Technical Report

Efficient, Proximity-Preserving Node Overlap Removal

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Subject presentation and state of the art

A graph is a data structure encoding information with the use of nodes and edges (which are binary relations between nodes).

Graph drawing aims to represent given information as a graph, generally through a "node-link" layout, letting nodes and edges be displayed.

Most of the layout algorithms consider nodes as points, but some need to let appear additional information as labels. For example, London subway maps would be useless without the indication of the stations on the lines.

This could lead to an overlap of some nodes. That must be avoided, as it clearly confuses the understanding of the graph.

Many approachs are generally considered; the easiest to apply is to "scale" the layout until no overlaps occur. This method has the advantage to preserve the global shape of the layout, but the area of the graph can become very inconvenient. That is why a compromise between the preservation of the shape of the graph and a minimization of the total area has to be found.

Different algorithms have been devised to answer the problem.

Our project consists in understanding the algorithm PRISM proposed by Gansner and Hu in [?] and in analyzing the feasability of its implementation as a plugin for the Tulip software.

PRISM algorithm

2.1 Description of the algorithm

The PRISM algorithm focuses on two main constraints for the final layout of the graph. First, the area taken by the layout must be minimal. The second constraint is to preserve the global "shape" of the original layout by maintaining all proximity relations between the nodes.

The PRISM algorithm runs in two main steps; in a first step, it removes iteratively the overlaps between near nodes of the given graph G. Then it finds the non-near overlaping nodes and removes these overlaps as well.

We consider for this algorithm that a node i has a certain width w_i and height h_i , thus forming a rectangle containing the label, likely to cause overlaps.

2.1.1 Overlap removal between near nodes

Use of a proximity graph - Delaunay Triangulation

To find easily the overlaps between near nodes of the graph G, it will efficient to work on a proximity graph of G.

A proximity graph is a graph in which two vertices are connected by an edge if (and only if) they satisfy a given geometrical property.

The *Delaunay triangulation* (DT) of a graph G is a triangulation of the graph such that none of the circumscribed circles of the triangles in DT(G)

contains a vertex. This particular triangulation also maximises the minimum angle of the triangles found.

The Delaunay triangulation of G, as a triangulation, is also a planar graph, and has thus at most 3n-6 edges (if |V(G)|=n), which is a very practical parameter for the algorithm.

The nearest neighbors of a vertex $v \in V(G)$ tend to form triangles with v and in particular, the closest neighbor of v has an edge with v in DT(G), as the nearest neighbor graph of G is a subgraph of DT(G).

In the PRISM algorithm, we consider that the near nodes in G are connected by an edge in the Delaunay triangulation of G.

Thus, the algorithm's first goal is to remove overlaps on the edges of the Delaunay triangulation of G.

Ideal edge length

The idea is to find the "ideal length" of the Delaunay triangulation edges: the "ideal length" of an edge is such that the two edge ends have no overlap.

In order to do that, we calculate an *overlap factor* f_{ij} for each edge (i, j) $(i, j \in V(G))$ of the Delaunay triangulation of G:

$$f_{ij} = \max(\min(\frac{w_i/2 + w_j/2}{x_i - x_j}, \frac{h_i/2 + h_j/2}{y_i - y_j}), 1)$$

where (x_i, y_i) are the coordinates of vertex i, w_i its width and h_i its height. If two nodes i and j have no overlap, then $f_{ij} = 1$. If i and j do overlap, then that overlap can be removed by expanding the edge (i, j) by the overlap factor found f_{ij} .

Thus, the "ideal length" of an edge of the Delaunay triangulation is $f_{ij}||p_i - p_j||$, where p_i is the initial set of coordinates of the node i.

Proximity stress model

Termination

2.1.2 Overlap removal between non-near nodes

Why do we need a second stage?

Scan-line algorithm

```
Algorithm 1: PRISM
  Input: p_i^0: coordinates of each vertex
   width w_i and height h_i of each vertex (i = 1, 2, ..., |V|)
 1 repeat
      G_{DT}: proximity graph of G by Delaunay triangulation
      for all edges of G_{DT} do
 3
       Compute the overlap factor
      \{p_i\} : solution of the proximity stress model
 7 until no more overlaps along edges of G_{DT};
 s repeat
      G_{DT}: proximity graph of G by Delaunay triangulation
      Find overlaps in G through a scan-line algorithm
10
      Add the overlapping edges to G_{DT}
11
      for all edges of G_{DT} do
12
          Compute the overlap factor
13
      \{p_i\}: solution of the proximity stress model
14
16 until no more overlaps found by the scan-line algorithm;
```

2.1.3 Dissimilarity metrics

Area

Edge length ratio

Vertices displacement

2.2 Complexity

Implementation within Tulip

3.1 Tulip framework

Tulip presentation

Tulip node structure (problems with label size)

Solution: forcing node size and labels

3.2 Resolution of the stress model

Stress majorization

Not possible natively in Tulip Too many dependencies in GraphViz Use of Eigen possible?

Newton-Raphson method - Kamada & Kawai

Implementation done?

3.3 Scan-line algorithm

Implementation details

Tests and results

4.1 Use of GraphViz

Conclusion