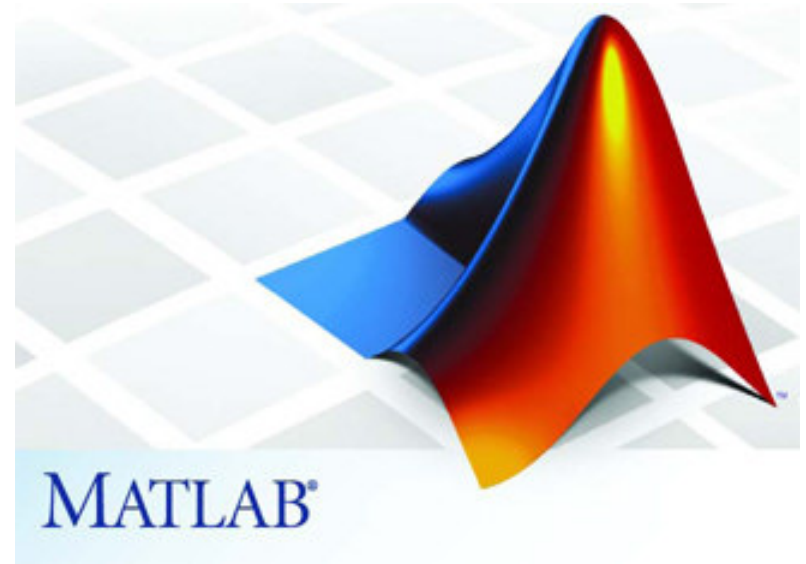


INTRODUCTION TO MATLAB

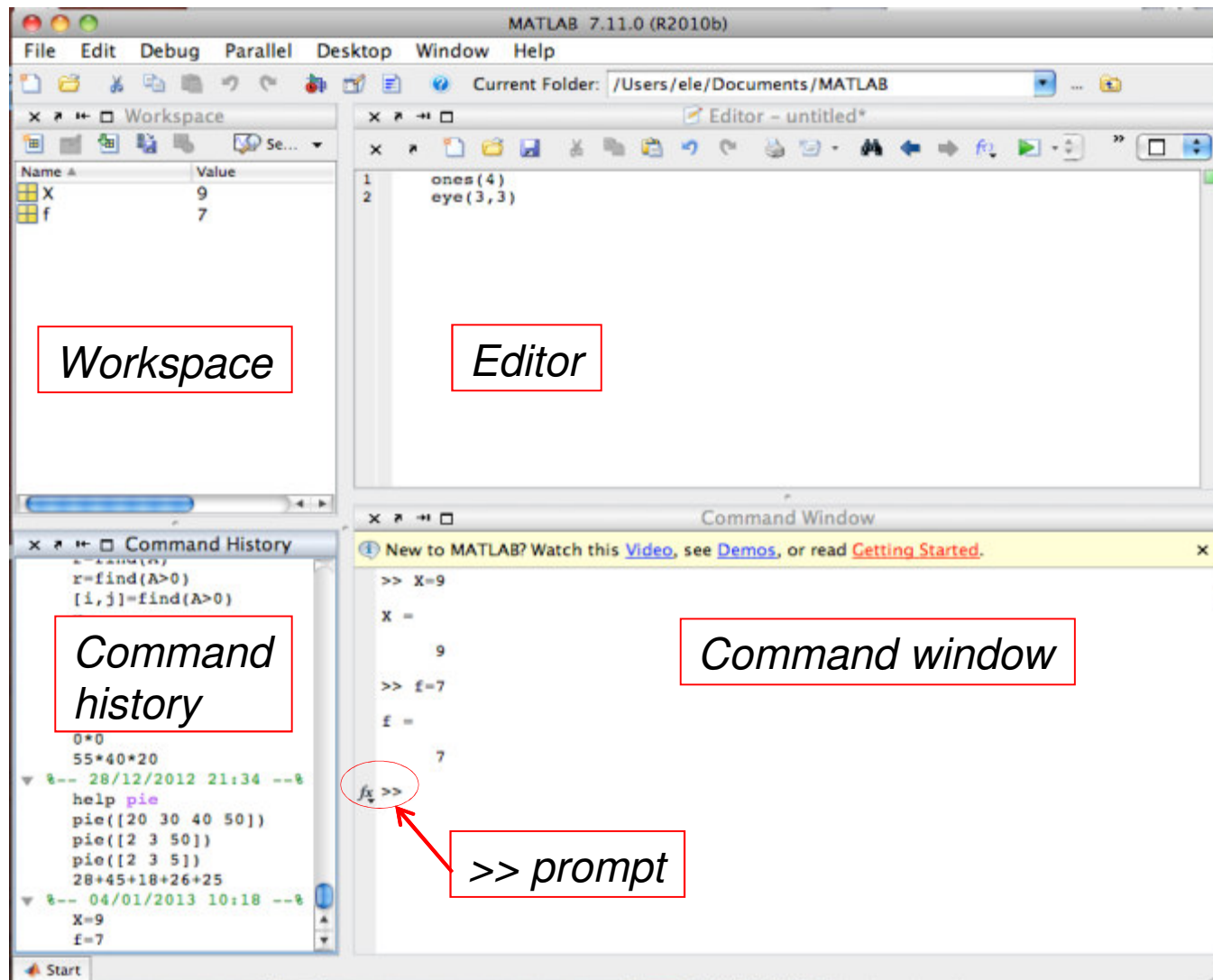


Course of
Intelligent Systems
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What is Matlab?

- ❑ *Matrix Laboratory*, interactive, matrix-based environment for scientific and engineering calculations
- ❑ **Matrix**: fundamental data structure
- ❑ Desktop tools in Matlab
 - *Command window*: to insert commands at the prompt **>>**, run functions or display results and error messages
 - *Editor*: to write or edit source code in a friendly framework (colored keywords, highlighted errors, tools for debugging)
 - *Workspace*: contains the set of variables **currently** defined (**in the current working session : time interval from startup**); a variable value can be viewed (in the *Variable Editor*) by double-clicking its name
 - *Command history*: lists all previously run commands in current and previous working sessions

Matlab's desktop tools



Main elements of language

1. Variables: Matlab works with one kind of object: the matrix
(**each variable is treated as a matrix**)

- **Matrix** is indicated with A, B, \dots
- **Array** (or vector) is treated as matrix with one only row (or column) a, b, \dots
 - the terms *array* and *matrix* are used interchangeably
- **Scalar** is a number, treated as a matrix 1×1

2. Functions

- built-in: already defined and ready to use , *mathematical*, *statistical*, etc.
(`sum`, `max`, `min`...)
- user-defined: can be written according to rules

3. Operators

- **Arithmetic:** `+` addition, `-` subtraction, `*` multiplication, `/` division,
`^` power, `'` transpose
- **Special:** `:` colon, `.` dot, `[]` square brackets

4. Statements are made of functions + operators + variables

Some important notes

- ❑ Matlab is *case sensitive*, *a* (lowercase) is not the same as *A* (uppercase)
- ❑ Matlab is an interpreted language
 - ❑ each instruction is translated in machine code and executed
 - ❑ there is no compiler
- ❑ The allocation of matrices and arrays is dynamic
 - ❑ no preallocation is required for variables
 - ❑ no declaration is required about dimensions and type of variables
 - it can be *useful* to preallocate very large matrices to speed up the code (when using program loops)

Statements

□ Matlab statements are of the form:

- `variable_name = expression;`
- `expression;`
- `x=log(y)+2;` complete statement

□ Expressions are composed from operators, functions, variable names, and scalars

- `c=3+2;` the evaluation of the expression `(3+2)` produces a result which is assigned to variable `c`
- `3+2;` If `c` and the `'='` are omitted, the result is assigned to the predefined variable *ans*
- Suppressing the output
 - If the semicolon `';`' at the end of the statement is omitted, the result is always displayed on the screen
 - to suppress the output, use the semicolon `';`' at the end of the statement
 - It is useful to suppress the output when managing large matrices or performing multiple operations

Entering matrices

❖ Matrices can be entered in different ways:

❑ Entered as list of elements

- separated by space or comma between square brackets

- each row ends with a semicolon ‘;’

- Matrix `A=[1 2 3; 4 5 6; 7 8 9]`

- Array `b=[10 20 30]`

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

❑ Loaded from numeric data files

- `B=load data.dat, B=load data.txt`

❑ Generated with built-in or user-defined functions

- `C=zeros(3,5)` 3x5 matrix of 0's elements

- `O=ones(1,5)` 1x5 matrix of 1's elements

- `M=magic(3)` magic square, sum of the elements on rows, columns, diagonals is equal

- `R=rand(4,5)` 4x5 matrix of randomly generated values in [0,1]

Entering matrices: examples

```
Z = zeros(2,4)
```

```
Z =
```

0	0	0	0
0	0	0	0

```
F = 5*ones(3,3)
```

```
F =
```

5	5	5
5	5	5
5	5	5

```
>> M=magic(3)
```

```
M =
```

8	1	6
3	5	7
4	9	2

```
>> rand(3,1)
```

```
ans =
```

0.3404
0.5853
0.2238

Subscripts (indexes)

the index starts from 1 not 0!

❖ A subscript notation between round brackets is used to access elements or submatrices in a given matrix:

□ **row-column** notation (two indexes, most used)

- we specify the name of the matrix and then the number of row and column of the element
- $A(i, j)$ extracts from A the element in position (i, j) where i is the row index and j is the column index
- $A(2, 3)$ is '6', the element in row 2, column 3

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

□ **linear** notation (a single index)

- we specify the name of the matrix and then the index of the element, as if the elements were arranged in a **long column vector**, composed by the columns of the matrix, arranged one above the other
- $A(k)$ extracts the k -th element
- $A(8)$ is '6', the 8-th element

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

Colon ':' operator

- ❑ The colon operator ':' is used mainly in two ways:
- ❑ For generating a **equally spaced vector**
 - `t = (start_val:end_val)` with default increment 1
 - `t = (4:10)` gives `t = 4 5 6 7 8 9 10`
 - `t2 = (start_val:increment:end_val)` with increment 2
 - `t2 = (4:2:10)` gives `t2 = 4 6 8 10`
- ❑ For **selecting a submatrix** (a portion of a matrix)
 - `a = t(1:3)` selects the elements in `t` from 1 to 3 and produces `a = 4 5 6`
 - `a = t(:)` selects **all** elements in `t` (":" used alone means "all", no selection)

Access to elements with subscripts and colon operator

- A subscripts notation is used to access elements in a matrix

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

- Access a **single element**

- $A(2, 3)$ is '6', the element in row 2, column 3

- Access a **submatrix**

- $B = A(1:2, 2:3)$ is the submatrix in A consisting of rows 1 and 2, and columns 2 and 3

$$B = \begin{pmatrix} 2 & 3 \\ 5 & 6 \end{pmatrix}$$

- $C = A(:, 2)$ is the submatrix (subarray) in A consisting of **all** elements of column 2

- the colon operator **':'** **used alone** as index of a row (column) denotes **all the elements** of the row (column)

$$C = \begin{pmatrix} 2 \\ 5 \\ 8 \end{pmatrix}$$

Square brackets '[']' operator

- The square brackets [] operator is used mainly in two ways:
- **Concatenation of matrices**: two matrices are joined to make a bigger matrix, by placing the one side by side to the other (A and B have same number of rows)

- $AB = [A \ B]$

$$A = \begin{pmatrix} 1 & 2 \\ 5 & 6 \end{pmatrix}, B = \begin{pmatrix} 3 & 4 \\ 7 & 8 \end{pmatrix}, AB = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{pmatrix}$$

- **Deleting rows or columns from a matrix**

- $AB(:, 2) = []$ deletes the second column (by assigning the **empty element** []) and directly modifies AB

- the colon operator as row subscript means that all rows are considered.

$$AB = \begin{pmatrix} 1 & 3 & 4 \\ 5 & 7 & 8 \end{pmatrix}$$

Matrix linear algebra operations

- ❑ The mathematical operations defined on matrices are the same of linear algebra
- ❑ **Addition** $A+B$ and **subtraction** $A-B$ act on involved matrices element by element
 - (A and B must have same size)
- ❑ **Multiplication** $A*B$ and **division** A/B act between entire matrices following the rules of linear algebra
 - (A and B must have compatible sizes)
 - If the dimensions of the involved matrices in the operation are incompatible, an error message is showed
- ❑ **Power** A^n
 - corresponds to repeat n times the multiplication of A by itself
- ❑ **Transpose** A'
 - the transpose matrix is the matrix with columns and rows reversed

Element by element operations

- ❑ Operations on matrices can also be performed between the corresponding elements of the matrices involved, by using the dot '.' operator before the arithmetic operator
 - Addition and subtraction are already element-wise operations!
 - Multiplication element by element $A .* B$
 - Division element by element $A ./ B$
 - Power element by element $A .^ n$
- ❑ $A .* B$ is different from $A * B$ because the former is a *element-wise* multiplication, the latter is a *row-column* multiplication

$$A * B = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix} * \begin{pmatrix} 1 & 1 \\ 2 & 2 \end{pmatrix} = \begin{pmatrix} 5 & 5 \\ 4 & 4 \end{pmatrix}$$

$$A .* B = \begin{pmatrix} 1 & 2 \\ 4 & 2 \end{pmatrix}$$

Scalar operations

- ❑ A scalar in Matlab is a 1x1 matrix
- ❑ The operation which involves a matrix and a scalar is applied between the scalar and each element of the matrix
- ❑ Scalar operations (involving a scalar s) are
 - Addition
 - Subtraction
 - Division
 - Multiplication

$$A = s + \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \begin{pmatrix} s+1 & s+2 \\ s+3 & s+4 \end{pmatrix}$$

$$A = s \cdot \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix} = \begin{pmatrix} s & 2s & 3s \\ 4s & 5s & 6s \\ 7s & 8s & 9s \end{pmatrix}$$

Strings and string functions

- ❑ A string is a matrix whose elements are characters surrounded by single quotes `' '`
 - `name = 'Mario'`
- ❑ `disp(s)` is the standard function used to display a string `s`
- ❑ `s=sprintf('the result is: %d', r)` writes formatted data (a string and a double value `r`) to a string `s`
 - useful when we need to insert carriage returns or values of variables in a string
 - `sprintf('first line \n second line')` produces a string on two lines
- ❑ `num2str(x)` converts the number `x` to a string
 - useful when displaying numerical results within a string with `sprintf`
- ❑ `strcat(s1, s2)` concatenates two strings `s1, s2`
 - `strcat('one', ' two')` produces the string `'one two'`
- ❑ `strcmp(s1, s2)` compares two strings and return a true (1) or false (0) value

Structures and cell arrays /1

- ❑ **Cell arrays** and **structures** are two useful Matlab objects
- ❑ they are multidimensional arrays used to store data related to each other of different size and type
 - for example, storing the **linguistic** and **numeric** information about a student (name, surname, age, marks) is not allowed in a matrix (elements of the same kind)
- ❑ **Structure**
 - organized by **fields**
 - creation or access to the fields is made by using the **name** of the field and the **. dot operator**
- ❑ **Cell array**
 - organized by **cells** (regular arrangement)
 - creation or access to the cells is made by using **subscripts** between curly brackets '{ }'

Structures and cell arrays /2

□ Structure: an example

- `mystruct=struct` builds an empty structure with name *'mystruct'*
- `mystruct.marks=[1 2 3; 4 5 6]` adds to the structure a field named `marks` and assigns a value to `marks` (2x3 matrix)
- `mystruct.name='text'` adds to the structure a field named `text` and assigns a string value to `text`
- `mystruct.age=30` adds to the structure a field named `age` and assigns a scalar value to `age`

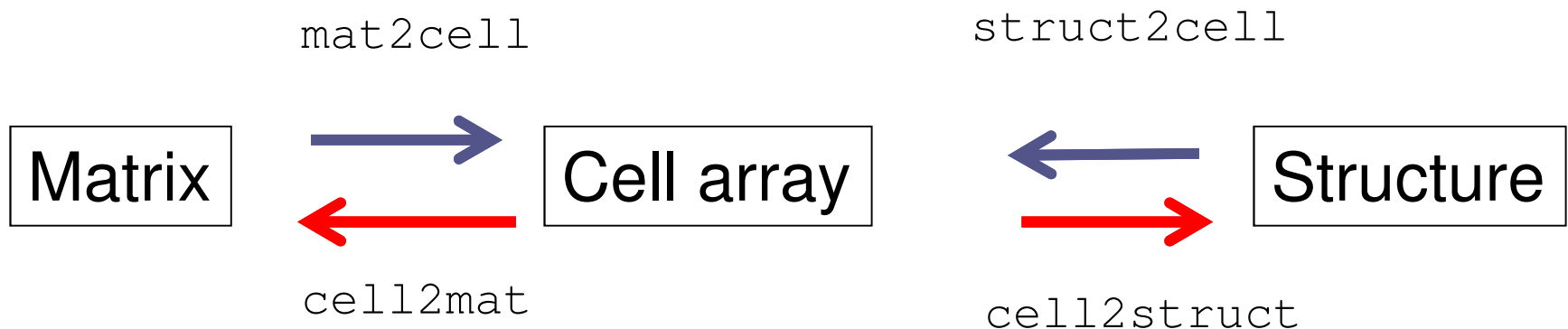
□ Cell array : an example

- `mycellarray=cell(2,1)` builds an empty cell array of size 2x1 with name *'mycellarray'*
- `mycellarray{1,1}=[1 2 3]` assigns a value of type vector to the cell in position {1,1}
- `mycellarray{2,1}=['text']` assigns a value of type string to the cell in position {2,1}

Structures and cell arrays /3

□ Conversion between matrices, cell arrays, and structures

- `C=mat2cell(M)`, `M=cell2mat(C)`
- `C=struct2cell(S)`, `S=cell2struct(C)`



Dot `.` operator

- ❑ The dot operator is used mainly in two ways:
- ❑ to perform **element by element (element-wise) operations** by altering the behaviour of some mathematical operations
 - `A.*B`
- ❑ to **access the fields in structures** (Matlab objects)
 - `mystruct.A`

Flow control statements

- ❑ In Matlab we can find the flow control statements
- ❑ They operate like those in many computer languages, by altering the default sequential flow control
- ❑ Conditional statements
 - `if...else` statement
 - `switch` statement
- ❑ Iterative statements (program loops)
 - `for` loop
 - `while` loop
 - `break` statement, is used to force the exit from a loop
 - `continue` statement, is used to go to the next loop iteration by skipping the remaining statements of the current iteration

if...else statement /1

- ❑ The `if` statement evaluates a condition (logical expression) and executes a statement (or group of statements) only if the specified condition is *true* (otherwise the statement is skipped)
- ❑ The `end` keyword terminates the `if` statement
- ❑ The keywords `elseif` and `else` are optional and provide alternative branches

(standard version)

```
if  condition  
    statement  
end
```

```
if  (x>0)  
    y=sqrt(x);  
end
```

if...else statement /2

(complete version)

```
if condition1
    statementA
elseif condition2
    statementB
else
    statementC
end
```

(mutually exclusive conditions)

The *statementA* is executed only if *condition1* is true, otherwise *condition2* is checked and *statementB* is executed

If no condition is true, *statementC* is executed

switch statement /1

- ❑ The *switch* statement evaluates a variable or an expression and executes a statement (or group of statements) based on the value of the expression
- ❑ It is used when several conditions must be handled
- ❑ The keyword `case` and `otherwise` identify groups of statements
- ❑ The `end` keyword terminates the *switch* statement

switch statement /2

```

switch expression
    case value0
        statementA
    case value1
        statementB
    otherwise
        statementC
end

```

```

switch x
    case 0
        disp('x is 0');
    case {1,2}
        disp('x is 1 or 2');
    otherwise
        disp('error');
end

```

The *expression* is evaluated and a value is obtained. The program flow enters the corresponding case, by executing the specified *statement*

If no **case** is verified, *statementC* is executed

Only the first matching case is executed!

for loop

- ❑ The *for* loop repeats the execution of a statement (or group of statements) a fixed number of times, as specified by the *condition*
- ❑ The *end* keyword terminates the *for* statement

```
for condition  
    statement  
end
```

```
x=0;  
for i=1:10,  
    x=x+1;  
end
```

while loop

- ❑ The *while* loop repeats the execution of a statement (or group of statements) an indefinite number of times, based on the control of a *relation* (logical condition)
- ❑ The *statement* is executed as long as the *relation* is true
- ❑ The **end** keyword terminates the *while* statement

```
while relation  
    statement  
end  
  
x=0;  
while (x<10)  
    x=x+1;  
end
```

Relational and logical operators /1

- The conditions in flow control statements can be expressed through relational and logical operators

- **Relational operators**

- < less than, <= less than or equal
- > greater than, >= greater than or equal
- == equal, ~= not equal
- Note that, a **single equal** '=' is used in **assignments** (a=3), while a **double equal** '==' is used in **comparisons** (a==3) ?

- **Logical operators** (are used to combine two or more relations)

- & and
 - | or
 - ~ not
- If the comparison involves matrices or arrays, the comparison is done element by element

Relational and logic operators /2

An example

- ❑ Multiple conditions are combined with a logical operator
- ❑ the statement in the body of the `if` is executed only if the two conditions are simultaneously met
 - the logical operator is the logic AND (&)

```
if ((x>0) & (y~=10))  
    z=y+sqrt(x);  
end
```

- Always use round parentheses to set priority!
- Result after evaluating a condition:
 - 1 (or any value different from 0) ➡ TRUE
 - 0 ➡ FALSE

Scalar functions

- ❑ built-in Matlab functions operating on **scalars**
- ❑ If applied to a **matrix** (or **vector**), they operate **element-wise** and produce a **matrix** (or **vector**) containing the result of the application of the function to the elements of the matrix
 - sine `sin(x)`, cosine `cos(x)`, ...
 - exponential base e `exp(x)`
 - natural logarithm `log(x)`
 - absolute value `abs(x)`
 - **Example:** square root `sqrt(x)`
 - `sqrt(4)` returns 2
 - `sqrt(A)`, with `A=[4 16 9 4]`, returns 2 4 3 2

Array functions /1

- ❑ built-in Matlab functions operating on **arrays** (row array or column array)
- ❑ If applied to a **matrix**, they operate column by column and produce a row array containing the result of the application of the function to the columns of the matrix
 - Matlab operates by working on columns
- ❑ `max(x)`, `min(x)`, `sum(x)`, `prod(x)`, `mean(x)`, `std(x)` . . .
 - the behavior changes when applied to matrices or vectors

Array functions /2

- ❑ $\text{sum}(A)$ calculates the **sum** of elements
 - If A is a **vector**, $\text{sum}(A)$ gives a **scalar** of value equal to the sum of the elements of the vector, if $A=[1\ 2\ 3]$, $\text{sum}(A)=6$
 - If A is a **matrix**, $\text{sum}(A)$ gives a **vector** containing the sum by columns of the elements of the matrix, if $A=[1\ 2\ 3; 4\ 5\ 6]$, $\text{sum}(A)=[5\ 7\ 9]$
- ❑ $\text{mean}(A)$, $\text{prod}(A)$
 - they compute **arithmetic mean** and **product** of a vector or a matrix in the same manner
- ❑ $\text{max}(A)$, $\text{min}(A)$ extract the **maximum** and **minimum** value among elements
 - If A is a **vector**, $\text{max}(A)$ extracts the maximum element in A (a **scalar**)
 - If A is a **matrix**, $\text{max}(A)$ gives a **vector** containing the maximum values extracted by columns of matrix A

Other useful functions

❑ Rounding functions

- `round(x)` rounds the value x to the nearest integer
- `floor(x)` rounds the value x to the nearest *lower* integer
- `ceil(x)` rounds the value x to the nearest *higher* integer

❑ `size(A)` returns the size of A as a 1x2 row vector containing the number of rows and columns of A

❑ `roots(c)` computes the roots of the n -degree polynomial whose coefficients are given in c

find function

- ❑ The `find` function returns the position of the elements in a matrix that meet a given condition
- ❑ `find(cond)` returns the **indices** of the elements which satisfy the condition `cond` on the specified array
- ❑ Behaviours of the `find` function:
 - `r=find(A>0)` finds the **linear indices** of positive elements in A (we assign the result to a single variable r)
 - `[i,j]=find(A>0)` finds the **row and column indices** of positive elements in A (we assign the result to a couple of variables i and j)

$$A = \begin{pmatrix} -1 & -2 & -3 \\ -4 & -5 & -6 \\ -7 & 8 & 9 \end{pmatrix}$$

$r = 6 \ 9$ (linear indexes)

$i = 3 \ 3$ (row indexes)

$j = 2 \ 3$ (column indexes)

M-files - file.m

- ❑ M-files are files containing source code written in the Matlab language
- ❑ They have extension .m
- ❑ Two kinds of M-files exist:
 - Script file
 - Function file

Script file

❑ Script file

- consists of a sequence of statements without any initial declaration
- can be executed by entering its name (the name of the script file) in the *Command window*
- its invocation produces the execution of the statements
 - Invoking a script is the same as writing directly the statements of the script into the *Command Window*!
- Variables in the script are **global** (visible outside the script)
- does not return output arguments and does not accept input arguments

Function file

□ Function file

- An initial declaration is required
 - the declaration starts with the keyword `function`
 - the declaration contains the function name, the input arguments and the output arguments
 - `function f= function_name(var1, var2)`
 - `function [a,b,c]= function_name(var1, var2)`
- can be called from other functions or scripts
- Variables in the function are **local** (except if the **global** scope is defined)
- The name given to the function must match the function file name !

User-defined function 'sum3numbers'

```
function f = sum3numbers(a,b,c)
    if nargin < 3,
        return;
    end
    f = a+b+c;
end
```

Diagram labels and arrows:

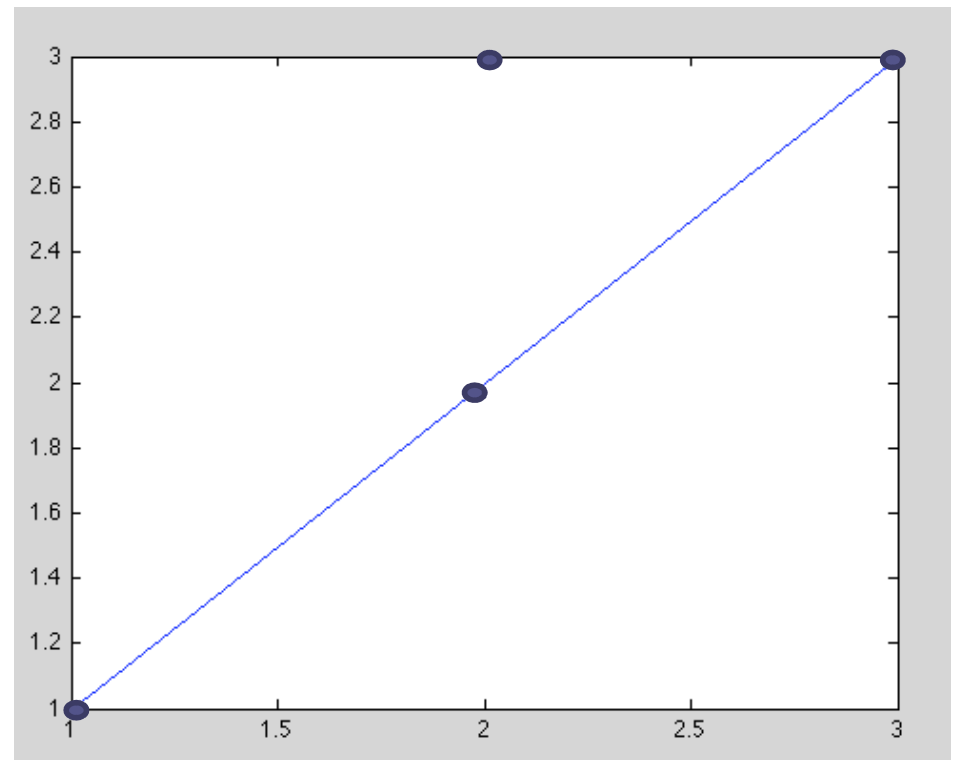
- Output variable** (blue box) points to `f` in the function definition.
- Function name** (yellow box) points to `sum3numbers` in the function definition.
- Input variables** (blue box) points to `a, b, c` in the function definition.

sum3numbers.m

- ❑ `nargin` = “**number of input arguments**”
- ❑ `return` causes a forced exit from the function if less than three input arguments are specified
- ❑ The name of the file ***must be sum3numbers.m!!!***

Graphics in Matlab / 1

- ❑ The main function is `plot`
- ❑ It creates linear two-dimensional graphics given data points with coordinates (x,y)
 - `plot(2,3)` opens a figure window and draws the **point (2,3)**
 - with possible customization
 - `plot(x,y)` opens a figure window (if no figure windows are already opened) and **draws the points connected with a line** identified by the vectors `x=[1 2 3]` and `y=[1 2 3]`



Graphics in Matlab / 2

- ❑ Change the appearance of the graph components
 - both from the command line and from the GUI (command `plottools`)
 - `plot(x,y,'color_line_marker')` produces a line graph of y versus x and at the same time changes the appearance of the line, by setting a **color**, a **line style** and a **marker symbol** for data

Specifier	Color
r	Red
g	Green
b	Blue
c	Cyan
m	Magenta
y	Yellow
k	Black
w	White

Specifier	Line Style
-	Solid line (default)
--	Dashed line
:	Dotted line
-. .	Dash-dot line

Specifier	Marker Type
+	Plus sign
o	Circle
*	Asterisk
.	Point
x	Cross
'square' or s	Square
'diamond' or d	Diamond
^	Upward-pointing triangle
v	Downward-pointing triangle

Graphics in Matlab / 3

❑ Add information to the graph

❑ Labels

- `xlabel('text on x-axis')` adds a text label on x-axis or y-axis
- `ylabel('text on y-axis')`

❑ Title

- `title('title of the figure')` adds a title to the figure

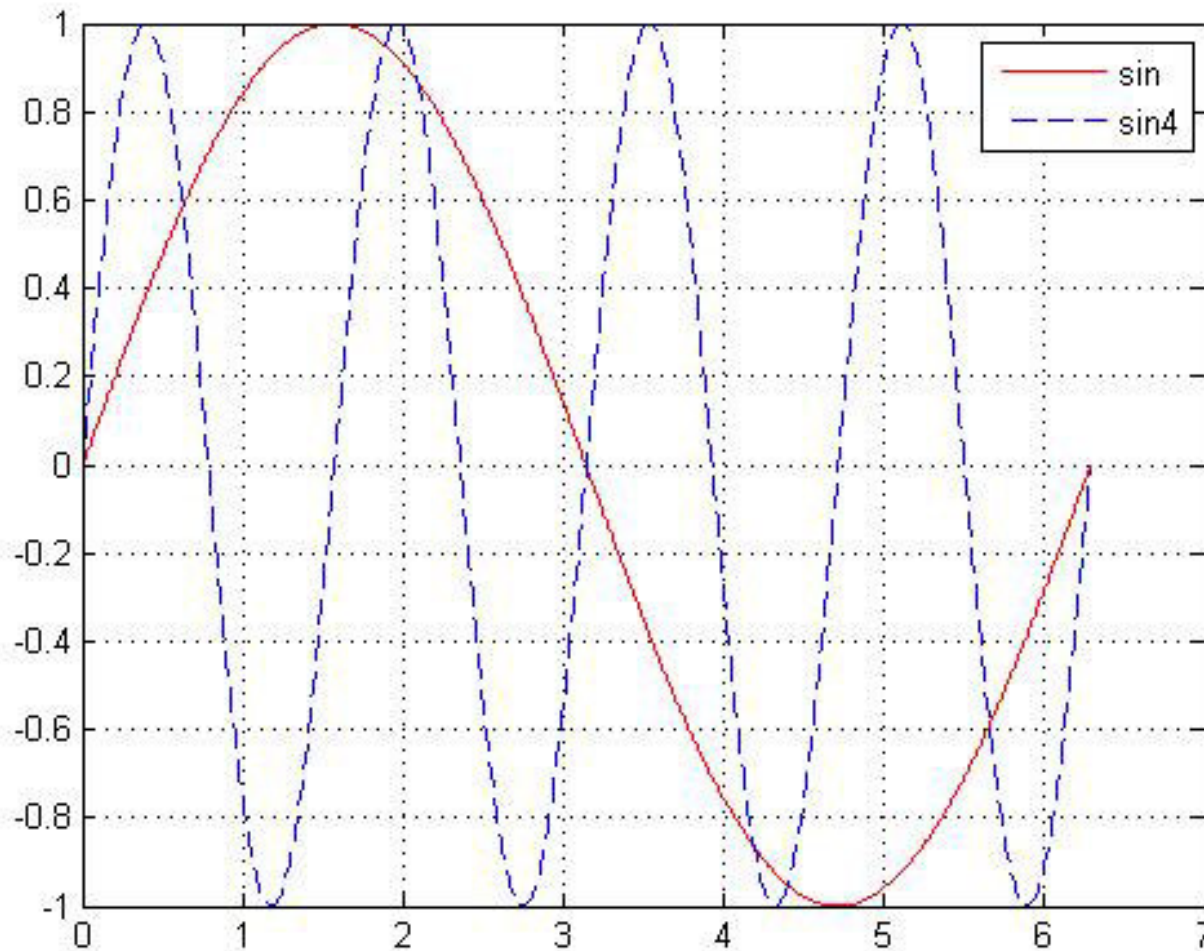
❑ Legend

- `legend('y versus x')` inserts a legend on the figure

Plot of the sine function /1

- ❑ `x=0:.01:2*pi` ; creates a vector of abscissa values ranging from 0 to 2π
- ❑ `y1=sin(x)` ; computes the sine values of x
- ❑ `plot(x,y1,'r-')` ; plots the function with a red (r) continuous (-) line and no marker specified
- ❑ `hold on` allows to add plots on the same figure, by holding the current figure, without replacing the previous plots
- ❑ `y2=sin(4*x)` ; computes the sine values of $4x$
- ❑ `plot(x,y2,'b--')` ; plots the function with a blue (b) dashed (--) line and no marker specified
- ❑ `grid on` shows a grid on the figure
- ❑ `legend('sin', 'sin4')` ; sets the legend

Plot of the sine function /2



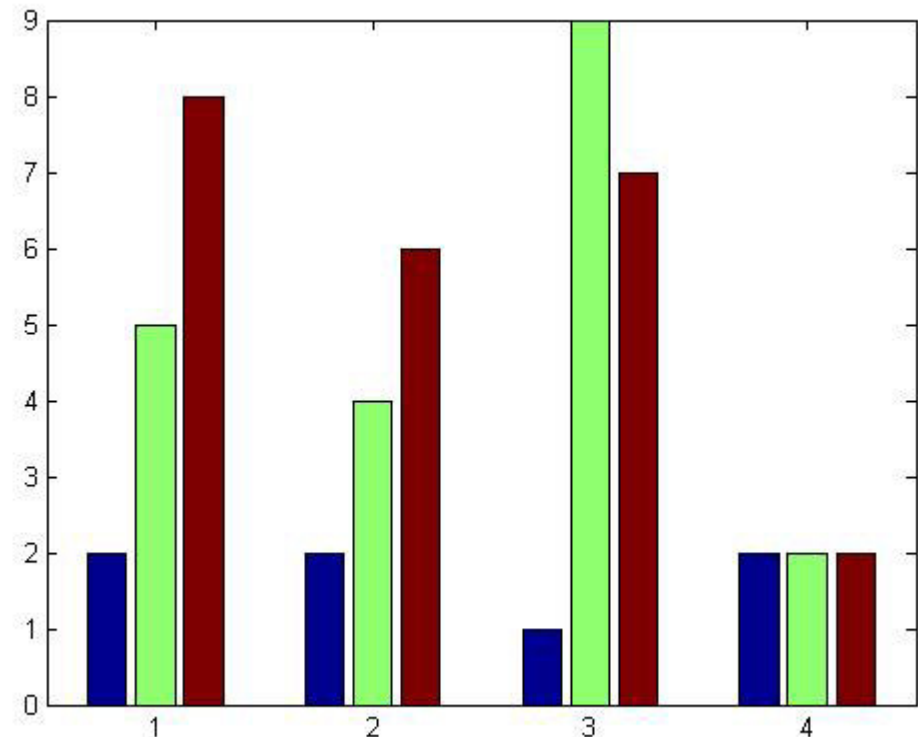
Bar diagrams

- ❑ Bar diagrams are used when we have groups of values to compare
- ❑ A bar graph displays the values in a matrix as vertical bars
- ❑ `bar(y)` builds the bar diagram of the values in `y`
- ❑ if `y` is a matrix 4x3, `bar` draws 4 groups of 3 bars each
 - on the abscissa is the index of the group

exams

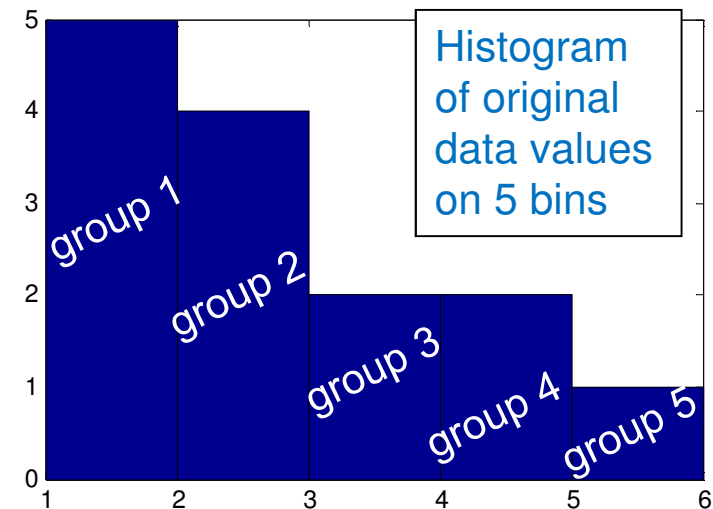
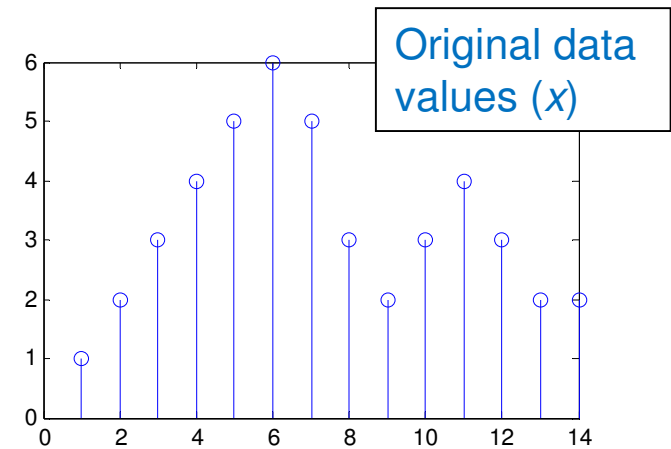
	blue	green	red	
$y =$	[2	5	8;	<i>student 1</i>
	2	4	6;	<i>student 2</i>
	1	9	7;	<i>student 3</i>
	2	2	2]	<i>student 4</i>

compare the marks of 4 students in 3 exams



Histograms /1

- ❑ Often is useful to consider groups (classes) on data
- ❑ A histogram shows the distribution in classes of the values of a variable
- ❑ `hist(x, c)` without output arguments
 - produces the histogram plot of the grouped data
 - groups the data x into:
 - c equally spaced bins, if c is a scalar
 - n bins having central values given in c , if c is a vector of length n
 - if c is omitted the default value is 10 bins



- `hist(x, 5)`
- 5 groupes of values (on the abscissa)
- on the ordinate are the **frequencies** (how many values fall in each class)

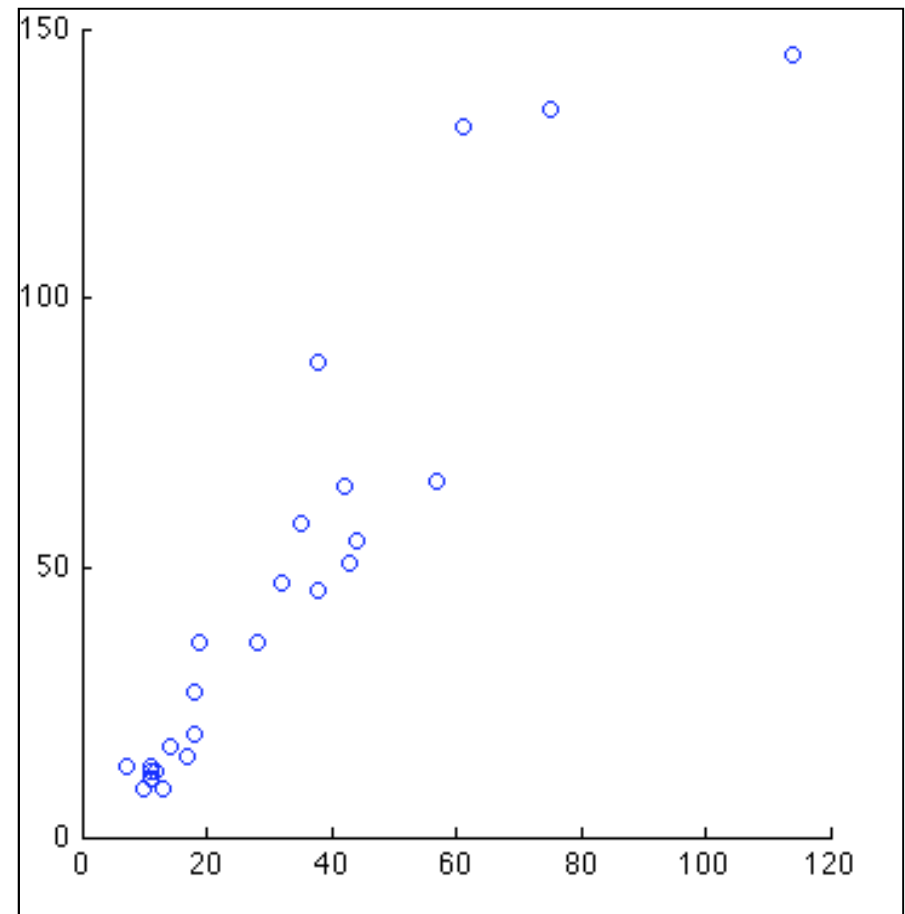
Histograms /2

□ `[f, r]=hist(x, c)` with two output arguments

- groups the data x as specified before
- returns the number f of elements in each bin (frequency) and the central value r of each class
- no histogram plot is produced this time!

Scatter plot

- ❑ A scatter plot displays a set of data as a collection of points represented by two variables
- ❑ `scatter(x, y)` displays the data (x, y) as a collection of single points
- ❑ Scatter diagrams are useful to show the kind of correlation existing between two variables x and y



Missing data /1

- ❑ When working with series of data we may find inconsistent data (special characters or missing values) due to:
 - ❑ black-out of the sensor
 - ❑ errors in the transfer or in the import of data
 - ❑ processing errors (such as division by 0)
- ❑ Matlab represents missing data or inconsistent data using the character **NaN** (**N**ot **a** **N**umber)
- ❑ **NaN** are not ignored in Matlab and may produce processing errors!

Missing data /2

□ How to identify missing data

- `isnan(x)` if applied to a matrix, shows which elements of `x` are NaN elements (value 1 means true)
- `f=find(isnan(x))` returns the indices that satisfy the condition on NaN values in `x`

□ How to solve missing data

- Several solutions are available:
 - `x(f)=val` replacement of the NaN value with the correct value `val` if it is known
 - `x(f)=[]` removal of the missing value
 - interpolation of the missing value

Outliers

- ❑ Outliers are values that deeply differ from the other values in the rest of data and can distort the analysis of data:
 - a measurement error or processing error
 - a real (actually significant) data but anomalous (due to an extraordinary event)
- ❑ How to identify outliers (in data having normal distribution)
 - *rule of thumb*: potential *outliers* are the data far away from the mean M for more than 3 times the standard deviation s
 - $\text{abs}(\text{data} - M) > 3 * s$

Other useful commands /1

- ❑ `who` lists the variables currently defined in the *Workspace*
- ❑ `whos variable_name` shows only the informations about the specified variable
- ❑ `clear` removes all the variables from the *Workspace*
- ❑ `clear variable_name` removes only the specified variable
- ❑ `clc` clears the *Command Window*

Other useful commands /2

- ❑ `disp('a text')` displays the text string between quotes
- ❑ Anything following a percent sign **%** is ignored as it is seen as a comment
 - **% this is a comment**
- ❑ File system-related commands
 - `cd` allows to change the current working directory and to move in the file system
 - `pwd` shows the name of current directory
 - `ls` shows the content of current directory
- ❑ `help function_name` displays information about the command or function specified (syntax and examples of use)
 - The Help is also available in the Help Browser (in the graphical format with `doc function_name`)

Load and save data /1

- ❑ When quitting Matlab all variables defined in the *Workspace* are lost
- ❑ To save or load the *Workspace*, use:
 - `save('mysession.mat')` saves the Workspace in the specified file `mysession.mat` (binary MAT-file)
 - MAT-file Matlab file to store data
 - `save('mysession.mat', p, q)` saves only the specified variables `p` and `q`
 - `load('mysession.mat')` loads in the Workspace the content of the specified binary file, restoring the former state of the Workspace
 - the *load* function reads binary files (such as **.mat** files or **.dat** files)
 - the *load* function reads text files (**.txt** files) well organized as a rectangular regular table of numbers

Load and save data /2

- ❑ To load data from external files

- ❑ Excel files

- `[txt, num]=xlsread('filename.xls')` reads data from an Excel file and puts data in `num` and textual data in `txt`
- `xlswrite('filename.xls', A)` writes data (contained in matrix `A`) in the specified Excel file

- ❑ Comma-separated-value files

- `M=csvread('filename.csv')` reads data from an csv file
- `csvwrite('filename.csv', A)` writes data (contained in matrix `A`) in the specified .csv file

- ❑ for more complex data structure, use the **Import... tool**