



ΠΑΝΕΠΙΣΤΗΜΙΟ  
ΔΥΤΙΚΗΣ ΑΤΤΙΚΗΣ  
UNIVERSITY OF WEST ATTICA

DEPARTMENT OF COMPUTER AND INFORMATION  
TECHNOLOGY AND COMPUTER ENGINEERING

PROJECT 4  
COORDINATION

# CIRCUIT THEORY

## STUDENT DETAILS :

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**NAME:** ATHANASIOU VASILEIOS EVANGELOS

**STUDENT ID:** 19390005

**STUDENT SEMESTER :** 6th

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**LABORATORY PROFESSORS :** CHRISTOS KAMPOURIS-GEORGIOS ANTONIOU



## ADDITIONAL INFORMATION :

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**DATE OF EXERCISE :** 25/5/2022

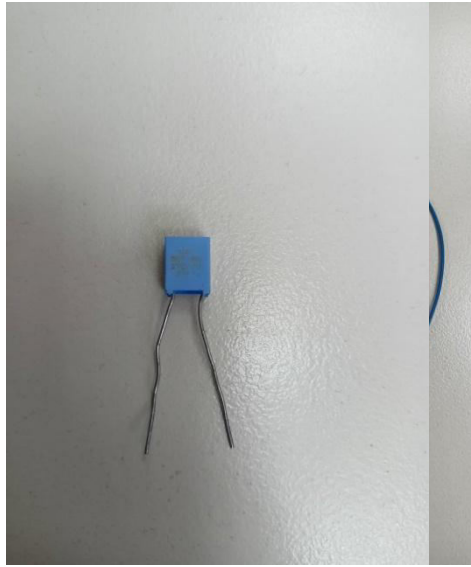
**DATE OF DELIVERY OF EXERCISE :** 23/6/2022

# CIRCUIT THEORY

## PHOTOS OF EQUIPMENT USED IN THE LABORATORY



Analog  
Multimeter  
Capacitor  
Cables  
Resistor



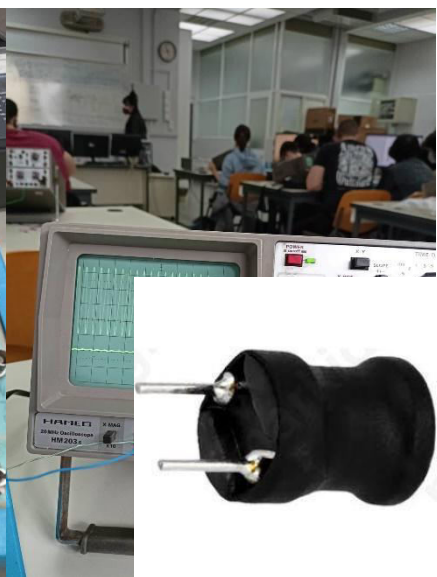
Breadboard



Oscilloscope

Inductor

Digital  
Multimeter



# CIRCUIT THEORY

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## 1.1 : Tuning in an RLC circuit in series

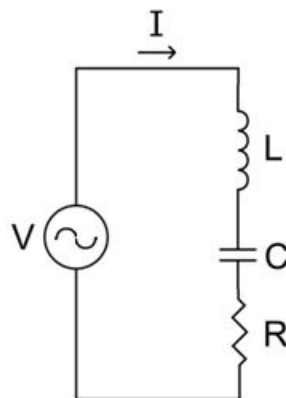
### General

In the chapters "Simulated Solution" and "Experimental Solution" the components used and the observations made during the experiment are presented in detail with snapshots from the "Multisim" software and photos of the experiment from the laboratory environment respectively, while in the chapter "Theoretical Solution" the behavior of the circuit is analyzed in general. The table below presents a summary for the selection of the appropriate coil value used in the circuits presented in the chapters "Simulated Solution" and "Experimental Solution".

**Table 1**

Implementation	C	L Theoretical	L Typical	Deviation from $f_R$
In Series	47nF	0.64 mH	6200 $\mu$ H	681 Hz
In parallel	27nF			

### Theoretical Solving



**Figure 1**

The circuit in Figure 1 achieves the resonance effect in an RLC circuit, where the inductor (L) and capacitor (C) are connected in series. The effect will be observed at a frequency where the inductive response ( $X_L$ ) and the capacitive response ( $X_C$ ) cancel each other out, ie, they are equal. The impedance of the circuit is :  $Z = \sqrt{R^2 + (X_L - X_C)^2}$  and therefore, during the resonance effect the impedance will be equal to the ohmic resistance (R). Also, during the effect the maximum current flowing through the circuit is observed, since from Ohm's law and Kirchhoff's law of voltages we have :

$$V = V_L + V_C + V_R \quad \text{⊕} \quad V = IX_L + IX_C + IR \quad \text{⊕} \quad V = IX_C + IX_C + IR \quad \text{⊕} \quad V = I(2X_C + R)$$

(From the resonance effect, where  $X_C = X_L$ )

$$I = V / Z \quad \text{⊕} \quad I = [I(2X_C + R)] / [\sqrt{R^2 + (X_L - X_C)^2}] \quad \text{⊕} \quad I = [I(2X_C + R)] / R$$

The third observation is that the sinusoidal signal emitted by the input of the circuit (capacitor) and the corresponding signal emitted by the output of the circuit (coil, which is observed using the oscilloscope) are in phase, ie, they have the same phase (cof = 1). Since, the voltages  $V_C$  and  $V_L$  are equal it means that the

# CIRCUIT THEORY

total voltage of the circuit can take large voltage values, ie, in the RLC circuit in series during the resonance effect, overvoltages are observed.

## Simulative Resolution

*Table 2*

F (Hz)	Z (Ω)	X (Ω)	X <sub>L</sub> (Ω)	X <sub>C</sub> (Ω)	I <sub>rms</sub> (A)	V <sub>Lrms</sub> (V)	V <sub>Crms</sub> (V)
1	3333333333. 3	0.004000 3	0.004	3 * 10 <sup>-6</sup>	296,788 * 10 <sup>-9</sup>	12 * 10 <sup>-10</sup>	9 * 10 <sup>-14</sup>
10	3333333333.3 3	0.040003	0.04	3 * 10 <sup>-5</sup>	2.968 * 10 <sup>-6</sup>	12 * 10 <sup>-8</sup>	9 * 10 <sup>-11</sup>
100	3333333333.33 3	0.40003	0.4	3 * 10 <sup>-4</sup>	29.625 * 10 <sup>-6</sup>	10 <sup>-5</sup>	9 * 10 <sup>-9</sup>
500							
1000	3333333333.333 3	4.0003	4	3 * 10 <sup>-3</sup>	295.179 * 10 <sup>-6</sup>	10 <sup>-3</sup>	9 * 10 <sup>-7</sup>
1500							
2500							
5000							
10k							
30k	333	40,003	40	3 * 10 <sup>-2</sup>	2.24 * 10 <sup>-3</sup>	9 * 10 <sup>-2</sup>	7 * 10 <sup>-5</sup>
50k							
100k	33.3	400,003	400	3 * 10 <sup>-1</sup>	2.01 * 10 <sup>-3</sup>	0.804	6 * 10 <sup>-4</sup>
200k							

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<b>500 k</b>							
<b>1M</b>							
<b>10M</b>							

<b>F (Hz)</b>	<b>Vi(V) Kan. A Measurement</b>	<b>Vo(V) Kan. B Measurement.</b>	<b>20log10(Vo/Vi) (db) Calculated</b>	<b>I<sub>rms</sub> (A) Measurement</b>
<b>1</b>	1,410	$7.165 * 10^{-6}$		$296,788 * 10^{-9}$
<b>10</b>	$61.647 * 10^{-3}$	$65.028 * 10^{-6}$		$2.968 * 10^{-6}$
<b>100</b>	$412.207 * 10^{-3}$	$7.562 * 10^{-3}$		$29.625 * 10^{-6}$
<b>500</b>	$5.417 * 10^{-3}$	$1.361 * 10^{-3}$		$147,994 * 10^{-6}$
<b>1000</b>	$2.260 * 10^{-3}$	$3.302 * 10^{-3}$		$295.179 * 10^{-6}$
<b>1500</b>	$6.370 * 10^{-3}$	$4.998 * 10^{-3}$		$440.775 * 10^{-6}$
<b>2500</b>	$4.487 * 10^{-3}$	$5,500 * 10^{-3}$		$724.203 * 10^{-6}$
<b>5000</b>	$1.118 * 10^{-3}$	$11.328 * 10^{-3}$		$1.361 * 10^{-3}$
<b>10k</b>	$3.094 * 10^{-3}$	$15.304 * 10^{-3}$		$2.24 * 10^{-3}$
<b>30k</b>	$25.755 * 10^{-3}$	$25.755 * 10^{-3}$		$3.002 * 10^{-3}$
<b>50k</b>	$1.577 * 10^{-3}$	$7.799 * 10^{-3}$		$2.785 * 10^{-3}$
<b>100k</b>	$1.691 * 10^{-3}$	$2.459 * 10^{-3}$		$2.01 * 10^{-3}$

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<b>200k</b>	$19.784 * 10^{-3}$	$3.891 * 10^{-3}$		$1.166 * 10^{-3}$
<b>500k</b>				
<b>1M</b>				
<b>10M</b>				

*Table 3*



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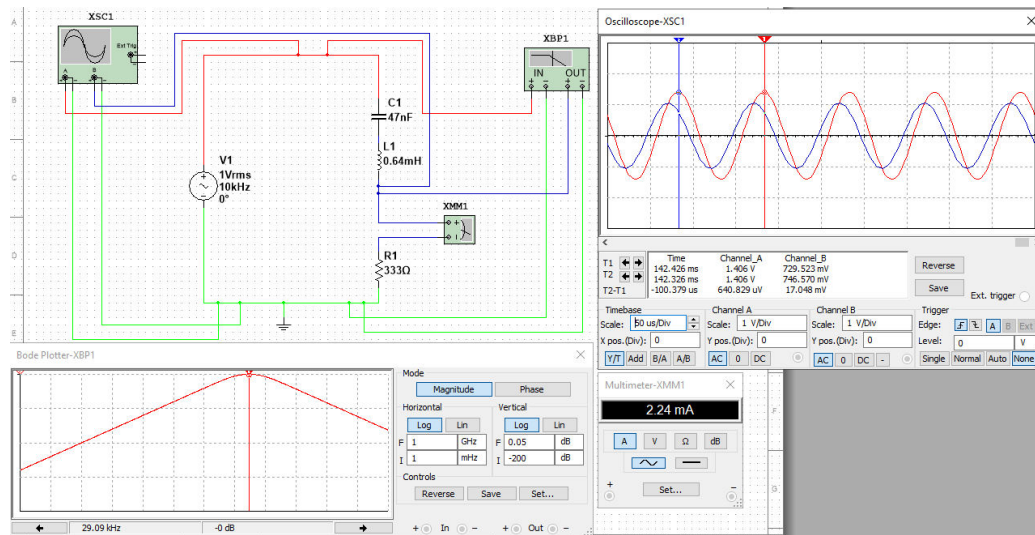


Figure 2

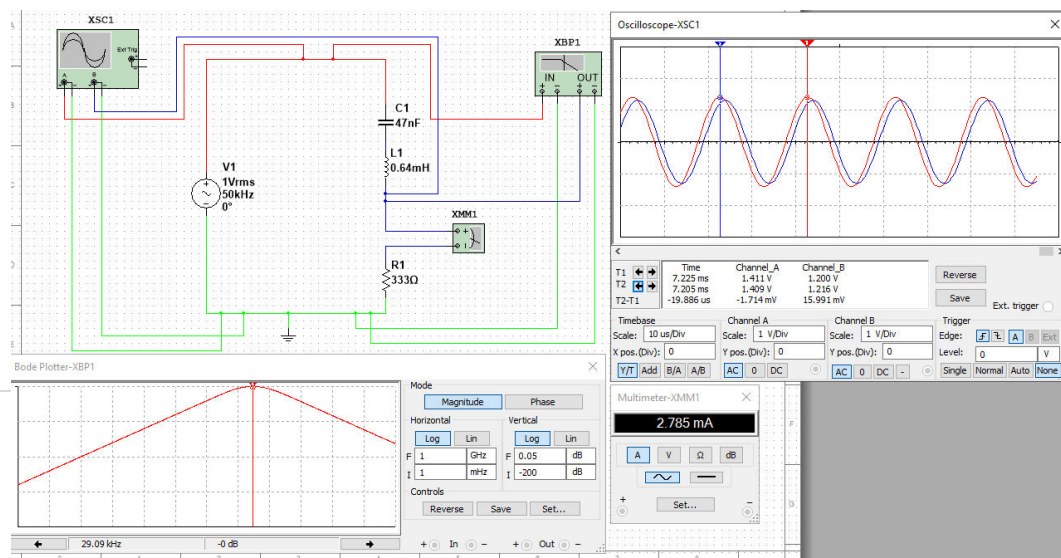
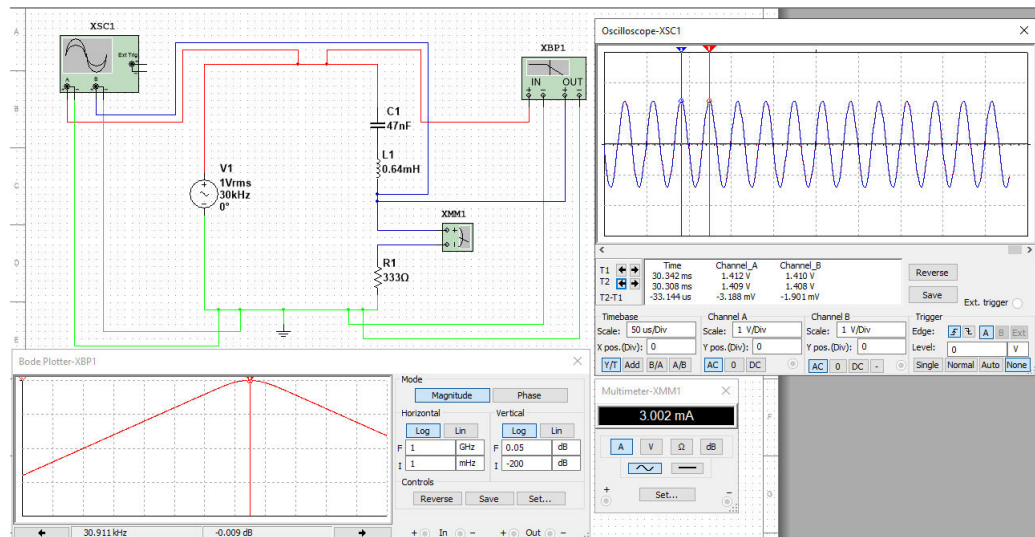


Figure 3

# CIRCUIT THEORY

**Figure 4**

From the simulated solution in the "Multisim" software (Figures 2, 3, 4) and from the measurements recorded in Tables 2 and 3, the resonance effect in an RLC circuit, where the inductor and capacitor are connected in series, is clearly illustrated.

First, the theoretical value of the coil noted in the 2nd<sup>line</sup> of Table 1 in the "General" section was calculated from the resonance frequency formula, which is :  $f_r = \frac{1}{2\pi\sqrt{LC}}$ , where "L" is the inductance of the coil, "C" is the capacitance of the capacitor and " $f_r$ " is the resonant frequency. In detail, in Table 2, the values were calculated using the following formulas:

$$\text{Complex resistance } Z = (R^2 + X^2)^{1/2} \quad (\text{in } \Omega)$$

$$\text{Active resistance } X = X_L - X_C \quad (\text{in } \Omega)$$

$$\text{Inductive reactance } X_L = 2\pi fL \quad (\text{in } \Omega)$$

$$\text{Capacitive reaction } X_C = 1 / 2\pi fC \quad (\text{in } \Omega)$$

$$I_{rms} = V_{rms} / Z \quad (\text{in A})$$

$$V_{Lrms} = I_{rms} * X_L \quad (\text{in V})$$

$$V_{Crms} = I_{rms} * X_C \quad (\text{in V})$$

In Table 3, the values were noted from the measurements made in "Multisim". From Tables 2 and 3 and Figures 2, 3 and 4, it is observed, and even in bright red (Figure 3), that the resonant frequency is 30 kHz. This is justified by the following three observations:

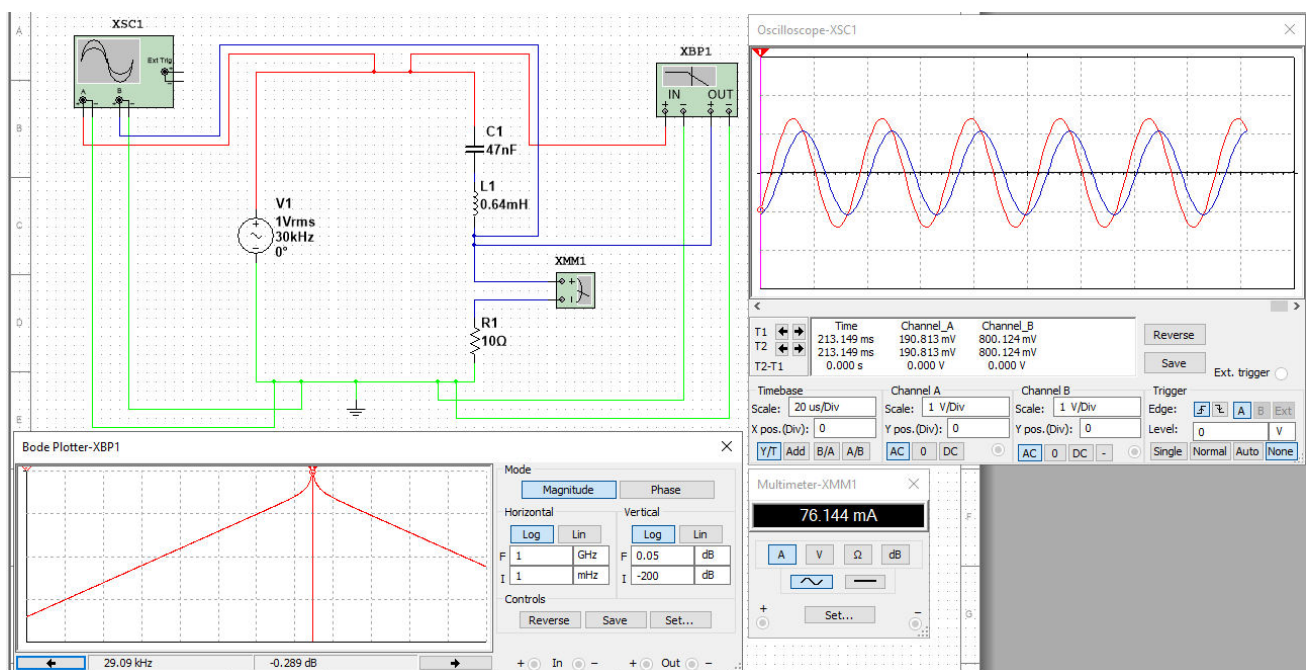
1. The sinusoidal signal emitted by the capacitor (input of the circuit) has the same phase as the corresponding signal emitted by the output of the circuit (coil) and this can be observed with the help of the oscilloscope in Figure 3.
2. The resistance of the circuit "Z" from the count in Table 2, is observed to be equal to the ohmic resistance "R" (333  $\Omega$ ). This is justified by the impedance formula "Z", which is:  $Z = \sqrt{R^2 + (X_L - X_C)^2}$  and during resonance, the inductive reaction " $X_L$ " cancels each other out with the capacitive reaction " $X_C$ ", ie, they are equal. Therefore,  $Z = R^2 \Rightarrow Z = R$ .
3. The current flowing in the circuit at the resonant frequency (Figure 3) is the maximum, as, at frequencies above the resonant frequency (Figure 4), the current decreases.

Finally, during resonance it is observed from Tables 2 and 3 that the values of the capacitor  $V_C$  and the inductor  $V_L$  voltage are quite high, proving the formulation in "Theoretical Solution" for the overvoltage phenomena that occur in an RLC circuit, where capacitor and inductor are connected in series, during resonance.

**Table 4**

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Resistance ( $\Omega$ )	$Q_{ser} = \frac{1}{R} \sqrt{\frac{L}{C}}$	IR (mA)
1k	0.117	$999,952 * 10^{-3}$
500	0.233	2
220	0.53	4,542
100	1.17	9,964
10	11.7	76,144
1	117	116.66



**Figure 5**

According to the measurements recorded in Table 4, as the ohmic resistance "R" of the circuit decreases, the current flowing through the circuit increases. This is justified by Ohm's law ( $I = V/R$ ), where the resistance (R) and the current intensity (I) are inversely proportional quantities. Also, as the resistance decreases, the efficiency of the circuit Q increases, from the formula  $Q = \frac{1}{R} \sqrt{\frac{L}{C}}$ . Finally, it is worth noting from Figure 5 that the resonant frequency of the circuit is not the frequency of 30 kHz, as long as the value of the ohmic resistance is 10  $\Omega$ . This is observed from the input and output signals presented in the oscilloscope. The two signals are not in phase and in fact the inductive reaction signal "X<sub>L</sub>" is preceded by the inductive reaction signal.

## Experimental Solution



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For the experimental solution carried out in the laboratory environment, the "breadboard", the oscilloscope, an analog multimeter set to calculate current intensity (ammeter), cables, three 1 k $\Omega$  resistors, a 470 nF capacitor and a 1 mH inductance coil were used.

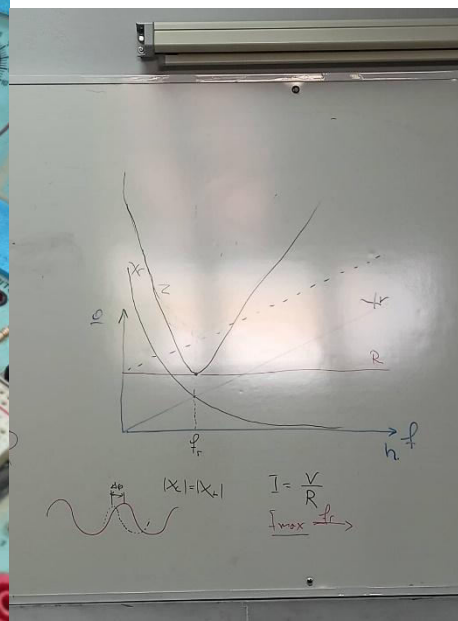
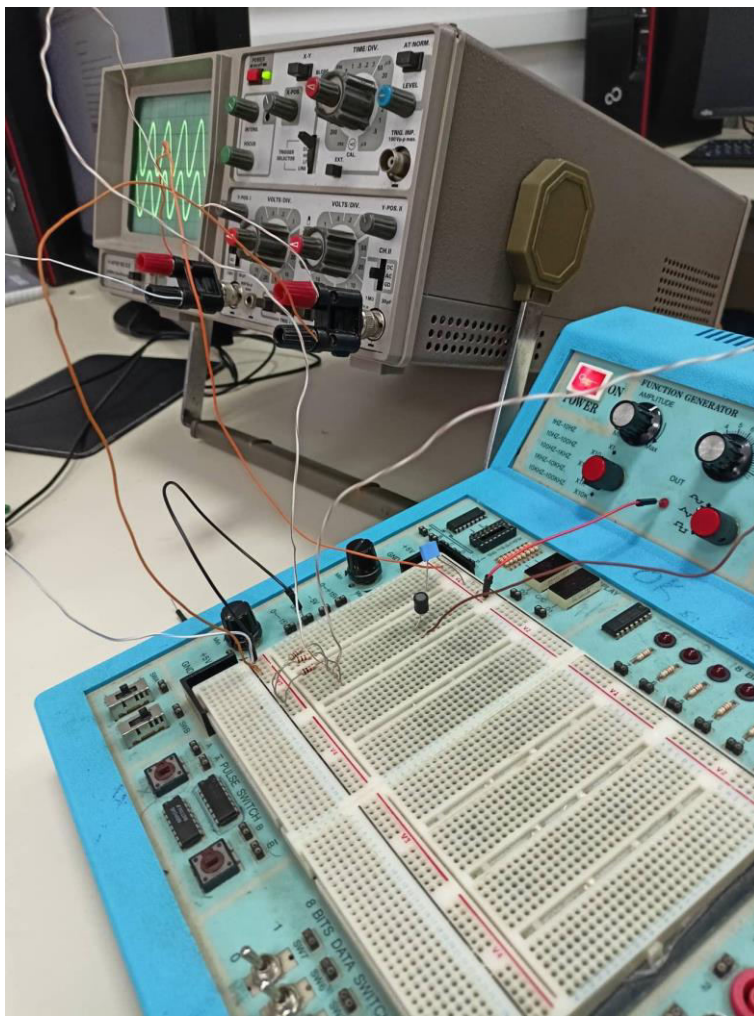
To start, we connected with a cable, the AC voltage source to a shorted line on the "breadboard" and the ground with another cable to another shorted line as well. We then took the three 1 k $\Omega$  resistors, and connected them in parallel to form, indirectly, the 333  $\Omega$  isodynamic resistor that we used in the "Simulated Solution". Immediately afterwards, we connected the capacitor and the inductor in series with the three resistors and started the experiment by connecting the measuring instruments as well. More specifically, in series with one end of the equivalent resistor and one end of the inductor (as shown in Figure 6), we connected the analog multimeter set to be an ammeter to measure the current flowing through the circuit. Also, we connected one channel of the oscilloscope to the source (input of the  $V_{in}$  circuit) and the other to the coil (output of the  $V_{out}$  circuit) to observe the waveforms emitted by the capacitor and the coil. As we observe in Figure 6, the phases of the two sinusoidal signals are equal (in-phase) at 5 kHz, which means that we are at the resonant frequency. Figure 7 shows the ammeter reading at a frequency greater than 5 kHz (which is the resonant frequency) at 2 mA. At the resonance frequency the current reached 9 mA, where it was at its maximum, as, as we increased the input frequency from the source, the current gradually decreased. Figure 8 shows the resistance-frequency plot, which depicts the value of the inductive response ( $X_L$ ) and the value of the capacitive response ( $X_C$ ) for various values of input frequency from the source. As, of course, observed the two values are equal at some frequency and the value of the circuit impedance is constant, ie, the ohmic resistance, signaling that it is



the resonant frequency.

In summary, both experiments are found to correctly verify the formulations recorded in "Theoretical Solution".

**Figure 7**



**Figure 6**

**Figure 8**

## 1.2 : Tuning in an RLC circuit in parallel

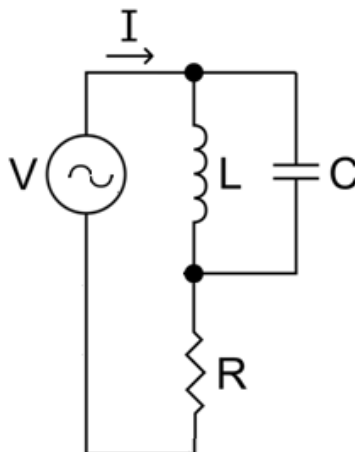
### General

In the chapter "Simulation Solution" the components used and the observations made during the experiment are presented in detail with snapshots from the "Multisim" software, while in the chapter "Theoretical Solution" the behavior of the circuit is analyzed in general. The table below presents a summary for the selection of the appropriate coil value used in the circuit presented in the "Simulated Solution" chapter.

**Table 5**

Implementation	C	L Theoretical	L Typical	Deviation from $f_R$
In Series	47nF	0.64 mH	6200 $\mu$ H	681 Hz
In parallel	27nF	3.3mH	3300 $\mu$ H	

### Theoretical Solving



**Figure 8**

The circuit in Figure 8 achieves the resonance effect in an RLC circuit, where the inductor (L) and capacitor (C) are connected in parallel. The effect will be observed at a frequency where the inductive response ( $X_L$ ) and the capacitive response ( $X_C$ ) cancel each other out, ie, they are equal. The impedance of the circuit is :  $Z = \sqrt{R^2 + (X_L - X_C)^2}$  and therefore, during the resonance effect the impedance will be equal to the ohmic resistance (R). Also, during the effect the maximum current flowing through the circuit is observed, since from Ohm's law and Kirchhoff's law of voltages we have :

$$V = V_L + V_C + V_R \quad V = IX_L + IX_C + IR \quad V = IX_C + IX_C + IR \quad V = I(2X_C + R)$$

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(From the resonance effect, where  $X_C = X_L$ )

$$I = V / Z \quad \text{④} \quad I = [I(2X_C + R)] / [\sqrt{R^2 + (X_L - X_C)^2}] \quad \text{④} \quad I = [I(2X_C + R)] / R$$

The third observation is that the sinusoidal signal emitted by the input of the circuit (capacitor) and the corresponding signal emitted by the output of the circuit (coil, which is observed using the oscilloscope) are in phase, ie, they have the same phase (cof = 1). In contrast to the RLC circuit, where the capacitor and coil are connected in series and the voltages  $V_C$  and  $V_L$  are equal which means that the total voltage of the circuit can take large voltage values, ie, in the circuit during the resonance effect, overvoltages are observed, in the corresponding circuit with parallel connection, large current intensities are observed during the resonance effect, ie, overvoltages are present in the circuit.

## Simulative Resolution

F (Hz)	Z ( $\Omega$ )	X ( $\Omega$ )	$X_L$ ( $\Omega$ )	$X_C$ ( $\Omega$ )	$I_{rms}$ (A)	$V_{Lrms}$ (V)	$V_{Crms}$ (V)
1	0.02	218430.2 5	0.02	218430.2 7	$3.003 * 10^{-3}$	0.00006	6559.5
10	0.2	21842.82 7	0.2	21843.02 7	$3.003 * 10^{-3}$	0.0006	655.95
100	2	2182.302 7	2	2184.302 7	$3.003 * 10^{-3}$	0.006	65.59
500	0.33	426.86	10	436.86	$3.003 * 10^{-3}$	0.03	1.31
1000	0.33	198.43	20	218.43	$2.997 * 10^{-3}$	0.06	0.6
1500	0.33	114.92	30	144.92	$2.99 * 10^{-3}$	0.09	0.4
2500	0.33	38.9	50	88.9	$2.965 * 10^{-3}$	0.1	0.3
5000	0.33	56.5	100	44.5	$2.841 * 10^{-3}$	0.3	0.12
10k	0.33	178.2	200	21.8	$2.159 * 10^{-3}$	0.4	0.05
30k	0.33	592.6	600	7.4	$2.28 * 10^{-3}$	1.3	0.02
50k	0.33	995.5	1000	4.5	$2.79 * 10^{-3}$	2.8	0.01
100k	0.33	1997.9	2000	2.1	$2.955 * 10^{-3}$	5.9	0.006

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<b>200k</b>	0.33	3999	4000	1	$2.991 * 10^{-3}$	12	0.003
<b>500k</b>	0.33	9999.5	10000	0.5	$3.001 * 10^{-3}$	30	0.002
<b>1M</b>	0.33	1999.5	20000	0.2	$3.003 * 10^{-3}$	60	0.0006
<b>10M</b>	0.33	19999.98	20000 0	0.02	$3.003 * 10^{-3}$	600	0.00006

*Table 6*

*Table 7*

<b>F (Hz)</b>	<b>Vi(V) Kan. A Measurement</b>	<b>Vo(V) Kan. B Measurement.</b>	<b>20log10(Vo/Vi) (db) proportional</b>	<b>I<sub>rms</sub> (A) Measurement</b>
<b>1</b>	$1.518 * 10^{-3}$	$166.442 * 10^{-3}$		$3.003 * 10^{-3}$
<b>10</b>	$829.431 * 10^{-3}$	1,433		$3.003 * 10^{-3}$
<b>100</b>	$75.065 * 10^{-3}$	$1.505 * 10^{-3}$		$3.003 * 10^{-3}$
<b>500</b>	$14.992 * 10^{-3}$	$8.228 * 10^{-3}$		$3.003 * 10^{-3}$
<b>1000</b>	$8.852 * 10^{-3}$	$3.734 * 10^{-3}$		$2.997 * 10^{-3}$
<b>1500</b>	$29.343 * 10^{-3}$	$36.154 * 10^{-3}$		$2.99 * 10^{-3}$
<b>2500</b>	$6.786 * 10^{-3}$	$1.161 * 10^{-3}$		$2.965 * 10^{-3}$
<b>5000</b>	$13.188 * 10^{-3}$	$1.021 * 10^{-3}$		$2.841 * 10^{-3}$
<b>10k</b>	$2.469 * 10^{-3}$	$18.884 * 10^{-3}$		$2.159 * 10^{-3}$
<b>30k</b>	$4.351 * 10^{-3}$	$3.521 * 10^{-3}$		$2.28 * 10^{-3}$
<b>50k</b>	$1.201 * 10^{-3}$	$7.637 * 10^{-3}$		$2.79 * 10^{-3}$
<b>100k</b>	$1.025 * 10^{-3}$	$11.740 * 10^{-3}$		$2.955 * 10^{-3}$
<b>200k</b>	$87.475 * 10^{-3}$	$61.391 * 10^{-3}$		$2.991 * 10^{-3}$

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500k				$3.001 * 10^{-3}$
1M				$3.003 * 10^{-3}$
10M				$3.003 * 10^{-3}$

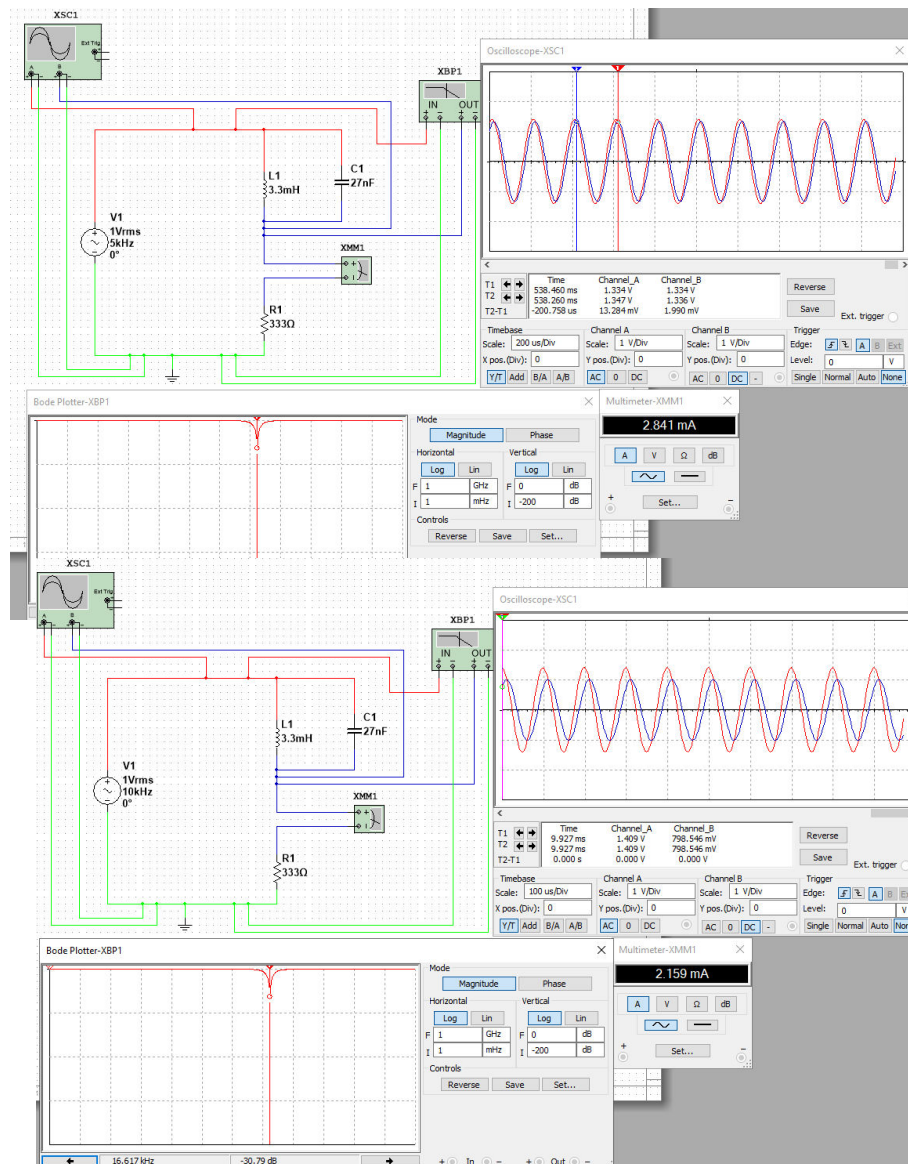
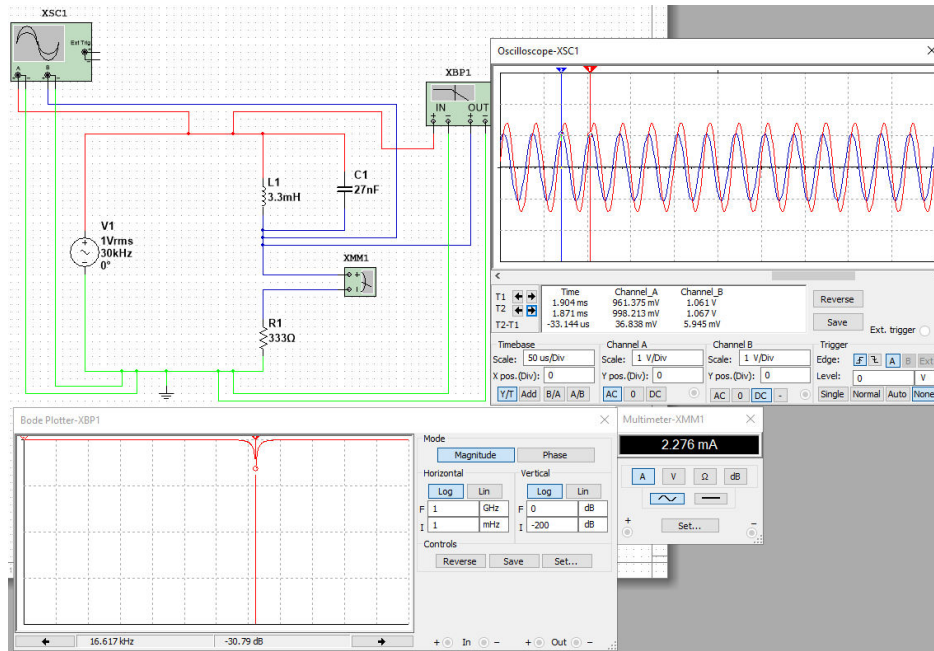


Figure 9

Figure 10





**Figure 11**

From the simulated solution in the "Multisim" software (Figures 9, 10, 11) and from the measurements recorded in Tables 6 and 7, the resonance effect in an RLC circuit, where the inductor and capacitor are connected in parallel, is clearly illustrated .

First, the theoretical value of the inductor noted in the 3rd<sup>line</sup> of Table 4 in the "General" section was calculated from the resonance frequency formula, which is :  $f_r = \frac{1}{2\pi\sqrt{LC}}$ , where "L" is the inductance of the coil, "C" is the capacitance of the capacitor and "  $f_r$  " is the resonant frequency. In detail, in Table 6, the values were calculated using the following formulas:

$$\text{Impedance } Z = 1 / (1 / R^2 + 1 / X)^{2/2} \quad (\text{in } \Omega)$$

$$\text{Active resistance } X = X_L - X_C \quad (\text{in } \Omega)$$

$$\text{Inductive reactance } X_L = 2\pi fL \quad (\text{in } \Omega)$$

$$\text{Capacitive reaction } X_C = 1 / 2\pi fC \quad (\text{in } \Omega)$$

$$I_{rms} = V_{rms} / Z \quad (\text{in A})$$

$$V_{Lrms} = I_{rms} * X_L \quad (\text{in V})$$

$$V_{Crms} = I_{rms} * X_C \quad (\text{in V})$$

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In Table 7, the values were noted from the measurements made in "Multisim". From Tables 6 and 7 and Figures 9, 10 and 11, it can be observed, and even in bright red (Figure 10), that the resonant frequency is 10 kHz. This is justified by the following three observations:

4. The sinusoidal signal emitted by the capacitor (input of the circuit) has the same phase as the corresponding signal emitted by the output of the circuit (coil) and this can be observed with the help of the oscilloscope in Figure 10.
5. The resistance of the circuit "Z" from the count in Table 6, is observed to be equal to the ohmic resistance "R" (333  $\Omega$ ). This is justified by the impedance formula "Z", which is:  $Z = \frac{1}{\sqrt{\frac{1}{R^2} + \left(\frac{1}{X_L} - \frac{1}{X_C}\right)^2}}$  and during resonance, the inductive reaction " $X_L$ " cancels each other out with the capacitive reaction " $X_C$ ", ie, they are equal. Therefore,  $Z = R^2 \square \square Z = R$ .
6. The current flowing in the circuit at the resonant frequency (Figure 10) is the minimum, as, at frequencies exceeding the resonant frequency (Figures 9, 11), the current fluctuates.

Finally, during resonance it is observed from Tables 6 and 7 that the Irms voltage values are quite high proving the formulation in "Theoretical Solution" for the overcurrent phenomena that occur in an RLC circuit, where capacitor and inductor are connected in parallel, during resonance .