Fine root senesence rates are determined by:
  - Aging (depending on temperature)

#### Note

- Leaf and fine root senescence create a need to constantly replace tissues.
- Sapwood senescence aims to keep sapwood area close to its functional target (either constant leaf area to sapwood area ratio or a constant whole-plant conductance).



## **Updating structural variables**

### **Trees**

New sapwood area,  $\Delta SA$ , is translated to an increment in DBH,  $\Delta DBH$ , following:

$$\Delta DBH = 2 \cdot \sqrt{(DBH/2)^2 + (\Delta SA/\pi)} - DBH$$

Increments in height are linearly related to increments in diameter through a coefficient depending on light conditions <sup>1</sup>, and are limited by a maximum height.

Crown ratios are updated following static allometric relationships.

### **Shrubs**

Leaf area changes are translated to changes in shrub volume, cover and shrub height via allometric equations.

As for trees, shrub height is limited to a maximum value.

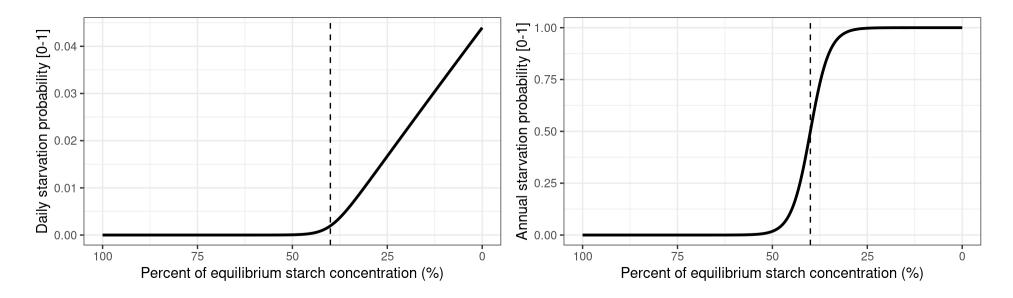


# 4. Mortality and recruitment



## **Plant mortality**

- 1. Small trees (1 < DBH < 7.5) die at a rate determined by a **self-thinning rule** depending on its size.
- 2. Species-specific parameters determine a daily constant baseline mortality rate for adults.
- 3. Daily mortality rates increase due to **carbon starvation** whenever sapwood metabolic carbon,  $SS_{sapwood}$ , becomes lower than a threshold, set by default to 40% of the homeostatic (equilibrium) concentrations. The daily starvation rate at the threshold corresponds to an annual mortality of 50%.



4. Daily mortality rates increase due to **dessication** whenever the average of *stem relative water content* and *stem relative hydraulic conductance* becomes lower than a pre-specified threshold, set to 40% by default.



### Recruitment

Unlike mortality, recruitment is simulated at the end of a simulated year (only in fordyn()).

#### **Recruitment from seed**

- Seed banks are full whenever trees of the species are present with a size above a maturity threshold (or a seed rain is forced).

  Otherwise, they are reduced following an exponential decay function.
- The following conditions need to be met for a species to recruit:
  - 1. Mean temperature of the coldest month is above a bioclimatic threshold.
  - 2. The fraction of light reaching the ground is above a bioclimatic threshold.
  - 3. The moisture index (annual precipitation over annual evapotranspiration) is larger than a bioclimatic threshold.
- A probability of recruitment is used to stochastically determine whether recruitment actually occurs.

### Resprouting

- Resprouting occurs if plants have been **cut**, **burned** or **dessicated**.
- Resprouting **survivorship** depends on the disturbance (different effects on buds).
- Resprouting **vigour** for trees depends on *DBH*.



# 5. Biomass balance



### **Biomass balance**

### Balance in structural carbon pools

The change in structural biomass of each **compartment** results from the interplay between growth and senescence:

$$\Delta B_{leaves} = B_{leaves,growth} - B_{leaves,senescence}$$

$$\Delta B_{sapwood} = B_{sapwood,growth} - B_{sapwood,senescence}$$

$$\Delta B_{fineroot} = B_{fineroot,growth} - B_{fineroot,senescence}$$

The following equation defines the structural biomass balance at the plant level:

$$\Delta B_{structure} = \Delta B_{leaves} + \Delta B_{sapwood} + \Delta B_{fineroot}$$

#### Balance at the cohort level

At the **cohort level** we need to take into account that some individuals will die, so that the biomass balance needs to incorporate mortality losses:

$$\Delta B_{cohort} = \Delta B_{plant} \cdot N_{cohort} - B_{mortality}$$

where  $N_{cohort}$  is the initial cohort density (before mortality occurred) and  $B_{mortality}$  is the biomass loss due to mortality of individuals, which in order to close the balance has to be defined as:

$$B_{mortality} = (B_{plant} + \Delta B_{plant}) \cdot N_{dead}$$

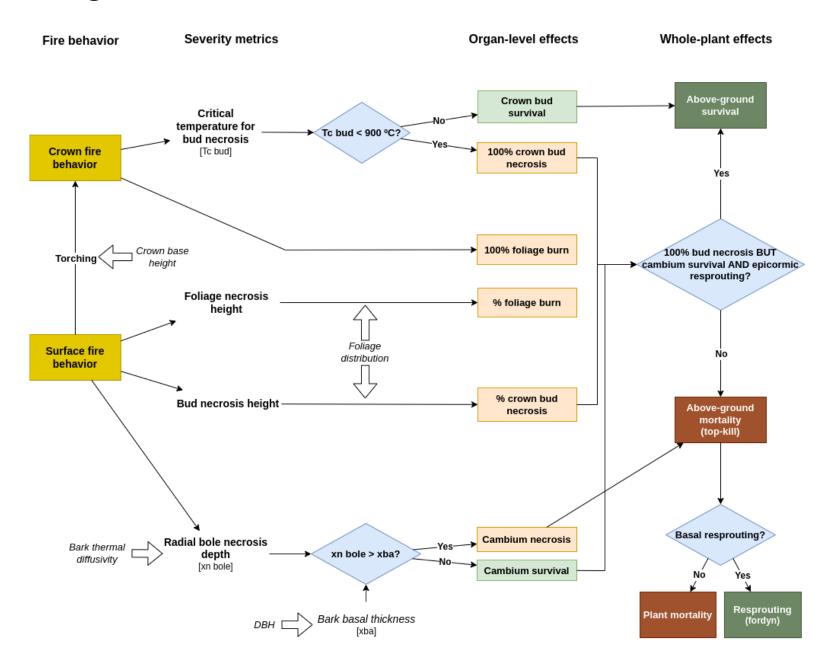
where  $N_{dead}$  is the density of dead individuals and  $B_{plant}$  is the initial plant biomass.



# 6. Fire effects



# **Design of fire effects**





# M.C. Escher - Three worlds, 1955



