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Molecular electrometer and binding of cations to phospholipid bilayers[†]

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Despite the vast amount of experimental and theoretical studies on the binding affinity of cations into phospholipid bilayers, especially the biologically relevant Na⁺ and Ca²⁺ ions, there is no consensus in the literature. In this paper, we show that the ion binding affinity can be directly compared between simulations and experiments by using the choline headgroup order parameters according to the 'molecular electrometer' concept [Seelig *et al., Biochemistry*, 1987, **26**, 7535]. Our findings strongly support the pre-2000 view that Na⁺ and other monovalent ions (except Li⁺) do not specifically bind to phosphatidylcholine lipid bilayers with sub-molar concentrations, in contrast to Ca²⁺ and other multivalent ions. Especially the Na⁺ binding affinity is overestimated by several molecular dynamics simulation models, leading to an artificially positively charged lipid bilayer and exaggerated structural effects in the headgroups. Qualitatively correct headgroup order parameter response is observed with Ca²⁺ binding in all the tested models, however, none of the them has a sufficient quantitative accuracy to interpret the Ca²⁺:lipid stoichiometry or the induced atomistic resolution structural changes. This work has been done as a fully open collaboration, using nmrlipids.blogspot.fi as a main communication platform; all the scientific contributions were made publicly on this blog.

1 Introduction

Due to its high physiological importance — nerve cell signalling being the prime example — interaction of cations with phospholipid membranes has been widely studied via theory, simulations, and experiments. The relative ion binding affinities are gener-

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ally agreed to follow the Hofmeister series ^{1–9}, however, consensus on the quantitative affinities is currently lacking. Until 1990, the consensus (documented in two extensive reviews ^{2,3}) was that while multivalent cations interact significantly with phospholipid bilayers, for monovalent cations (with the exception of Li⁺) the interactions are weak. This conclusion has since been strengthened by further studies showing that bilayer properties remain unaltered upon the addition of sub-molar concentrations of monovalent salt ^{4,10,11}. Since 2000, however, another view has emerged, suggesting much stronger interactions between phospholipids and monovalent cations, and strong Na⁺ binding in particular ^{6–9,12–18}.

The pre-2000 view has the experimental support that (in contrast to the significant effects caused by any multivalent cations) sub-molar concentrations of NaCl have a negligible effect on phospholipid infrared spectra⁴, area per molecule ¹⁰, dipole potential ¹⁹, lateral diffusion ¹¹, and choline head group order parameters ²⁰; in addition, the water sorption isotherm of a NaCl-phospholipid system is highly similar to that of a pure NaCl solution — indicating that the ion–lipid interaction is very weak ⁴.

The post-2000 'strong binding' view rests on experimental and above all simulation findings. At sub-molar NaCl concentrations, the rotational and translational dynamics of membrane-

embedded fluorescent probes decrease 7,9,12 , and Atomic Force Microscopy (AFM) experiments show changes in bilayer hardness $^{14-18}$; in atomistic molecular dynamics (MD) simulations, phospholipid bilayers consistently bind Na $^+$, although the binding strength depends on the model used $^{12,13,21-26}$.

Some observables have been interpreted in favour of both views. For example, as the effect of monovalent ions (except Li⁺) on the phase transition temperature is tiny (compared to the effect of multivalent ions), it was initially interpreted as an indication that only multivalent ions and Li⁺ specifically bind to phospholipid bilayers²; however, such a small effect in calorimetric measurements was later interpreted to indicate that also Na⁺ binds^{8,12}. Similarly, the lack of significant positive electrophoretic mobility of phosphatidylcholine (PC) vesicles in the presence of NaCl (again in contrast to multivalent ions and Li⁺) suggested weak binding of Na^{+1,8,14,15,27}; however, these data have also been explained by a countering effect of the Clions ^{22,28}. To reduce the area per lipid in scattering experiments, molar concentrations of NaCl are required 10, which indicates weak ion-lipid interaction; in MD simulations, however, already orders of magnitude lower concentrations result in Na⁺ binding and clear reduction of area per lipid ^{12,23}. Finally, in noninvasive NMR experiments, lipid lateral diffusion is unaltered by NaCl¹¹; however, it is reduced in simulations upon Na⁺ binding, which supports interpreting the reduced lateral diffusion of fluorescent probes ^{7,9,12} as favouring the post-2000 view.

In this paper we set out to solve the apparent contradictions between the pre-2000 and post-2000 views. To this end we employ the 'molecular electrometer' concept, according to which the changes in the order parameters of the α and β carbons in the phospholipid head group (see Fig. 1) can be used to measure the ion affinity to PC lipid bilayer ^{20,29–31}. As order parameters can be accurately measured in experiments and directly compared to simulations 32, employing the molecular electrometer as a function of cation concentration allows the comparison of binding affinity between simulations and experiments. In addition to demonstrating the usefulness of this general concept, we show that the response of order parameters to penetrating cations is qualitatively correct in MD simulations, but that in several models the affinity of Na⁺ for PC bilayers is grossly overestimated. Moreover, we show that the accuracy of lipid-Ca²⁺ interactions in current models is not enough for atomistic resolution interpretation of NMR experiments.

This work has been done as an Open Collaboration at nmrlipids.blogspot.fi; all the related files (https://github.com/NMRLipids/lipid_ionINTERACTION) and almost all the simulation data (https://zenodo.org/collection/user-nmrlipids) are openly available.

2 Results and Discussion

2.1 Background: Molecular electrometer in experiments

The molecular electrometer concept is based on the experimental observation that binding of any charged objects on a PC bilayer interface induces systematic changes in the choline β and α segment order parameters $^{20,29-31,33-38}$. Thus, these changes can

Fig. 1 Chemical structure of 1-palmitoyl-2-oleoylphosphatidylcholine (POPC), and the definition of γ , β , α , g_1 , g_2 and g_3 segments.

be used to determine binding affinities of the charged objects. Molecular electrometer was originally devised for cations 20,29 , but further experimental quantification with various positively and negatively charged molecules showed that the choline order parameters S_{CH}^{α} and S_{CH}^{β} in general vary linearly with small amount of bound charge per lipid $^{29-31,33-38}$. The empirically observed linear relation can be written as 39

$$S_{\text{CH}}^{i}(X^{\pm}) = S_{\text{CH}}^{i}(0) + \frac{4m_{i}}{3\chi}X^{\pm},$$
 (1)

where $S_{\mathrm{CH}}^{i}(0)$ is the order parameter in the absence of bound charges, m_{i} is empirical constant depending on the valency and position of bound charge, X^{\pm} is the amount of bound charge per lipid, i refers to either α or β , and the value of quadrupole coupling constant is $\chi \approx 167$ kHz. The order parameter change with respect to a bilayer without bound charges then becomes

$$\Delta S_{\text{CH}}^{i} = S_{\text{CH}}^{i}(X^{\pm}) - S_{\text{CH}}^{i}(0) = \frac{4m_{i}}{3\chi}X^{\pm}.$$
 (2)

For Ca²⁺ binding to POPC bilayer (in the presence of 100 mM NaCl), combination of atomic absorption spectra and ²H NMR experiments gave $m_{\alpha} = -20.5$ and $m_{\beta} = -10.0^{29}$.

The absolute values of order parameters increase for β and decrease for α segment with bound positive charge and *vice versa* for negative charge $^{20,29-31,33,38}$. However, as the β carbon order parameter is negative while α carbon order parameter is positive $^{40-42}$, we can conclude that both $\Delta S_{\text{CH}}^{\beta}$ and $\Delta S_{\text{CH}}^{\alpha}$ decrease with bound positive charge and increase with bound negative charge. Consequently, values of m_i are negative for bound positive charges and *vice versa*. This can be rationalised by electrostatically induced changes in choline P-N dipole tilt 30,31,44 , which is also seen in simulations 23,24,45,46 . This is in line with order parameter decrease related to the P-N vector tilting more parallel to membrane plane seen with decreasing hydration levels 43 .

The quantification of $\Delta S_{\text{CH}}^{\beta}$ and $\Delta S_{\text{CH}}^{\alpha}$ with different cations have revealed that $\Delta S_{\text{CH}}^{\beta}/\Delta S_{\text{CH}}^{\alpha}\approx 0.5$ for a wide range of different cations (aqueous cations, cationic peptides, cationic anesthet-

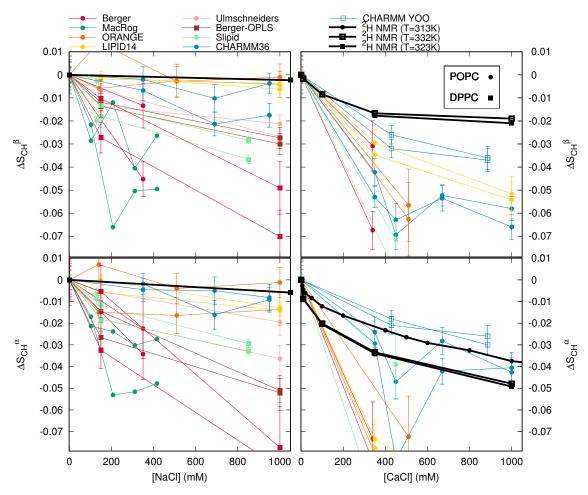


Fig. 2 The order parameter changes for β and α segments as a function of NaCl (left column) and CaCl₂ (right column) concentration, from simulations and experiments ²⁰ (POPC with CaCl₂ from ²⁹). The signs of the experimental order parameters, taken from experiments without ions ^{40–42}, can be assumed to be unchanged with concentrations represented here ^{29,32}. It should be noted that none of the models used here reproduces the order parameters within experimental error for pure PC bilayer without ions, indicating structural inaccuracies with varying severity in all models ⁴³. Note that the relatively large decrease in CHARMM36 with 450 mM CaCl₂ arise from more equilibrated binding affinity due to long simulation times, see ESI[†].

ics) 36,38 . More specifically, the relation $\Delta S_{\text{CH}}^{\beta}=0.43\Delta S_{\text{CH}}^{\alpha}$ was found for a DPPC bilayer with various CaCl₂ concentrations 20 .

2.2 Molecular electrometer concept in MD simulations

The headgroup order parameter changes as a function of ion concentration in solution from $\rm H^2$ NMR experiments are shown in Fig. 2 for DPPC and POPC bilayers 20,29 . Only minor changes in order parameters are seen as a function of NaCl in solution, while the effect of CaCl $_2$ is an order of magnitude larger. Thus, according to the molecular electrometer concept, monovalent Na $^+$ ions have negligible affinity for PC lipid bilayers at concentrations up to 1 M, while binding of Ca $^{2+}$ ions at the same concentration is significant 20,29 .

Figure 2 also reports order parameter changes calculated from MD simulations of DPPC and POPC lipid bilayers as a function of NaCl or CaCl₂ concentrations in solution (for details of the simulated systems see Tables 1, 2 and ESI[†]). Note that none of these MD models reproduced within experimental uncertainty the order parameters for a pure PC bilayer without ions (Figure 2 in Ref. 43), indicating structural inaccuracies of varying severity in

all models ⁴³. However, the experimentally observed headgroup order parameter increase with dehydration was qualitatively reproduced by all the models ⁴³, and similarly here the presence of cations leads to the decrease of $S_{\rm CH}^{\beta}$ and $S_{\rm CH}^{\alpha}$ (Fig. 2), in qualitative agreement with experiments. The changes are, however, overestimated by most models. According to the electrometer concept this indicates overbinding of cations in most MD simulation models.

While electrometer concept is well established in experiments (see previous section), it is not *a priori* clear that it works in simulations. The overestimated order parameter decrease could, in principle, arise also from the oversensitivity of choline headgroups on cation binding, instead of overbinding. Here we analyse the relation between cation binding and choline order parameter decrease in simulations in order to evaluate usability of electrometer concept in MD simulations.

According to the molecular electrometer concept, order parameter changes are linearly proportional to the amount of bound cations in bilayer (Eq. (2)). Figure 3 shows the order parameter changes as a function of bound charge in MD simulations

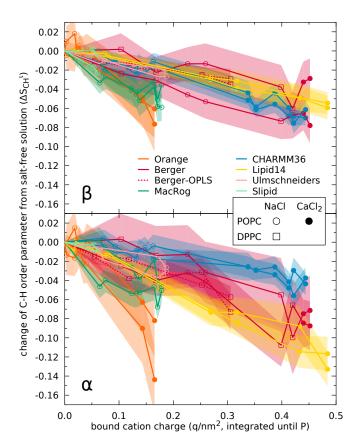


Fig. 3 Change of order parameters (from salt-free solution) of the β and α segments, $\Delta S_{\mathrm{CH}}^{\beta}$ and $\Delta S_{\mathrm{CH}}^{\alpha}$, shown as a function of bound cation charge. Eight MD simulation models compared. The order parameters as well as the bound charge calculated separately for each leaflet; cations residing between the bilayer centre and the density maximum of Phosphorus considered bound; error bars show standard error of mean over lipids.

(see ESI † for the definition of bound ions); in keeping with the molecular electrometer, roughly linear correlation between bound charge and order parameter change is found in all models. Note that quantitative comparison of the proportionality constants (i.e. slopes in Fig. 3) between different models and experimental slopes ($m_{\alpha} = -20.5$ and $m_{\beta} = -10.0$ for Ca²⁺ binding in DPPC bilayer in the presence of 100mM NaCl in Eq. 1²⁹) is not straightforward since the simulation slopes depend on the definition used for bound ions (see ESI †).

The comparison of order parameter changes in response to bound charge is more straightforward for systems with charged amphiphiles fully associated in bilayer, as the amount of bound charge is then explicitly known in both simulations and experiments. Such comparison between previously published simulation data ⁴⁷ and experiments ^{31,48} could not rule out overestimation of order parameter response to bound cations (i.e., slopes m_{β} and m_{α}) in a Berger-based model (ESI †). This might, in principle, explain the overestimated order parameter response of Berger model to CaCl₂, but not to NaCl (see discussion in ESI †). Since simulation data with charged amphiphiles from other models is not available, the extended comparison with different models is left for further studies.

Figure 3 shows that the order parameter decrease clearly corre-

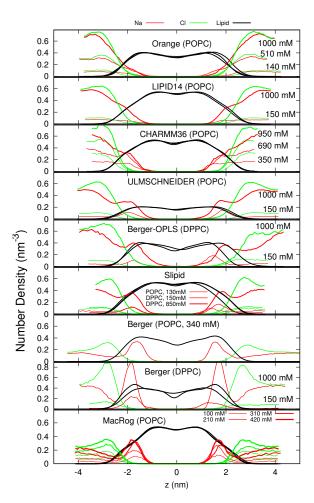


Fig. 4 Atom number density profiles along the membrane normal for lipids, Na⁺, and Cl⁻ ions from simulations with different force fields and different NaCl concentrations. The force fields are ordered according to the order parameter changes reported in Fig. 2, from the smallest (top panel) to the largest (bottom panel). The lipid densities are scaled by 100 (united atom) or 200 (all atom model) to improve readability.

lates with the amount of bound cations also in simulations. This is also evident from Fig. 4, which shows the Na⁺ density profiles of the MD models ordered according to the order parameter change (reported in Fig. 2) from the smallest (top) to the largest (bottom). The Na⁺ density peaks are larger for models with larger changes in order parameters, in line with the observed correlation between cation binding and order parameter decrease in Fig. 3.

Figure 5 compares the relation between $\Delta S_{\text{CH}}^{\beta}$ and $\Delta S_{\text{CH}}^{\alpha}$ in experiments 20 and different simulation models. Only Lipid14 gives $\Delta S_{\text{CH}}^{\beta}/\Delta S_{\text{CH}}^{\alpha}$ ratio in agreement with the experimental ratio. In all the other models the α order parameter decrease with bound cations is underestimated with respect to β order parameter decrease.

In conclusion, the clear correlation between bound cations and order parameter decrease is observed in all the tested simulation models. Consequently, the electrometer concept can be used to compare the cation binding affinity between experiments and simulations. However, we find that the quantitative response of α and β segment order parameters to bound cations in simulations

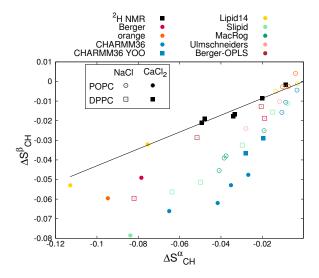


Fig. 5 Relation between ΔS_{CH}^{β} and ΔS_{CH}^{α} from experiments 20 and different simulation models. Solid line is $\Delta S_{CH}^{\beta}=0.43\Delta S_{CH}^{\alpha}$ determined for DPPC bilayer from 2 H NMR experiment with various CaCl $_2$ concentrations 20

do not generally agree with the experiments. The $\Delta S_{\text{CH}}^{\beta}/\Delta S_{\text{CH}}^{\alpha}$ ratio agrees with experiments only in Lipid14 model (Fig. 5). Thus, the observed overestimation of the order parameter changes with cation concentrations may, in principle, arise from overbinding of ions or from too sensitive lipid headgroup response on bound cation (see also discussion in ESI†). A careful analysis with current lipid models is performed in the next section.

2.3 Cation binding in different simulation models

The order parameter changes (Fig. 2) and density distributions (Fig. 4) demonstrate significantly different Na⁺ binding affinities in different simulation models. The best agreement with experiments (lowest $\Delta S_{\text{CH}}^{\alpha}$ and $\Delta S_{\text{CH}}^{\beta}$) is observed for those models (Orange, CHARMM36, and Lipid14; see Fig. 2) that also predict the lowest Na⁺ densities in the membrane proximity (Fig. 4). In all the other tested models, the choline order parameter responses to NaCl are clearly overestimated (Fig. 2), and the strength of the overestimation is clearly linked to the strength of the Na⁺ binding affinity (compare Figs. 2 and 4); this leads us to conclude that sodium binding affinity is overestimated in all these models.

In the best three models, the order parameter changes with NaCl are small (< 0.02), so with the achieved statistical accuracy we cannot conclude which of the three has the most realistic Na $^+$ binding affinity, especially at physiological NaCl concentrations (\sim 150mM) relevant for most applications. The overestimated binding in the other models raise questions on the quality of the predictions from these models when NaCl is present. Especially interactions between charged molecules and lipid bilayer might be significantly affected by the strong Na $^+$ binding, as it makes the bilayer effectively positively charged.

Significant Ca^{2+} binding affinity to a phosphatidylcholine bilayer at mM concentrations is agreed in the literature 2,3,20,29 , however, several details are yet under discussion. Simulations suggest that Ca^{2+} bind to lipid carbonyl oxygens with coordi-

nation number of 4.2^{13} , while interpretation of NMR and scattering experiments suggest that one Ca^{2+} interacts mainly with choline groups $^{102-104}$ of two phospholipid molecules 29 . Simulation model correctly reproducing the order parameter changes would resolve the discussion by giving atomistic resolution interpretation for the experiments.

As a function of CaCl2 concentration, all but one (CHARMM36 with recent ion model by Yoo et al. 73), model overestimate the order parameter decrease (Fig. 2). According to the molecular electrometer, this indicates overestimated Ca²⁺ binding. This is the most likely scenario for the models where changes in both order parameters were overestimated, however, in the case of CaCl₂ we cannot exclude the possibility that the headgroup response is oversensitive to bound cations (see ESI[†]). In CHARMM36 with ion model by Yoo et al. 73, ΔS_{CH} is overestimated for β but underestimated for α , in line with Fig. 5 where $\Delta S_{CH}^{\beta}/\Delta S_{CH}^{\alpha}$ ratio in CHARMM36 is larger than in experiments. Since we do not know if ΔS_{CH}^{β} or ΔS_{CH}^{α} is more realistic in CHARMM36, we cannot conclude if Ca²⁺ binding is too strong or weak in this simulation model. This could be resolved by comparing CHARMM36 model to the experimental data with known amount of bound charge (e.g., experiments with amphiphilic cations ^{31,48}), however, such simulation data are not currently available.

The ion density distributions with $CaCl_2$ in Fig. 6 show significant Ca^{2+} binding in all models, however, some differences occur in details. The Berger model predicts deeper penetration depth (density maxima close to ± 1.8 nm) compared to other models (density maxima close to ± 2 nm). The latter value is probably more realistic since 1H NMR and neutron scattering data indicate that Ca^{2+} interacts mainly with the choline group $^{2,102-104}$. In CHARMM36, almost all Ca^{2+} ions present in simulation bind in bilayer indicating strongest binding affinity among the tested models. The difference is not as clear in Fig. 2 because α carbon order parameters are the least sensitive to bound charge in CHARMM36 (Fig. 3).

The origin of inaccuracies in lipid-ion interactions and binding affinities in different models is far from clear. Potential candidates could be, for example, discrepancies in the ion models 105-107, incomplete treatment of electronic polarizability 108, or inaccuracies in the lipid headgroup description 43. Cordomi et al. 24 showed that the Na+ binding affinity decreases when ion radius increases in the model, however, also the models with the largest radius show significant binding in DPPC bilayer simulated with OPLS-AA force field 109. In our results, the Slipid model gives essentially similar binding affinity with ion parameters from Refs. ⁸⁹ and ^{84,85}. Further, the compensation of missing electronic polarizability by scaling ion charge 108,110 reduced Na⁺ binding in Berger, BergerOPLS and Slipid models, but not enough to be in agreement with experiments (ESI[†]). The charge-scaled Ca²⁺ model 111 slightly reduced binding in CHARMM36, but did not have significant influence on binding in Slipids (ESI[†]). Significant reduction of Ca²⁺ binding was observed with ion model by Yoo et al ⁷³, however, the CHARMM36 lipid model must be further analysed to fully interpret the results.

On the other hand, also the lipid models may have significant influence on ion binding behaviour. For example, the same ion

Table 1 List of simulations performed in this work. The ion concentrations are calculated as $[ion]=(N_{ion}\times[water])/N_w$, where [water]=55.5M. These correspond the concentrations reported in the experiments by Akutsu et al. ²⁰. The lipid force fields are named as in our previous work ⁴³.

MacRog ⁷⁴ , OPLS ⁶⁰	MacRog ⁷⁴	CHARMM36 ⁶³ , Yoo ⁷³	CHARMM36 ⁶³ , Yoo ⁷³	CHARMM36 ⁶³ , CHARMM36 ⁶⁵	CHARMM36 ⁶³ , CHARMM36 ⁶⁵	CHARMM36 ⁶³ , CHARMM36 ⁶⁵	CHARMM36 ⁶³	BergerOPLS-DPPC-06 ⁵⁸ , OPLS ⁶⁰	BergerOPLS-DPPC-06 ⁵⁸ , OPLS ⁶⁰	BergerOPLS-DPPC-06 ⁵⁸	Berger-DPPC-97 ⁵⁴ , ffgmx ⁵¹	Berger-DPPC-97 ⁵⁴ , ffgmx ⁵¹	Berger-DPPC-97 ⁵⁴	Berger-POPC-07 ⁴⁹ , ffgmx ⁵¹	Berger-POPC-07 ⁴⁹ , ffgmx ⁵¹	Berger-POPC-07 ⁴⁹	Force field (lipid, ion)							
POPC	POPC	POPC	POPC	POPC	DPPC	DPPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	DPPC	DPPC	DPPC	DPPC	DPPC	DPPC	POPC	POPC	POPC	lipid
420 (NaCl)	310 (NaCl)	210 (NaCl)	100 (NaCl)	0	886 ($CaCl_2$)	430 (CaCl ₂)	1000 (CaCl ₂)	670 (CaCl ₂)	450 (CaCl ₂)	$350 (CaCl_2)$	950 (NaCl)	690 (NaCl)	350 (NaCl)	0	1000 (NaCl)	150 (NaCl)	0	1000 (NaCl)	150 (NaCl)	0	$340 (CaCl_2)$	340 (NaCl)	0	[Ion] mM
288	288	288	288	288	128	128	128	128	200	128	72	72	72	72	72	72	72	72	72	72	128	128	128	$^a\mathrm{N}_\mathrm{l}$
14392	14446	14500	14554	14400	7520	7760	6400	6400	9000	6400	2168	2085	2085	2242	2778	2880	2880	2778	2880	2880	7157	7202	7290	$^b\mathrm{N_w}$
108	81	54	27	0	120	60	0	0	0	0	37	26	13	0	51	8	0	51	8	0	0	44	0	$^c\mathrm{N}_{\mathrm{Na}}$
0	0	0	0	0	0	0	100	67	73	35	0	0	0	0	0	0	0	0	0	0	44	0	0	$^d\mathrm{N}_{\mathrm{Ca}}$
108	81	54	27	0	240	120	200	134	146	70	37	26	13	0	51	8	0	51	8	0	88	44	0	$^e\mathrm{N}_\mathrm{Cl}$
310	310	310	310	310	323	323	303	303	310	303	303	303	303	303	323	323	323	323	323	323	298	298	298	^f T (K)
90	90	90	90	90	200	200	200	200	2000	200	80	73	80	30	120	120	120	120	120	60	108	110	270	$^g t_{\mathrm{sim}}(ns)$
50	50	50	50	40	170	170	100	120	100	100	60	60	60	20	60	60	60	60	60	50	58	50	240	$^g t_{sim}(ns)$ $^h t_{anal}(ns)$ Files
76	76	76	76	75			72	71	70	69	68	67	66	64	62	61	59	57	56	55	53	52	50	Files

a The number of lipid molecules b The number of water molecules c The number of Na $^+$ molecules d The number of Ca $^{2+}$ molecules h Time frames used in the analysis e The number of Cl molecules fSimulation temperature

Table 2 List of simulations performed in this work. The ion concentrations are calculated as [ion]=(N_{ion}×[water])/N_w, where [water]=55.5M. These correspond the concentrations reported in the experiments by Akutsu et al. ²⁰. The lipid force fields are named as in our previous work ⁴³.

Files	77	78	79	80	81	83	,	98	88	06	91	93	94	95	96	26	66	100	101
$^h t_{\rm anal}$ (ns)	50	09	100	80	09	100	40	100	150	100	100	200	200	200	100	100	200	200	200
$^g t_{\mathrm{sim}} (\mathrm{ns})$	09	120	120	120	120	150	100	105	200	105	2000	205	205	205	200	200	205	205	202
$f_{\mathrm{T}}(\mathrm{K})$	298	298	298	298	298	323	323	323	303	310	310	298	298	298	298	298	298.15	298.15	298.15
$^{ ho}N_{Cl}$	0	7	26	20	52	0	49	57	0	21	146	0	12	77	70	200	0	12	77
$^d\mathrm{N}_\mathrm{Ca}$	0	0	0	0	26	0	0	0	0	0	73	0	0	0	35	100	0	0	0
$^{c}N_{Na}$	0	7	26	20	0	0	49	22	0	21	0	0	12	77	0	0	0	12	77
$^{\mathrm{w}}\mathrm{N}_{q}$	2880	2866	2802	2780	2802	3840	18000	3726	5120	0006	0006	5120	5120	5120	6400	6400	5120	5120	5120
$^{a}N_{1}$	72	72	72	72	72	128	009	128	128	200	200	128	128	128	128	128	128	128	128
[Ion] mM	0	140 (NaCl)	510 (NaCl)	1000 (NaCl)	510 (CaCl ₂)	0	150 (NaCl)	850 (NaCl)	0	130 (NaCl)	450 (CaCl)	0	150 (NaCl)	1000 (NaCl)	350 (CaCl ₂)	1000 (CaCl ₂)	0	150 (NaCl)	1000 (NaCl)
lipid	POPC	POPC	POPC	POPC	POPC	DPPC	DPPC	DPPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC	POPC
Force field (lipid, ion)	Orange, OPLS ⁶⁰	Orange, OPLS ⁶⁰	Orange, OPLS ⁶⁰	Orange, OPLS ⁶⁰	Orange, OPLS	Slipid ⁸²	Slipid ⁸² , AMBER ^{84,85}	Slipid ⁸² , AMBER ^{84,85}	Slipid ⁸⁷	Slipid ⁸⁷ , AMBER ⁸⁹	Slipid 87 , AMBER 60	Lipid14 ⁹² , AMBER ⁶⁰	$Lipid14^{92}$, $AMBER^{60}$	Ulmschneiders ⁹⁸ , OPLS ⁶⁰	Ulmschneiders ⁹⁸ , OPLS ⁶⁰	Ulmschneiders ⁹⁸ , OPLS ⁶⁰			

 $[\]it b$ The number of water molecules α The number of lipid molecules

c The number of Na $^+$ molecules d The number of Ca $^{2+}$ molecules

e The number of Cl molecules fSimulation temperature

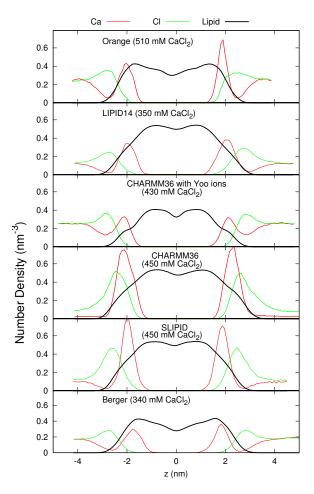


Fig. 6 Atom number density profiles along the membrane normal coordinate z for lipids, Ca^{2+} and Cl^- ions from simulations with different force fields. The profiles only with smallest available CaCl_2 concentration are shown for clarity. Figure including all the available concentrations is shown in $\operatorname{ESl}^{\uparrow}$. The lipid densities are scaled with 100 (united atom) or 200 (all atom model) to make them visible with the used y-axis scale. The Cl^- density is scaled with 2 to equalise charge density of ions.

model and non-bonded parameters are used in the Orange and BergerOPLS ⁵⁸ simulations, but while Na⁺ ion binding affinity appears realistic in the Orange model, it is significantly overestimated in the BergerOPLS (Fig. 4). However, realistic Na⁺ binding does not directly relate to realistic Ca²⁺ binding (see Orange, Lipid14 and CHARMM36 in Fig. 2) or realistic choline order parameter response to bound charge (see Orange and CHARMM36 in Fig. 5). It should be also noted that the low binding affinity of Na⁺ in CHARMM36 model is due to the additional repulsion added between sodium ions and lipid oxygens (NBFIX) ⁶⁵ (ESI[†]). Altogether, our results indicate that probably both, lipid and ion force field parameters, need improvement to correctly predict the cation binding affinity, and the associated structural changes.

3 Conclusions

As suggested by the molecular electrometer concept $^{20,29-31}$, the decrease in order parameters of α and β carbons in the PC head group of lipids bilayers is related to cation binding in all tested simulation models (Fig. 3), despite of known inaccuracies in the

actual atomistic resolution structures ⁴³. Hence molecular electrometer allows direct comparison of Na⁺ binding affinity between simulations and noninvasive NMR experiments. The comparison reveals that most models overestimate Na⁺ binding; only Orange, Lipid14, and CHARMM36 predict realistic binding affinity. None of the tested models has the required accuracy to interpret the Ca²⁺:lipid stoichiometry or induced structural changes with atomistic resolution.

In general, our results support the pre-2000 view that at mM concentrations, in contrast to Ca²⁺ and other multivalent ions 1-4,10,11,19,20,27,29, Na⁺ and other monovalent ions (except Li⁺) do not specifically bind to phospholipid bilayers. Concerning the interpretation of existing experimental data, our work supports Cevc's view² that the observed small shift in phase transition temperature is not indicative of Na⁺ binding. Further, our findings are in line with the noninvasive NMR spectroscopy work of Filippov et al. 11 that proved the results of Refs. 7,9,12 to be explainable by direct interactions between Na⁺ ions and fluorescent probes. Finally, as spectroscopic methods are in general more sensitive to atomistic details in fluid-like environment than AFM, our work indirectly suggests that the ion binding reported from AFM experiments on fluid-like lipid bilayer systems 14-18 might be confounded with other physical features of the system. Concerning contradictions in MD simulation results, we reinterpret strong Na⁺ binding as an artefact of several simulation models, e.g., the Berger model used in Refs. 12,13.

The artificial specific Na⁺ binding in simulations may lead to doubtful results, since it effectively leads to positively charged phosphatidylcholine (PC) lipid bilayers even at physiological NaCl concentration. Such a PC bilayer has distinctly different interactions with charged objects compared to a (more realistic) model without specific Na⁺ binding. Furthermore, the overestimation of Na⁺ binding affinity may extend also to other positively charged objects, say, membrane protein segments. This would affect lipid-protein interactions and could explain, for example, contradicting results on electrostatic interactions between charged protein segments and lipid bilayer^{112,113}. In conclusion, more careful studies and model development on lipid bilayer–charged object interactions are called for to make molecular dynamics simulations directly usable in a physiologically relevant electrolytic environment.

This work has been done as a fully open collaboration, using nmrlipids.blogspot.fi as the communication platform. All the scientific contributions have been communicated publicly through this blog or GitHub repository https://github.com/NMRLipids/lipid_ionINTERACTION. All the related content and data is available at https://github.com/NMRLipids/lipid_ionINTERACTION.

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