# Binding of cations to phospholipid bilayers

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Despite of vast amount of experimental and theoretical studies the binding affinity of cations, especially biologically relevant  $\mathrm{Na^+}$  and  $\mathrm{Ca^{2+}}$  ions, into a phosholipid bilayer is not agreed in the literature. Here we directly compare the measured choline headgroup order parameters to the simulations with different models in the presence of different cations. We conclude that the least complicated explanation for the experimental and theoretical observations is that the  $\mathrm{Na^+}$  ions do not penetrate into a phosphatidylcholine lipid bilayer in mM concentrations, in contrast to  $\mathrm{Ca^{2+}}$ . Further, the binding affinity of  $\mathrm{Na^+}$  is overestimated in almost all molecular dynamics simulation models. However, the electrometer concept connecting the choline order parameter changes to the penetrating charges is valid also in simulations. This work has been, and continues to be, progressed and discussed through the blog: nmrlipids.blogspot.fi. Everyone is invited to join the discussion and make contributions through the blog. The manuscript will be eventually submitted to an appropriate scientific journal. Everyone who has contributed to the work through the blog will be offered coauthorship. For more details see: nmrlipids.blogspot.fi.

### I. INTRODUCTION

The cation interactions with phospholipid membranes are present in large amount of physiological processes, nerve cell signalling being the prime example. Thus, the interactions between different cations and phospholipid bilayers have been very widely studied experimentally and theoretically. It is practically agreed that the relative binding affinity of different ions follows the Hofmeister series [1–9], however the quantitative binding affinities of different ions are not agreed in the literature. The extensive reviews about work done prior 1990 [2, 3] concluded that monovalent cations (lithium being an exception) interact only weakly with phopholipid bilayers, while the interactions are significant for multivalent ions. This conclusion has been supported by further studies where the bilayer poperties have been intact with increasing monovalent salt concentration [4, 10, 11]. On the other hand, the weak interactions of monovalent ions, especially sodium, has been also questioned in several more recent studies suggesting stronger binding [6–9, 12–18]. In this work we concentrate on the interactions between phospholipid bilayer and two widely studied and biologically relevant cations, monovalent sodium and divalent calcium.

The experimental studies supporting the weak interactions between sodium ions and phospholipid bilayer have shown that NaCl with mM concentrations has a negligible effect on choline headgroup order parameters [19], area per molecule [10], dipole potential [20] and lipid lateral diffusion [11] while these properties were significantly affected by the presense of CaCl<sub>2</sub> or other multivalent ions. In addition, water sorption isotherm for POPC/NaCl system was essentially similar to NaCl in pure water indicating only weak interaction between ion and lipid [4]. Only minor changes in POPC infrared spectra were observed in the presense of NaCl compared to the significant changes in the presense of CaCl<sub>2</sub> and other multivalent ions, and it was again concluded that the Na<sup>+</sup>-lipid interactions are weak [4].

In contrast, experimentally observed decrease in fluorescent probe rotational and translational dynamics in lipid bilayer due to addition of NaCl has suggested significant ion binding also with mM concentrations [7, 9, 12]. However, the reduced lateral diffusion is not observed in NMR experiments without probes suggesting that it would arise from interactions between probe and ion, not between lipid and ion [11]. NaCl binding to phospholipids leading to the change of the strength of bilayer against rupture and area per lipid reduction has been also suggested from Atomistic Force Microscopy (AFM) [14–18]. Interpretation of calorimetric measurements has been controversial: Previously the small effect of monovalent ions (except Lithium) on phase transition temperature compared to multivalent ions was interpreted such that only multivalent ions and Lithium specifically bind to phosholipid bilayer [2], however more recently the small changes in calorimetric experiments have been interpreted to indicate also Na<sup>+</sup> binding [8, 12]. In electrophoresis measurements of phosphatidylcholine vesicles the NaCl can increase the originally negative zeta potential close to zero, however positive zeta potential can be typically reached only with multivalent ions or Lithium ions [1, 8, 14, 15, 21]. The lack of significant positive electrophoretic mobility in the presence of NaCl has been rekognized to contradict with suggested strong binding of Na<sup>+</sup> and the contradiction has been explained by the effect of cl ions to the electrophoretic mobility [22, 23].

In atomistic resolution molecular dynamics simulations all

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FIG. 1: Chemical structure of POPC.

the generally used models seems to predict binding of Na<sup>+</sup> ions into a phoshatidylcholine lipid bilayer, but the strength of binding depends on the force field [12, 13, 22, 24–27]. The reduction of lipid lateral diffusion due to Na binding in simulations is in agreement with fluorescent probe measurements [7, 9, 12], but not with the NMR experiments [11]. The AFM experiments are interpereted to agree with the area per lipid reduction due to Na binding in simulations [14–18], however compared to the scattering experiments the are reduction is observed with too low concentrations in simulations compared to experiments [10]. The simulations has been suggested to predict larger positive electrophoretic mobility than experimentally measured with NaCl, which has been explained by choride ion behaviour [22, 23].

It is agreed in the literature that the Ca<sup>2+</sup> ions do penetrate in the phosphatidylcholine bilayer and signifincantyl affect membrane properties already with mM concentrations of CaCl<sub>2</sub>, however the strength of the binding is not agreed [13, 21, 28].

One of the experimental methods used to measure the ion binding is the so called "electrometer concept" where the changes of the C-H bond order parameters for the choline  $\alpha$ and  $\beta$  segments (see Fig. 1 for definitions and 1-palmitoyl-2-oleoylphosphatidylcholine (POPC) chemical structure) are used to determine the amount of penetrating charges into a bilayer [19, 28–30]. The concept is based on the findings that the absolute value of the  $\beta$  order parameter increases and the  $\alpha$  order parameter decreases with inceasing amount of penetrating charges [19, 28–30]. From the simulation point of view the electrometer concept is particularly interesting since one can directly compare the actual measurable quantity, i.e. order parameters, to the simulations. In this work we compare the ion induced changes in phosphatidylcholine headgroup order parameters between different simulation models to resolve the above discussed controversies in the literature.

In our recent work we showed that the experimental order parameters for choline and glycerol backbone were not quantitatively reproduced by any available lipid model in fully hydrated conditions, however, the response of the choline order parameters to the dehydration were qualitatively correct in all models and the response to the cholesterol concentration was correct for the CHARMM36 model [31]. In this work, we show that the qualitative response of order parameters to penetrating cations is qualitatively correct but the partition of ions is too strong in all the studied models.

### II. RESULTS AND DISCUSSION

The effect of NaCl on the choline and glycerol bakebone order parameters from experiments by Akutsu et al. [19] and various simulations are shown in Fig. 2. The simulated systems are described in the table I and further details are given in Supplementary Information. The experimental results are shown for DPPC bilayer due to more extensive data set [19], however the measurements for POPC gave essentially the same results [28].

The most important observation is that the experimental order parameters for the headgroup and glycerol bakebone  $g_3$  segment are practically unhanged even though 1M NaCl concentration was added to the system. Thus, the presense of mM concentrations of NaCl do not affect the structure of these parts of lipids. On the other hand, the presence of multivalent ions or charged amphiphiles changes the  $\alpha$  and  $\beta$  order parameters in a systematic way suggesting that the amount and sign of charge penetrated into a bilayer can be measured from the changes of these parameters [19, 28–30]. This is known as the "electrometer concept". Thus, the most straightforward explanation for the experimental results shown in Fig. 2 is that the Na<sup>+</sup> and Cl<sup>-</sup> ions do not essentially penetrate into a phospholipid bilayer below 1M concentrations.

The response of order parameters to the NaCl concentration in simulations depends on the used model in Fig. 2: The addition of NaCl leads to a significant changes for choline and  $g_2$  and  $g_3$  segments in glycerol bakebone in Berger and MacRog models, while only moderate changes are seen in CHARMM36 and Orange force fields. The experimental data for glycerol backbone as a function of NaCl concentration is available only for the  $g_3$  segment. The changes in  $g_1$  and  $g_2$  are unlikely since all the other order parameters are unaffected and  $^1H$  NMR data indicates that multivalent cations binding to phospholipid interact mainly with choline group leaving glycerol backbone conformations intact [43, 44].

The core idea of the electrometer concept is that the decrease (increase) of  $\beta$ - and  $\alpha$ -carbon order parameters is related to cation (anion) penetration into a lipid bilayer. It should be noted that in the original experiments the absolute value of  $\beta$  order parameter was increasing with the presense of cations, however it was shown later on that the  $\beta$  order parameter is negative [32, 33, 45], thus the value is actually increasing (becoming less negative). The order parameter changes for  $\beta$ - and  $\alpha$ -segments are plotted in Fig. 4 in the presense of NaCl and CaCl<sub>2</sub> from experiments and different simulations. The clear decrease seen with CaCl<sub>2</sub> compared to the negligible effect of NaCl. Interpreted in terms of electrometer concept, the result indicates that the Ca<sup>2+</sup> ions signifincantly

TABLE I: Simulated lipid bilayers with ions. The ion concentrations are the concentration of ions in buffer to solute the lipid bilayers and calculated as [ion]= $(N_{\rm ion}\times[water])/N_{\rm w}$ , where [water]=55.5M. These correspond the concentrations reported in the experiments by Akutsu et al. [19].

| Force field                     | lipid | [Ion] mM                 | $^{a}N_{l}$ | $^{\rm b}N_{\rm w}$ | $^cN_{\rm Na}$ | $^dN_{\rm Ca}$ | $^eN_{\rm Cl}$ | $^{f}T(K)$ | $^{\rm g}t_{\rm sim}({\rm ns})$ | ht <sub>anal</sub> (ns) | Files             |
|---------------------------------|-------|--------------------------|-------------|---------------------|----------------|----------------|----------------|------------|---------------------------------|-------------------------|-------------------|
| Berger-POPC-07[34]              | POPC  | 0                        | 128         | 7290                | 0              | 0              | 0              | 298        | 270                             | 240                     | [35]              |
| Berger-POPC-07[34], ionFF [?]1. | POPC  | 340 (NaCl)               | 128         | 7202                | 44             | 0              | 44             | 298        | 110                             | 50                      | ? <mark>2.</mark> |
| Berger-POPC-07[34], ionFF [?]3. | POPC  | 340 (CaCl <sub>2</sub> ) | 128         | 7157                | 0              | 44             | 88             | 298        | 110                             | 50                      | ? <b>4.</b>       |
| CHARMM36[36]                    | POPC  | 0                        | 72          | 2242                | 0              | 0              | 0              | 303        | 30                              | 20                      | [37]              |
| CHARMM36[36], ionFF [?]5.       | POPC  | 350 (NaCl)               | 72          | 2085                | 13             | 0              | 13             | 303        | 80                              | 60                      | ? <mark>6.</mark> |
| CHARMM36[36], ionFF [?]7.       | POPC  | 690 (NaCl)               | 72          | 2085                | 26             | 0              | 26             | 303        | 80                              | 60                      | ? <mark>8.</mark> |
| CHARMM36[36], ionFF [?]         | POPC  | 950 (NaCl)               | 72          | 2168                | 37             | 0              | 37             | 303        | 80                              | 60                      | ?                 |
| CHARMM36[36], ionFF [?]9.       | POPC  | 1380 (NaCl)              | 72          | 2085                | 52             | 0              | 52             | 303        | 80                              | 60                      | ?10.              |
| CHARMM36[36], ionFF [?]11.      | POPC  | 2080 (NaCl)              | 72          | 2085                | 78             | 0              | 78             | 303        | 73                              | 60                      | ?12.              |
| CHARMM36[36], ionFF [?]         | POPC  | $670~(\text{CaCl}_2)$    | 72          | 2164                | 26             | 0              | 52             | 303        | 200                             | 120                     | ?                 |
| MacRog[38]13.                   | POPC  | 0                        | 288         | 14400               | 0              | 0              | 0              | 310        | 90                              | 40                      | [39]              |
| MacRog[38]14., ionFF [?]15.     | POPC  | 100 (NaCl)               | 288         | 14554               | 27             | 0              | 27             | 310        | 90                              | 50                      | [40]              |
| MacRog[38]16., ionFF [?]17.     | POPC  | 210 (NaCl)               | 288         | 14500               | 54             | 0              | 54             | 310        | 90                              | 50                      | [40]              |
| MacRog[38]18., ionFF [?]19.     | POPC  | 310 (NaCl)               | 288         | 14446               | 81             | 0              | 81             | 310        | 90                              | 50                      | [40]              |
| MacRog[38]20., ionFF [?]21.     | POPC  | 420 (NaCl)               | 288         | 14392               | 108            | 0              | 108            | 310        | 90                              | 50                      | [40]              |
| Orange, ionFF [? ]22.           | POPC  | 0                        | 72          | 2880                | 0              | 0              | 0              | 298        | 60                              | 50                      | ? <b>23.</b>      |
| Orange, ionFF [?]               | POPC  | 140 (NaCl)               | 72          | 2866                | 7              | 0              | 7              | 298        | 120                             | 100                     | ?                 |
| Orange, ionFF [? ]24.           | POPC  | 510 (NaCl)               | 72          | 2802                | 26             | 0              | 26             | 298        | 120                             | 100                     | ? <b>25.</b>      |
| Orange, ionFF [?]               | POPC  | 1000 (NaCl)              | 72          | 2780                | 50             | 0              | 50             | 298        | 120                             | 80                      | ?                 |
| Orange, ionFF [? ]26.           | POPC  | $510  (CaCl_2)$          | 72          | 2802                | 0              | 26             | 52             | 298        | 120                             | 60                      | ? <b>27.</b>      |
| Slipid[41]                      | DPPC  | 0                        | 128         | 3840                | 0              | 0              | 0              | 323        | 150                             | 100                     | [42]              |
| Slipid[41], ionFF [?] 28.       | DPPC  | 150 (NaCl)               | 600         | 18000               | 49             | 0              | 49             | 323        | 100                             | 40                      | ?                 |

<sup>&</sup>lt;sup>a</sup> The number of lipid molecules

penetrate into PC bilayer in contrast to Na<sup>+</sup> [19, 28].

The differences in NaCl behaviour between different models already seen in Fig. 2 are seen more clearly in Fig. 4 showing the changes. 32.The discussion about simulation results with CaCl<sub>2</sub> to be written once we have all the results.

To study the correlation between order parameter changes and ion partitioning into a bilayer, suggested by the electrometer concept [19, 28–30], the density distributions as a function of membrane normal are shown in Fig. 5 for lipids and cations from different simulation models. It is evident from the figure that the Na<sup>+</sup> density peaks at the lipid bilayer interface are higher (indicating stronger ion binding) for the models experiencing also larger changes in order parameters with NaCl concentration shown in Fig. 2. The both Na<sup>+</sup> binding affinity and order parameter changes are smallest, thus closest to the experiments, for the Orange model, and then incease in order CHARMM36, MacRog, and Berger having the highest binding affinity and order parameter changes. Thus, the correla-

tion between decreasing choline order parameters and amount of penetrating cations (i.e. the electrometer concept) is also seen in simulations, independently of the quantitative quality of the used simulation model.

The most straightforward explanation for our results is that Na<sup>+</sup> ions do not practically penetrate into a PC lipid bilayer with mM concentrations, thus the presense of NaCl does not affect the bilayer properties as observed in various experiments [4, 10, 11, 19, 20, 28]. Consequently, the Na<sup>+</sup> penetration and concominant changes in order parameters, area per molecule and lateral diffusion seen in almost all simulation models would be artefact due to overestimated attraction between ions and lipid bilayer. Even though this would also explain the absense of positive zeta potential in electrophoresis experiments [1, 8, 14, 15, 21], the presented data do not rule out the suggested possiblity of equal binding of Na<sup>+</sup> and Cl<sup>-</sup> ions [23], however, this equal binding should happen in such a way that the bilayer properties are unaffected. Negli-

b The number of water molecules

<sup>&</sup>lt;sup>c</sup> The number of Na<sup>+</sup> molecules

<sup>&</sup>lt;sup>d</sup> The number of Ca<sup>2+</sup> molecules

<sup>&</sup>lt;sup>e</sup> The number of Cl molecules <sup>f</sup> Simulation temperature

g The total simulation time

<sup>&</sup>lt;sup>h</sup> Time frames used in the analysis

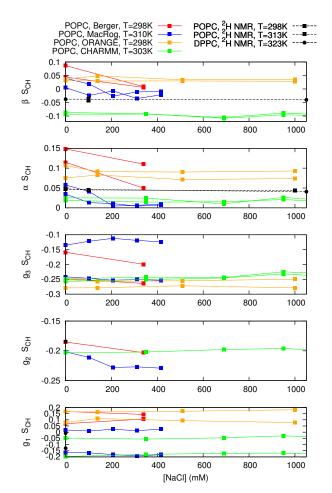


FIG. 2: Order parameters as a function of NaCl concentration from simulations with the Berger, CHARMM36, MacRog and Orange force fields compared to the experiments by Akutsu et al. [19] and Altenbach et al. [28]. The signs are assumed to be the same as measured by Hong et al. [32], Hong et al. [32] and Gross et al. [33]. The experimental data for the effect of ions to the glycerol backbone is not found, thus only the values without ions are shown. The straight line between the results with and without ions is plotted to guide the eye.

gible binding of Na<sup>+</sup> with mM concentrations suggested here differs from the conclusions made from measurements of fluorescent probe dynamics [7, 9, 12], membrane hardiness with AFM [14–18] and calorimetry [8, 12]. However, the fluorescent measurement results may arise from direct interactions between probe and ions, as already suggested by Filippov et al. [11]. Further, the calorimetric results have been also interpreted to support negligible binding [2], and AFM result is relatively indirect, thus there may be alternative explanations as well.

The effect of Ca<sup>2+</sup> on the  $\alpha$  and  $\beta$  order parameters is over-

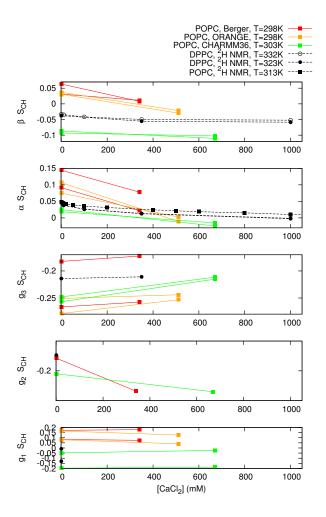


FIG. 3: Order parameters as a function of CaCl concentration from simulations with the Berger and Orange force fields compared to the experiments by Akutsu et al. [19] and Altenbach et al. [28]. The signs are assumed to be the same as measured by Hong et al. [32], Hong et al. [32] and Gross et al. [33]. The effect of ions to the g1 and g2 were not measured, thus only the values without ions are shown. The straight line between the results with and without ions is plotted to guide the eye.

estimated in all the simulation models, however, qualitatively the change is correct, i.e. order parameters are decreasing. The overestimation of the effect could be due to too strong partitioning or too sensitive headgroup model to the presense of ions. 34.The discussion should be finished when we have CHARMM results with CaCl<sub>2</sub>.

35.The  $^1$ H NMR experiments suggest that the N- $\beta$ - $\alpha$ -O dihedral is only in gaughe conformation in the absense of ions, but in the presense of multivalent ions there would be also anti conformations present [Hauser et al. BBA 508, 450 (1978), Hauser et al. Chem. Phys. Lipids 29, 103 (1981)]. I have now calculated the dihedral distributions for this dihedral with different CaCl<sub>2</sub> concentrations in different models, see Fig. 9. The change suggested by the  $^1$ H NMR experiments is not seen

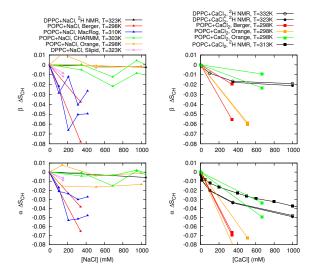


FIG. 4: The change of order parameters for  $\beta$  and  $\alpha$  segments as a function of NaCl (left column) and CaCl<sub>2</sub> (right column) concentrations from simulations and experiments by Akutsu et al. [19]. The signs of the order parameters without ions are taken from [32, 33, 45] and it is reasonable to assume that the sign do not change with concentrations repsented here [28]. Note that the  $\beta$  order parameter with negative sign decreases here with cation penetration in contrast to measured absolute value increase in the origical studies [19, 28]. Regarding the actual electrometer concept this not relevant, however. The experimental accuracy of order parameter changes is much higher than the accuracy of quantitative values due to high resolution of <sup>2</sup>H NMR spectroscopy [?].

29.I have now added the new results with ORANGE (140mM and 1M) and CHARMM36 (950mM). I think that based on the current results we cannot say that the CHARMM36 has too strong Na binding compared to experiments. This conclusion was originally partly based on simulations with much higher concentration (see discussion at: http://nmrlipids.blogspot.com/2015/02/the-first-draft-of-ion-lipid.html?showComment=1423750867868#c3435589938183508901). The text should be modified accordignly. It would be reasonable also to run longer CHARMM36 simulations since the model seems to be quite close to experiments.

The new results did not change the conclusion about the Orange model.
30.I have now also ran simulation with CaCl2 using CHARMM36 and the results are in the figure. The agreement with experiments is pretty good. The text should be modified accordingly.

31. I think that it would be very interesting to test the modified CHARMM ions: Venable et al. dx.doi.org/10.1021/jp401512z, J. Phys. Chem. B 2013, 117, 1018310192. According to the paper, these parameters improve the ion binding to the charged lipid bilayers. Even though I think that testing this would be highly relevant, I do not have time to do it now.

in the CHARMM36 model. In Orange model this dihedral is mostly in anti conformation also without  $CaCl_2$ , oppositely as suggested by  $^1H$  NMR experiments. With  $CaCl_2$  anti conformations become slightly more pronounced, however, the conformation seems to be unrealistic from the beginning so the studies of structural response to the  $CaCl_2$  might not be reasonable with this model. I think we need more simulations with CHARMM36 to see how good the order parameter response to the  $CaCl_2$  actually is. Then we can discuss more about its structural response.

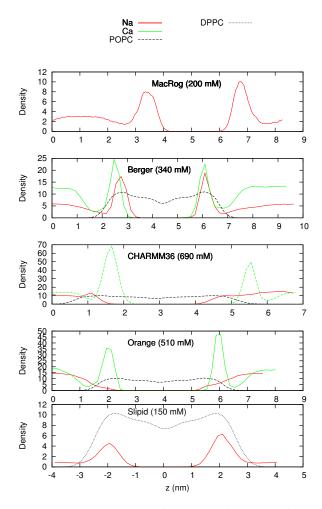


FIG. 5: Mass density profiles for lipids and ions from simulations with different force fields. The lipid densities are divided with 100 to make them visible with the used y-axis scale.

33.This figure is in progress, however, the main point can be seen.

- I think that we should use number densities instead of mass densities to make the difference between Na and Ca distributions more clear. Now the difference comparison is little bit distracted due to the different mass of the atoms.

- The lipid density from MacRog simulation is missing. Maybe Matti Javanainen

The lipid density from MacRog simulation is missing. Maybe Matti Javanainer could provide this? If the data will be uploaded to Zenodo, it also trivial to calculate it with script.

- CONCENTRATION CALCULATION ISSUE FIXED, SEE

http://nmrlipids.blogspot.com/2015/02/the-first-draft-of-ion-lipid.html?showComment=1423750867868#c3435589938183508901.
The systems are here now with quite different concentrations so comparison is not straigthforward. One option would be to run simulations of all systems with 150mM which would be close to physiological concentrations, and show the density distributions from those here.

- The CHARMM36 simulations with  $CaCl_2$  is now done. With a first look it seems that the partition is similar or stronger than in Orange model even though the order parameter change was much larger in the Orange model (see Fig. 4). This would indicate that the different order parameter response in the Orange model would be due to the reaction of headgroup into penetrating charge, not due to the difference in partition. However, this requires more detailed studies. Since the CHARMM36 results are pretty good, it would be reasonable to run the simulations also with different concentrations. The text should be updated accordingly.

- Figure editing will be finished (centering of the graphs, labels, etc.) will be done once the above issues have been sorted out.

The origin for suggested inaccuracies in lipid-ion interactions in simulation models us unknown. In principle, the incorrect choline structure [31], lack of polarizability [46] or the used water model could cause such results. The effect of changes in lipid and ion model ot the ion partition is discussed in supplementary material. 36.In the Orange simulation only lipid model is changed, respect to Berger, and Jukka tested the effect of 0.7 charge scaling for Na ion (suggested by Leontyev et al. [46] to compensate to the lack of electronic polarizability in the model). I think we should discuss these things in supplementary material. Even though we cannot be fully conclusive, there is some essential information also in these results.

#### III. CONCLUSIONS

We have compared phosholipid bilayer interactions with NaCl and CaCl<sub>2</sub> between different molecular dynamics simulation models and <sup>2</sup>H NMR experiments. The comparison led to the following conclusions

- The most straighforward explanation for the various experimental obsevations is that there is no Na<sup>+</sup> ion binding into the phospholipid bilayer with mM concentrations, in constrast to Ca<sup>2+</sup> which specifically binds.
- The Na<sup>+</sup> is overestimated in almost all molecular dynamics simulation models, however, from the publicly available models the CHARMM36 has the most realistic description.
- The electrometer concept suggesting connection between  $\alpha$  and  $\beta$  order parameter decrease and cation partitioning [19, 28–30] works also in simulations, despite of inaccuracies in actual atomistic resolution structures.
- 37.Final conclusions about the structural response to be written once we have all the results

This work has been, and will be further, progressed and discussed through the blog: nmrlipids.blogspot.fi. Everyone is invited to join the discussion and make contributions through the blog. The manuscript will be eventually submitted to an appropriate scientific journal. Everyone who has contributed to the work through the blog will be offered coauthorship. For more details see: nmrlipids.blogspot.fi.

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### SUPPLEMENTARY INFORMATION

# Appendix A: methods

# 1. Simulated systems

All simulations are ran with a standard setup for planar lipid bilayer in zero tension with periodic boundary conditions with Gromacs software package (version numbers 4.5-X-4.6.X).

### 2. Simulation details

#### a. Berger

The simulation without ions is the same as in [31]. The starting structures for simulations with ions is made by replacing water molecules with appropriate amount of ions under study. 38.Samuli, finalize and check the methods.

The Berger force field was used for the POPC [47], with the dihedral potential next to the double bond taken from [48]. The simulations are identical to previous publications [34, 49, 50]. Timestep of 2 fs was used with leap-frog integrator. Covalent bond lengths were constrained with LINCS algorithm [51, 52]. Coordinated were written every 10 ps. PME with real space cut-off 1.0 nm was used for electrostatics. Plain cut-off was used for the Lennart-Jones interactions with a 1.0 nm cut-off. The neighbour list was updated every 5th step with cut-off 1.0 nm. Temperature was coupled separately for lipids and water to 298 K with the velocity-rescale method [53] with coupling constant 0.1 ps<sup>-1</sup>. Pressure was semi-isotropically coupled to the athmospheric pressure with the Berendsen method [54].

# b. CHARMM36

The simulation without ions is the same as in [31]. The starting structures for simulations with ions is made by replacing water molecules with appropriate amount of ions under study. 39,Samuli, finalize and check the methods.

Timestep of 1 fs was used with leap-frog integrator. Covalent bonds with hydrogens were constrained with LINCS algorithm [51, 52]. Coordinated were written every 5 ps. PME with real space cut-off 1.4 nm was used for electrostatics. Lennart-Jones interactions were switched to zero between 0.8 nm and 1.2 nm. The neighbour list was updated every 5th step with cut-off 1.4 nm. Temperature was coupled separately for lipids and water to 303 K with the velocity-rescale method [53] with coupling constant 0.2 ps. Pressure was semi-isotropically coupled to the athmospheric pressure with the Berendsen method [54].

### c. MacRog

40.DONE The simulation parameters are identical to those employed in our earlier study [31] for the full hydration and dehydration simulations. The initial structures with varying amounts of NaCl were constructed from an extensively hydrated bilayer by replacing water molecules with ions using the gromacs tool genion. Even at the highest considered salt concentration, the amount of water molecules per lipid after this replacement process was still greater than 50.

# d. Orange

41. Jukka Maatta and Luca Monticelli, please deliver as much details as you can.

#### e. Slipids

The simulation without ions is the same as in [31]. 42.DONE For the simulations with ions, the starting DPPC lipid bilayer, which was built with the online CHARMM-GUI (http://www.charmm-gui.org/), contained 600 lipids, 30 water molecules/lipid, Na+ and Cl- ions (150 mM NaCl). The TIP3p water model was used to solvate the system. AA MD simulations of DPPC lipid bilayers were performed at ten different temperatures (283, 298, 303, 308, 312, 313, 314, 318, 323, and 333 K) using the GROMACS software package version 4.5.5 and the Stockholm lipids (Slipids) force field parameters for phospholipids. After energy minimization and a short equilibration run of 50 ps (time step 1fs), 100 ns production runs were performed using a time step of 2 fs with leap-frog integrator. All covalent bonds were constrained with the LINCS algorithm. Coordinates were written every 100 ps. PME with real space cut-off at 1.0 nm was used for Coulomb interactions. Lennard-Jones (LJ) interactions were switched to zero between 1.0 nm and 1.4 nm. The neighbour lists were updated every 10th step with a cut-off of 1.6 nm. Temperature was coupled separately for upper and bottom leaflets of the lipid bilayer, and for water to one of the temperatures reported above with the Nos-Hoover thermostat using a time constant of 0.5 ps. Pressure was semi-isotropically coupled to the atmospheric pressure with the Parrinello-Rahman barostat using a time constant of 10 ps. The last 40 ns of each simulation was employed for the analysis of DPPC choline and glycerol backbone order parameters.

# 3. analysis

The order parameters were calculated from simulation trajectories directly applying the equation  $S_{\rm CH}=\frac{3}{2}\langle\cos^2\theta-1\rangle$ .

For united atom models the hydrogen locations were regenerated for each molecule in each frame after the simulation trajectory was created. ??The statistical error estimate for each order parameter calculated from simulation was roughly 0.01, which is much smaller than the differences discussed in this work.??

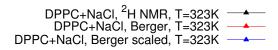
### 4. Effect of ion model and polarization

We also tested if different ion models and implicit accounting of polarization would affect ion binding. Changing the model description from Berger-DPPC-98 [55] and Gromos ion parameters [?] 43. to OPLS-AA compatible Berger-DPPC-06 [56] and Åqvist ions [57] results in slightly decreased ion binding affinity as seen from the density plots in Figure 7 [58, 59]. The failure of Gromos ions to properly account ion-ion and ion-water binding propensities of sodium and chloride ions has been reported previously [60]. The Åqvist ions have been parameterized in aqueous solutions with good agreement to experimental energies [57]. Yet, the binding affinity of ions to lipid bilayers has not been calibrated - instead it is assumed to work based purely on forces obtained using combination rules. Compared to Gromos ions Åqvist parameters are better, yet sodium overbinding still occurs.

To take account for polarization effects in non-polarizable models, Leontyev et al. [46] have suggested that ion charges should be scaled by a factor of 0.7. We scaled the charges of both Gromos and Aqvist ions. After scaling the order parameter changes due to ions and ion affinity into a bilayer of both ion models is decreased, see Figs. 6, 7 and 8 [61, 62]. The intuitive explanation is that by scaling the partial charges the charge discrepancy between the ion and water partial charges is decreased. This means that there is a lesser driving force for ions to bind to the highly-charged phosphate group. Furthermore, with Berger-DPPC-06 and scaled qvist ions (Q=0.7) we obtain that there is only very weak binding of sodium to DPPC as observed experimentally (right side of Figure 8). In scaled models the order parameter changes are also small. However, the ion concentraion is also small. To be fully conclusive, if the affinity can be fixed by scaling we need to run simulations also with large concentrations.

The results indicate that the polarization effect actually improves ion binding affinities irrespectively of the model. However, the drawback of the scaled charges is that the total charge of the simulation box is non-zero whenever counterions and charged molecules are present. This may cause simulation artefacts. Even though in methods such as PME the residual charge does not affect the forces (and thus nor dynamics), it still has an effect to the energies. This is because the potential from the residual charge is 'smeared in the box' and so depends on the possibly fluctuating (at least in NPT conditions) volume of the simulation box.

# 5. Structural changes induced by CaCl<sub>2</sub>



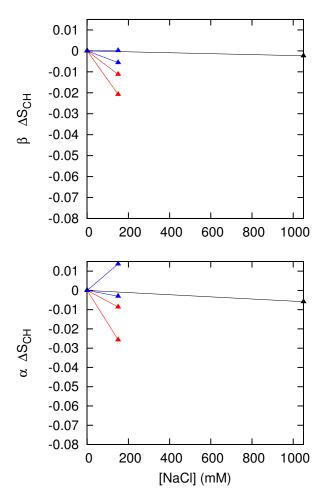
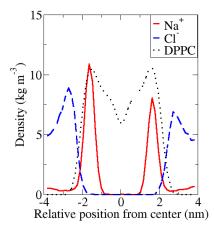


FIG. 6: Order parameter changes in scaled and non-scaled models. The Berger-OPLS compatible model results are missing since there are no results without ions for this.

| Appropriate reference for the ion model?    |
|---|
| Samuli put to Zenodo                        |
| Appropriate reference for the ion model?    |
| Samuli put to Zenodo                        |
| Appropriate reference for the ion model?    |
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| Samuli put to Zenodo                        |
| Appropriate reference for the ion model?    |
| O. Samuli put to Zenodo                     |
| 1. Appropriate reference for the ion model? |
| 2. Samuli put to Zenodo                     |
| B. DONE                                     |
| 4. DONE                                     |
| 5. Appropriate reference for the ion model? |



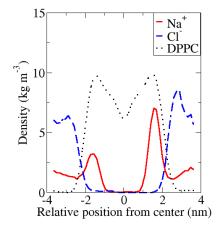
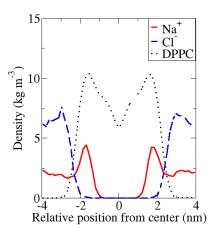


FIG. 7: Density plots of DPPC bilayer and ions. DPPC density has been scaled down by a factor of 100 for clarity. Left: Berger-DPPC-98 model with Gromos ions. Right: Berger-DPPC-06 model with Åqvist ions.



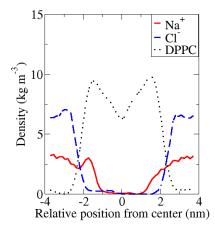


FIG. 8: Density plots of DPPC bilayer and polarization corrected ions, where ion charges are scaled by 0.7. DPPC density has been scaled down by a factor of 100 for clarity. Left: Berger-DPPC-98 model with scaled Gromos ions. Right:

Berger-DPPC-06 model with scaled Åqvist ions.

| 16. DONE .    |                         |               |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
|---------------|-------------------------|---------------|------|------|------|------|------|------|-----|------|------|------|------|-------|------|-----|------|-----|------|-----|------|-----|-----|-----|------|----|
| 17. Appropri  | ate reference for the i | ion model?    |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 18. DONE .    |                         |               |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 19. Appropri  | ate reference for the   | ion model?    |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 20. DONE .    |                         |               |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 21. Appropri  | ate reference for the   | ion model?    |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 22. Samuli ch | eck the numbers .       |               |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 23. Jukka Mt  | and Luca Monticell      | i, please let | us l | knov | w if | we   | can  | sha  | are | son  | ne f | iles | . T  | his   | is ı | ınp | ubl  | ish | ed   | mo  | ode  | 1.  |     |     |      |    |
| 24. Appropri  | ate reference for the   | ion model?    |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 25. Jukka M   | t and Luca Monticel     | li, please le | t us | kno  | ow   | if w | e ca | an s | har | e so | ome  | file | es t | hro   | oug  | h Z | end  | odo | ). I | Γhi | s is | s u | npi | ubl | lish | ed |
| model         |                         |               |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 26. Appropri  | ate reference for the   | ion model?    |      |      |      |      |      |      |     |      |      |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 27. Jukka Mt  | and Luca Monticell      | i, please let | us l | knov | w if | we   | can  | sha  | are | son  | ne f | iles | . T  | his   | is t | ınp | ubl  | ish | ed   | mo  | ode  | 1.  |     |     |      |    |
| 28. Andrea C  | atte, please let us kno | ow if you sl  | are  | son  | ne f | iles | thro | ougl | hZ  | eno  | do   |      |      |       |      |     |      |     |      |     |      |     |     |     |      |    |
| 32 The discu  | ssion about simulation  | on results w  | ith  | CaC  | lo t | o be | wr   | itte | n o | nce  | we   | hav  | ve a | ıll t | he   | res | ults |     |      |     |      |     |     |     |      |    |

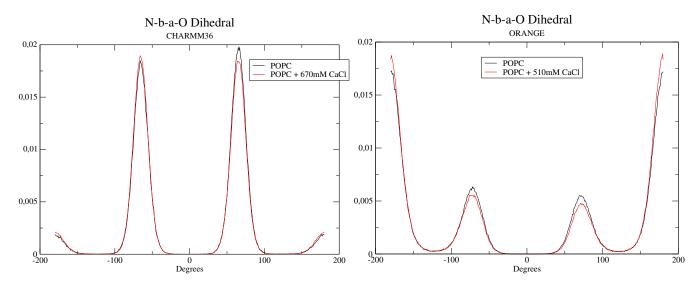


FIG. 9: Dihedral angle distributions for O- $\beta$ - $\alpha$ -N dihedral with different CaCl $_2$  concentrations.

| 54. The discussion should be finished when we have CHARIVIN fesults with CaCi <sub>2</sub>  | 4    |
|---|------|
| 29. I have now added the new results with ORANGE (140mM and 1M) and CHARMM36 (950mM). I think that based on the current results we cannot say that the CHARMM36 has too strong Na binding compared to experiments. This conclusion was originally partly based on simulations with much higher concentration (see discussion at: http://nmrlipids.blogspot.com/2015/02/the-first-draft-of-ion-lipid.html?showComment=1423750867868#c3435589938183508901). The text should be modified accordignly. It would be reasonable also to run longer CHARMM36 simulations since the model seems to be quite close to experiments. The new results did not change the conclusion about the Orange model  | 5    |
| 30. I have now also ran simulation with CaCl <sub>2</sub> using CHARMM36 and the results are in the figure. The agreement with experiments is pretty good. The text should be modified accordingly  | 5    |
| 31. I think that it would be very interesting to test the modified CHARMM ions: Venable et al. dx.doi.org/10.1021/jp401512z, J. Phys. Chem. B 2013, 117, 1018310192. According to the paper, these parameters improve the ion binding to the charged lipid bilayers. Even though I think that testing this would be highly relevant, I do not have time to do it now.   | 5    |
| 35. The $^1$ H NMR experiments suggest that the N- $\beta$ - $\alpha$ -O dihedral is only in gaughe conformation in the absense of ions, but in the presense of multivalent ions there would be also anti conformations present [Hauser et al. BBA <b>508</b> , 450 (1978), Hauser et al. Chem. Phys. Lipids <b>29</b> , 103 (1981)]. I have now calculated the dihedral distributions for this dihedral with different CaCl <sub>2</sub> concentrations in different models, see Fig. 9. The change suggested by the $^1$ H NMR experiments is not seen in the CHARMM36 model. In Orange model this dihedral is mostly in anti conformation also without CaCl <sub>2</sub> , oppositely as suggested by $^1$ H NMR experiments. With CaCl <sub>2</sub> anti conformations become slightly more pronounced, however, the conformation seems to be unrealistic from the beginning so the studies of structural response to the CaCl <sub>2</sub> might not be reasonable with this model. I think we need more simulations with CHARMM36 to see how good the order parameter response to the CaCl <sub>2</sub> actually is. Then we can discuss more about its structural response | 5    |
| - I think that we should use number densities instead of mass densities to make the difference between Na and Ca distributions more clear. Now the difference comparison is little bit distracted due to the different mass of the ator - The lipid density from MacRog simulation is missing. Maybe Matti Javanainen could provide this? If the data will be uploaded to Zenodo, it also trivial to calculate it with scri - CONCENTRATION CALCULATION ISSUE FIXED, SEE http://nmrlipids.blogspot.com/2015/02/the-first-draft-of-ion-lipid.html?showComment=1423750867868#c3435589938183508901.  |      |
| The systems are here now with quite different concentrations so comparison is not straigth-forward. One option would be to run simulations of all systems with 150mM which would be close to physiological concentrations, and show the density distributions from those he   | ere. |

| - The CHARMM36 simulations with CaCl <sub>2</sub> is now done. With a first look it seems that the partition is sim-          |
|---|
| ilar or stronger than in Orange model even though the order parameter change was much larger in the Or-                       |
| ange model (see Fig. 4). This would indicate that the different order parameter response in the Orange                        |
| model would be due to the reaction of headgroup into penetrating charge, not due to the difference in parti-                  |
| tion. However, this requires more detailed studies. Since the CHARMM36 results are pretty good, it would                      |
| be reasonable to run the simulations also with different concentrations. The text should be updated accordingly               |
| - Figure editing will be finished (centering of the graphs, labels, etc.) will be done once the above issues have been sorted |
| out   |
| 36. In the Orange simulation only lipid model is changed, respect to Berger, and Jukka tested the effect of 0.7 charge        |
| scaling for Na ion (suggested by Leontyev et al. [46] to compensate to the lack of electronic polarizability in the model). I |
| think we should discuss these things in supplementary material. Even though we cannot be fully conclusive, there is some      |
| essential information also in these results   |
| 37. Final conclusions about the structural response to be written once we have all the results                                |
| 38. Samuli, finalize and check the methods  |
| 39. Samuli, finalize and check the methods  |
| 40. DONE  |
| 41. Jukka Maatta and Luca Monticelli, please deliver as much details as you can   |
| 42. DONE  |
| 43. Appropriate reference for the ion model?  |

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