

Yu Qian Ang

LO4.1 Design Space Exploration

DSE Basics

Random Search

Grid Search

L04.2 Optimization

Basics

Paper Plane Design of Experiment

Genetic Algorithm

L04.3 Beyond Form

Rhino | Grasshopper

Galapagos

Nano Banana

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"if you want to have good ideas, you must have lots of ideas and learn to throw away the bad ones"

- Linus Pauling -

Design Space Exploration

Design space exploration (DSE) is the systematic process of analyzing and evaluating a wide range of possible design alternatives to identify solutions that best meet specific requirements, such as performance, cost, and other parameters

DSE involves generating and examining different design options and systematically narrowing these down based on set criteria or optimization goals.

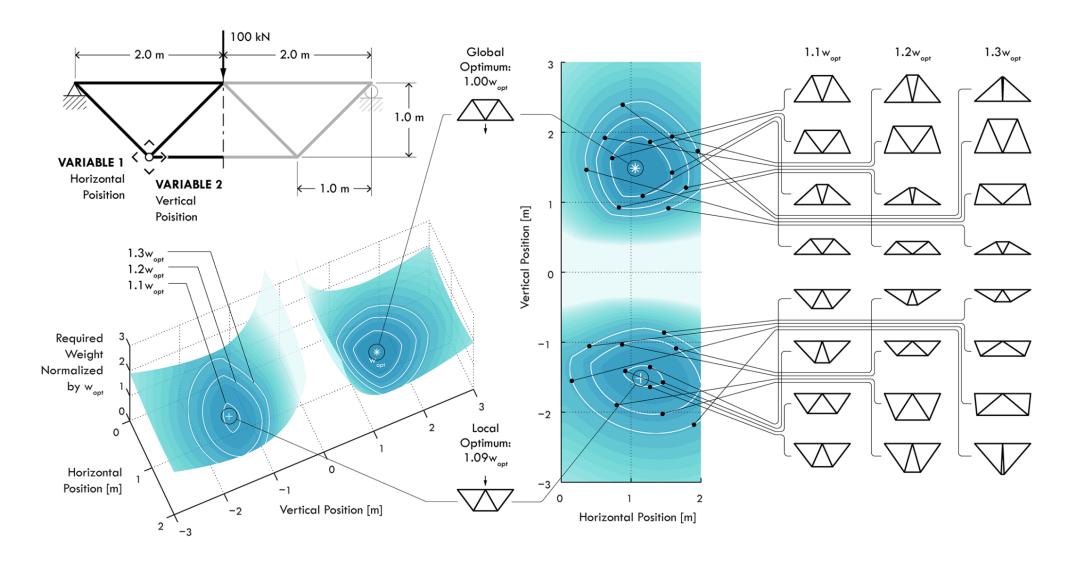
Why is Design Space Exploration important?

Early Stage Optimization: allows for optimization and adjustments before implementation, reducing costly changes later in the process.

Handling Complexity: helps manage the complexity brought by numerous design choices and requirements, making it critical for large systems with millions or billions of possible configurations.

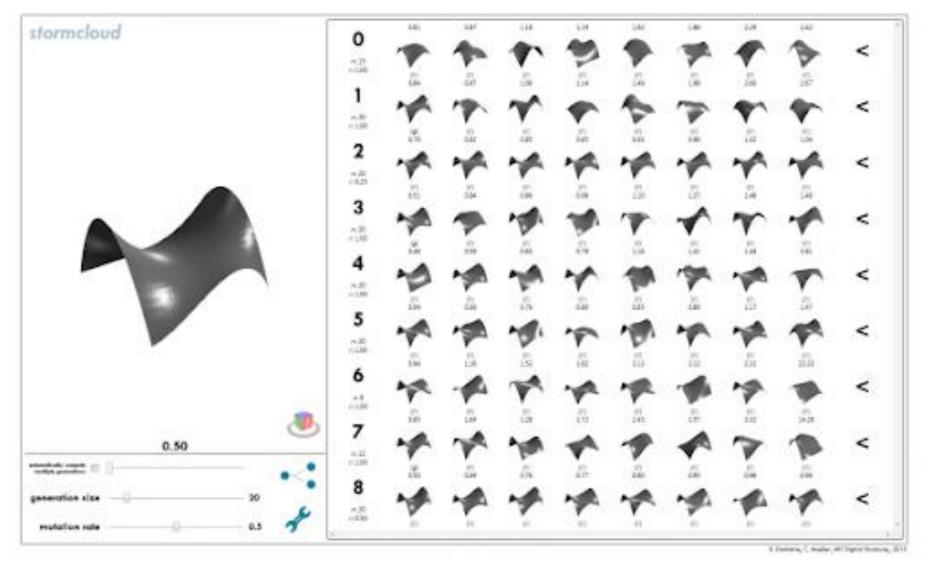
Tradeoff Analysis: By considering multiple objectives, such as performance vs. power consumption, DSE supports multi-objective decision-making and innovation

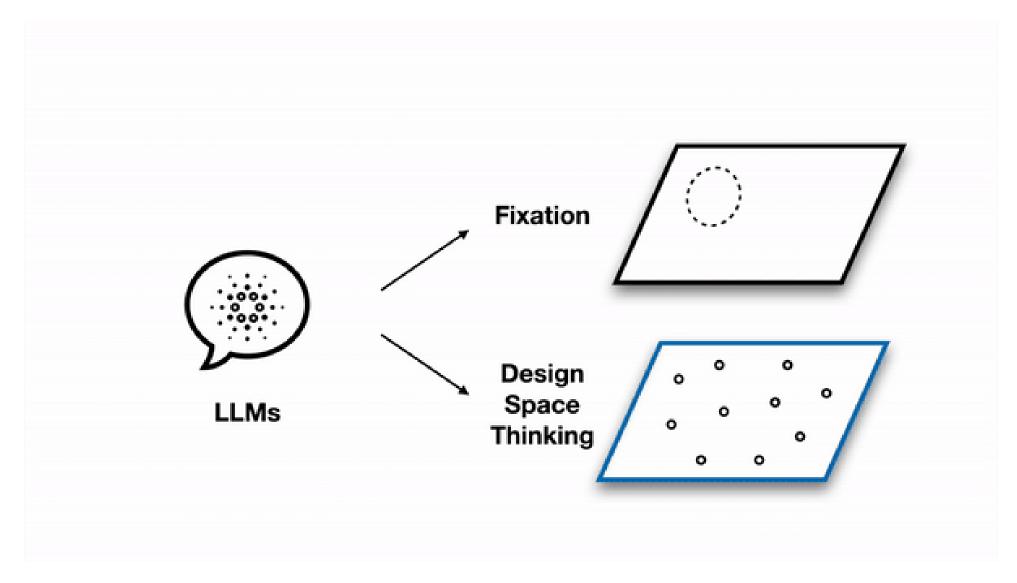
Applicable in many domains, especially sustainable building design



Source: Professor Caitlin Mueller, MIT

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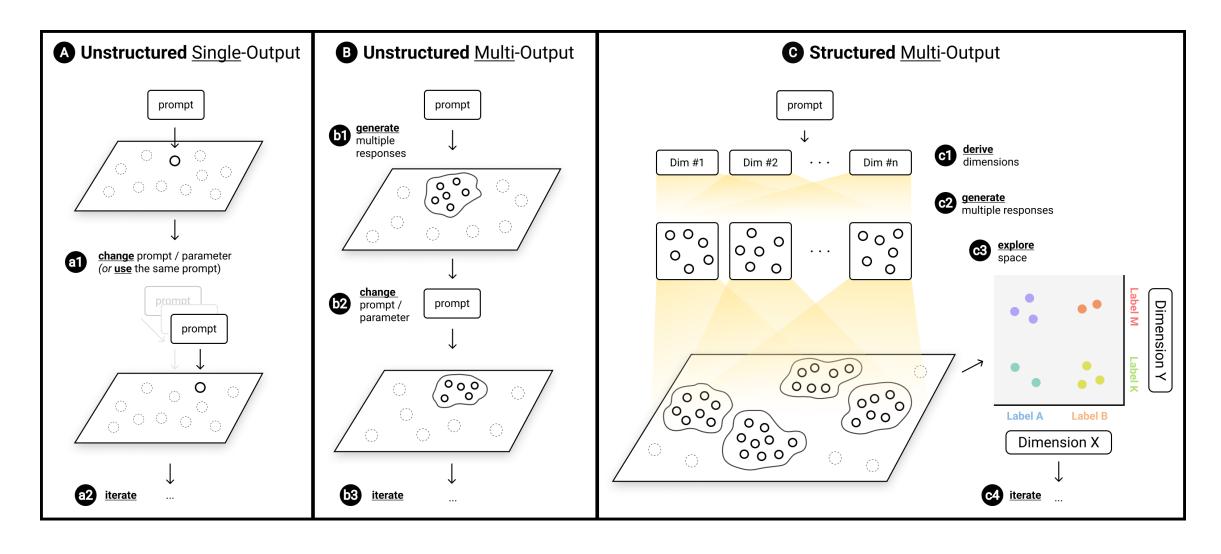


Source: Suh, et al. (2024). Luminate: Structured Generation and Exploration of Design Space with Large Language Models for Human-AI Co-Creation

DESIGN SPACE

SUPERVISE 2

DESIGN SPACE

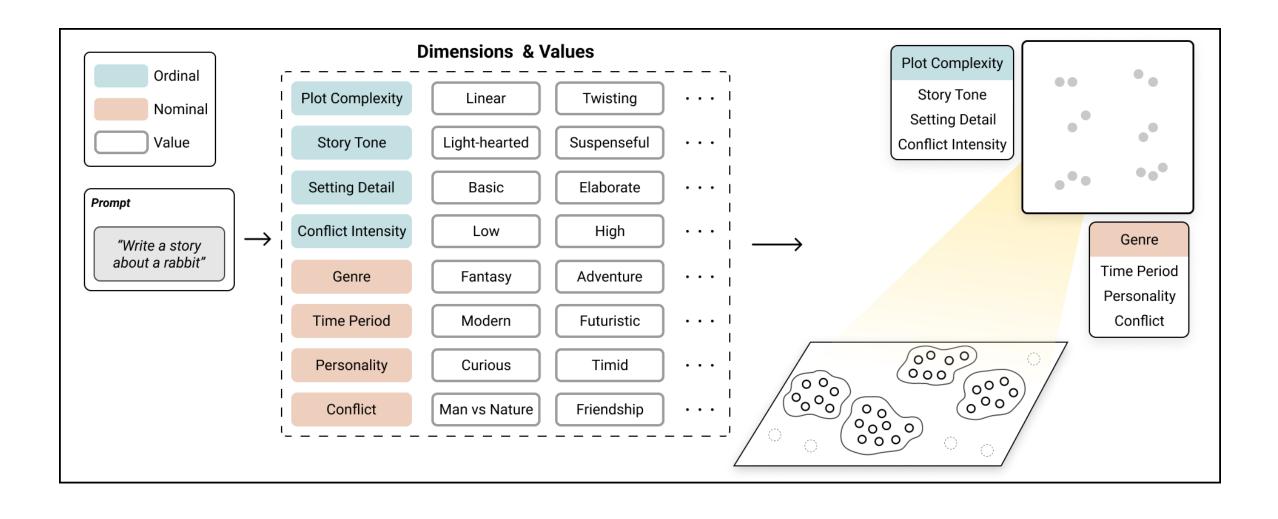


Source: Suh, et al. (2024). Luminate: Structured Generation and Exploration of Design Space with Large Language Models for Human-AI Co-Creation

DESIGN SPACE

SUPERUTSE 2

DESTRN SPACE



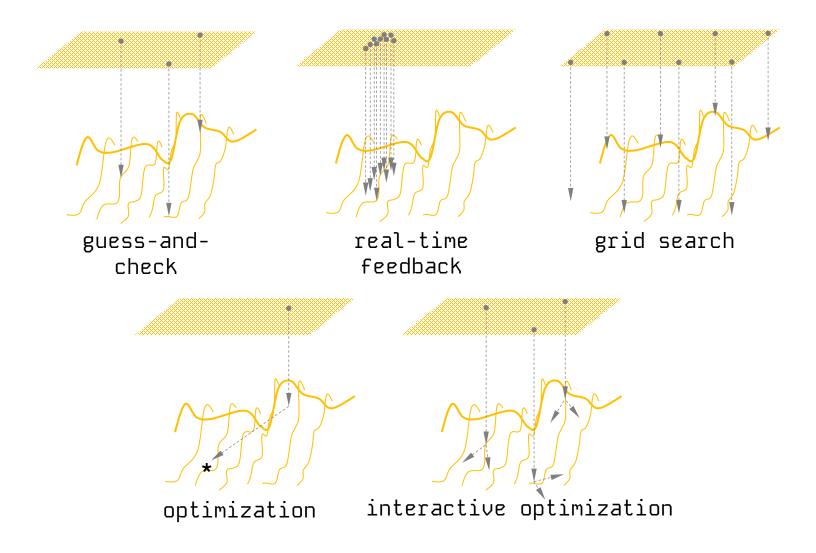
Source: Suh, et al. (2024). Luminate: Structured Generation and Exploration of Design Space with Large Language Models for Human-AI Co-Creation

DESIGN SPACE

Yu Qian Ang

SUPERVISE 2

DESTRN SPACE



Google Colab bit.ly/BPS5231-L4



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Here are 5 verified passes (rounded values):
```

WWR 0.183, Shading 0.021 m, Insulation 0.872, Orientation 94.3° → EUI 118.25, Daylight 55.1, TDH 14.6 h/yr, Cost 99.1

WWR 0.190, Shading 0.046 m, Insulation 0.845, Orientation 98.0° → EUI 119.69, Daylight 55.0, TDH 16.1 h/yr, Cost 99.6

WWR 0.183, Shading 0.0048 m, Insulation 0.899, Orientation 84.0° → EUI 117.21, Daylight 55.8, TDH 14.5 h/yr, Cost 100.0

WWR 0.183, Shading 0.0046 m, Insulation 0.887, Orientation 76.4° → EUI 117.74, Daylight 55.5, TDH 15.9 h/yr, Cost 99.0

WWR 0.197, Shading 0.0018 m, Insulation 0.877, Orientation 66.8° → EUI 119.21, Daylight 56.7, TDH 18.6 h/yr, Cost 99.2

Possible ways to steer your sliders to a pass

Keep WWR low ~ 0.18–0.20 to control cost and TDH while still scraping into daylight ≥55.

Insulation high ~ 0.85-0.90 to drag EUI below 120 (this eats cost, so compensate elsewhere).

Shading almost zero (≈ 0 to 0.05 m) — shading helps EUI/TDH, but it kills daylight and adds cost in this toy.

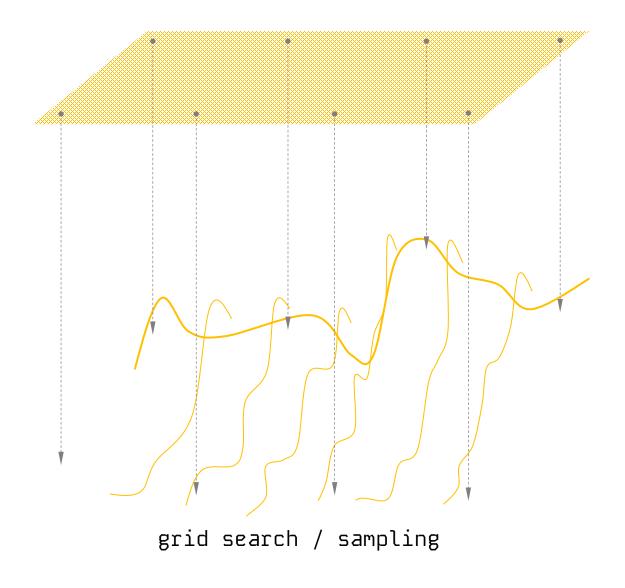
Orientation around 70–100° (roughly E/W-ish) works with the daylight and TDH balance in the surrogate.

If you'd like the feasible region to be less difficult / knife-edge, you can tweak any of these (in the surrogate):

Lower EUI_base slightly (e.g., 145 → 150 currently)

Reduce the cost weight on insulation or shading (e.g., 75.0 insulation → 65.0 insulation)

Ease the daylight lower bound (e.g., 55 → 52)

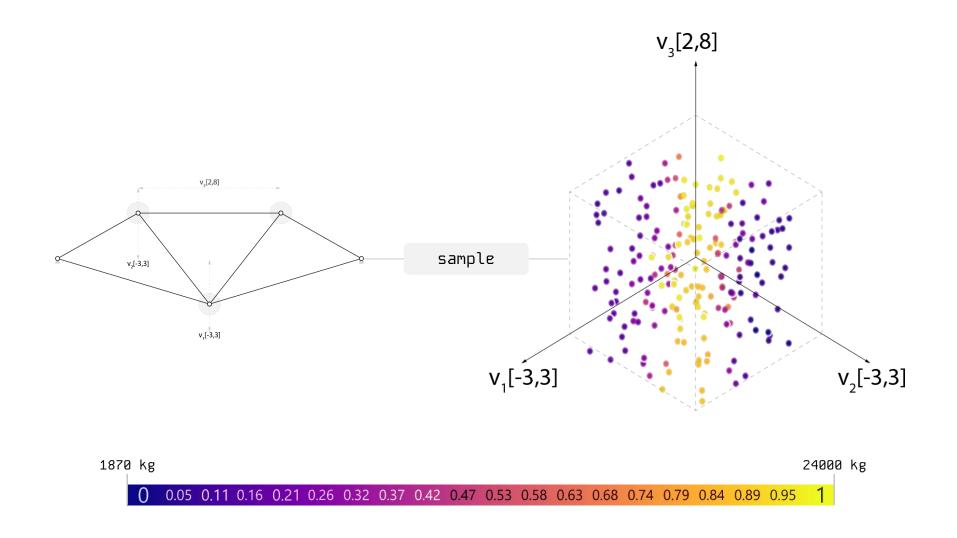


Source: Professor Caitlin Mueller, MIT

DESIGN SPACE

SUPERVISE 2

DESIGN SPACE



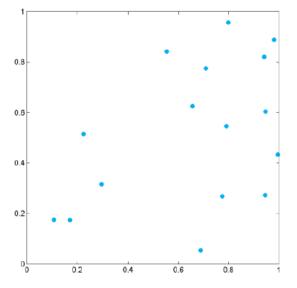
Source: Professor Caitlin Mueller, MIT

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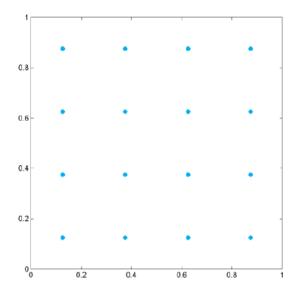
SUPERVISE 2

DESIGN SPACE

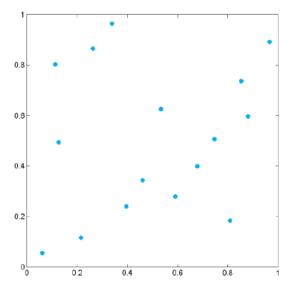
Random / Uniform



Grid



Latin Hypercube



Source: Professor Caitlin Mueller, MIT

DESIGN SPACE

SUPERVISE 2

ESIGN SPACE

Google Colab bit.ly/BPS5231-L4



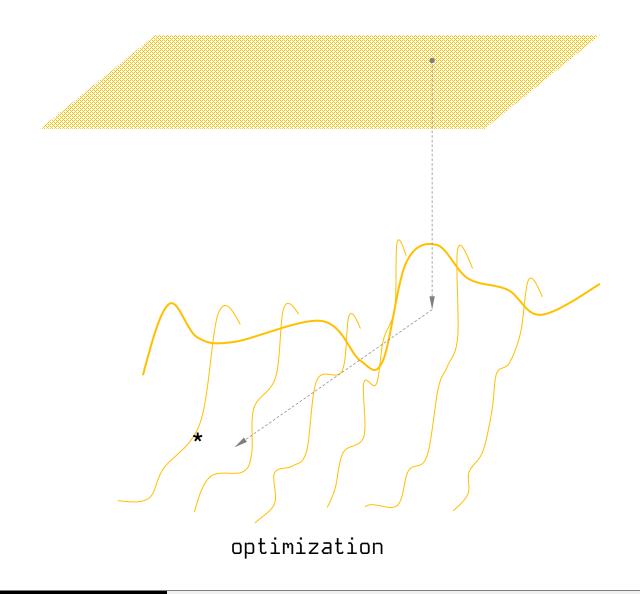
L04.2 Optimization Basics Paper Plane Design of Experiment Genetic Algorithm

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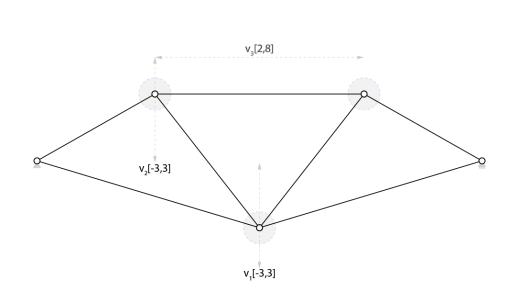


Source: Professor Caitlin Mueller, MIT

ERVISED 1 OPTIMIZATION

DESIGN SPACE

Design Space Exploration (Problem Statement)



Scottish Parliament Miralles, Edinburgh, 2014



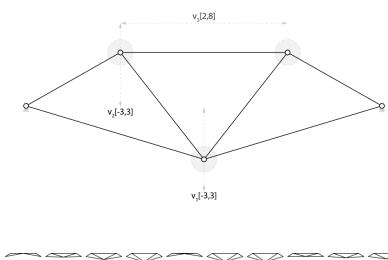
Source: Professor Caitlin Mueller, MIT

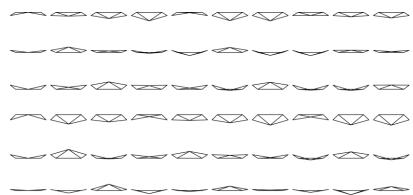
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OPTIMIZATION

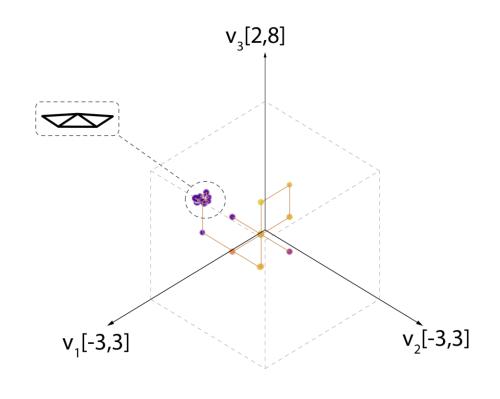
DESIGN SPACE

Design Space Exploration (Problem Statement)





3D Design Space [3 variables, 1 objective]



Weight Optimization

Source: Professor Caitlin Mueller, MIT

PERVISED 1 OPTIMIZATION

DESTAN SPACE

Types of Design Variables

- Continuous:
 e.g., Window-to-wall ratio, shading depth, insulation thickness
- Discrete / Integer:
 e.g., Number of floors, orientation
 (in fixed increments)
- Binary (0/1):
 e.g., "Green roof installed or not"
- Boolean (True/False):
 e.g., "Use natural ventilation?"

Constraints

Comfort thresholds
Regulatory codes
(e.g., max glazing ratio)
Budget / material limits

What are we optimizing?

- Energy Use Intensity (EUI)
- Daylight availability
- Thermal comfort (TDH)
- Cost / Embodied carbon

```
Minimize f_1(x) = Energy Use Intensity (EUI)
Maximize f_3(x) = Daylight availability
Minimize f_2(x) = Cost / Embodied Carbon
Minimize f(x) = Thermal discomfort hours
```

OPTIMIZATION

Optimization Workflow

- 1.Define design variables (controlled by designers)
- 2.Set objectives & constraints (targets: energy, daylight, comfort, cost)
- 3. Search the design space using algorithms
 - Random / grid search
 - Gradient-based optimization
 - Evolutionary / genetic algorithms
 - Multi-objective optimization (Pareto front)
- 4. Select optimal solutions that balance performance + sustainability goals

OPTIMIZATION

objective function

Minimize the building's energy use intensity (EUI) by tuning design variables such as window-to-wall ratio and shading, while ensuring daylight availability and occupant comfort requirements within budget.

constraints

design variables

SUPERVISED

OPTIMIZATION

DESIGN SPACE

Design Experiment

Objective: Maximize Airplane Glide Distance

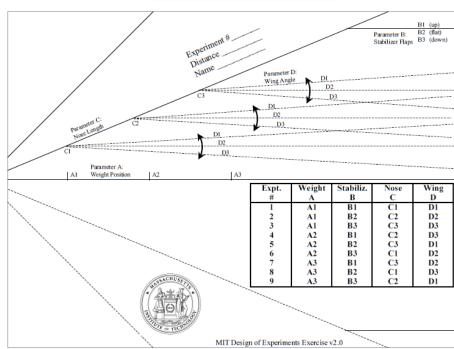
Design variables:

- 1. Weight distribution
- 2. Stabilizer orientation
- 3. Nose length
- 4. Wing angle

Three levels for each design variable

Full factorial design: 34 = 81 experiments





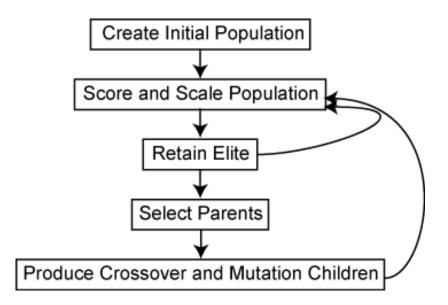
Record your scores:
(choose 3 variable set/experiments)
bit.ly/BPS5231-class

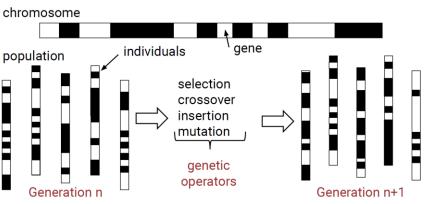


Optimization Approaches

- 1. Gradient-based optimization (gradient descent)
- 2. Evolutionary / genetic algorithms
- 3. Multi-objective optimization

Genetic Algorithm



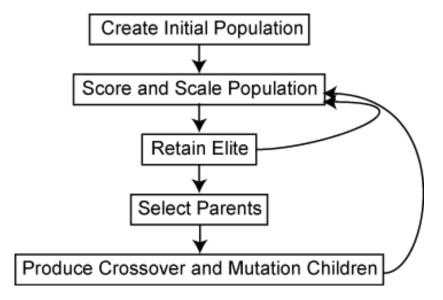


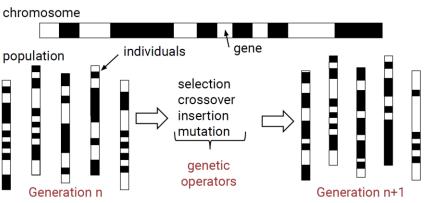
The genetic algorithm is a method for solving both constrained and unconstrained optimization problems that is based on natural selection, the process that drives biological evolution.

The genetic algorithm repeatedly modifies a population of individual solutions. At each step, the genetic algorithm selects individuals from the current population to be parents and uses them to produce the children for the next generation.

Over successive generations, the population "evolves" toward an optimal solution. You can apply the genetic algorithm to solve a variety of optimization problems that are not well suited for standard optimization algorithms, including problems in which the objective function is discontinuous, nondifferentiable, stochastic, or highly nonlinear.

Genetic Algorithm



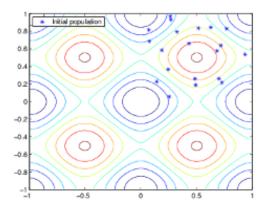


Algorithm flow:

- Initialize a population of random design solutions (e.g., different combinations of WWR, shading, insulation, orientation)
- 2. Evaluate fitness of each design
 (objectives: energy, daylight, comfort, cost)
- 3. Select the fittest designs to "reproduce"
- 4. Crossover combine parts of two designs to form new solutions
- 5. Mutation randomly tweak a variable to introduce diversity
- 6. Repeat until stopping criteria met (e.g., convergence or generations)

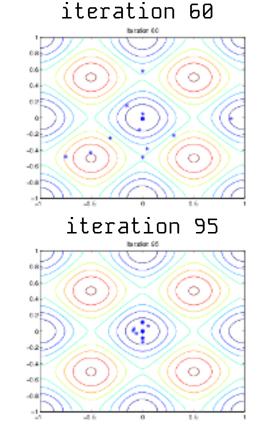
Genetic Algorithm

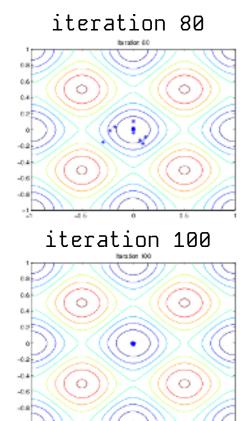
initial population



The algorithm begins by creating a random initial population







The algorithm creates crossover children by combining pairs of parents in the current population, and creates mutation children by randomly changing the genes of individual parents

Further reading: https://www.mathworks.com/help/gads/how-the-genetic-algorithm-works.html

Outline of Genetic Algorithm

- 1. The algorithm begins by creating a random initial population.
- 2. The algorithm then creates a sequence of new populations. At each step, the algorithm uses the individuals in the current generation to create the next population. To create the new population, the algorithm performs the following steps:
- 3. Scores each member of the current population by computing its fitness value. These values are called the raw fitness scores.
- 4. Scales the raw fitness scores to convert them into a more usable range of values. These scaled values are called expectation values.
- 5. Selects members, called parents, based on their expectation.
- 6. Some of the individuals in the current population that have lower fitness are chosen as elite. These elite individuals are passed to the next population.
- 7. Produces children from the parents. Children are produced either by making random changes to a single parent—mutation—or by combining the vector entries of a pair of parents—crossover.
- 8. Replaces the current population with the children to form the next generation.
- 9. The algorithm stops when one of the stopping criteria is met. See Stopping Conditions for the Algorithm.
- 10. The algorithm takes modified steps for linear and integer constraints. See Integer and Linear Constraints.
- 11. The algorithm is further modified for nonlinear constraints. See Nonlinear Constraint Solver Algorithms for Genetic Algorithm.

Read up on other optimization techniques (e.g. particle swarm, simulated annealing)

Multi-objective Optimization

Real-world design problems rarely have just one goal

Example in building design:

Minimize Energy Use Intensity (EUI)

Minimize Cost / Carbon

Maximize Daylight availability

Minimize Thermal discomfort

Trade-offs exist → improving one may worsen another

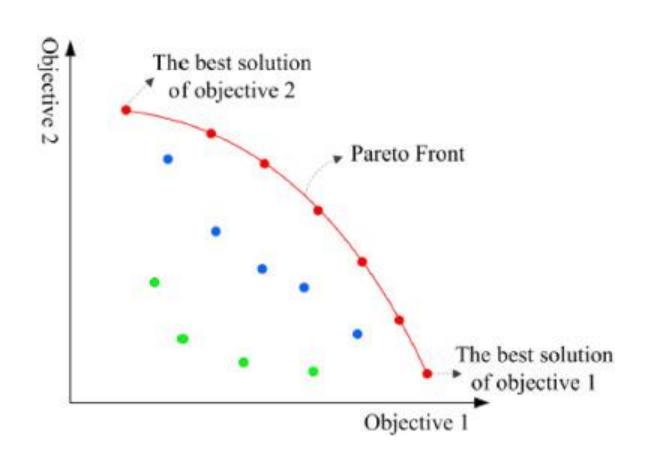
Instead of one "best" solution → we find a set of optimal compromises

Pareto Optimality

Pareto Optimal Solution No other solution is better in all objectives simultaneously

Pareto Front
The set of non-dominated
solutions representing the tradeoff curve/surface

Helps designers see the spectrum of choices and make informed decisions



Source: Stir Welding and Processing, 2014

Pareto Optimality

Each point = a design option (a unique combination of WWR, shading, insulation, etc.).

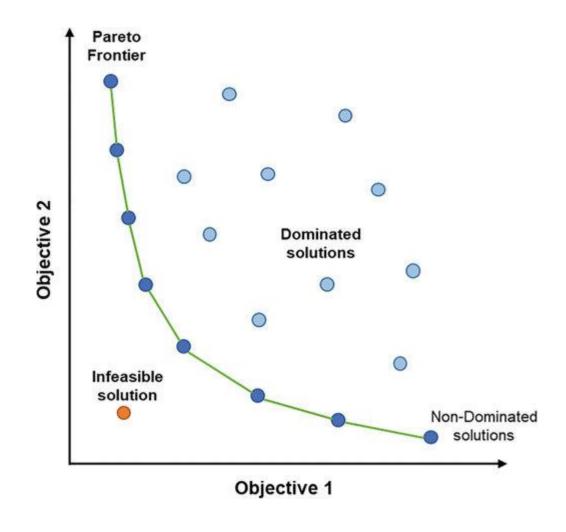
The Pareto front = the set of nondominated designs:

You cannot improve one objective (e.g., lower EUI) without worsening another (e.g., higher cost or less daylight).

The front shows the trade-off boundary of what is achievable.

You can see how improving one objective sacrifices another.

Example: Lowering EUI usually increases cost



Source: Xuhan Liu

Eastport, Maine





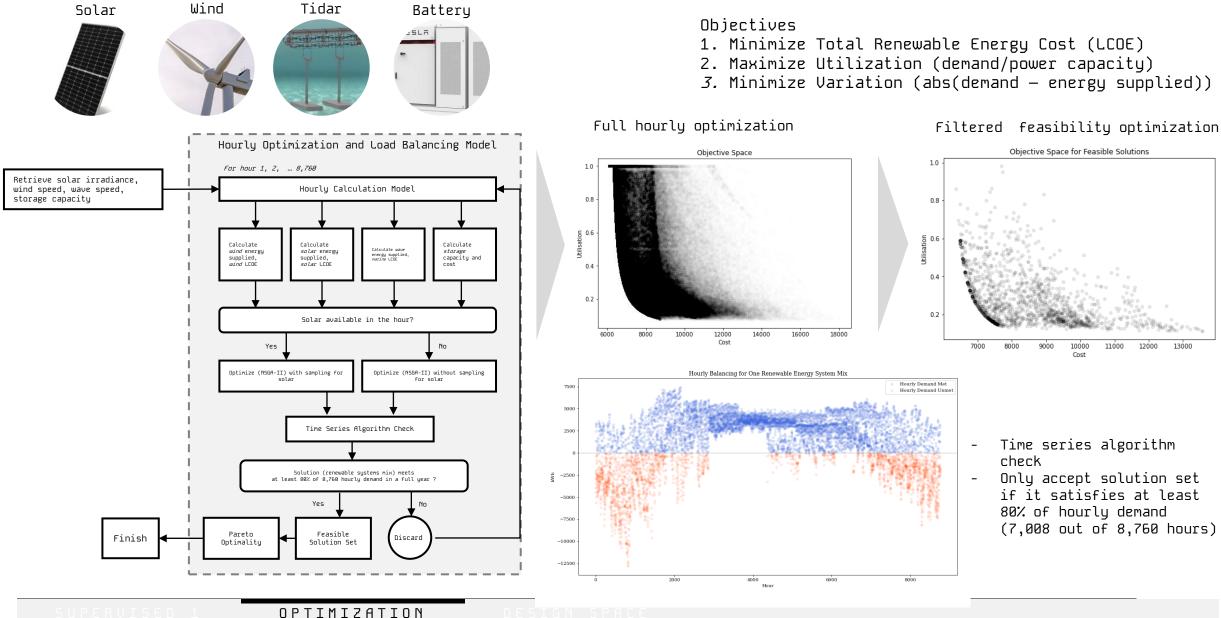
What renewable energy systems mix is feasible for the town?

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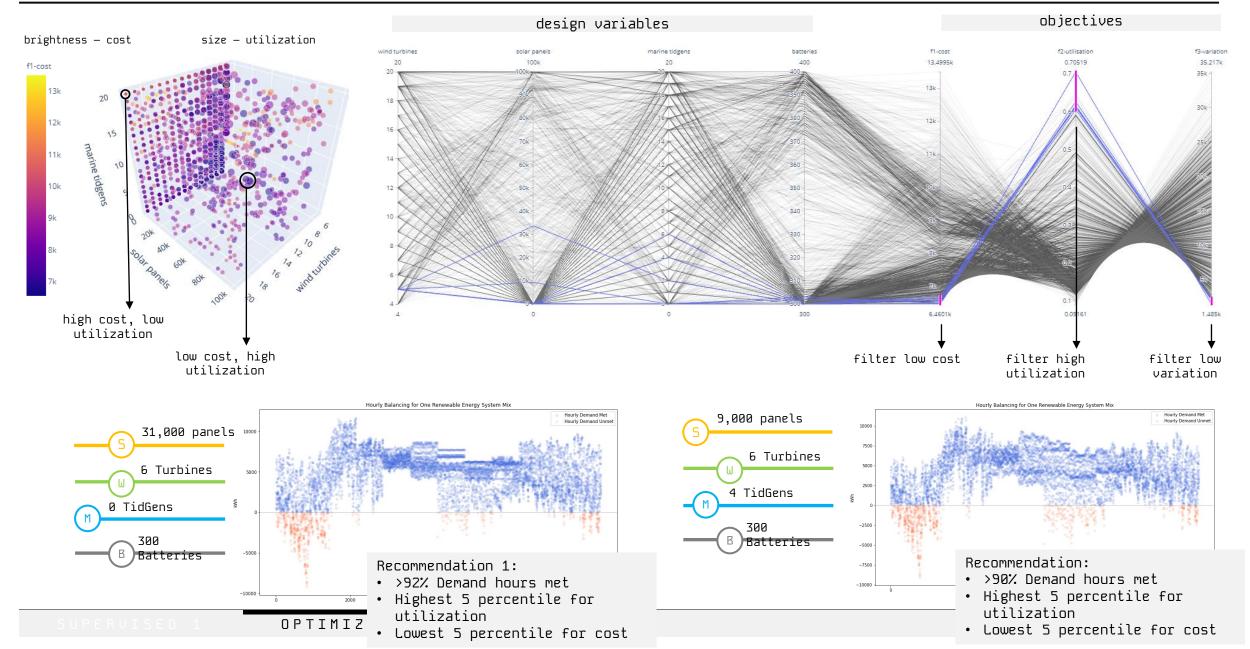
OPTIMIZATION

DESIGN SPACE

Optimization (Multi-Objective Optimization Example)



Optimization (Multi-Objective Optimization Example)

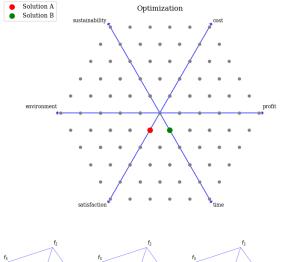


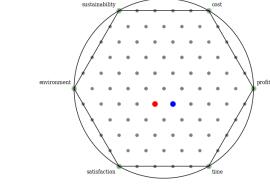
Yu Qian Ang |

Pymoo

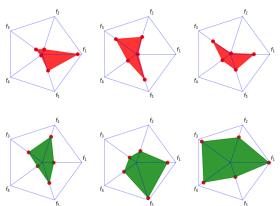


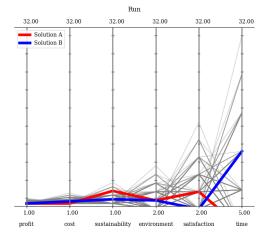
Solution B





Optimization





List Of Algorithms ¶

Algorithm	Class	Objective(s)	Constraints	Description
Genetic Algorithm	GA	single	х	A modular implementation of a genetic algorithm. It can be easily customized with different evolutionary operators and applies to a broad category of problems.
Differential Evolution	DE	single	x	Different variants of differential evolution which is a well-known concept for in continuous optimization especially for global optimization.
Biased Random Key Genetic Algorithm	BRKGA	single	x	Mostly used for combinatorial optimization where instead of custom evolutionary operators the complexity is put into an advanced variable encoding.
Nelder Mead	NelderMead	single	x	A point-by-point based algorithm which keeps track of a simplex with is either extended reflected or shrunk.
Pattern Search	PatternSearch	single	x	Iterative approach where the search direction is estimated by forming a specific exploration pattern around the current best solution.
CMAES	CMAES	single		Well-known model-based algorithm sampling from a dynamically updated normal distribution in each iteration.
Evolutionary Strategy	ES	single		The evolutionary strategy algorithm proposed for real-valued optimization problems.
Stochastic Ranking Evolutionary Strategy	SRES	single	x	An evolutionary strategy with constrained handling using stochastic ranking.
Improved Stochastic Ranking Evolutionary Strategy	ISRES	single	x	An improved version of SRES being able to deal dependent variables efficiently.
NSGA-II	NSGA2	multi	х	Well-known multi-objective optimization algorithm based on non- dominated sorting and crowding.
R-NSGA-II	RNSGA2	multi	x	An extension of NSGA-II where reference/aspiration points can b provided by the user.

OPTIMIZATION

DESIGN SPACE



L04.3 Beyond Form

Rhino | Grasshopper

Galapagos

Nano Banana



bit.ly/BPS5231-L4-Beyondform



