```
In [1]: import numpy as np
from matplotlib import pyplot as plt
import h5py
```

Task 1: CNNs for Galaxy Classification

```
In [2]: # create data folder if it does not exist
        import os
        os.makedirs("data", exist_ok=True)
        import urllib.request
        _, msg = urllib.request.urlretrieve(
            "http://www.astro.utoronto.ca/~bovy/Galaxy10/Galaxy10.h5",
            "data/Galaxy10.h5"
In [2]: label_names =
            'Disk, Face-on, No Spiral',
             'Smooth, Completely round',
            'Smooth, in-between round',
             'Smooth, Cigar shaped',
             'Disk, Edge-on, Rounded Bulge',
            'Disk, Edge-on, Boxy Bulge',
             'Disk, Edge-on, No Bulge',
            'Disk, Face-on, Tight Spiral',
            'Disk, Face-on, Medium Spiral',
            'Disk, Face-on, Loose Spiral'
        n_classes = len(label_names)
        # To get the images and labels from file
        with h5py.File('data/Galaxy10.h5', 'r') as F:
            images = np.array(F['images'])
            labels = np.array(F['ans'])
        images = images.astype(np.float32)
        # comply to (batch, channel, height, width) convention of pytorch
```

```
# convert to torch
            print(f'{images.shape=}, {labels.shape=}')
          images.shape=(21785, 3, 69, 69), labels.shape=(21785,)
            (a)
In [ ]: # TODO: plot three samples of each class
            np.random.seed(42)
            fig, axs = plt.subplots(3, n_classes, figsize=(30, 10))
            for i in range(n_classes):
                 for j in range(3):
                       idx = np.random.choice(np.where(labels == i)[0])
                       axs[j, i].imshow(images[idx, 0], cmap='gray')
                       axs[j, i].set_title(label_names[i])
                       axs[j, i].axis('off')
         Disk, Face-on, No Spiral Smooth, Completely round Smooth, in-between round Smooth, Edge-on, Rounded BulgeDisk, Edge-on, Rounded BulgeDisk, Edge-on, Tight Spiral Disk, Face-on, Medium Spiral Disk, Face-on, Loose Spiral
          Disk, Face-on, No Spiral Smooth, Completely round Smooth, in-between round Smooth, Edge-on, Boxy Bulge Disk, Edge-on, No Bulge Disk, Face-on, Tight Spiral Disk, Face-on, Medium Spiral Disk, Face-on, Medium Spiral Disk, Face-on, Medium Spiral Disk, Face-on, Loose Spiral
         Disk, Face-on, No Spiral Smooth, Completely round Smooth, in-between round Smooth, Cigar shaped Disk, Edge-on, Rounded BulgeDisk, Edge-on, No Bulge Disk, Face-on, Tight Spiral Disk, Face-on, Medium Spiral Disk, Face-on, Loose Spiral
```

images = np.moveaxis(images, -1, 1)

```
from torchvision.transforms import Normalize
         import torch
         from torch.utils.data import TensorDataset, DataLoader
         images = torch.from_numpy(images)
         labels = torch.from_numpy(labels)
In [57]: # TODO: Split the data and normalize the images:
         import torch.utils
         train_dataset, val_dataset, test_dataset = torch.utils.data.random_split(TensorDataset(images, labels), [0.8, 0.1, 0.1])
         print(f'{len(train_dataset)=}, {len(val_dataset)=}, {len(test_dataset)=}')
         # TODO: Create tensordatasets and data Loaders:
         train_loader = DataLoader(train_dataset, batch_size=64, shuffle=True)
         val_loader = DataLoader(val_dataset, batch_size=64)
         test_loader = DataLoader(test_dataset, batch_size=64)
         normalized_images = Normalize(images.mean(), images.std())(images)
        len(train_dataset)=17429, len(val_dataset)=2178, len(test_dataset)=2178
```

(b)

```
In [68]: #TODO: implement a small CNN as specified on the sheet
    from torch import nn
    import torch.nn.functional as F

class GalaxyCNN(nn.Module):
    def __init__(self, num_classes=10):
        super(GalaxyCNN, self).__init__()

    # First convolutional block
        self.conv1 = nn.Conv2d(in_channels=3, out_channels=8, kernel_size=5)
        self.pool1 = nn.MaxPool2d(kernel_size=2, stride=2)
```

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# Second convolutional block
        self.conv2 = nn.Conv2d(in_channels=8, out_channels=16, kernel_size=5)
        self.pool2 = nn.MaxPool2d(kernel_size=2, stride=2)
        # Fully connected MLP layers
        self.fc1 = nn.Linear(3136, 64) # Adjust dimensions based on input size
        self.fc2 = nn.Linear(64, 32)
        self.fc3 = nn.Linear(32, num_classes)
    def forward(self, x):
        # First block
        x = F.relu(self.conv1(x))
        x = self.pool1(x)
        # Second block
        x = F.relu(self.conv2(x))
        x = self.pool2(x)
        # Flatten
        x = torch.flatten(x, 1) # Flatten all dimensions except the batch size
        # Fully connected layers
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x) # Final output layer (logits)
        return x
# Instantiate the model
num_classes = 10 # Update based on the number of classes
model = GalaxyCNN(num_classes=num_classes)
# Print the model architecture
print(model)
```

```
GalaxyCNN(
  (conv1): Conv2d(3, 8, kernel_size=(5, 5), stride=(1, 1))
  (pool1): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (conv2): Conv2d(8, 16, kernel_size=(5, 5), stride=(1, 1))
  (pool2): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (fc1): Linear(in_features=3136, out_features=64, bias=True)
  (fc2): Linear(in_features=64, out_features=32, bias=True)
  (fc3): Linear(in_features=32, out_features=10, bias=True)
)
```

(c) + (d) + (e)

```
In [78]: # TODO: Instantiate the model, optimizer and criterion
         model = GalaxyCNN()
         optimizer = torch.optim.Adam(model.parameters(), lr=0.001)
         criterion = nn.CrossEntropyLoss()
         train_losses = []
         train_accs = []
         val_losses = []
         val_accs = []
         # TODO: Implement the training loop, validating after every epoch, and make the requested plots.
         def train(model, optimizer, criterion, train_loader):
             losses = []
             correct = []
             model.train()
             for images, labels in train_loader:
                 optimizer.zero_grad()
                 # Forward pass
                 outputs = model(images)
                 # Compute Loss
                 loss = criterion(outputs, labels)
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losses.append(loss.item())
        # Compute gradients
        loss.backward()
        # Update weights
       optimizer.step()
        # Compute accuracy
        _, preds = torch.max(outputs, 1)
        correct.append((preds == labels).sum().item() / len(labels))
   avg_loss = np.mean(np.array(losses))
   accuracy = np.mean(np.array(correct))
   # print(f'{accuracy=:.2f}, {avg_loss=:.2e}')
   return avg_loss, accuracy
def validate(model, criterion, val_loader):
   losses = []
   correct = []
   model.eval()
   with torch.no_grad():
        for images, labels in val_loader:
            # Forward pass
           outputs = model(images)
            # Compute Loss
            loss = criterion(outputs, labels)
           losses.append(loss.item())
            # Compute accuracy
            _, preds = torch.max(outputs, 1)
            correct.append((preds == labels).sum().item() / len(labels))
   avg_loss = np.mean(np.array(losses))
   accuracy = np.mean(np.array(correct))
   # print(f'{accuracy=:.2f}, {avg_loss=:.2e}')
   return avg_loss, accuracy
```

```
val_loss, val_acc = validate(model, criterion, val_loader)
val_losses.append(val_loss)
val_accs.append(val_acc)

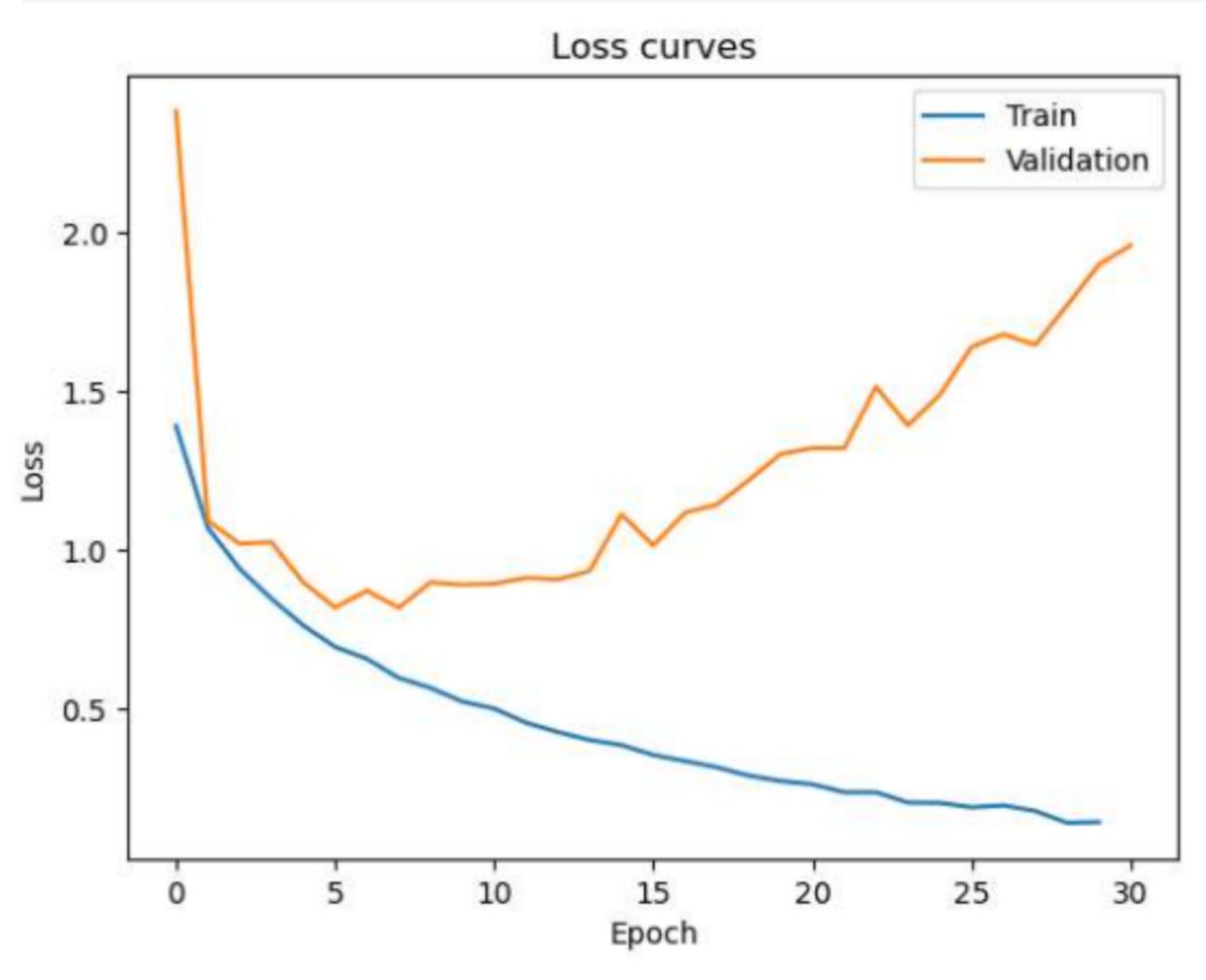
for epoch in range(30):
    # TODO: Implement the training loop, validating after every epoch and a visialization of the loss curves
    print(epoch+1, end = "\r")
    train_loss, train_acc = train(model, optimizer, criterion, train_loader)
    val_loss, val_acc = validate(model, criterion, val_loader)
    train_losses.append(train_loss)
    train_accs.append(train_acc)
    val_losses.append(val_loss)
    val_accs.append(val_loss)
    val_accs.append(val_acc)

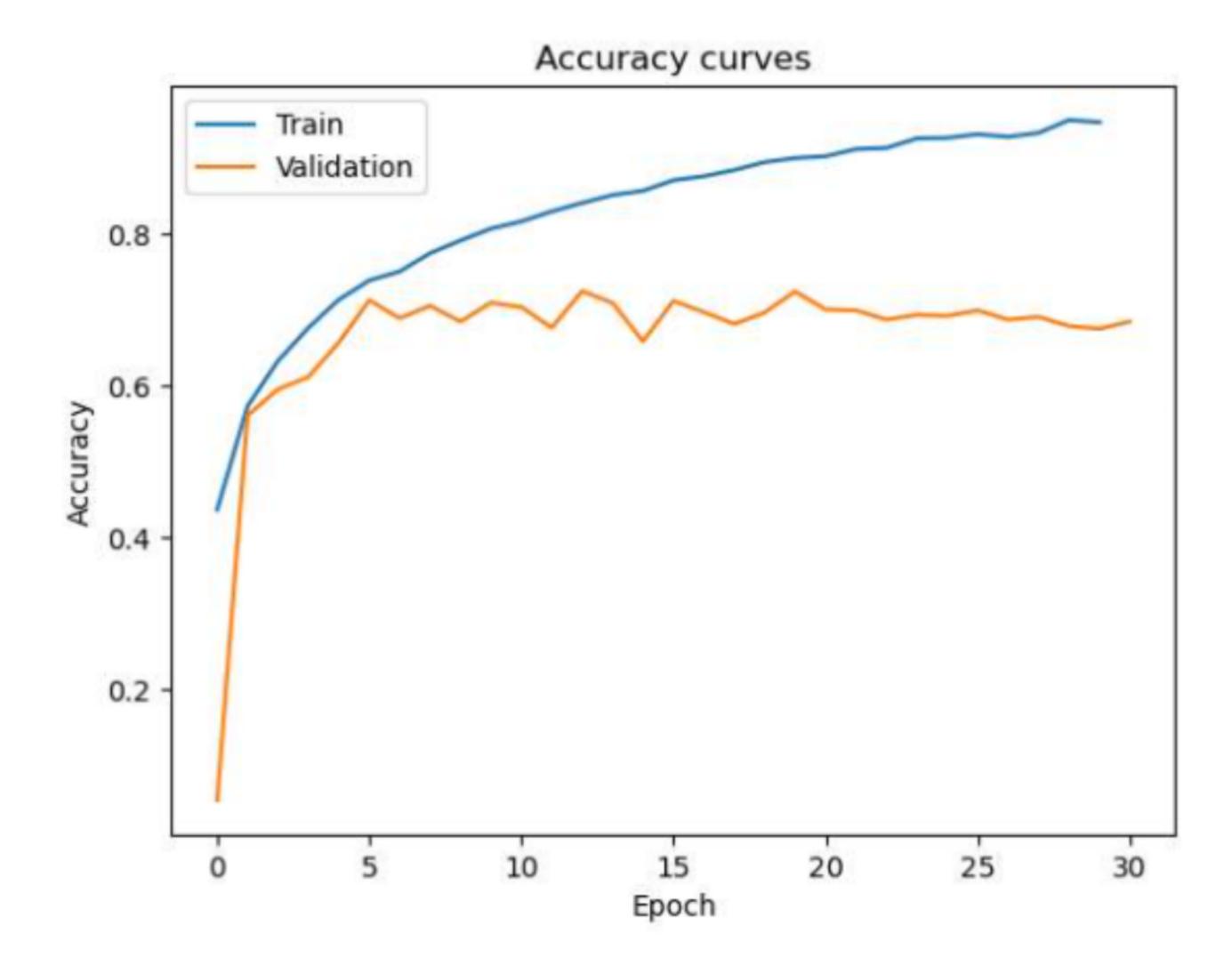
if val_loss == min(val_losses):
    bestmodel = model
```

accuracy=0.44, avg_loss=1.39e+00

```
accuracy=0.57, avg_loss=1.07e+00
        accuracy=0.63, avg_loss=9.41e-01
        accuracy=0.68, avg_loss=8.47e-01
        accuracy=0.71, avg_loss=7.63e-01
        accuracy=0.74, avg_loss=6.95e-01
        accuracy=0.75, avg_loss=6.58e-01
        accuracy=0.77, avg_loss=5.98e-01
        accuracy=0.79, avg_loss=5.66e-01
        accuracy=0.81, avg_loss=5.23e-01
        accuracy=0.82, avg_loss=5.01e-01
        accuracy=0.83, avg_loss=4.56e-01
        accuracy=0.84, avg_loss=4.27e-01
        accuracy=0.85, avg_loss=4.02e-01
        accuracy=0.86, avg_loss=3.86e-01
        accuracy=0.87, avg_loss=3.55e-01
        accuracy=0.88, avg_loss=3.36e-01
        accuracy=0.88, avg_loss=3.16e-01
        accuracy=0.89, avg_loss=2.90e-01
        accuracy=0.90, avg_loss=2.73e-01
        accuracy=0.90, avg_loss=2.62e-01
        accuracy=0.91, avg_loss=2.37e-01
        accuracy=0.91, avg_loss=2.37e-01
        accuracy=0.93, avg_loss=2.05e-01
        accuracy=0.93, avg_loss=2.04e-01
        accuracy=0.93, avg_loss=1.90e-01
        accuracy=0.93, avg_loss=1.96e-01
        accuracy=0.93, avg_loss=1.78e-01
        accuracy=0.95, avg_loss=1.41e-01
        accuracy=0.95, avg_loss=1.44e-01
         plt.plot(train_losses, label='Train')
In [79]:
         plt.plot(val_losses, label='Validation')
         plt.title('Loss curves')
         plt.xlabel('Epoch')
         plt.ylabel('Loss')
         plt.legend()
         plt.show()
         plt.plot(train_accs, label='Train')
         plt.plot(val_accs, label='Validation')
```

```
plt.title('Accuracy curves')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend()
plt.show()
```





(e) continued

```
In [ ]: # TODO: Evaluate the best validation model on the test set and create a confusion matrix
    from sklearn.metrics import confusion_matrix
    from sklearn.metrics import ConfusionMatrixDisplay

def evaluate(model, test_loader):
    predictions = []
    ground_truth = []

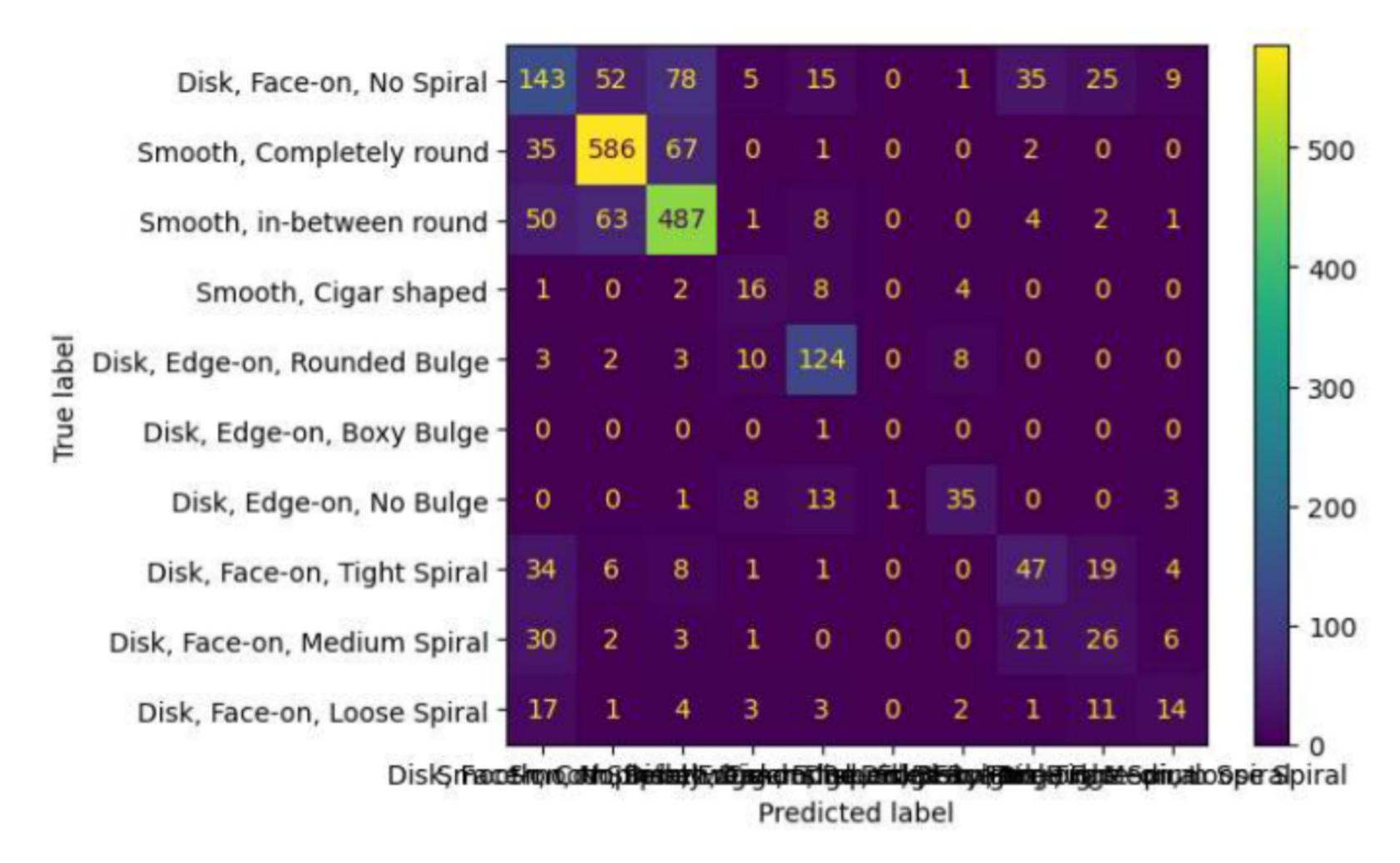
model.eval()
```

```
with torch.no_grad():
    for images, labels in test_loader:
        outputs = model(images)
        _, preds = torch.max(outputs, 1)
        predictions.extend(preds.tolist())
        ground_truth.extend(labels.tolist())

return predictions, ground_truth

predictions, ground_truth = evaluate(bestmodel, test_loader)
cm = confusion_matrix(ground_truth, predictions)
disp = ConfusionMatrixDisplay(confusion_matrix=cm, display_labels=label_names)
disp.plot()
```

Out[]: <sklearn.metrics._plot.confusion_matrix.ConfusionMatrixDisplay at 0x1e79c334190>



3 Positional Encoding

$$E \in \mathbb{R}^{p \times n}$$

$$E_{(2k),i} = \sin\left(i \cdot \exp\left(-\frac{2k \cdot \log(10000)}{p}\right)\right)$$

$$E_{(2k+1),i} = \cos\Bigl(i\cdot\exp\Bigl(-rac{2k\cdot\log(10000)}{p}\Bigr)\Bigr)$$

Nice