

# Simulating Collisional Dark Matter

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September 19, 2018

# Contents

<b>1</b>	<b>Objectives</b>	<b>3</b>
1.1	General Objective . . . . .	3
1.2	Specific Objectives . . . . .	3
<b>2</b>	<b>Introduction</b>	<b>4</b>
2.1	The Boltzmann Equation . . . . .	4
2.2	Mesoscopic Modeling . . . . .	4
2.3	Lattice Automata and Lattice Boltzmann . . . . .	4
2.4	BGK Approximation . . . . .	4
<b>3</b>	<b>The Lattice Boltzmann Algorithm</b>	<b>5</b>
3.1	The Mass Integral and the Poisson Equation . . . . .	5
3.2	Kick and Drift . . . . .	5
3.3	The Collisional Step . . . . .	5
3.4	Units and Initial Conditions . . . . .	5
<b>4</b>	<b>Results</b>	<b>6</b>
4.1	No Collisional . . . . .	6
4.2	$\tau = 10$ . . . . .	6
4.3	$\tau = 100$ . . . . .	6
4.4	$\tau = 250$ . . . . .	6
4.5	$\tau = 500$ . . . . .	6
4.6	$\tau = 1000$ . . . . .	6
<b>5</b>	<b>Conclusions</b>	<b>7</b>
5.1	A Numerically Stable Simulation . . . . .	7

# Chapter 1

## Objectives

### 1.1 General Objective

To simulate the phase space of a collisional dark matter fluid using a Lattice-Boltzmann Method

### 1.2 Specific Objectives

- To implement a Lattice-Boltzmann simulation using a 4-dimensional phase space and a varying collisional term.
- To implement a Lattice-Boltzmann simulation using a 6-dimensional phase space and a varying collisional term.
- To study the dynamical behavior of a dark matter fluid using different equilibrium distributions in the collisional term.
- To compare the phase space of a collisional dark matter fluid with its collisionless version.

# Chapter 2

## Introduction

### 2.1 The Boltzmann Equation

### 2.2 Mesoscopic Modeling

Traditionally, fluid dynamics have been modeled using the Navier-Stokes equation, or some modification of it.

### 2.3 Lattice Automata and Lattice Boltzmann

### 2.4 BGK Approximation

# Chapter 3

## The Lattice Boltzmann Algorithm

### 3.1 The Mass Integral and the Poisson Equation

asdfasdf

### 3.2 Kick and Drift

asd

### 3.3 The Collisional Step

asd

### 3.4 Units and Initial Conditions

# Chapter 4

## Results

4.1 No Collisional

4.2  $\tau = 10$

4.3  $\tau = 100$

4.4  $\tau = 250$

4.5  $\tau = 500$

4.6  $\tau = 1000$

4.7 Different Equilibrium Distributions

# Chapter 5

## Conclusions

### 5.1 A Numerically Stable Simulation