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Program Structures & Algorithms

Fall 2021

Assignment No. 2

◉ Task (List down the tasks performed in the Assignment)

1. You are to implement three methods of a class called Timer. Please see the skeleton class that I created in the repository. Timer is invoked from a class called Benchmark_Timer which implements the Benchmark interface.
2. Implement InsertionSort (in the InsertionSort class) by simply looking up the insertion code used by Arrays.sort. You should use the helper.swap method although you could also just copy that from the same source code. You should of course run the unit tests in InsertionSortTest.
3. Implement a main program (or you could do it via your own unit tests) to actually run the following benchmarks: measure the running times of this sort, using four different initial array ordering situations: random, ordered, partially-ordered and reverse-ordered. I suggest that your arrays to be sorted are of type Integer. Use the doubling method for choosing n and test for at least five values of n. Draw any conclusions from your observations regarding the order of growth.
4. Report on your observations and show screenshots of the runs and also the unit tests.

Relationship Conclusion:

1. Time cost t 's relation with different array types, under same array length, is:

$$t(\text{ordered}) < t(\text{partially - ordered}) < t(\text{random}) < t(\text{reverse - ordered})$$

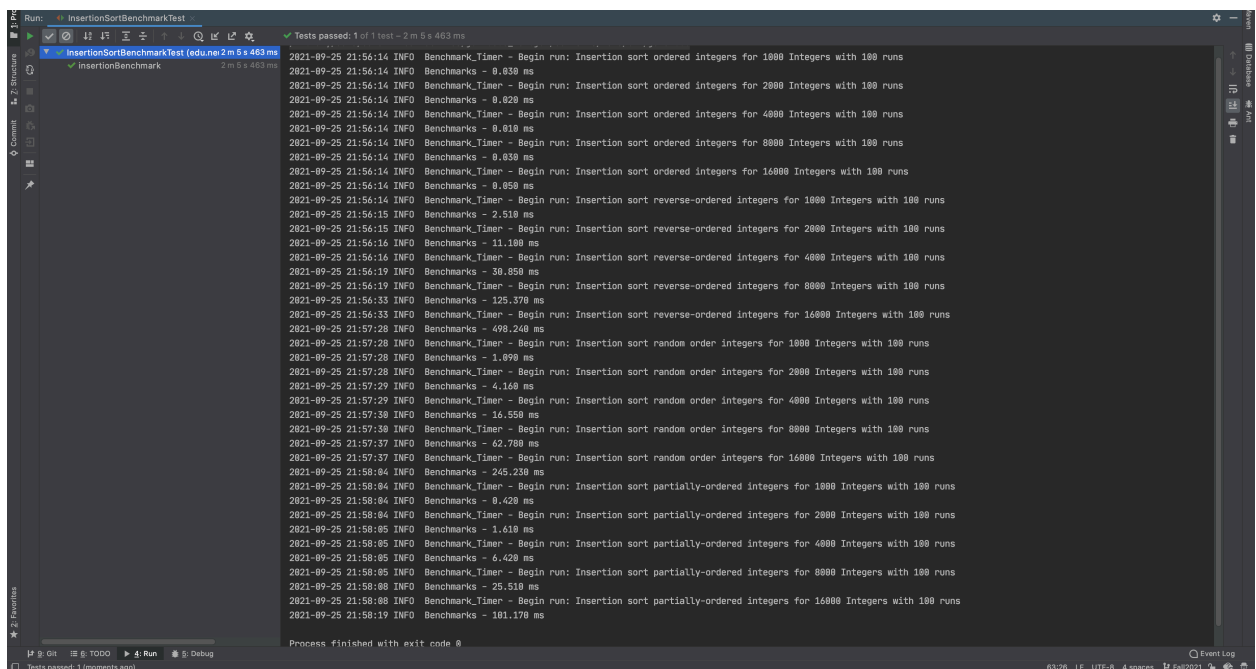
2. When we are using the doubling method for choosing N , $\log t$ increases linearly with $\log N$, and we have the following k value, which is the growth rate of insertion sort algorithms:

$$\bar{k} = 0.51383778 \approx \frac{1}{2}$$

*As for the $\log t$ with ordered array on the \log/\log graph, array size and time t are both too small, it is not accurate. So, I do not take using it to calculate the average value of k .

Evidence to support the conclusion:

1. Output/Test Result (Snapshot of Code output in the terminal)



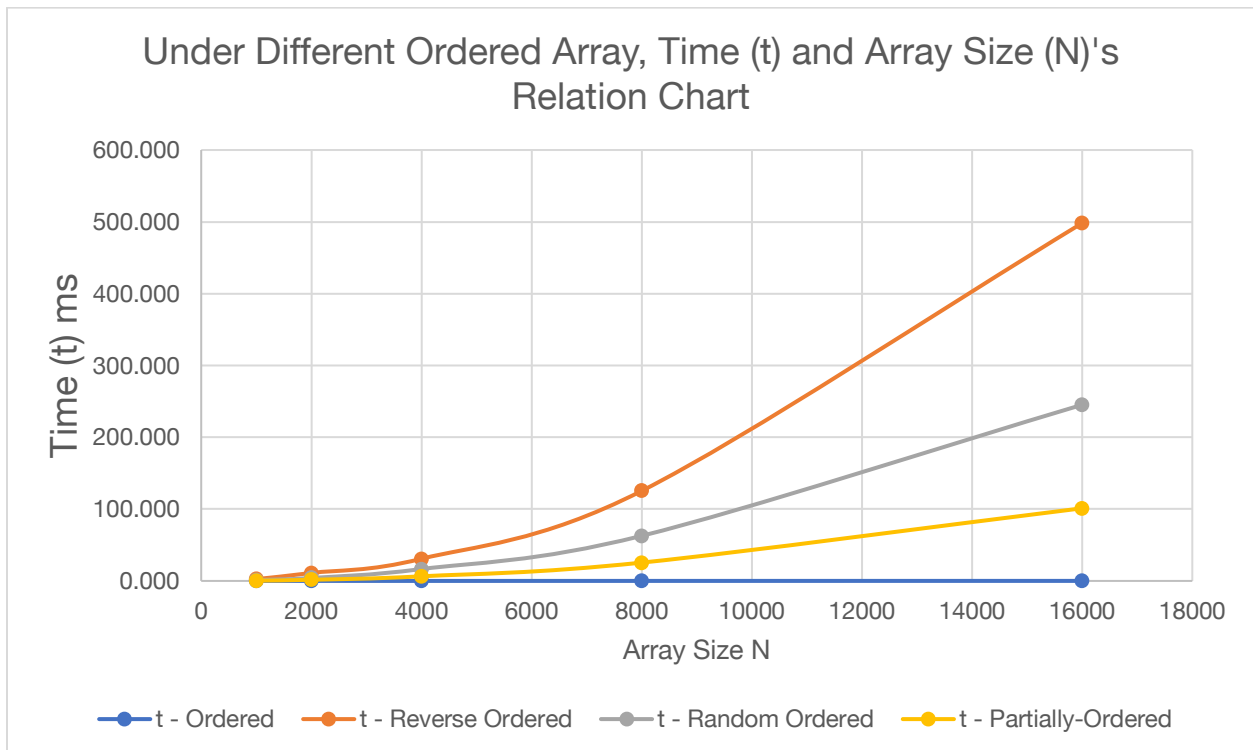
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Run: InsertionSortBenchmarkTest
Tests passed: 1 of 1 test - 2 m 5 s 463 ms

InsertionSortBenchmarkTest (edu.neu.2 m 5 s 463 ms)
  InsertionBenchmark
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort ordered integers for 1000 Integers with 100 runs
    2021-09-25 21:56:14 INFO Benchmarks - 0.030 ms
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort ordered integers for 2000 Integers with 100 runs
    2021-09-25 21:56:14 INFO Benchmarks - 0.020 ms
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort ordered integers for 4000 Integers with 100 runs
    2021-09-25 21:56:14 INFO Benchmarks - 0.010 ms
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort ordered integers for 8000 Integers with 100 runs
    2021-09-25 21:56:14 INFO Benchmarks - 0.030 ms
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort ordered integers for 16000 Integers with 100 runs
    2021-09-25 21:56:14 INFO Benchmarks - 0.050 ms
    2021-09-25 21:56:14 INFO Benchmark_Timer - Begin run: Insertion sort reverse-ordered integers for 1000 Integers with 100 runs
    2021-09-25 21:56:15 INFO Benchmarks - 2.510 ms
    2021-09-25 21:56:15 INFO Benchmark_Timer - Begin run: Insertion sort reverse-ordered integers for 2000 Integers with 100 runs
    2021-09-25 21:56:16 INFO Benchmarks - 11.100 ms
    2021-09-25 21:56:16 INFO Benchmark_Timer - Begin run: Insertion sort reverse-ordered integers for 4000 Integers with 100 runs
    2021-09-25 21:56:19 INFO Benchmarks - 30.050 ms
    2021-09-25 21:56:19 INFO Benchmark_Timer - Begin run: Insertion sort reverse-ordered integers for 8000 Integers with 100 runs
    2021-09-25 21:56:33 INFO Benchmarks - 125.370 ms
    2021-09-25 21:56:33 INFO Benchmark_Timer - Begin run: Insertion sort reverse-ordered integers for 16000 Integers with 100 runs
    2021-09-25 21:57:28 INFO Benchmarks - 490.240 ms
    2021-09-25 21:57:28 INFO Benchmark_Timer - Begin run: Insertion sort random order integers for 1000 Integers with 100 runs
    2021-09-25 21:57:28 INFO Benchmarks - 1.090 ms
    2021-09-25 21:57:28 INFO Benchmark_Timer - Begin run: Insertion sort random order integers for 2000 Integers with 100 runs
    2021-09-25 21:57:29 INFO Benchmarks - 4.160 ms
    2021-09-25 21:57:29 INFO Benchmark_Timer - Begin run: Insertion sort random order integers for 4000 Integers with 100 runs
    2021-09-25 21:57:30 INFO Benchmarks - 16.550 ms
    2021-09-25 21:57:30 INFO Benchmark_Timer - Begin run: Insertion sort random order integers for 8000 Integers with 100 runs
    2021-09-25 21:57:37 INFO Benchmarks - 62.780 ms
    2021-09-25 21:57:37 INFO Benchmark_Timer - Begin run: Insertion sort random order integers for 16000 Integers with 100 runs
    2021-09-25 21:58:04 INFO Benchmarks - 245.230 ms
    2021-09-25 21:58:04 INFO Benchmark_Timer - Begin run: Insertion sort partially-ordered integers for 1000 Integers with 100 runs
    2021-09-25 21:58:04 INFO Benchmarks - 0.420 ms
    2021-09-25 21:58:04 INFO Benchmark_Timer - Begin run: Insertion sort partially-ordered integers for 2000 Integers with 100 runs
    2021-09-25 21:58:05 INFO Benchmarks - 1.610 ms
    2021-09-25 21:58:05 INFO Benchmark_Timer - Begin run: Insertion sort partially-ordered integers for 4000 Integers with 100 runs
    2021-09-25 21:58:05 INFO Benchmarks - 6.420 ms
    2021-09-25 21:58:05 INFO Benchmark_Timer - Begin run: Insertion sort partially-ordered integers for 8000 Integers with 100 runs
    2021-09-25 21:58:08 INFO Benchmarks - 25.510 ms
    2021-09-25 21:58:08 INFO Benchmark_Timer - Begin run: Insertion sort partially-ordered integers for 16000 Integers with 100 runs
    2021-09-25 21:58:19 INFO Benchmarks - 101.170 ms

Process finished with exit code 0
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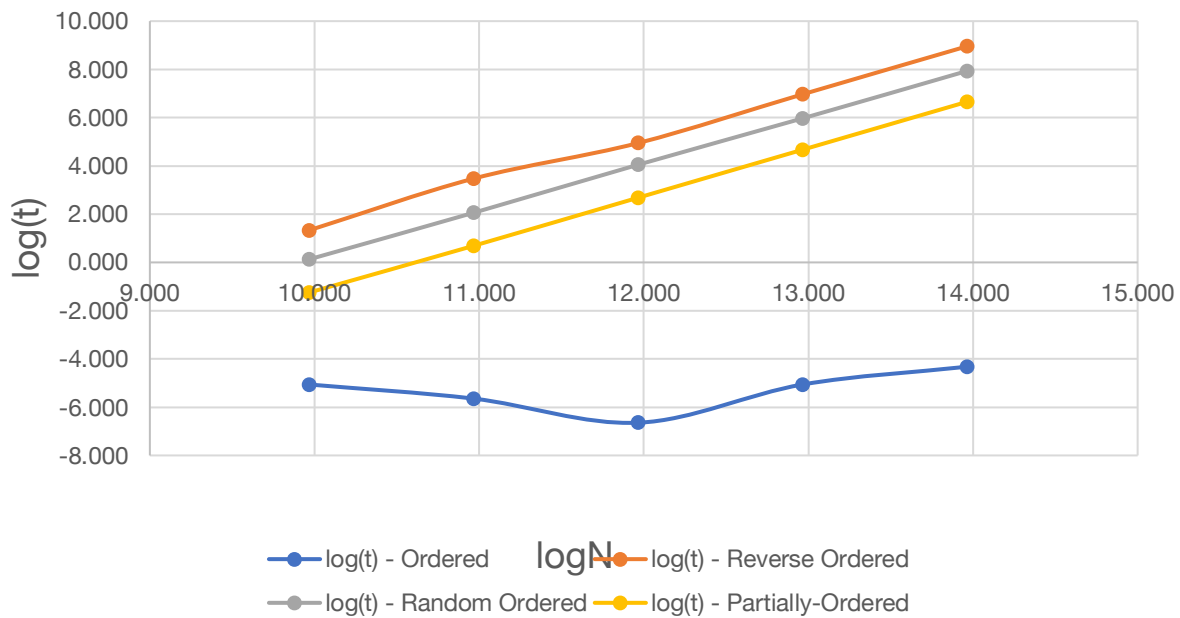
2. **Graphical Representation**(Observations from experiments should be tabulated and analyzed by plotting graphs(usually in excel) to arrive on the relationship conclusion)

Under Different Ordered Array, Time (t) and Array Size (N)'s Relation Table				
N	t - Ordered	t - Reverse Ordered	t - Random Ordered	t - Partially-Ordered
1000	0.030	2.460	1.000	0.410
2000	0.020	9.140	4.040	1.580
4000	0.020	30.240	14.850	6.240
8000	0.030	120.670	59.560	24.250
16000	0.060	484.520	233.490	96.630



Under Different Ordered Array, Time ($\log t$) and Array Size ($\log N$)'s Relation Chart				
$\log N$	$\log t$ - Ordered	$\log t$ - Reverse Ordered	$\log t$ - Random Ordered	$\log t$ - Partially-Ordered
9.966	-5.059	1.328	0.124	-1.252
10.966	-5.644	3.472	2.057	0.687
11.966	-6.644	4.947	4.049	2.683
12.966	-5.059	6.970	5.972	4.673
13.966	-4.322	8.961	7.938	6.661

Under Different Ordered Array, Time (logt) and Array Size (logN)'s Relation Chart



Unit tests result:(Snapshot of successful unit test run)

