

MA

$$a) f(x) = \frac{1}{2}x^2 - 3x \quad f'(x) = 0$$

$$x(\frac{1}{2}x - 3) = 0 \quad \frac{1}{2}x = 6$$

$$0 = 0,5x - 3 \quad +3$$

$$3 = 0,5x \quad | :0,5$$

$$6 = x$$

$$f'(x) = 0 = x - 3 \quad +3$$

$$3 = x$$

$$f''(3) = 1 > 0 = \text{Minimum}$$

$$\frac{1}{2} \cdot 3^2 - 3 \cdot 3 = -4,5$$

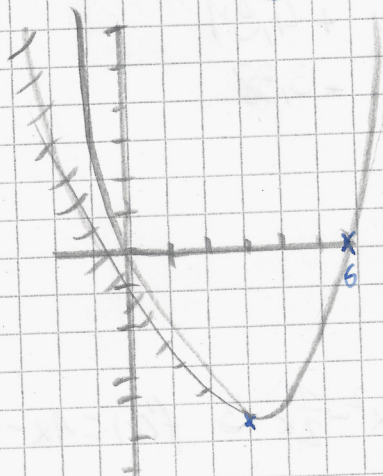
$$TP = [3 | -4,5]$$

$$f'(x) = x - 3 \quad f''(x) = 1$$

$$\frac{1}{6}x^3 - 1,5x^2$$

$$A = \int_0^6 (\frac{1}{2}x^2 - 3x) dx = [\frac{1}{6}x^3 - 1,5x^2]$$

$$\frac{1}{6} \cdot 0^3 - 1,5 \cdot 0^2 - [\frac{1}{6} \cdot 6^3 - 1,5 \cdot 6^2] = -18$$



$$b) f(x) = \frac{1}{2}x^4 + x^3 \quad x_1 = x_2 = 0$$

$$x^3(\frac{1}{2}x + 1) = 0 \quad x_3 = -2$$

$$f'(x) = 2x^3 + 3x^2$$

$$f''(x) = 6x^2 + 6x$$

$$0 = \frac{1}{2}x + 1 \quad +1$$

$$-1 = \frac{1}{2}x \quad | : \frac{1}{2}$$

$$x = -2$$

$$f'(-2) = 2x^3 + 3x^2 = 0$$

$$x^2(2x + 3) = 0$$

$$0 = 2x + 3 \quad -3$$

$$-3 = 2x \quad | :2$$

$$-1,5 = x$$

$$f''(-1,5) = -29,25 < 0 = \text{MAX}$$

$$HOP = -1,51 - 0,84$$

$$f(-1,5) = -0,84$$

$$A = \int$$





$$c) f(x) = -x^4 + 6x^3 - 9x^2 \quad f'(x) = 20x^3 + 18x^2 - 18x$$

$$x^2(-x^2 + 6x - 9)$$

$$\Delta = 36 - 36 = 0$$

$$x = \frac{6 \pm \sqrt{6^2 - 9}}{2}$$

$$\frac{2 \pm \sqrt{18}}{2}$$

$$\frac{2 \pm 3\sqrt{2}}{2} = 1 \pm 2,12$$

$$x_1 = 0$$

$$x_2 = 4,91$$

$$x_3 = -3,58$$

$$A = \int_{-3,58}^{4,91} (-x^4 + 6x^3 - 9x^2) dx = \left[ -\frac{1}{5}x^5 + \frac{3}{2}x^4 - 3x^3 \right]$$

$$-3,58 \quad -\frac{1}{5} \cdot 4,91^5 + \frac{3}{2} \cdot 4,91^4 - 3 \cdot 4,91^3 = (-54)$$

$$- \left( -\frac{1}{5} \cdot (-3,58)^5 + \frac{3}{2} \cdot (-3,58)^4 - 3 \cdot (-3,58)^3 \right) = 50,65$$

$$= -54 - 50,65 = -104,65$$



$$d) f(x) = \frac{1}{2}x^2 - \frac{1}{2}x - 3 \quad f'(x) = 1x - \frac{1}{2}$$

$$f(x) = \frac{1}{2}x^2 - \frac{1}{2}x - 3 \quad | : \frac{1}{2}$$

$$x^2 - x - 6$$

$$x = \frac{1 \pm \sqrt{1^2 + 24}}{2}$$

$$x = \frac{1 \pm 5}{2}$$

$$x = \frac{1+5}{2} = 3$$

$$x = \frac{1-5}{2} = -2$$

$$y_{\text{AAS}} = -3$$

$$F(x) = \frac{1}{6}x^3 - \frac{1}{4}x^2 - 3x$$

$$A = \int_{-2}^3 \left( \frac{1}{2}x^2 - \frac{1}{2}x - 3 \right) dx = \left[ \frac{1}{6}x^3 - \frac{1}{4}x^2 - 3x \right]$$

$$-6,75 - 3,66 = -10,41$$

