данной нам на лекциях, но yre. ∠yıŝt pc ŝiy> => < 4 | L + guaren L | 4> Заданне 9 ÎÎ => Ît Ît Î S) Â+Â++ A+ Â++ Â++ Â+ Â+ Â+ Â+ Â+ $=\hat{\beta}+\hat{J}=-i\hat{J}+i\hat{\beta}-i(\hat{\beta}+\hat{J})^{\dagger}=-i\hat{J}+i\hat{\beta}-i(\hat{\beta}+i\hat{J})^{\dagger}=-i\hat{J}+i\hat{\beta}-i(\hat{\beta}+i\hat{J})^{\dagger}=-i\hat{J}+i\hat{J}$ $\left\{ \stackrel{\wedge}{A}, \stackrel{\wedge}{B} \right\} = \stackrel{\wedge}{A} \stackrel{\wedge}{B} + \stackrel{\wedge}{B} \stackrel{\wedge}{A} = \stackrel{\wedge}{B} \stackrel{\wedge}{A} + \stackrel{\wedge}{A} \stackrel{+}{B} = \stackrel{\wedge}{B} \stackrel{\wedge}{A} + \stackrel{\wedge}{A} \stackrel{\wedge}{B} = \stackrel{\wedge}{A} \stackrel{\wedge}{A} \stackrel{\wedge}{B} = \stackrel{\wedge}{A} \stackrel$ 2) {Â, B} $\left[\hat{A}, \hat{B} \right] = \hat{A}\hat{B} - \hat{B}\hat{A} = -i\hat{B}^{\dagger}\hat{A}^{\dagger} + i\hat{A}^{\dagger}\hat{B}^{\dagger} = \hat{A}\hat{B} - i\hat{B}\hat{A}$ 8):[Â,B] $|\hat{A}|\hat{B}|\varphi > = \hat{A}(\hat{B}|\varphi >) \xrightarrow{Dc} \langle \varphi | \hat{B}^{\dagger} A^{\dagger} | => B^{\dagger} A^{\dagger} = (AB)^{\dagger}$ $|\hat{A}|\hat{B}|\varphi > \xrightarrow{Dc} \langle \varphi | (\hat{A}\hat{B})^{\dagger} | => B^{\dagger} A^{\dagger} = (AB)^{\dagger}$ n Quantum Mechanics Dokuxen 400 $\exists \hat{\beta}, \hat{J}, \forall \hat{\mathcal{L}} : \hat{\beta}^{\dagger} = \hat{\beta}, \hat{J}^{\dagger} = \hat{J}, \hat{\mathcal{L}} = \hat{\beta} + \hat{J}$ $\widehat{J}_{\text{punep}}$ $\beta = \frac{1}{2} \left(\hat{\mathcal{L}} + \hat{\mathcal{L}}^{\dagger} \right)$ $J = \frac{1}{2} \left(\hat{\mathcal{L}} - \hat{\mathcal{L}}^{\dagger} \right)$ Bagathe 2 J. J. Sakurai "Modern Quantum Mechanics < \psi \hat{L} t \hat{L} |\psi > = 1.39 < qlêt be êly> Its - Springe Зазание з $[\hat{A}, \hat{B}\hat{C}] = \hat{A}\hat{B}\hat{C} - \hat{B}\hat{C}\hat{A}$ $[\hat{A},\hat{B}] = \hat{A}\hat{B} - \hat{B}\hat{A}$ $[\hat{A},\hat{c}] = \hat{A}\hat{C} - \hat{C}\hat{A}$

 $[\hat{A}, \hat{B}]\hat{c} - \hat{B}[\hat{A}, \hat{c}] = \hat{A}\hat{B}\hat{C} - \hat{B}\hat{C}\hat{A} = [\hat{A}, \hat{B}\hat{C}]$

Задание ч

$$\hat{\rho}_{i} = -i \hbar \frac{\partial}{\partial x_{i}} \qquad \hat{r}_{i} = x_{i} \qquad \partial_{i} = \frac{\partial}{\partial x_{i}}$$

$$\alpha) \left[\hat{\rho}_{i}, \hat{\rho}_{j} \right] = \left(-i \hbar \right)^{2} \frac{\partial^{2}}{\partial x_{i} \partial x_{j}} - \left(-i \hbar \right)^{2} \frac{\partial^{2}}{\partial x_{j} \partial x_{j}} = -\hbar \left(\frac{\partial}{\partial x_{i} \partial x_{j}} - \frac{\partial}{\partial x_{j} \partial x_{i}} \right) =$$

$$\left(-h\left(\frac{\partial x_{i}\partial x_{j}}{\partial x_{j}}-\frac{\partial x_{i}\partial x_{i}}{\partial x_{j}}\right)\right)$$

6)
$$[\hat{r}_{ij}, \hat{r}_{j}] = x_i x_j - x_j x_i = 0$$

2)
$$[\hat{p}_x, f(x)] = -i \hbar f'(x) - i \hbar f(x) \partial_x + i \hbar f(x) \partial_x = -i \hbar f'(x)$$

δ) [ρ̂, x̂,] = -ihx, ο, - ih ? x, +ihx, ο, = -ih δ,

$$g) \left[\hat{\beta}_{x}^{2}, \hat{\beta}_{\infty} \right] = h^{2}(x) \hat{\partial}_{x}^{2} - h^{2}(x) \hat{\partial}_{x}^{2} - 2h^{2} \hat{\beta}'(x) \hat{\partial}_{x} - h^{2} \hat{\beta}''(x) = -h^{2}(2\hat{\beta}'(x) \hat{\partial}_{x} + \hat{\beta}''(x))$$

$$\mathcal{G}_{r}^{x} \, \xi(x) = \mathcal{G}^{x} \, \xi(x) + \mathcal{G}^{x} \, \xi \, \mathcal{G}^{x} = \xi_{n} + \xi_{n} \mathcal{G}^{x} + \xi_{n} \mathcal{G}^{x} + \xi_{n} \mathcal{G}^{x}$$