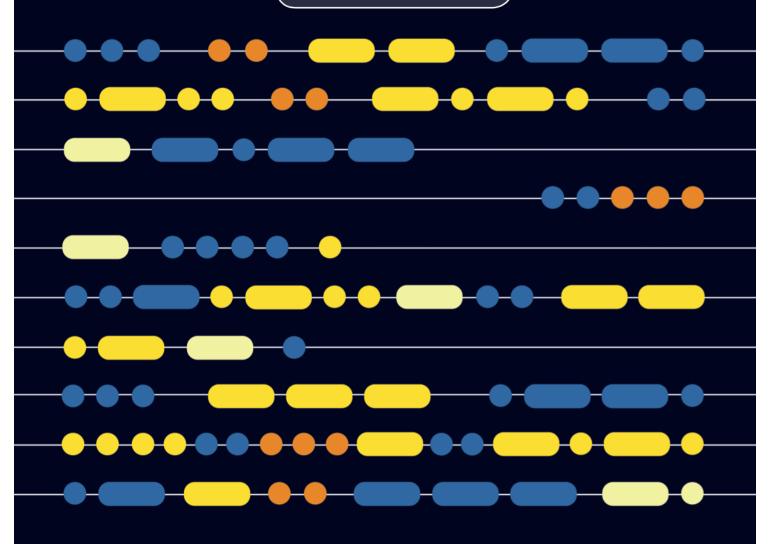
MACHINE LEARNING REFINED

Foundations, Algorithms, and Applications

SECOND EDITION



To our families:

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