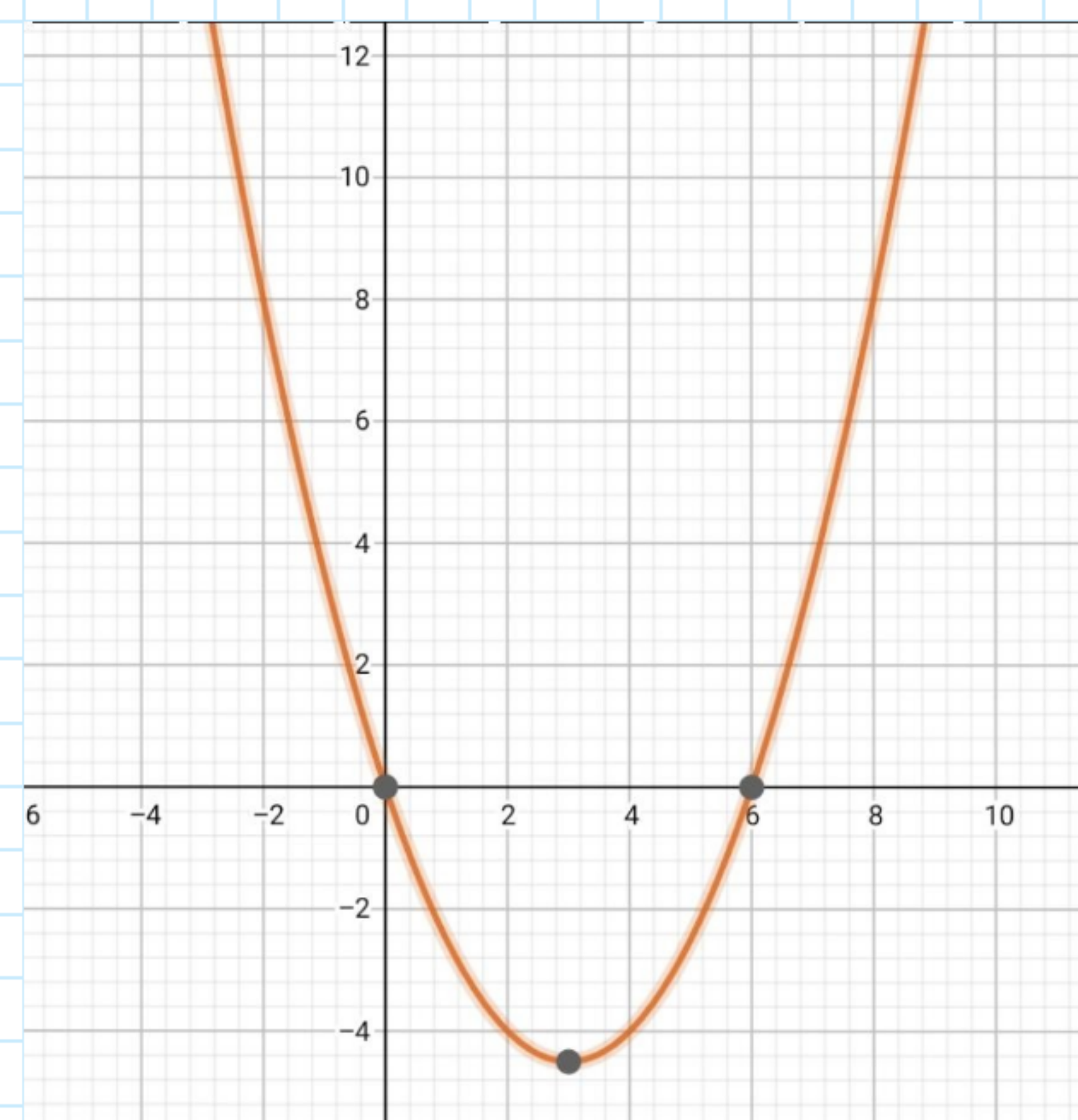


$$a) f(x) = \frac{1}{2}x^2 - 3x$$

$$f(x) = \frac{1}{2}(x^2 - 6x + 0)$$

$$\frac{6}{2} \pm \sqrt{\left(\frac{-6}{2}\right)^2 + 0}$$

$$x_1 = 0 \quad x_2 = 6$$



$$\int_0^6 \left( \frac{1}{2}x^2 - 3x \right) dx \left[ \frac{0.5}{3}x^3 - \frac{3}{2}x^2 + c \right]_0^6$$

$$\frac{0.5}{3} \cdot 6^3 - \frac{3}{2} \cdot 6^2 + c - \left( \frac{0.5}{3} \cdot 0^3 - \frac{3}{2} \cdot 0^2 + c \right)$$

$$(36 - 54) - (0 - 0)$$

$$-18 - 0 = -18 \text{ €}$$

$$c) f(x) = -x^4 + 6x^3 - 9x^2$$

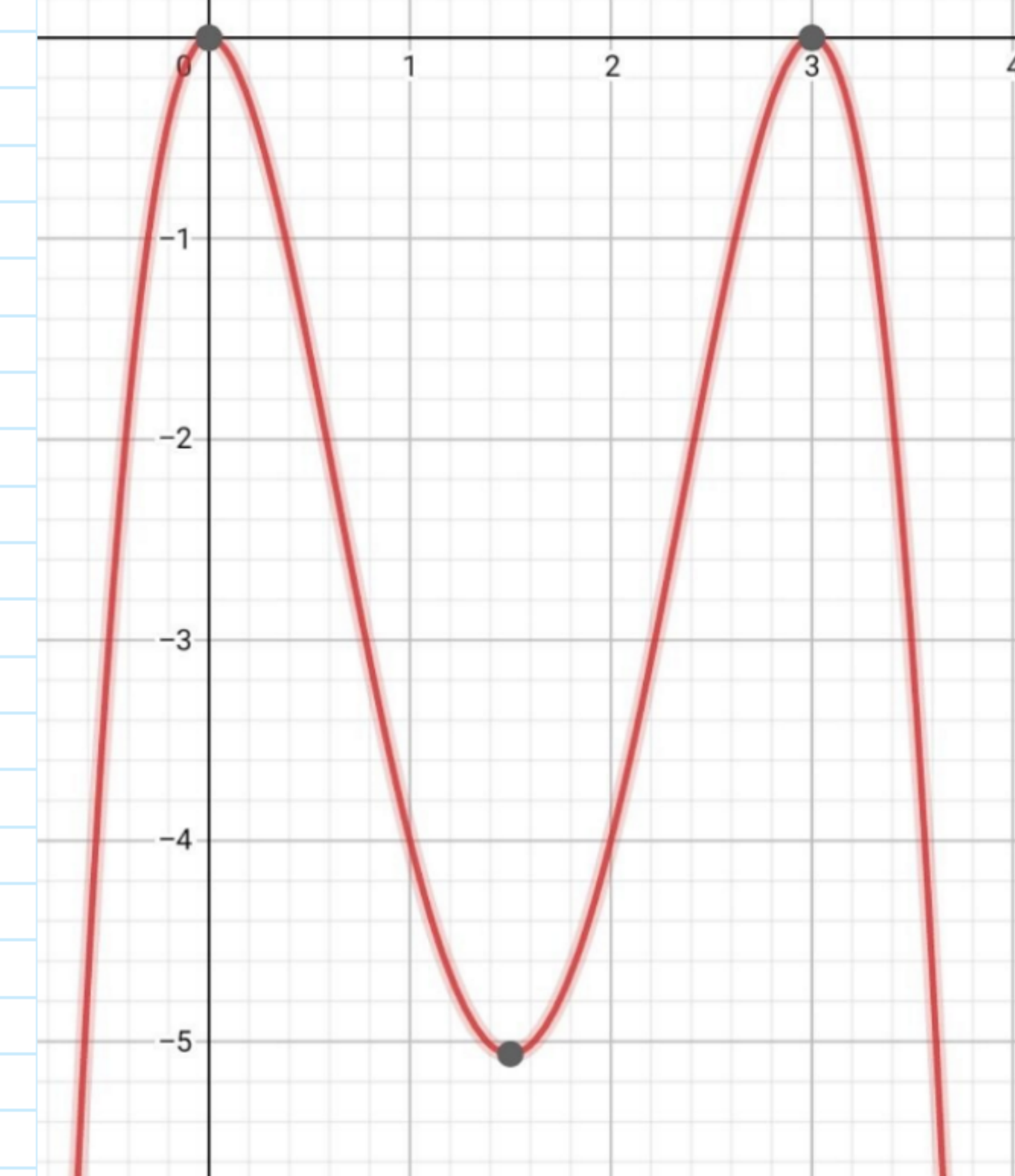
$$f(x) = x^2(-x^2 + 6x - 9) \quad | :(-1)$$

$$f(x) = -x^2(x^2 - 6x + 9)$$

$$\frac{6}{2} \pm \sqrt{\left(\frac{-6}{2}\right)^2 - 9}$$

da eine Nullstelle ergibt 0

$$x_1 = 3 \quad x_2 = 3 \quad x_3 = 0 \quad x_4 = 0$$



$$\int_3^0 (-x^4 + 6x^3 - 9x^2) dx \left[ -\frac{1}{5}x^5 + \frac{6}{4}x^4 - \frac{9}{3}x^3 + c \right]_3^0$$

$$-81 - 0 = -81 \text{ €}$$

$$b) f(x) = \frac{1}{2}x^4 + x^3 \quad | x^3 \text{ ausklammern}$$

$$f(x) = \left( \frac{1}{2}x + 1 \right) \cdot x^3 = 0$$

$$\frac{1}{2}x + 1 = 0 \quad | -1$$

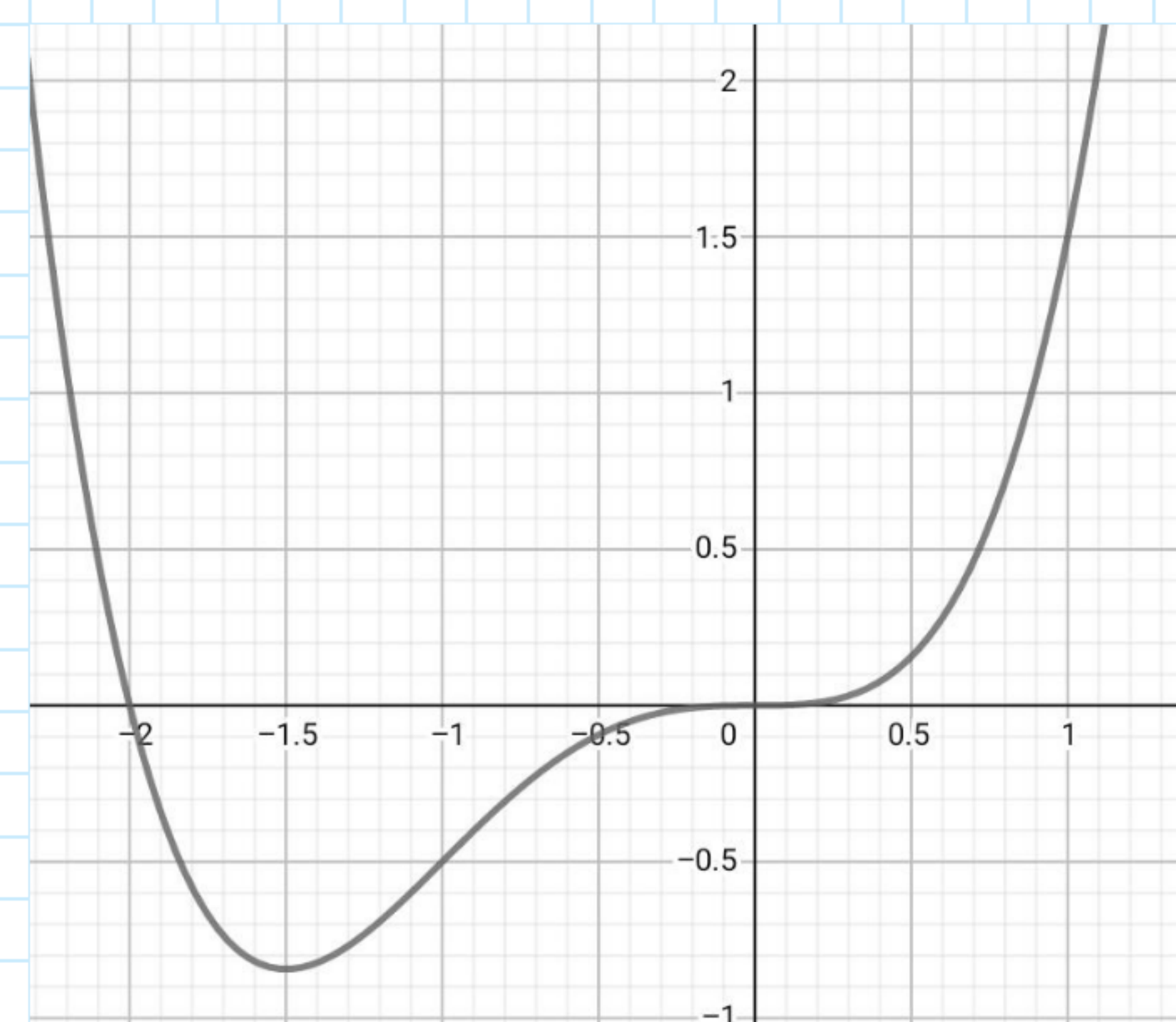
$$\frac{1}{2}x = -1 \quad | : \frac{1}{2}$$

$$x = -2$$

$$x^3 = 0 \quad | \sqrt[3]{\phantom{x}}$$

$$x = 0$$

$$x_1 = 0 \quad x_2 = -2$$



$$\int_0^{-2} \left( \frac{1}{2}x^4 + x^3 \right) dx \left[ \frac{0.5}{5}x^5 + \frac{1}{4}x^4 \right]_0^{-2}$$

$$\left( \frac{0.5}{5} \cdot (-2)^5 + \frac{1}{4} \cdot (-2)^4 \right) - \left( \frac{0.5}{5} \cdot 0^5 + \frac{1}{4} \cdot 0^4 \right)$$

$$(-3.2 + 4) - (0 + 0)$$

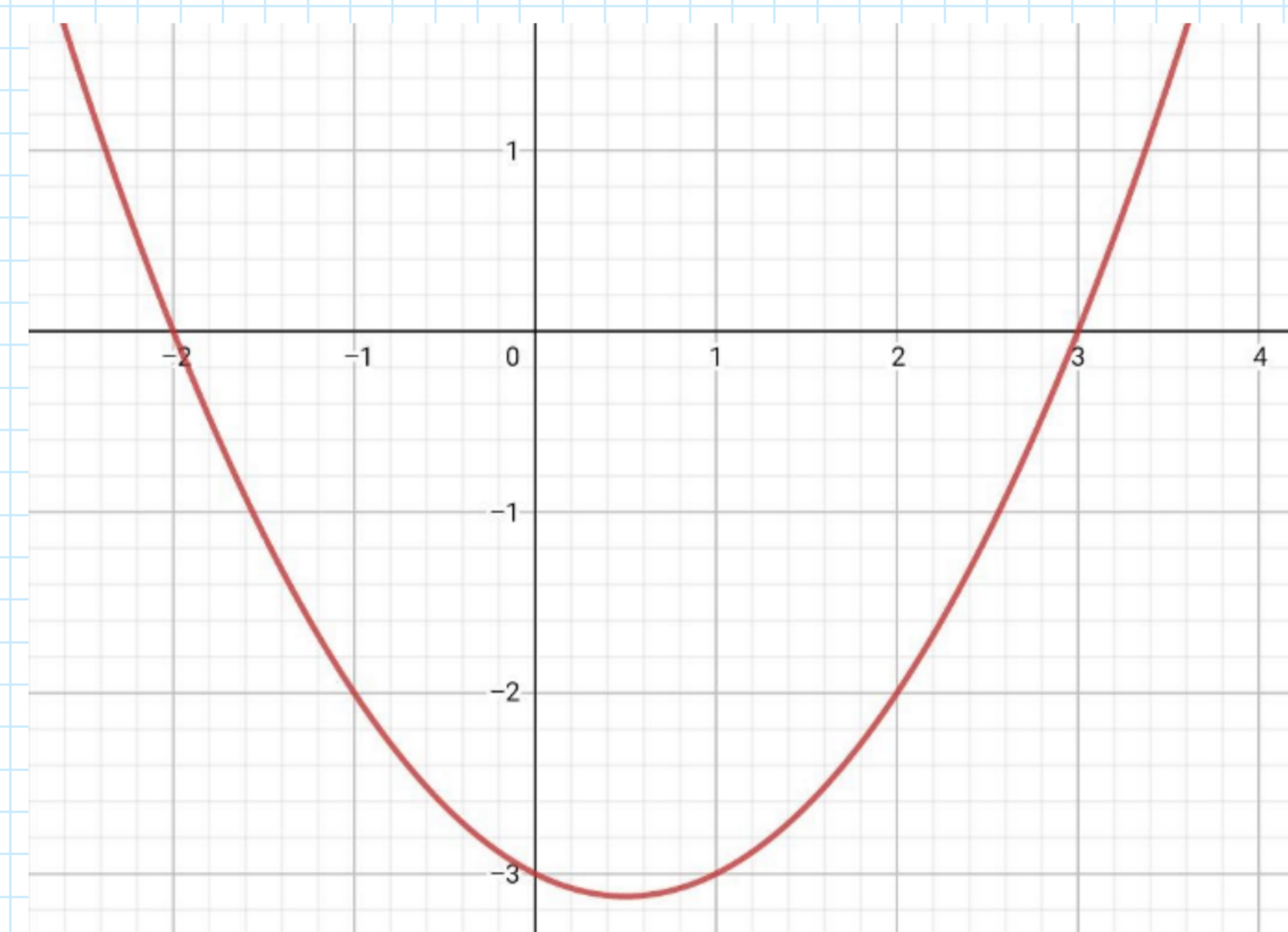
$$\frac{4}{5} - 0 = \frac{4}{5} \text{ €}$$

$$d) f(x) = \frac{1}{2}x^2 - \frac{1}{2}x - 3$$

$$f(x) = \frac{1}{2}(x^2 - x - 6)$$

$$\frac{1}{2} \pm \sqrt{\left(\frac{-1}{2}\right)^2 + 6}$$

$$x_1 = 3 \quad x_2 = -2$$



$$\int_3^{-2} \left( \frac{1}{2}x^2 - \frac{1}{2}x - 3 \right) dx \left[ \frac{0.5}{3}x^3 - \frac{0.5}{2}x^2 - 3x + c \right]_3^{-2}$$

$$\left( \frac{0.5}{3} \cdot (-2)^3 - \frac{0.5}{2} \cdot (-2)^2 - 3 \cdot (-2) + c \right) - \left( \frac{0.5}{3} \cdot (3)^3 - \frac{0.5}{2} \cdot (3)^2 - 3 \cdot (3) + c \right)$$

$$13.17 - (-38.08) = 24.91 \text{ €}$$