

Aufgabe 1

a) $5 \cdot (a + b + c) = 5a + 5b + 5c$

b) $(6x - 5y + 9z) \cdot (-2x) = -12x^2 + 10xy - 18xz$

c) $5(2a + 4b) + 2(a - b) - 3(2a - 3b)$
 $= 10a + 20b + 2a - 2b - 6a + 9b$
 $= 6a + 27b$

Aufgabe 2

a) $(x + y)^2 = x^2 + 2xy + y^2$

b) $(x + 1)^2 = x^2 + 2x + 1$

c) $(2x - y)^2 = (2x - y)(2x - y)$
 $= 4x^2 - 2xy - 2xy + y^2$
 $= 4x^2 - 4xy + y^2$

d) $(x - y)(x + y) = x^2 - y^2$

1. Binomische Formel

$$(a + b)^2 = a^2 + 2ab + b^2$$

2. Binomische Formel

$$(a - b)^2 = a^2 - 2ab + b^2$$

3. Binomische Formel

$$(a + b)(a - b) = a^2 - b^2$$

Aufgabe 3

a) $16a^2 + 20ab = 16a \cdot a + 20ab = 4 \cdot 4a \cdot a + 5 \cdot 4a \cdot b$
 $= 4a(4a + 5b)$

b) $ab + ab^2 + a^2b = 1 \cdot ab + 1 \cdot ab \cdot b + 1 \cdot ab \cdot a = ab(1 + b + a)$

c) $12x^2 - 12y^2 = 12(x^2 - y^2) = 12 \cdot [(x - y) \cdot (x + y)]$

d) $3a^2 + 6a + 3 = 3(a^2 + 2a + 1) = 3(a + 1)^2$

$$\left[\begin{array}{l} a^2 + 10a + 25 \\ a^2 + 2 \cdot 5a + 5^2 \end{array} \right]$$

$$12xy \left(\frac{x}{y} - \frac{y}{x} \right)$$

Aufgabe 4

a) $5x + 4 = 3x + 10 \quad | -3x; -4$

$$2x = 6 \quad | :2$$

$$\underline{\underline{x = 3}}$$

$$b) 2(x-1) = 3(2-x)$$

$$2x - 2 = 6 - 3x \quad | +3x ; +2$$

$$5x = 8 \quad | :5$$

$$x = \frac{8}{5}$$

$$c) 2ax + 4b = 2b - 4ax \quad | +4ax ; -4b$$

$$6ax = -2b \quad | :6a$$

$$x = \frac{-2b}{6a} = -\frac{b}{3a}$$

Aufgabe 5

$$a) \frac{2a + 2ab}{2a^2b} = \frac{2a}{2a^2b} + \frac{2ab}{2a^2b} = \frac{\cancel{2a}}{\cancel{2a} \cdot ab} + \frac{\cancel{2ab}}{\cancel{2ab} \cdot a} = \frac{1}{ab} + \frac{1}{a}$$

$$\frac{2a + 2ab}{2a^2b} = \frac{2a(1+b)}{2a \cdot ab} = \frac{1+b}{ab} = \frac{1}{ab} + \frac{b}{ab} \quad \text{||}$$

$$b) \frac{24ab + 36ab^2}{12a^2b} = \frac{12ab(2+3b)}{12ab \cdot a} = \frac{2+3b}{a}$$

$$c) \frac{x^2 - 1^2}{x+1} = \frac{(\cancel{x+1})(x-1)}{(\cancel{x+1})} = x-1$$