

Task 1

Last week you wrote a Fortran program that calculates the mean and standard deviation of a series of real numbers. Now edit the program to calculate these properties for an array. The program should:

- Ask for the number of numbers
- If the entered number is negative, repeatedly ask for a positive number
- Allocate the array
- Read the values into the array
- Calculate the mean and standard deviation of the array
- Display the result

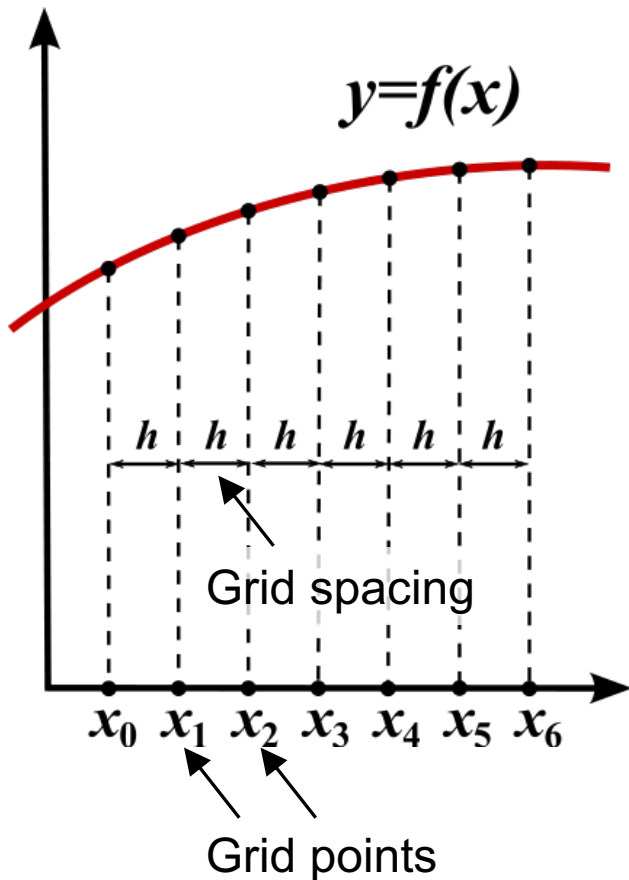
Use as many whole array operations and as few loops as possible.

Task 2

Write a Fortran program that uses the sieve of Eratosthenes to find all prime numbers less than or equal to a given number.

	2	3	4	5	6	7	8	9	10	Prime numbers
11	12	13	14	15	16	17	18	19	20	
21	22	23	24	25	26	27	28	29	30	
31	32	33	34	35	36	37	38	39	40	
41	42	43	44	45	46	47	48	49	50	
51	52	53	54	55	56	57	58	59	60	
61	62	63	64	65	66	67	68	69	70	
71	72	73	74	75	76	77	78	79	80	
81	82	83	84	85	86	87	88	89	90	
91	92	93	94	95	96	97	98	99	100	
101	102	103	104	105	106	107	108	109	110	
111	112	113	114	115	116	117	118	119	120	

Finite differences



First derivative

$$\frac{dy}{dx} = f'(x) = \lim_{dx \rightarrow 0} \frac{f(x + dx) - f(x)}{dx}$$

Computer version of the first derivative

$$\frac{dy}{dx} \approx \frac{\Delta y}{\Delta x} \approx \frac{y_{i+1} - y_i}{x_{i+1} - x_i} = \frac{y_{i+1} - y_i}{h}$$

Computer version of the second derivative

$$\frac{d^2y}{dx^2} \approx \frac{y_{i+1} - 2y_i + y_{i-1}}{h^2}$$

Task 3

Write a Fortran program that computes the second derivative of a 1D array using the finite difference method for a given number of grid points (n) and grid spacing (h).

- The second derivative is calculated at the points $i = 2 \dots n-1$.
- At the boundaries ($i=1$ and n) the derivative is set to 0.
- The result is another 1D array.

Test the program for two idealized functions for which you know the correct result, e.g. $\sin(x)$ or x^2 . Compare the result of your program with the correct result and calculate the error.

Exercise 2

Deadline:

- Please hand in your solutions (.f90 files and results of the two tests) until Tuesday, **19 March 2024, 23:59** at the latest.

Questions?

- Email me (marina.duetsch@univie.ac.at)
Or pass by my office (UZA II, 2G551).