# **Examples for Testing of the MIcroSimulation Tool (MIST)**

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## Introduction

This document contains a set of examples that demonstrates the simulation capabilities of the MIcroSimulation Tool (MIST). These capabilities are demonstrated by a set of examples that are presented in increasing level of complexity. These tests have known results and are used for testing the system integrity. In addition to the example descriptions, the results of each example are shown and the appendix for this document contains programs that show how these results were calculated.

These examples are incorporated in the file InputExample.py to verify system integrity. They are also shown in the file testing.zip that can be loaded by the system.

Each example in this file is shown in the following format:

## **Example #:** The example title and number

## Model

Containing the diagram that shows the states and transitions. Transition probabilities are presented below the diagram.

### **Population:**

Defines the structure of the population the simulation works on.

#### **Simulation Rules:**

Defines additional simulation rule that can be added to the simulation. Also defined are the Number of Repetitions and the Max Time Iterations / simulation steps.

### **Expected Outcome:**

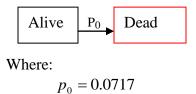
Contains the expected outcome. Usually this includes the mean counts of population at each stage at the end of simulation. The appendix at the end of the document contains Matlab code that calculates these means. In addition, to these expected outcomes, each example may contain additional tests that verify integrity of the example. These tests are implemented in the verification script InputExample.py.

For further information about the project, please visit the author web site: <a href="http://sites.google.com/site/jacobbarhak/">http://sites.google.com/site/jacobbarhak/</a>

## **Examples for Simulation Module Testing**

## **Example 1:** Simple Example:

### Model



## **Population:**

10 Individuals with the following characteristics: All Alive except one, all with Age = 30

## **Simulation Rules:**

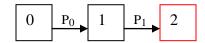
Phase 1: Pre-State Transition Rules: Age = Age +1 Phase 3: Post-State Transition Rules: None

Number of Repetitions: 100 Max Time Iterations: 3

- Age in all alive people should be 33.
- Average age at death = 31.2540
- Distribution at the end of simulation:
  - o 719.9587 Alive
  - o 280.0413 Dead

## **Example 2:** Multiple Transitions in a Chain

## Model



Where:

$$p_0 = 0.1$$

$$p_1 = 0.2$$

## **Population:**

2 Individuals with the following characteristics:

1 in state 0, 1 in state 1 
$$Age = 30$$

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

$$Age = Age + 1$$

Phase 3: Post-State Transition Rules:

None

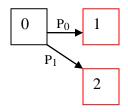
Number of Repetitions: 500

Max Time Iterations: 5

- Distribution at the end of simulation:
  - o 295.2450 State 0,
  - o 295.2450 State 1
  - o 409.5100 State 2
- Age in all alive people should be 35.

## **Example 3:** A fork state

## Model



Where:

$$p_0 = 0.3$$

$$p_1 = 0.6$$

## **Population:**

1 Individual with the following characteristics:

$$Age = 30$$

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

$$Age = Age + 1$$

Phase 3: Post-State Transition Rules:

None

Number of Repetitions: 1000

Max Time Iterations: 2

## **Expected Outcome:**

• At the end of simulation, the distribution should be:

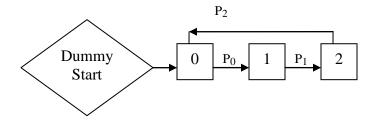
o 10.0000 State 0

o 330.0000 State 1

o 660.0000 State 2

## **Example 4:** Funny Loop Example

#### Model



Where:

$$p_0 = 0.1$$

$$p_1 = 0.2$$

$$p_2 = 0.3$$

## **Population:**

3 Individuals with the following characteristics:

Age = 30 Starting at state 0

Age = 40 Starting at state 1

Age = 50 Starting at state 2

#### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

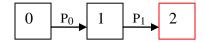
None

Number of Repetitions: 500 Max Time Iterations: 5

- The Dummy Start Event state is never entered or set as it exists as a start indicator alone, rather than a meaningful state.
- All Individuals should be at ages 35, 45, 55 no termination before the end
- At the end of simulation, the distribution should be:
  - o 791.1000 State 0
  - o 393.1950 State 1
  - o 315.7050 State 2

# **Example 5a:** Multiple Transitions in a Chain with an Expression and Boolean Covariate - (Extending the example from figure 2d in Isaman, 2006)

### Model



Where:

$$p_0 = \exp(-(b_0+b_1*Z))$$
 Z Gender b\_o=.4 b\_1=.3  
 $p_1 = \exp(-(g_0+g_1*Z))$  Z Gender g\_o=.4 g\_1=.5

## **Population:**

1 man (Z=1) starting at state 0 1 woman (Z=0) starting at state 0 ages should be irrelevant in this example

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

None

Phase 3: Post-State Transition Rules:

None

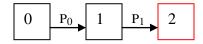
Number of Repetitions: 1000

Max Time Iterations: 2

- Distribution at the end of simulation:
  - o 253.4264 men, 108.6889 women in State 0
  - o 544.6771 men, 441.9822 women in State 1
  - o 201.8965 men, 449.3290 women in State 2

# **Example 5b:** Multiple Transitions in a Chain with an Expression and Continuous Covariate - (Extending the example from figure 2d in Isaman, 2006)

#### Model



Where:

$$p_0 = \exp(-(b_0+b_1*Z))$$
 Z Age b\_o=.04 b\_1=.03  
 $p_1 = \exp(-(g_0+g_1*Z))$  Z Age g\_o=.04 g\_1=.05

## **Population:**

1 man (Z=45) starting at state 0 1 woman (Z=60) starting at state 0 gender should be irrelevant in this example

### **Simulation Rules:**

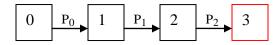
Phase 1: Pre-State Transition Rules:
Age=Age+1
Phase 3: Post-State Transition Rules:
None

Number of Repetitions: 1000 Max Time Iterations: 2

- Distribution at the end of simulation:
  - o 580.4146 men (age=47), 719.3598 women (age=62) in State 0
  - o 397.4372 men, and 273.9693 women in State 1
  - o 22.1482 men, and 6.6709 women in State 2

# **Example 6:** Multiple Transitions in a Long Chain with an Expression Containing a Continuous Covariate - (Extending the example from figure 2a,2b in Isaman, 2006)

#### Model



#### Where:

$$p_0 = \exp(-(b_0+b_1*Z))$$
 Z Age b\_o=.04 b\_1=.03  
 $p_1 = \exp(-(g_0+g_1*Z))$  Z Age g\_o=.04 g\_1=.05  
 $p_2 = \exp(-(g_0+g_1*Z))$  Z Age g\_o=.04 g\_1=.05

## **Population:**

1 man (Z=45) starting at state 0 1 woman (Z=60) starting at state 0

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age=Age+1

Phase 3: Post-State Transition Rules:

None

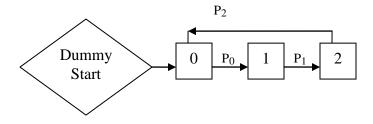
Number of Repetitions: 10000

Max Time Iterations: 3

- Distribution at the end of simulation:
  - o 4482.904 men (age=48), 6149.460 women (age=63) in State 0
  - o 4949.205 men, and 3671.033 women in State 1
  - o 548.587 men, and 176.761 women in State 2
  - o 19.305 men, and 2.747 women in State 3

# **Example 7:** Funny Loop Example with an Expression - (Extending the example from figure 2c in Isaman, 2006)

#### Model



Where:

$$p_0 = \exp(-(b_0+b_1*Z))$$
 Z Age b\_o=.02 b\_1=.02  
 $p_1 = \exp(-(g_0+g_1*Z))$  Z Age g\_o=.02 g\_1=.01  
 $p_2 = \exp(-(g_0+g_1*Z))$  Z Age g\_o=.02 g\_1=.01

### **Population:**

1 man (Z=45) starting at state 0 1 woman (Z=60) starting at state 0

### **Simulation Rules:**

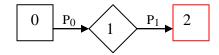
Phase 1: Pre-State Transition Rules:
Age=Age+1
Phase 3: Post-State Transition Rules:
None

Number of Repetitions: 1000 Max Time Iterations: 3

- Distribution at the end of simulation:
  - o 380.0611 men (age=48), 447.1718 women (age=63) in State 0
  - o 292.4802 men, and 303.2561 women in State 1
  - o 327.4586 men, and 249.5721 women in State 2

## **Example 8:** An Event State in a Chain

### Model



Where:

$$p_0 = 0.0717$$
  
 $p_1 = 1$ 

## **Population:**

10 Individuals with the following characteristics:

All in states 0 except one at state 2. all with Age = 30,

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

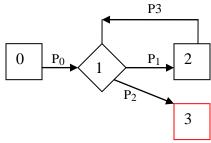
None

Number of Repetitions: 100 Max Time Iterations: 3

- Similar to Example 1
- The Event state indicator is never set in the results.
- The Entered indicator of the event state remains set at the transition to the final state.

## **Example 9:** Combined Fork Loop and Event state

## Model



Where:

$$p_0 = 0.1$$
  
 $p_1 = 0.8$   
 $p_2 = 1 - p_1 = 0.2$   
 $p_3 = 0.1$ 

## **Population:**

10 Individuals with the following characteristics:

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

$$Age = Age + 1$$

Phase 3: Post-State Transition Rules:

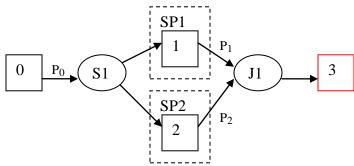
None

Number of Repetitions: 100 Max Time Iterations: 10

- No individuals in the event state
- The event State indicator for Entered is set for every transition the occurred and is reset otherwise
- Distribution at the end of simulation:
  - o 139.4714 at State 0
  - o 595.8942 at State 2
  - o 264.6345 at State 3

## **Example 10:** Split, Join, Simple Test

### Model



Where:

$$p_0 = 0.1$$
  $p_1 = p_2 = 1 - \frac{2}{5}\sqrt{5}$ . Note that  $p_1 + p_1(1 - p_1) = 0.2$  as in example 2

## **Population:**

2 Individuals with the following characteristics:

1 in state 0, 1 in states 1 and 2 together Age = 30

#### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

None

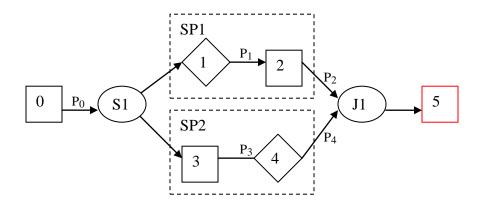
Number of Repetitions: 500 Max Time Iterations: 5

- Similar to the results of example 2, where state 3 corresponds to state 2 in Example 2 and all states and subprocesses SP1 and SP2 both correspond to State 1 in Example 2. Note that the number of people in the subprocess should be counted to figure out if the population sum is correct as states may remain set at the time of reaching the terminal state.
- The subprocess indicators for Sp1 and Sp2 are equal
- The main subprocess indicator is always set
- If the state indicator in state 1 or 2 are set, then the other one and the indicators for the subprocesses SP1 and SP2 are also set, unless the indicator for the terminal state is set, in which case, the other one is reset and both subprocess states are reset. All States may be reset.
- If a subprocess indicator in SP1, SP2 are set, then state indicators 1 and 2 are set.

- The entered indicators of the subprocess and the subprocess states equal to the entered indicator of the splitter state
- The indicator of the splitter and joiner states are never set
- The entered indicator of the joiner state is equal to the terminal state indicator which is equal to the entered indicator of the terminal state.

## **Example 11:** Split, Join, and Event Test

#### Model



Where:

$$p_0 = 0.1$$
  
 $p_1 = 1$   
 $p_2 = p_3 = 1 - \frac{2}{5}\sqrt{5}$  Note that  $p_2 + p_2(1 - p_2) = 0.2$  as in example 2  
 $p_4 = 1$ 

## **Population:**

2 Individuals with the following characteristics: 1 in state 0, 1 in states 2 and 3 together

Age = 30

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

None

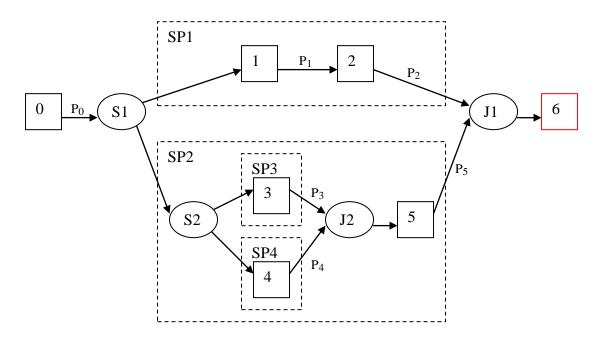
Number of Repetitions: 500 Max Time Iterations: 5

- Similar to the results of example 2, where state 5 corresponds to state 2 in Example 2 and all states and subprocesses SP1 and SP2 both correspond to State 1 in Example 2. Note that the number of people in the subprocess should be counted to figure out if the population sum is correct as states may remain set at the time of reaching the terminal state.
- The subprocess indicators for Sp1 and Sp2 are equal
- The main subprocess indicator is always set

- If the state indicator in state 2 or 3 are set, then the other one and the indicators for the subprocesses SP1 and SP2 are also set, unless the indicator for the terminal state 5 is set, in which case, the other one is reset and both subprocess states are reset. All States may be reset.
- If a subprocess indicator in SP1, SP2 are set, then state indicators 2 and 3 are set.
- State 3 and state 5 are never set together unless state 2 is reset
- The entered indicators of the subprocesses and states 1,2,3 equal to the entered indicator of the splitter state
- The indicator of the splitter, joiner, and event states are never set
- The entered indicator of the joiner state is equal to the terminal state indicator which is equal to the entered indicator of the terminal state.

## Example 12: Nested split/join test

## Model



Where:

$$p_0 = 0.1$$
  
 $p_1 = 0.2$   
 $p_2 = p_5 = 1 - \sqrt{7/10}$  Note that  $p_2 + p_2(1 - p_2) = 0.3$   
 $p_3 = p_4 = 1 - \frac{2}{5}\sqrt{5}$  Note that  $p_3 + p_3(1 - p_3) = p_1$ 

## **Population:**

2 Individuals with the following characteristics:

Age = 30

One starts in state 0 and one in states 1,3,4.

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

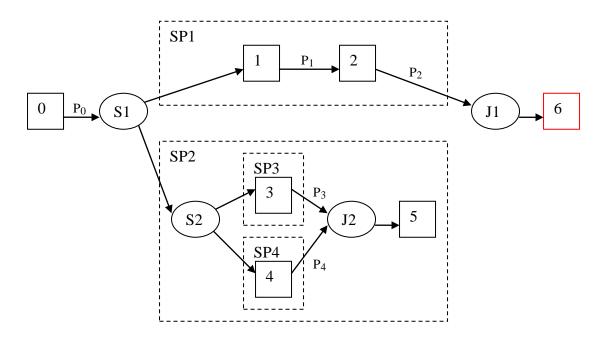
None

Number of Repetitions: 500 Max Time Iterations: 10

- At the end of simulation, the distribution should be:
  - o 174.3392 State 0
  - o 125.6437 State 1 while SP1 is set
  - o 157.7785 State 2 while SP1 is set
  - o 542.2386 State 6
- Age of all alive people should be 40
- The number of people only in active processes should be counted to figure out if the population sum is correct as states may remain set at the time of reaching the terminal state.
- The subprocess indicators for Sp1 and Sp2 are equal
- The subprocess indicators for Sp3 and Sp4 are equal
- The main subprocess indicator is always set
- If the state indicator in state 1 or 3 are set, then the indicators for the subprocesses SP1 and SP2 are also set, unless the indicator for the terminal state 6 is set, in which case, both subprocess states are reset. All States may be reset, also both subprocesses may be set together without setting states 1,3.
- If a subprocess indicator in SP1, SP2 are set, then state indicators (1 or 2) and (3 or 4 or 5) are set, while 3,4,5 are never set together. Also 2,3,4,5,6 can be set without SP1 and SP2 begin set.
- State 3 and state 6 are never set together unless state 2 is reset
- States 3,4,5 are never all set together.
- The entered indicators of subprocesses SP1, SP2, SP3, SP4 and states 1,3,4 equal to the entered indicator of the splitter states S1 and S2.
- The indicator of the splitter and joiner states S1, S2, J1, J2 are never set
- The entered indicator of the joiner state J1 is equal to the terminal state indicator which is equal to the entered indicator of the terminal state 6.

## **Example 13:** Split and join test without termination in a subprocess

## Model



Where:

$$p_0 = 0.1$$
  
 $p_1 = 0.2$   
 $p_2 = 0.3$   
 $p_3 = p_4 = 1 - \frac{2}{5}\sqrt{5}$  Note that  $p_3 + p_3(1 - p_3) = p_1$ 

## **Population:**

2 Individuals with the following characteristics:

Age = 30

One starts in state 0 and one in states 1,3,4.

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

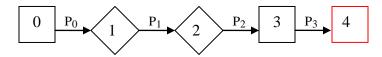
None

Number of Repetitions: 500 Max Time Iterations: 10

- At the end of simulation, the distribution should be:
  - o 174.3392 State 0
  - o 174.3392 State 1 while SP1 is set
  - o 160.2155 State 2 while SP1 is set
  - o 491.1061 State 6
- Age of all alive people should be 40
- The number of people only in active processes should be counted to figure out if the population sum is correct as states may remain set at the time of reaching the terminal state.
- The subprocess indicators for Sp1 and Sp2 are equal
- The subprocess indicators for Sp3 and Sp4 are equal
- The main subprocess indicator is always set
- If the state indicator in state 1 or 3 are set, then the indicators for the subprocesses SP1 and SP2 are also set, unless the indicator for the terminal state 6 is set, in which case, both subprocess states are reset. All States may be reset, also both subprocesses may be set together without setting states 1,3.
- If a subprocess indicator in SP1, SP2 are set, then state indicators (1 or 2) and (3 or 4 or 5) are set, while 3,4,5 are never set together. Also 2,3,4,5,6 can be set without SP1 and SP2 begin set.
- State 3 and state 6 are never set together unless state 2 is reset
- States 3,4,5 are never all set together.
- The entered indicators of subprocesses SP1, SP2, SP3, SP4 and states 1,3,4 equal to the entered indicator of the splitter states S1 and S2.
- The indicator of the splitter and joiner states S1, S2, J1, J2 are never set
- The entered indicator of the joiner state J1 is equal to the terminal state indicator which is equal to the entered indicator of the terminal state 6.
- If State 6 is set then either State 5 or State 4 are also set. In other words, there is no path from state 5 to state 6 and State 6 can be reached only from state 2.

## **Example 14:** Multiple events

### Model



Where:

$$p_0 = p_1 = p_2 = p_3 = 1$$

## **Population:**

1 Individual in State 0

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

None

Phase 3: Post-State Transition Rules:

None

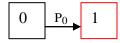
Number of Repetitions: 100

Max Time Iterations: 1

- Distribution at the end of simulation:
  - o 100 in State 3
  - o 100 with State 1 Entered and State 2 Entered
  - o 0 in State 1, 2, 4

## **Example 15:** Simple Table Example

#### Model



Where:

 $p_0$  is defined by the following table

|  | Gender = 0 | Gender =1 |
|--|------------|-----------|
| Age≤ 20  | 0.1        | 0.4       |
| 20 <age≤40< td=""><td>0.2</td><td>0.5</td></age≤40<> | 0.2        | 0.5       |
| 40 <age< td=""><td>0.3</td><td>0.6</td></age<>       | 0.3        | 0.6       |

## **Population:**

6 Individuals all in state 0 with the following characteristics:

• Gender = 0, Age = 5

• Gender = 0, Age = 25

• Gender = 0, Age = 45

• Gender = 1, Age = 5

• Gender = 1, Age = 25

• Gender = 1, Age = 45

### **Simulation Rules:**

Phase 0: Pre-State Transition Rules:

AgeAtStart = Age

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

None

Number of Repetitions: 100

Max Time Iterations: 3

## **Expected Outcome:**

- Age in all people in state 0 should be either 8,28,48.
- Distribution at the end of simulation:

o 198.9000 in State 0

o 401.1000 in State 1

• Distribution at the end of simulation where Gender =0 is:

o 158.4000 in State 0

- o 141.6000 in State 1
- Distribution at the end of simulation where AgeAtStart≤ 20 is:

o 94.5000 in State 0

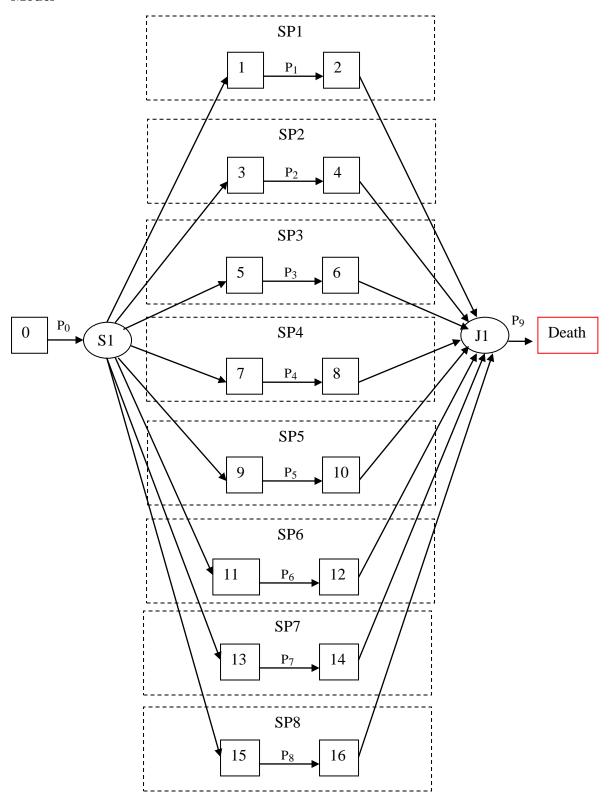
o 105.5000 in State1

- Distribution at the end of simulation where 20<AgeAtStart≤40 is: 63.7000 in State 0

  - o 136.3000 in State 1

## **Example 16:** Function test

## Model



Where:

```
\begin{split} p_0 &= 1 \\ p_1 &= \text{Le}(\text{Ls}(\text{Eq}(\text{Eq}(-1,-1),\text{Ne}(-1,1)),1),0) * \text{Not}(\text{Or}(0,0)+\text{And}(0,1)) * \\ &\quad \text{IsTrue}(.1) * .5 \\ p_2 &= \text{Ge}(\text{Gr}(1,1),0)*\text{Or}(0,0,0,1)*\text{And}(1,1,1,1)*.5 \\ p_3 &= \text{IsInvalidNumber}(\text{NaN}) * \text{IsInfinteNumber}(-\text{Inf}) * \\ &\quad \text{Not}(\text{IsFiniteNumber}(\text{Inf})) * (1/\text{Sqrt}(\text{Log}(16,2))) \\ p_4 &= \text{Ln}(\text{Exp}(\text{Max}(.25,0,-3)+\text{Min}(.25,100,25)))) \\ p_5 &= \text{Pi}()+1/\text{Log}10(10**2)-3.1415926535897931 \\ p_6 &= \text{Abs}(-.5)*\text{Floor}(1.9)*\text{Ceil}(.1)*\text{Mod}(3,2) \\ p_7 &= 4/\text{Pow}(2,3) \\ p_8 &= .5 \\ p_9 &= 1 \end{split}
```

## **Population:**

One individual in state 0 with BP = 0

Note that  $p_1$  through  $p_8$  should all equal .5

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

```
BP = BP + Le(Ls(Eq(Eq(-1,-1),Ne(-
1,1)),1),0)*Not(Or(0,0)+And(0,1))*IsTrue(.1)*.5 +
Ge(Gr(1,1),0)*Or(0,0,0,1)*And(1,1,1,1)*.5 +
IsInvalidNumber(NaN)*IsInfiniteNumber(-
Inf)*Not(IsFiniteNumber(Inf))*(1/Sqrt(Log(16,2)))
+ Ln(Exp(Max(.25,0,-3)+Min(.25,100,25))) +
Pi()+1/Log10(10**2)-3.1415926535897931 + Abs(-
.5)*Floor(1.9)*Ceil(.1)*Mod(3,2) + 4/Pow(2,3) +
.5
```

Phase 3: Post-State Transition Rules:

None

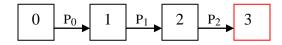
Number of Repetitions: 1,000

Max Time Iterations: 2

- At the end of simulation, the distribution should be:
  - o 500 in each of States 1 through 16
  - $\circ$  Final BP =  $\sim$ 8 always

## **Example 17:** Tests lif(), conditionals, and feedback to indicators

## Model



Where:

$$p_0 = 1$$
  
 $p_1 = \text{Iif}(\text{Gr}(\text{Age}, 32), 1, 0)$   
 $p_2 = \text{Iif}(\text{State2\_Diagnosed}, 1, 0)$ 

## **Population:**

1 Individual in State 0

## **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

a. 
$$Age = Age + 1$$

b. If State0:

Ex17TestCovariate = Ex17TestCovariate+1

c. Occurrence Probability = Iif(State0, 1, 0):

Ex17TestCovariate2 = Iif(State0, Ex17TestCovariate2 + 1, Ex17TestCovariate2)

Phase 3: Post-State Transition Rules:

a. If State2:

i. State2\_Diagnosed = Iif(Gr(Age, 34), 1, 0)

Number of Repetitions: 50 Max Time Iterations: 10

## **Expected Outcome:**

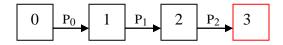
• Results according to the following table:

| Iteration          | 0  | 1  | 2  | 3  | 4  | 5  | 6  |
|--------------------|----|----|----|----|----|----|----|
| Age                | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| State0             | 1  | 0  | 0  | 0  | 0  | 0  | 0  |
| State1             | 0  | 1  | 1  | 0  | 0  | 0  | 0  |
| State2             | 0  | 0  | 0  | 1  | 1  | 1  | 0  |
| State3             | 0  | 0  | 0  | 0  | 0  | 0  | 1  |
| State2_Diagnosed   | 0  | 0  | 0  | 0  | 0  | 1  | 0  |
| Ex17TestCovariate  | 0  | 1  | 1  | 1  | 1  | 1  | 1  |
| Ex17TestCovariate2 | 0  | 1  | 1  | 1  | 1  | 1  | 1  |

- Distribution at the end of simulation:
  - o 0 in State 0,1, 2
  - o 50 in State 3

## Example 18: Tests Cost/QoL Wizard

#### Model



Where:

$$p_0 = 1$$
  
 $p_1 = 0.5$   
 $p_2 = 0.5$ 

## **Population:**

1 Individual in State 0, with Ex18TestCost = 10 and Ex18TestQoL = 0.1

#### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

a. Age = Age + 1

Phase 3: Post-State Transition Rules:

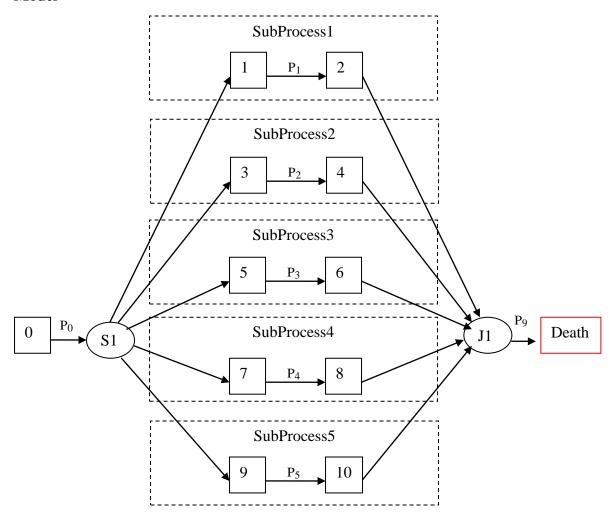
- b. Ex18TestCost=CostWizard(0,100,[State1,State2],[Iif(Gr(Age,31),3,0),Iif(Gr(Age,33),2,0)])
- c. Ex18TestQoL=CostWizard(1,.5,[State1,State2],[Iif(Gr(Age,31),.1,0),Iif(Gr(Age,33),.2,0)])
  None

Number of Repetitions: 100 Max Time Iterations: 5

- If state 1 and age>31 then:
  - o Ex18TestCost = 100000, Ex18TestQoL = 0.6
- If state 2 and age>33 then:
  - $\circ$  Ex18TestCost = 10000, Ex18TestQoL = 0.7
- If state 3 or (state 1 and age<=31) or (state 2 and age<=33) then:
  - $\circ$  Ex18TestCost = 100, Ex18TestQoL = 0.5
- If state 0 then:
  - $\circ$  Ex18TestCost = 10, Ex18TestQoL = 0.1
- Distribution at the end of simulation:
  - o 0 in State 0
  - o 6.25 in State 1
  - o 25 in State 2
  - o 68.75 in State 3

## **Example 19:** Equivalent Parallel Process Test and Distribution Function Rule Test

## Model



Where:

$$p_0 = 1$$
  
 $p_1 = 0.5$   
 $p_2 = 0.5$   
 $p_3 = 0.5$   
 $p_4 = 0.5$   
 $p_5 = 0.5$   
 $p_9 = 1$ 

Note that  $p_1$  through  $p_5$  should all equal 0.5

## **Population:**

One individual in state 0 with:

- CovTemp1=0
- CovTemp2=0
- CovTemp3=0
- CovTemp4=0
- CovTemp5=0

#### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

- $\circ$  TestCov1 = Le(Bernoulli(0.5), 0.5)
- $\circ$  TestCov2 = Le(Binomial(3,0.5), 1)
- $\circ$  TestCov3 = Le(Geometric(1-0.5\*\*0.5), 2)
- $\circ$  TestCov4 = Le(Uniform(0,2),1)
- o TestCov5 = Le(Gaussian(3,1), 3)

Phase 3: Post-State Transition Rules:

None

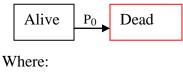
Number of Repetitions: 1,000

Max Time Iterations: 2

- At the end of simulation, the distribution should be:
  - o 500 in each of States 1 through 10
  - At the end of simulation, the sum of each covariate over the population TestCov1..5 contains 500 individuals.

## **Example 20:** Simple Example with Initial Population Defined by Distributions:

## Model



$$p_0 = 0.0717$$

## **Population:**

Individuals defined by distributions with the following characteristics:

Alive=Bernoulli(0.9)

Dead=1-Alive

Age = Min(Max(20,Gaussian(30,5)),40)

### **Simulation Rules:**

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

None

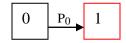
Number of Repetitions: 1000 (defines population size)

Max Time Iterations: 3

- Age in all records should be between 20 and 43.
- There should be 25 individuals at age 20 check this is correct within 3 STD
- Distribution at the end of simulation Same as example 1:
  - o 719.9587 Alive
  - o 280.0413 Dead

## **Example 21:** Initial Population Defined by Distributions and simple Objectives:

## Model



Where:

 $p_0$  is defined by the following table

|  | Gender = 0 | Gender =1 |
|--|------------|-----------|
| Age≤ 20  | 0.1        | 0.4       |
| 20 <age≤40< td=""><td>0.2</td><td>0.5</td></age≤40<> | 0.2        | 0.5       |
| 40 <age< td=""><td>0.3</td><td>0.6</td></age<>       | 0.3        | 0.6       |

## **Population:**

600 Individuals all in state 0 defined by distributions with the following characteristics:

Age = Uniform(1,59)

Gender = Bernoulli(0.6)

The following objectives will be used – disregarding the test error:

| Filter Expression           | Statistics       | Statistics | Target | Weight | Test  |
|-----------------------------|------------------|------------|--------|--------|-------|
| _                           | Expression       | Function   | _      |        | Error |
| Le(Age,20)                  | Age              | MEAN       | 5      | 1      | 2     |
| And(Gr(Age,20), Le(Age,40)) | Age -25          | MEAN       | 0      | 1      | 2     |
| Gr(Age,40)                  | Age              | MEAN       | 45     | 1      | 2     |
| 1                           | Gender           | MEAN       | 0.5    | 1      | 0.05  |
| 1                           | Age*(Gender-0.5) | MEDIAN     | 0      | 1      | 1     |
| Le(Age,20)                  | Age              | STD        | 1      | 0.1    | 1     |
| And(Gr(Age,20), Le(Age,40)) | Age              | PERCENT25  | 24     | 0.1    | 1     |
| And(Gr(Age,20), Le(Age,40)) | Age              | PERCENT75  | 26     | 0.1    | 2     |
| Gr(Age,40)                  | Age              | MIN        | 42     | 0.1    | 2     |
| Gr(Age,40)                  | Age              | MAX        | 48     | 0.1    | 6     |
| And(Le(Age,20),             | 1                | SUM        | 100    | 0.02   | 10    |
| Eq(Gender,0))               |                  |            |        |        |       |
| And(Gr(Age,20), Le(Age,40), | 1                | SUM        | 100    | 0.02   | 10    |
| Eq(Gender,0))               |                  |            |        |        |       |
| And(Gr(Age,40),             | 1                | SUM        | 100    | 0.02   | 10    |
| Eq(Gender,0))               |                  |            |        |        |       |
| And(Le(Age,20),             | Age **2          | COUNT      | 100    | 0.02   | 10    |
| Eq(Gender,1))               |                  |            |        |        |       |
| And(Gr(Age,20), Le(Age,40), | Age **2          | COUNT      | 100    | 0.02   | 10    |
| Eq(Gender,1))               |                  |            |        |        |       |
| And(Gr(Age,40),             | Age **2          | COUNT      | 100    | 0.02   | 10    |
| Eq(Gender,1))               |                  |            |        |        |       |

#### **Simulation Rules:**

Phase 0: Pre-State Transition Rules:

AgeAtStart = Age

Phase 1: Pre-State Transition Rules:

Age = Age + 1

Phase 3: Post-State Transition Rules:

None

Number of Repetitions: 600 (defines population size)

Max Time Iterations: 3

- Distribution at the end of simulation:
  - o 198.9000 in State 0
  - o 401.1000 in State 1
- Distribution at the end of simulation where Gender =0 is:
  - o 158.4000 in State 0
  - o 141.6000 in State 1
- Distribution at the end of simulation where AgeAtStart \( \) 20 is:
  - o 94.5000 in State 0
  - o 105.5000 in State1
- Distribution at the end of simulation where 20< AgeAtStart ≤40 is:
  - o 63.7000 in State 0
  - o 136.3000 in State 1
- Distribution at the end of simulation where 40< AgeAtStart ≤60 is:
  - o 40.7000 in State 0
  - o 159.3000 in State 1
- At the end of simulation the average AgeAtStart of individuals of 0< AgeAtStart <=20 should be between 4 and 6 this is an approximated range not absolute
- At the end of simulation the average Age of individuals of 20< AgeAtStart <=40 should be between 24 and 26 this is an approximated range not absolute
- At the end of simulation the average Age of individuals of 40< AgeAtStart should be between 44 and 46 this is an approximated range not absolute
- Check that objectives have been reached within a reasonable margins noted as Test Error in the Objectives table
  - A critical test is that the first 3 objectives should be the same as the previous three tests for AgeAtStart – this tests the code is ok
  - o The rest of the tests are not critical

## **APPENDIX:**

# Matlab code to generate the mean expected results

```
% This file contains analytic results to which the simulation results
% should be compared to.
% Example 1: Simple Example:
disp ('Example 1: Simple Example:')
P0 = 0.0717
t = 3
Pop = [9 1]*100
Mat = [1-P0, P0; 0, 1]
Result = Pop*(Mat^t)
OldDeadNum = 0
for i = 0:t.
 DeadNum = Pop*Mat^i;
  DeadAtYear(i+1) = DeadNum(2) - OldDeadNum;
 OldDeadNum = DeadNum(2);
end
AverageAgeAtDeath = sum((30+(0:t)).*DeadAtYear)/sum(DeadAtYear)
% Example 2: Multiple Transitions in a Chain
disp ('Example 2: Multiple Transitions in a Chain')
P0 = 0.1
P1 = 0.2
t = 5
Pop = [1 \ 1 \ 0] * 500
Mat = [1-P0, P0, 0; 0, 1-P1, P1; 0, 0, 1]
Result = Pop*(Mat^t)
```

```
% Example 3: A fork state
disp ('Example 3: A fork state')
P0 = 0.3
P1 = 0.6
t = 2
Pop = [1 \ 0 \ 0] * 100
Mat = [1-P0-P1, P0, P1; 0, 1, 0; 0, 0, 1]
Result = Pop*(Mat^t)
% Example 4: Funny Loop Example
disp ('Example 4: Funny Loop Example')
P0 = 0.1
P1 = 0.2
P2 = 0.3
t = 5
Pop = [1 \ 1 \ 1] *500
Mat = [1-P0, P0, 0; 0, 1-P1, P1; P2, 0, 1-P2]
Result = Pop*(Mat^t)
% Example 5a: Multiple Transitions in a Chain with an Expression and
% Boolean Covariate
disp ('Example 5a: Multiple Transitions in a Chain with an Expression
and Boolean Covariate')
```

MaxTime=2

```
for Gender = 0:1,
  Pop = [1 \ 0 \ 0] * 1000
  MultMat = eye(3)
  for t= 1:MaxTime
     P0 = \exp(-(0.4 + 0.3*Gender))
     P1 = \exp(-(0.4 + 0.5 * Gender))
     Mat = [1-P0, P0, 0; 0, 1-P1, P1; 0, 0, 1]
     MultMat = MultMat * Mat
   disp (sprintf ('Results for Gender = %g', Gender))
  Result = Pop*(MultMat)
end
% Example 5b: Multiple Transitions in a Chain with an Expression and
% Continuous Covariate - (Extending the example from figure 2d in
Isaman, 2006)
disp ('Example 5b: Multiple Transitions in a Chain with an Expression
and Continuous Covariate')
MaxTime=2
Ages = [60, 45]
for Gender = 0:1,
  Age = Ages (Gender+1)
  Pop = [1 \ 0 \ 0] * 1000
  MultMat = eye(3)
   for t= 1:MaxTime
     Age = Age + 1
     P0 = \exp(-(0.04 + 0.03*Age))
     P1 = \exp(-(0.04 + 0.05*Age))
     Mat = [1-P0, P0, 0; 0, 1-P1, P1; 0, 0, 1]
     MultMat = MultMat * Mat
   disp (sprintf ('Results for Gender = %g', Gender))
  Result = Pop*(MultMat)
end
% Example 6: Multiple Transitions in a Long Chain with an Expression
Containing a Continuous Covariate - (Extending the example from figure
2a,2b in Isaman, 2006))
```

```
disp ('Example 6: Multiple Transitions in a Long Chain with an
Expression Containing a Continuous Covariate')
MaxTime = 3
Ages = [60, 45]
for Gender = 0:1,
  Age = Ages (Gender+1)
  Pop = [1 \ 0 \ 0 \ 0] * 1000
  MultMat = eye(4)
  for t= 1:MaxTime
    Age = Age + 1
    P0 = \exp(-(0.04 + 0.03*Age))
    P1 = \exp(-(0.04 + 0.05*Age))
    P2 = \exp(-(0.04 + 0.05*Age))
    Mat = [1-P0 , P0 , 0 , 0 ; 0 , 1-P1, P1 ,0 ; 0, 0, 1-P2, P2;
0, 0, 0, 1]
    MultMat = MultMat * Mat
  disp (sprintf ('Results for Gender = %q', Gender))
  Result = Pop*(MultMat)
end
% Example 7: Funny Loop Example with an Expression - (Extending the
example from figure 2c in Isaman, 2006)
disp ('Example 7: Funny Loop Example with an Expression - (Extending
the example from figure 2c in Isaman, 2006)')
MaxTime = 3
Ages = [60, 45]
for Gender = 0:1,
  Age = Ages (Gender+1)
  Pop = [1 \ 0 \ 0] * 1000
  MultMat = eye(3)
  for t= 1:MaxTime
    Age = Age + 1
    P0 = \exp(-(0.02 + 0.02*Age))
    P1 = \exp(-(0.02 + 0.01*Age))
    P2 = \exp(-(0.02 + 0.01*Age))
    Mat = [1-P0, P0, 0; 0, 1-P1, P1; P2, 0, 1-P2]
```

```
MultMat = MultMat * Mat
  end
  disp (sprintf ('Results for Gender = %g', Gender))
  Result = Pop*(MultMat)
end
% Example 9: Combined Fork Loop and Event state
disp ('Example 9: Combined Fork Loop and Event state')
P0 = 0.1
P1 = 0.8
P2 = 1 - P1
P3 = 0.1
t = 10
Pop = [4 \ 5 \ 1] * 100
Mat = [1-P0, P0*P1, P0*P2; 0, 1-P3*P2, P3*P2; 0, 0, 1]
Result = Pop*(Mat^t)
% Example 12: Nested split/join test
disp ('Example 12: Nested split/join test ')
P0 = 0.1
P1 = 0.2
P2 = 0.3
% claculate probability for the two joiners to be the same as P1
disp 'Joiner Probabilities P3, P4 Should be:'
syms JoinProb
solve ( JoinProb + JoinProb* (1-JoinProb) - P1 , JoinProb )
Pop = [1 \ 0 \ 0 \ 0] *1000
```

```
Mat = [1-P0, P0, 0, 0; 0, 1-P1, P1, 0; 0, 0, 1-P2, P2; 0, 0, 0, 0, 0]
1]
Result = Pop*(Mat^t)
% Example 12: Nested split/join test
% This example is simulated as a simpler chain of 4 stages similar to
% example 6
disp ('Example 12: Nested split/join test ')
MaxTime = 10
P0 = 0.1
P1 = 0.2
P2 = 1 - sqrt(7/10) %0.3
P3 = 1 - 2/5*sqrt(5) % 0.2
P4 = P3
P5 = P2
% Combined probabilities of transfer
P34 = P3 + (1-P3) *P4
P25 = P2 + (1-P2) * P5
P134 = P1*P34
% The following mapping of states occurs:
% A = 0
% B = 1,3,4
% C = 2,3,4
% D = 1,5
% E = 2.5
% F = 6
% Define the mapping Matrix from A-F to 0-6
            ABCDEF
Mapping = [ 1 0 0 0 0 0
                         응 0
            0 1 0 1 0 0
                          %1
            0 0 1 0 1 0
                          응2
            0 1 1 0 0 0
                         응3
            0 1 1 0 0 0
                        응4
            0 0 0 1 1 0 %5
            0 0 0 0 0 1 1 %6
Pop = [1 \ 1 \ 0 \ 0 \ 0]*500
                      В
                                      C
                                                    D
                                                               Ε
                                                                    F
Mat=[1-P0
                     PΟ
                                                                    0
응A
        0 1-P1-P34+P134
                            P1*(1-P34) P34*(1-P1)
                                                            P134
응B
                    0 1-P2-P34+P2*P34
                                                    0 P34*(1-P2)
        0
                                                                   Ρ2
응C
        0
                                     0 1-P1-P5+P1*P5 P1*(1-P5)
응D
```

```
0
               0
                          0
                                    0
                                        1-P25 P25
응E
               0
                          0
                                   0 0 1
     0
]%F
MultMat = Mat ^ MaxTime
DetailedResult = Pop*(MultMat)
% Convert the detailed result back to the mapped result
Result = DetailedResult * Mapping'
Res = Result ([1,2,3,7])
% Example 13: Split and join test without termination in a subprocess
% This example is similar to example 12 when there is no transition
from
% one sub-process
disp ('Example 13: Nested split/join test ')
MaxTime = 10
P0 = 0.1
P1 = 0.2
P2 = 0.3
P3 = 1 - 2/5*sqrt(5) % 0.2
P4 = P3
P5 = 0
% Combined probabilities of transfer
P34 = P3 + (1-P3) *P4
P25 = P2 + (1-P2) * P5
P134 = P1*P34
% The following mapping of states occurs:
% A = 0
% B = 1,3,4
% C = 2,3,4
% D = 1.5
% E = 2,5
% F = 6
% Define the mapping Matrix from A-F to 0-6
^{\circ} A B C D E F
Mapping = [ 1 0 0 0 0 0
                 응 0
        0 1 0 1 0 0 %1
        0 0 1 0 1 0 %2
        0 1 1 0 0 0 %3
        0 1 1 0 0 0
                 응4
```

```
0 0 0 1 1 0 %5
        0 0 0 0 0 1 ] %6
Pop = [1 \ 1 \ 0 \ 0 \ 0] *500
              В
                            D E F 0 0 0
                         С
Mat=[1-P0
             PΟ
                         0
     0 1-P1-P34+P134 P1*(1-P34) P34*(1-P1) P134 0
응B
         0 1-P2-P34+P2*P34
                                   0 P34*(1-P2) P2
응C
              0
                        0 1-P1-P5+P1*P5 P1*(1-P5) P5
     0
응D
     0
                         0
                                  0
                                       1-P25 P25
응E
     0
              0
                         0
                                  0
                                       0 1
]%F
MultMat = Mat ^ MaxTime
DetailedResult = Pop* (MultMat)
% Convert the detailed result back to the mapped result
Result = DetailedResult * Mapping'
Res = Result ([1,2,3,7])
% Example 15: Simple Table Example:
disp ('Example 15: Simple Table Example:')
Pop = [1 \ 0] * 100
t = 3
Outcome = [0 \ 0];
P0=0;
IndividualResult = [];
for Gender = 1:2,
  for AgeGroup = 1:3,
     P0 = P0 + 0.1
     Mat = [1-P0, P0; 0, 1]
     ResultAdd = Pop*(Mat^t)
     IndividualResult(:,Gender,AgeGroup) = ResultAdd;
  end
Outcome = sum(sum(IndividualResult,3),2)
OutcomeGender1 = sum(IndividualResult(:,1,:),3)
```

```
OutcomeAgeGroup1 = sum(IndividualResult(:,:,1),2)
OutcomeAgeGroup2 = sum(IndividualResult(:,:,2,:),2)
% Example 18: Tests Cost/QoL Wizard
disp ('Example 4: Tests Cost/QoL Wizard')
P0 = 1
P1 = 0.5
P2 = 0.5
t = 5
Pop = [1 \ 0 \ 0 \ 0] *100
Mat = [1-P0, P0, 0, 0, 0; 0, 1-P1, P1, 0; 0, 0, P2, 1-P2; 0, 0, 0, 0]
Result = Pop*(Mat^t)
```

# Results generated by running this code:

```
***********
*************
*************
Example 1: Simple Example:
*************
************
************
P0 =
  0.0717
t =
  3
Pop =
 900 100
Mat =
  0.9283 0.0717
       1.0000
Result =
 719.9587 280.0413
OldDeadNum =
  0
AverageAgeAtDeath =
 31.2540
```

```
************
************
Example 2: Multiple Transitions in a Chain
*************
************
************
P0 =
 0.1000
P1 =
 0.2000
t =
  5
Pop =
   500
 500
       0
Mat =
 0.9000
      0.1000
          0.2000
   0
      0.8000
   0
        \Omega
          1.0000
Result =
295.2450 295.2450 409.5100
***********
************
***********
Example 3: A fork state
************
************
```

\*\*\*\*\*\*\*\*\*\*\*\*\*

```
P0 =
  0.3000
P1 =
  0.6000
t =
  2
Pop =
 100 0
        0
Mat =
       0.3000
            0.6000
  0.1000
       1.0000
    0
    0
         0
            1.0000
Result =
  1.0000 33.0000 66.0000
************
*************
************
Example 4: Funny Loop Example
*************
***********
***********
P0 =
  0.1000
P1 =
  0.2000
```

```
P2 =
  0.3000
t =
  5
Pop =
 500 500
        500
Mat =
  0.9000
        0.1000
        0.8000
             0.2000
             0.7000
  0.3000
          0
Result =
 791.1000 393.1950 315.7050
************
*************
*************
Example 5a: Multiple Transitions in a Chain with an
Expression and Boolean Covariate
************
************
************
MaxTime =
  2
Pop =
    1000
             0
                    0
```

MultMat =

1 0 0 0 1 0 0 0 1

P0 =

0.6703

P1 =

0.6703

Mat =

MultMat =

P0 =

0.6703

P1 =

0.6703

Mat =

0.3297 0.6703 0 0 0.3297 0.6703 0 0 1.0000

```
MultMat =
   0
            0
                     1.0000
Results for Gender = 0
Result =
 108.6889 441.9822 449.3290
Pop =
       1000
                   0
                              0
MultMat =
    1 0
               0
    0
         1
    0
         0
               1
P0 =
  0.4966
P1 =
  0.4066
Mat =
   0.5034 0.4966 0
0 0.5934 0.4066
0 0 1.0000
MultMat =
   0.5034 0.4966
0 0.5934
```

0.5934 0.4066

0

1.0000 0 0 P0 =0.4966 P1 = 0.4066 Mat =0.5034 0.4966 0 0.5934 0.4066 0 0 1.0000 MultMat = 0.2534 0.5447 0.2019 0.3522 0.6478 0  $\Omega$  $\Omega$ 1.0000 Results for Gender = 1Result = 253.4264 544.6771 201.8965 \*\*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\* Example 5b: Multiple Transitions in a Chain with an Expression and Continuous Covariate \*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\* MaxTime =2

Ages =

60 45 Age = 60 Pop = 1000 0 0 MultMat = 1 0 0 0 1 0 0 0 1 Age = 61 P0 = 0.1541 P1 = 0.0455 Mat = 0.8459 0.1541 0 0.9545 0 0 1.0000 MultMat = 0.8459 0.1541

0.9545 0.0455

0

0 0 1.0000 Age = 62 P0 = 0.1496 P1 = 0.0433 Mat = 0.8504 0.1496 0 0 0.9567 0.0433 0 0 1.0000 1.0000 MultMat = 0.7194 0.2740 0.0067 0 0.9132 0.0868 0 0 1.0000 Results for Gender = 0Result = 719.3598 273.9693 6.6709 Age = 45 Pop =

1000 0

0

MultMat = 1 0

1 0 0 0 1 0 0 0 1

Age =

46

P0 =

0.2417

P1 =

0.0963

Mat =

0.75830.2417000.90370.0963001.0000

MultMat =

Age =

47

P0 =

0.2346

P1 = 0.0916 Mat = 0.7654 0.2346 0.9084 0.0916 0 0 1.0000 MultMat = 0.5804 0.3974 0.0221 0.8209 0.1791 1.0000 Results for Gender = 1Result = 580.4146 397.4372 22.1482 \*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\*\* Example 6: Multiple Transitions in a Long Chain with an Expression Containing a Continuous Covariate \*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\*\* \*\*\*\*\*\*\*\*\*\*\*\* MaxTime =3 Ages = 60 45 Age = 60

| Pop  | _                |                  |                        |                            |                            |   |  |  |  |  |
|------|------------------|------------------|------------------------|----------------------------|----------------------------|---|--|--|--|--|
| гор  |                  |                  |                        |                            |                            | _ |  |  |  |  |
|      | 10               | 00               |                        | 0                          | 0                          | 0 |  |  |  |  |
| Mult | tMat =           |                  |                        |                            |                            |   |  |  |  |  |
|      | 1<br>0<br>0<br>0 | 0<br>1<br>0<br>0 | 0<br>0<br>1<br>0       | 0<br>0<br>0<br>1           |                            |   |  |  |  |  |
| Age  | =                |                  |                        |                            |                            |   |  |  |  |  |
|      | 61               |                  |                        |                            |                            |   |  |  |  |  |
| P0 = | =                |                  |                        |                            |                            |   |  |  |  |  |
|      | 0.1541           |                  |                        |                            |                            |   |  |  |  |  |
| P1 = | =                |                  |                        |                            |                            |   |  |  |  |  |
|      | 0.0455           |                  |                        |                            |                            |   |  |  |  |  |
| P2 = | =                |                  |                        |                            |                            |   |  |  |  |  |
|      | 0.0455           |                  |                        |                            |                            |   |  |  |  |  |
| Mat  | =                |                  |                        |                            |                            |   |  |  |  |  |
|      | 0.8459           | 0.               | 1541<br>9545<br>0<br>0 | 0<br>0.0455<br>0.9545<br>0 | 0<br>0<br>0.0455<br>1.0000 |   |  |  |  |  |
| Mult | MultMat =        |                  |                        |                            |                            |   |  |  |  |  |
|      | 0.8459           | 0.               | 1541<br>9545<br>0      | 0<br>0.0455<br>0.9545      | 0<br>0<br>0.0455           |   |  |  |  |  |

0 0 0 1.0000

Age =

62

P0 =

0.1496

P1 =

0.0433

P2 =

0.0433

Mat =

0 0.8504 0.1496 0 0 0.9567 0.0433 0 0.9567 0 0 0.0433 0 0 0 1.0000

MultMat =

Age =

63

P0 =

0.1451

```
P1 =
    0.0412
P2 =
    0.0412
Mat =
    0.8549
             0.1451
                                      0
         0
              0.9588
                       0.0412
                                      0
                       0.9588
         0
                   0
                                 0.0412
                   0
         0
                                 1.0000
                            0
MultMat =
    0.6149
             0.3671
                       0.0177
                                 0.0003
         0
              0.8756
                       0.1190
                                 0.0055
                  0
                        0.8756
         0
                                 0.1244
         0
                  0
                            0
                                 1.0000
Results for Gender = 0
Result =
  614.9460 367.1033 17.6761 0.2747
Age =
    45
Pop =
        1000
                      0
                                              0
                                 0
MultMat =
     1 0
                0
                      0
```

| 0 | 1 | 0 | 0 |
|---|---|---|---|
| 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 |

Age =

46

P0 =

0.2417

P1 =

0.0963

P2 =

0.0963

Mat =

MultMat =

Age =

47

P0 =

P1 = 0.0916

0.2346

P2 =

0.0916

Mat =

0.7654 0.2346 0 0 0.0916 0.9084 0.9084 0 0 0 0 0.9084 0.0916 0 0 0 1.0000

MultMat =

0.5804 0.3974 0.0221 0 0 0.8209 0.1703 0.0088 0 0 0.8209 0.1791 0 0 0 1.0000

Age =

48

P0 =

0.2276

P1 =

0.0872

P2 =

0.0872

Mat =

| 0      | 0      | 0.2276 | 0.7724 |
|--------|--------|--------|--------|
| 0      | 0.0872 | 0.9128 | 0      |
| 0.0872 | 0.9128 | 0      | 0      |
| 1.0000 | 0      | 0      | 0      |

MultMat =

| 0.4483 | 0.4949 | 0.0549 | 0.0019 |
|--------|--------|--------|--------|
| 0      | 0.7493 | 0.2270 | 0.0237 |
| 0      | 0      | 0.7493 | 0.2507 |
| 0      | 0      | 0      | 1.0000 |

Results for Gender = 1

Result =

448.2904 494.9205 54.8587 1.9305

\*\*\*\*\*\*\*\*\*\*\*

MaxTime =

3

Ages =

60 45

Age =

60

 0.7106
 0.2894
 0

 0
 0.4674
 0.5326

 0.5326
 0
 0.4674

MultMat =

Age = 62 P0 = 0.2837 P1 = 0.5273 P2 = 0.5273 Mat = 

 0.7163
 0.2837
 0

 0
 0.4727
 0.5273

 0.5273
 0
 0.4727

 MultMat = 

 0.5090
 0.3384
 0.1526

 0.2808
 0.2209
 0.4982

 0.6280
 0.1511
 0.2209

 Age = 63 P0 = 0.2780 P1 =

0.5220

```
P2 =
     0.5220
Mat =

\begin{array}{ccccc}
0.7220 & 0.2780 & 0 \\
0 & 0.4780 & 0.5220 \\
0.5220 & 0 & 0.4780
\end{array}

MultMat =
     0.4472 0.3033
0.4628 0.1837
0.5687 0.2468
                                 0.2496
                                 0.3535
                                 0.1845
Results for Gender = 0
Result =
   447.1718 303.2561 249.5721
Age =
     45
Pop =
           1000
                          0
                                                0
MultMat =
       1
               0
                        0
       0
               1
                        0
       0
               0
                        1
```

Age =

46

P0 = 0.3906 P1 = 0.6188 P2 =0.6188 Mat = 

 0.6094
 0.3906
 0

 0
 0.3812
 0.6188

 0.6188
 0
 0.3812

 MultMat = 

 0.6094
 0.3906
 0

 0
 0.3812
 0.6188

 0.6188
 0
 0.3812

 Age = 47 P0 = 0.3829 P1 = 0.6126

P2 =

0.6126

Mat =

0.6171 0.3829 0 0 0.3874 0.6126 0.6126 0 0.3874

MultMat =

0.37600.38460.23930.37910.14770.47320.61540.23690.1477

Age =

48

P0 =

0.3753

P1 =

0.6065

P2 =

0.6065

Mat =

 0.6247
 0.3753
 0

 0
 0.3935
 0.6065

 0.6065
 0
 0.3935

MultMat =

```
0.3801
       0.2925
             0.3275
  0.5238
        0.2004
             0.2758
  0.4740
        0.3242
             0.2018
Results for Gender = 1
Result =
 380.0611 292.4802 327.4586
************
*************
************
Example 9: Combined Fork Loop and Event state
************
************
************
P0 =
  0.1000
P1 =
  0.8000
P2 =
  0.2000
P3 =
  0.1000
t =
  10
Pop =
 400
     500
        100
```

```
Mat =
  0.9000 0.0800 0.0200
0 0.9800 0.0200
     0
          0
              1.0000
Result =
 139.4714 595.8942 264.6345
************
***********
************
Example 12: Nested split/join test
*************
*************
************
P0 =
  0.1000
P1 =
  0.2000
P2 =
  0.3000
Joiner Probabilities P3, P4 Should be:
ans =
1-2/5*5^{(1/2)}
1+2/5*5^{(1/2)}
t =
  10
```

Pop = 1000 0 0 Mat = 0.9000 0.1000 0 0.8000 0.2000 0 0 0.7000 0 0 0.3000 0 1.0000 0 0 Result = 348.6784 241.3043 162.1776 247.8397 Example 12: Nested split/join test MaxTime = 10 P0 = 0.1000 P1 = 0.2000 P2 = 0.1633 P3 = 0.1056

P4 =

0.1633

| 0 1622   | 0     |         | 0     |       |     |     |     | 0  |       | 0   | . 6 | 69         | 3       |               |      | 0        | . 1     | 6        | 73     |          |            |
|----------|-------|---------|-------|-------|-----|-----|-----|----|-------|-----|-----|------------|---------|---------------|------|----------|---------|----------|--------|----------|------------|
| 0.1633   | 0     |         | 0     |       |     |     |     | 0  |       |     |     |            | 0       |               |      | 0        | . 7     | 0(       | 0 0    |          |            |
| 0.3000   | 0     |         | 0     |       |     |     |     | 0  |       |     |     |            | 0       |               |      |          |         |          | 0      |          |            |
| 1.0000   |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| MultMat  | =     |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| 0.34     | 187   | 0.12    | 97    |       | 0   | .0  | 74  | 15 |       | 0   | .0  | 74         | 15      |               |      | 0        | . 0     | 95       | 58     |          |            |
| 0.2768   | 0     | 0.01    | 15    |       | 0   | .0  | 35  | 6  |       | 0   | .0  | 35         | 6       |               |      | 0        | . 1     | 0.9      | 96     |          |            |
| 0.8077   | 0     |         | 0     |       | 0   | .0  | 18  | 30 |       |     |     |            | 0       |               |      | 0        | . 0     | 55       | 57     |          |            |
| 0.9263   | 0     |         | 0     |       |     |     |     | 0  |       | 0   | .0  | 18         | 30      |               |      | 0        | . 0     | 55       | 57     |          |            |
| 0.9263   | 0     |         | 0     |       |     |     |     | 0  |       |     |     |            | 0       |               |      | 0        | . 0     | 28       | 32     |          |            |
| 0.9718   | 0     |         | 0     |       |     |     |     | 0  |       |     |     |            | 0       |               |      |          |         |          | 0      |          |            |
| 1.0000   |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| Detailed | lResi | ult =   |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
|          |       | 70.60   | 10    |       | 55  | .0  | 42  | 27 |       | 55  | .0  | 42         | 27      |               | 10   | )2       | . 7     | 35       | 57     |          |            |
| 542.2386 | )     |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| Result = | =     |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
|          |       | 125.64  |       | 1     | 57  | .7  | 78  | 35 | 1     | 25  | . 6 | 43         | 37      |               | 12   | 25       | . 6     | 43       | 37     |          |            |
| 157.7785 | ) 54  | 42.2386 | )     |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| Res =    |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| 174.33   | 392   | 125.64  | 37    | 1     | 57  | .7  | 78  | 35 | 5     | 42  | . 2 | 38         | 86      |               |      |          |         |          |        |          |            |
| *****    |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| *****    |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| Example  |       |         |       |       |     |     |     |    |       |     |     | <b>↓</b> J | ـ ـ ـ ـ | <b>.</b> . l. | ا۔ ب | <b>.</b> | مليد مل | <b>.</b> | مليا ا | <b>.</b> | L J.       |
| *****    |       |         |       |       |     |     |     |    |       |     |     |            |         |               |      |          |         |          |        |          |            |
| *****    | ***   | *****   | * * * | * * * | * * | * * | * * | *  | * * * | * * | **  | * *        | *       | * *           | * *  | *        | * *     | * >      | * *    | * *      | <b>*</b> * |

MaxTime = 10 P0 = 0.1000 P1 = 0.2000 P2 = 0.3000 P3 = 0.1056 P4 = 0.1056 P5 = 0 P34 = 0.2000 P25 = 0.3000

P134 =

0.0400

| Mapping =                  |                                 |                            |                                 |                                 |                            |        |  |  |  |  |
|----------------------------|---------------------------------|----------------------------|---------------------------------|---------------------------------|----------------------------|--------|--|--|--|--|
| 1<br>0<br>0<br>0<br>0<br>0 | 0<br>1<br>0<br>1<br>1<br>0<br>0 | 0<br>0<br>1<br>1<br>1<br>0 | 0<br>1<br>0<br>0<br>0<br>0<br>1 | 0<br>0<br>1<br>0<br>0<br>1<br>0 | 0<br>0<br>0<br>0<br>0<br>0 |        |  |  |  |  |
| Pop =                      |                                 |                            |                                 |                                 |                            |        |  |  |  |  |
| 500                        | 500                             | 0                          | 0                               | 0                               | 0                          |        |  |  |  |  |
| Mat =                      |                                 |                            |                                 |                                 |                            |        |  |  |  |  |
| 0.9                        | 000                             | 0.1000 0                   |                                 | 0                               | 0                          | 0      |  |  |  |  |
| 0                          | 0                               | 0.6400                     | 0.                              | 1600                            | 0.1600                     | 0.0400 |  |  |  |  |
| 0.3000                     | 0                               | 0                          | 0.5600                          |                                 | 0                          | 0.1400 |  |  |  |  |
| 0                          | 0                               | 0                          |                                 | 0                               | 0.8000                     | 0.2000 |  |  |  |  |
| 0.3000                     | 0                               | 0                          |                                 | 0                               | 0                          | 0.7000 |  |  |  |  |
| 1.0000                     | 0                               | 0                          |                                 | 0                               | 0                          | 0      |  |  |  |  |
| 1.0000                     |                                 |                            |                                 |                                 |                            |        |  |  |  |  |
| MultMat                    | =                               |                            |                                 |                                 |                            |        |  |  |  |  |
| 0.3                        | 487                             | 0.1297                     | 0.0                             | 0560                            | 0.1116                     | 0.1062 |  |  |  |  |
| 0.7344                     | 0                               | 0.0115                     | 0.0                             | 0170                            | 0.0958                     | 0.1413 |  |  |  |  |
| 0.9718                     | 0                               | 0                          | 0.0                             | 0030                            | 0                          | 0.0252 |  |  |  |  |
| 0.7344                     | 0                               | 0                          |                                 | 0                               | 0.1074                     | 0.1583 |  |  |  |  |

```
0
     0
           0
                       0
                          0.0282
0.9718
     0
           0
                 0
                       0
                             0
1.0000
DetailedResult =
       70.6010 36.5085 103.7382 123.7069
 174.3392
491.1061
Result =
 174.3392 174.3392
            160.2155 107.1095 107.1095
227.4451 491.1061
Res =
 174.3392 174.3392 160.2155 491.1061
***********
****************
************
Example 15: Simple Table Example:
*************
************
***********
Pop =
 100
      0
t =
   3
P0 =
  0.1000
Mat =
```

ResultAdd =

72.9000 27.1000

P0 =

0.2000

Mat =

0.8000 0.2000 0 1.0000

ResultAdd =

51.2000 48.8000

P0 =

0.3000

Mat =

0.7000 0.3000 0 1.0000

ResultAdd =

34.3000 65.7000

P0 =

0.4000

Mat =

ResultAdd =

21.6000 78.4000

P0 =

0.5000

Mat =

0.5000 0.5000 0 1.0000

ResultAdd =

12.5000 87.5000

P0 =

0.6000

Mat =

0.4000 0.6000 0 1.0000

ResultAdd =

6.4000 93.6000

Outcome =

198.9000 401.1000

```
OutcomeGender1 =
 158.4000
 141.6000
OutcomeAgeGroup1 =
 94.5000
 105.5000
OutcomeAgeGroup2 =
 63.7000
 136.3000
***********
*************
***********
Example 4: Tests Cost/QoL Wizard
**************
*************
************
P0 =
  1
P1 =
  0.5000
P2 =
  0.5000
t =
  5
Pop =
```

| 100    | 0 | 0      | 0       |         |
|--------|---|--------|---------|---------|
| Mat =  |   |        |         |         |
| riac   |   |        |         |         |
|        | 0 | 1.0000 | 0       | 0       |
|        | 0 | 0.5000 | 0.5000  | 0       |
|        | 0 | 0      | 0.5000  | 0.5000  |
|        | 0 | 0      | 0       | 1.0000  |
|        |   |        |         |         |
| Result | = |        |         |         |
|        | 0 | 6.2500 | 25.0000 | 68.7500 |