

# Faktorisieren (Ausklammern)

$$\begin{aligned} \text{a) } 16a^2 + 20ab &= 4 \cdot 4a \cdot a + 5 \cdot 4a \cdot b \\ &= 4a \cdot (4a + 5b) \end{aligned}$$

$$\begin{aligned} \text{b) } 36ar - 60ab + 24b^2 &= 6(6ar - 10ab + 4b^2) \\ &= 12(3ar - 5ab + 2b^2) \end{aligned}$$

$$\begin{aligned} \text{c) } 25ab^2 - 15a^2b + 30ab &= 5 \cdot 5ab \cdot b - 3 \cdot 5ab \cdot a + 6 \cdot 5ab \\ &= 5ab(5b - 3a + 6) \end{aligned}$$

$$\begin{aligned} \text{d) } 27x + 36 - 15x^2 - 20x &= (3x+4)(9-5x) \\ &= 9(3x+4) - 5x(3x+4) \end{aligned}$$

$$\begin{aligned} \text{e) } 8x - 16x^2 + 12x - 6 &= 8x(1-2x) + (-6)(1-2x) = (1-2x) \cdot (8x-6) \\ 4x(2-4x) + 3(2-4x) &= 4x(2-4x) - 3(2-4x) = (2-4x)(4x-3) \end{aligned}$$

$$\begin{aligned} \text{f) } 4a^2 - 12ab + 9b^2 &= (2a-3b)^2 \\ &= \begin{matrix} 4a^2 & -2 \cdot 6ab & +9b^2 \\ \downarrow & \parallel & \downarrow \\ 2a \cdot 2a & 2 \cdot 3 & 3b \cdot 3b \end{matrix} \end{aligned}$$

$$\begin{aligned} 1: (a+b)^2 &= a^2 + 2ab + b^2 \\ 2: (a-b)^2 &= a^2 - 2ab + b^2 \\ 3: (a+b)(a-b) &= a^2 - b^2 \end{aligned}$$

Lösen von Gleichungen nach x

$$\text{a) } 5x + 4 = 3x + 10 \quad | -3x$$

$$\Leftrightarrow 2x + 4 = 10 \quad | -4$$

$$\Leftrightarrow 2x = 6 \quad | :2$$

$$\Leftrightarrow x = 3$$

$$\text{b) } 2(x-1) = 3(2-x)$$

$$\Leftrightarrow 2x - 2 = 6 - 3x \quad | +3x$$

$$\Leftrightarrow 5x - 2 = 6 \quad | +2$$

$$\Leftrightarrow 5x = 8 \quad | :5$$

$$\Leftrightarrow x = \frac{8}{5}$$

$$\text{c) } 2x - 11 = 6 - 11x \quad | +11x$$

$$c) \quad 2ax + 4b = 2b - 4ax \quad | + 4ax$$

$$6ax + 4b = 2b \quad | - 4b$$

$$6ax = -2b \quad | : 6a$$

$$x = \frac{-2b}{6a} = -\frac{b}{3a}$$