

# DISCRETE MATHEMATICS (DM)

Formulas, Rules, & Principles: Overview (limited to Course reqs.)

SETS

$$A = \{x \mid x \text{ is a positive, even integer}\}$$

A equals the set of all x such that x is a positive, even integer

Sets can contain any elements; the types don't have to match.

$$x \in A$$

↑ x is in the set A

$$y \notin A$$

↑ y is NOT in the set A

MULT.  
PRINCIPLE

Multiplication Principle: If an activity/action can be done in t ways successive steps and step 1 can be done in  $n_1$  ways, Step 2 in  $n_2$  ways..., and step t can be done in  $n_t$  ways, then the number of different possibilities of the activity/actions is  $n_1 \cdot n_2 \cdots \cdot n_t$

ADD.  
PRINCIPLE

Addition Principle: Suppose that  $X_1, \dots, X_t$  are sets and that the i<sup>th</sup> set  $X_i$  has  $n_i$  elements. If  $\{X_1, \dots, X_t\}$  is a pairwise disjoint family (i.e. if  $i \neq j, X_i \cap X_j = \emptyset$ ), the number of possible elements that can be selected from  $X_1$  or... $X_t$  is  $n_1 + \dots + n_t$

↑  
If i does not equal j, then the intersection of  $X_i$  and  $X_j$  is empty.

PERMS  
&  
COMS

Permutation: A permutation of n distinct elements

$x_1 \dots x_n$  is an ordering of the n elements  $x_1 \dots x_n$

• alt. def. A way in which a set can be arranged.

Combination:

## Permutation Formula

$$nPr \rightarrow \frac{n!}{(n-r)!}$$

The "!" denotes factorial.

This symbol indicates a number multiplied by all of its predecessors up until "1".

## Combination Formula

$$nCr \rightarrow \frac{n!}{(n-r)!r!}$$

$$\text{or } C(k+t-1, + - 1) \rightarrow \frac{(k+t-1)!}{(k-1)! (t-0)!}$$

- $n$  = the total # of distinct objects
- $R$  = the # selected