

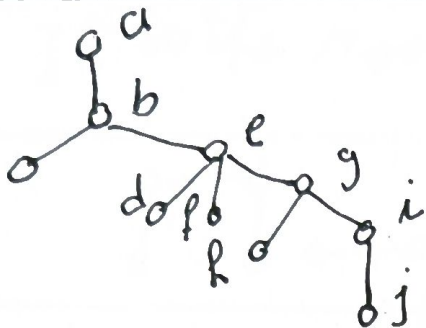
HW 14

Solution HW 9.1  
Discrete Mathematics

P6) If either  $m$  or  $n$  or both, equals 1

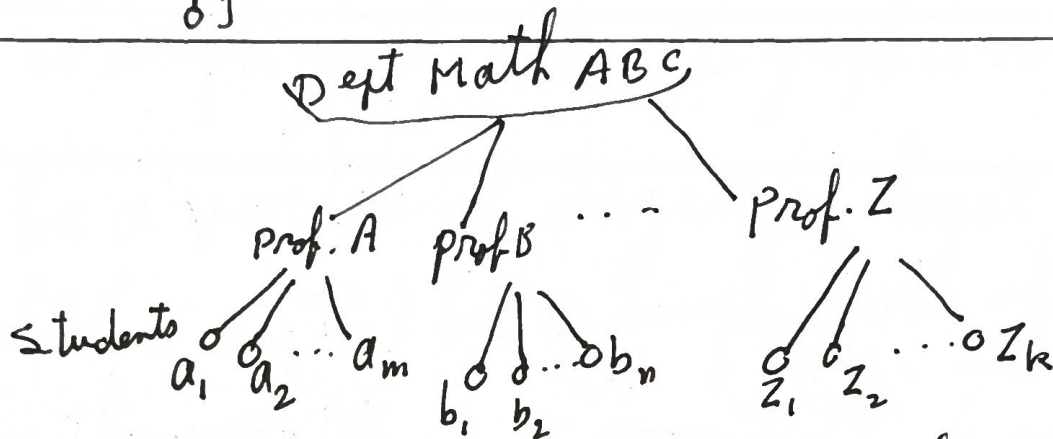


P10)



5

P12)



P30) A tree cannot contain a subgraph homeomorphic to  $K_{3,3}$  and  $K_5$ .  
Since Tree does not contain cycles.

P31) A terminal vertex has degree 1

Q. M.

# HW 15

HW 9.2

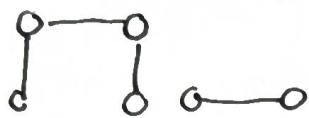
Discrete Mathematics

P12) sibling of  $f$ :  $e, g$

sibling  $h$ :  $i$

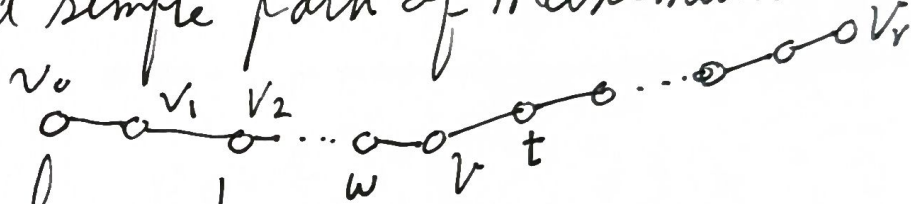
P18) It is the root.

P24)



P28) A tree is simple graph. Thus the graph is not a tree.

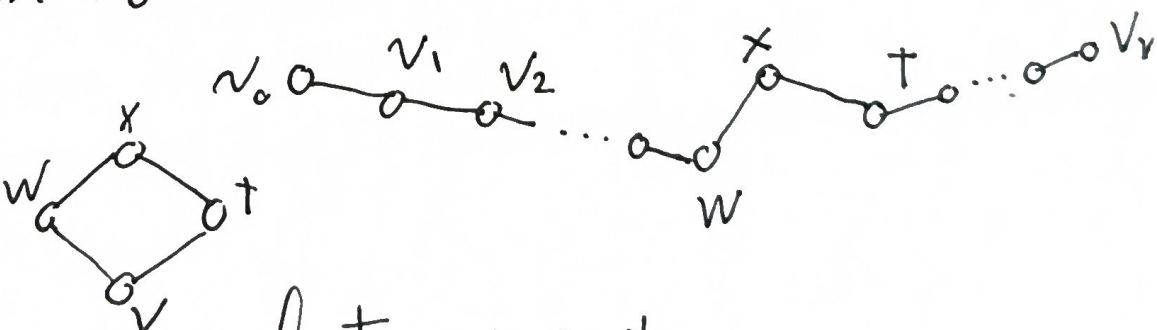
P35) Let  $v$  be a vertex of degree at least 2 in a tree  $G$  and let  $P = (v_0, \dots, v_n)$  be a simple path of maximum length passing through  $v$ .



Since  $G$  is a tree,  $P$  is not a cycle and, since  $v$  has degree at least 2,  $v \neq v_0$  and  $v \neq v_n$ .

If removing  $v$  and all edges incident on  $v$  leaves a connected graph, then there is a simple path, distinct from  $P$ , from  $v_0$  to  $v_n$ .

Thus we have a cycle



Therefore  $v$  is an articulation point.

Def: A vertex  $v$  in a connected  $G$  is an articulation point if the removal of  $v$  and all edges incident on  $v$  disconnects  $G$ .

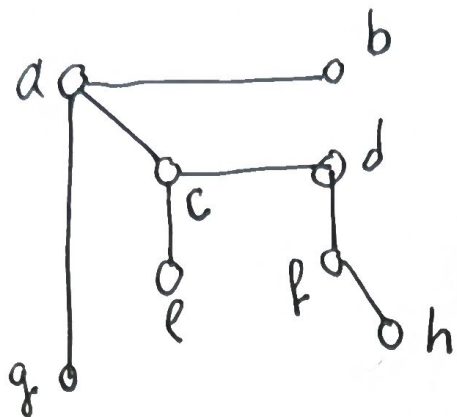
D. M.



# HW16

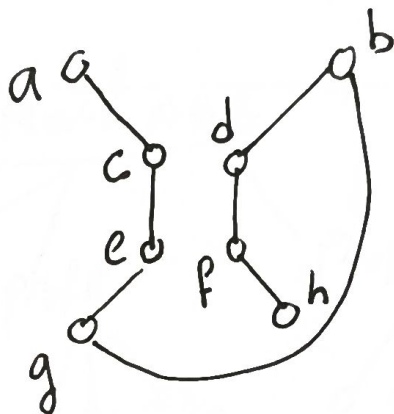
## 9.3 Discrete Mathematics

P2)

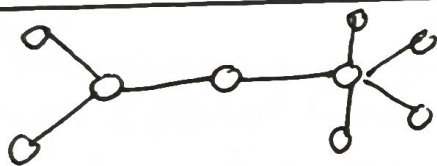


chbgadfe

P6) hfdbgeca



P8)



P18) If  $T$  is a tree, every ordering with the same initial vertex produces the same spanning tree, namely  $T$  itself.

P25) Both algorithms find simple path  $v$  in increasing order of length

P31) Modify: Change the line return  $T$  to  
 if  $(|V| == n)$  return true else return false  
 if the graph is connected, the value true is returned; otherwise the value of false is returned.

P32) Modify: Change the line return true to  
 print solution

① delete the line return false.