



Fizica III – Electromagnetism

Aplicatii # 6 – Propagare neghidata. Radiatie. Antene.

Prof.dr.ing. Gabriela Ciuprina gabriela@lmn.pub.ro

As.dr.ing. Mihai Popescu mihai_p@lmn.pub.ro

S.I..dr.ing. Sorin Lup sorin@lmn.pub.ro

Propagare neghidata. Radiatie. Antene.

1. Concepte utile*
 - ▶ 1.1. Propagare neghidata. Radiatie. Antene.
 - ▶ 1.2. Sistem de 2 antene
 - ▶ 1.3. Principiul unui sistem de comunicatie radio
2. Experimente virtuale
3. Experiment real

*Pentru detalii vedeti cursul, cap 5 si cap6.

1. Concepte utile

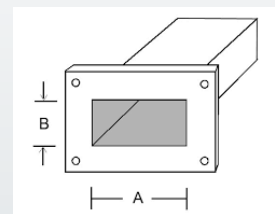
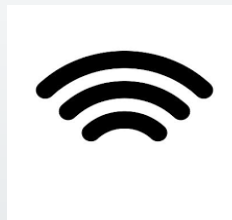
1.1. a) Propagare neghidata

La P5 am studiat propagarea campului electromagnetic, **ghidat de linii** electrice.

Linia electrica poate fi inteleasa ca un circuit electric cu parametri distribuiti, caracterizabil local prin parametri lineici. Propagarea ghidata de-a lungul liniilor electrice este cel mai simplu mod de propagare a campului EM, ea poate fi modelata cu circuite cu parametri distribuiti si simulata in simulatoare de circuit, de tip SPICE.

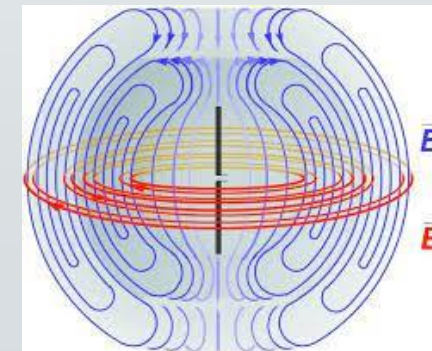
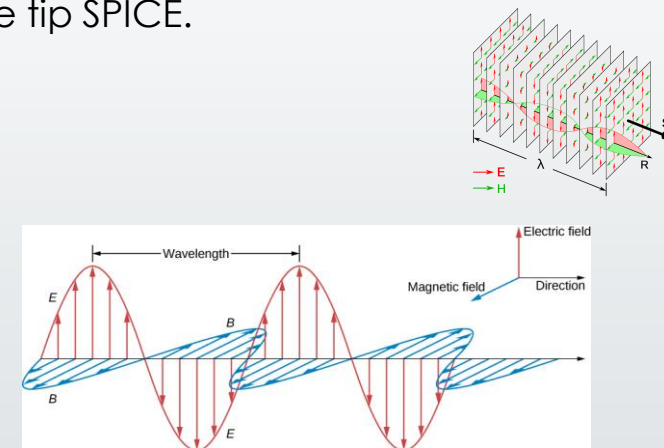
Propagarea campului EM in general poate fi

- Neghidata (in intreg spatiul)
- Ghidata de "ghiduri de unda" (nu neaparat linii)



In general, probleme de analiza a campului EM in regim general variabil sunt

- **Probleme de propagare** – in domenii nu exista surse interne de camp, campul EM se propaga in spatiul liber sau in domenii marginite de frontiere metalice (numite dispozitive de radio frecventa-RF sau de microunde-MW), datorita unor conditii initiale in domeniu, sau pe frontiera lui. Intereseaza modul in care campul se propaga.
- **Probleme de radiatie** – in domenii exista surse de camp – antene (de emisie). O unda EM poate fi si receptata de antenna (prin curentii care se induc in ea, antenna fiind acum de receptie) sau poate fi reflectata (imprastiata) de diferite obiecte (de exemplu in radar), acest din urma caz nu face obiectul acestui curs.



1. Concepte utile

1.1. a) Propagare neghidata

- ➔ **Dielectric cu pierderi** = un dielectric in care unda EM isi pierde din putere pe masura ce se propaga, datorita de exemplu unor proprietati de conductie (slabe) ale mediului. $\sigma \neq 0$.
- ➔ **Dielectric fara pierderi**: $\sigma = 0$

Ipoteze de studiu: 1) mediu **liniar**, **omogen**, **izotrop**, **neelectrizat**

Materiale liniare din toate punctele de vedere: electric (ϵ), magnetic (μ), conductie (σ)

Proprietatile de material nu depind de punctul din spatiu, sunt aceleasi in toate punctele domeniului de studiu.

Proprietatile de material nu depend de directia campului. Constantele de material sunt scalari, nu tensori.

$$\rho = 0$$

2) Vom presupune un regim armonic permanent (r.a.p), de pulsatie ω

1. Concepte utile

1.1. a) Propagare neghidata

Ecuatii de ordinul I

$$\nabla \cdot \underline{\vec{E}} = 0 \quad (1)$$

$$\nabla \cdot \underline{\vec{H}} = 0 \quad (2)$$

$$\nabla \times \underline{\vec{E}} = -j\omega\mu\underline{\vec{H}} \quad (3)$$

$$\nabla \times \underline{\vec{H}} = (\sigma + j\omega\varepsilon)\underline{\vec{E}} \quad (4)$$

$\underline{\vec{E}}$ si $\underline{\vec{H}}$ satisfac ecuatii identice de ordinul II, dar ele nu sunt independente, ci legate prin relatii de ordinul I.

In rezolvare, se alege una din ecuatiile de ordinul II care se rezolva (de exemplu (**E)) iar cealalta marime se determina dintr-o ecuatie de ordinul I (de exemplu (3)).

Ecuatii de ordinul II – in E sau H (ambele sunt de tip Helmholtz complex)

$$\Delta \underline{\vec{E}} - j\omega\mu(\sigma + j\omega\varepsilon)\underline{\vec{E}} = 0 \quad \Delta \underline{\vec{E}} - \underline{\gamma}^2 \underline{\vec{E}} = 0 \quad (**E)$$

$$\Delta \underline{\vec{H}} - j\omega\mu(\sigma + j\omega\varepsilon)\underline{\vec{H}} = 0 \quad \Delta \underline{\vec{H}} - \underline{\gamma}^2 \underline{\vec{H}} = 0 \quad (**H)$$

$\underline{\gamma}$ constanta de propagare complexa.

$$\underline{\gamma} = \sqrt{j\omega\mu(\sigma + j\omega\varepsilon)}$$

$$\underline{\gamma} = \alpha + j\beta$$

$\alpha = \text{Real}(\gamma) > 0$ factor de atenuare [Np/m]

$\beta = \text{Imag}(\gamma) > 0$ constanta de faza (numar de unda) [rad/m]

1. Concepte utile

1.1. a) Propagare neghidata

γ constanta de propagare complexa.

$$\underline{\gamma} = \sqrt{j \omega \mu (\sigma + j \omega \varepsilon)}$$

$$\underline{\gamma} = \alpha + j \beta$$

$\alpha = \text{Real}(\gamma) > 0$ factor de atenuare [Np/m]

$\beta = \text{Imag}(\gamma) > 0$ constanta de faza (numar de unda) [rad/m]

α si β se pot calcula in functie de parametrii de material si frecventa:

α si β depinde de frecventa
(prin ω explicit dar si proprietatile de material pot depinde de frecventa – materialele se numesc in acest caz “dispersive”)

$$\alpha = \omega \frac{\mu \varepsilon}{2} \left[-1 + \sqrt{1 + \left(\frac{\sigma}{\omega \varepsilon} \right)^2} \right]$$

$$\beta = \omega \frac{\mu \varepsilon}{2} \left[+1 + \sqrt{1 + \left(\frac{\sigma}{\omega \varepsilon} \right)^2} \right]$$

OBS:

daca $\sigma = 0$



atunci $\alpha = 0$

Similar cu Obs: la linii in r.a.p. constanta de propagare complexa era

$$\underline{\gamma} = \sqrt{(R_l + j \omega L_l) (G_l + j \omega C_l)}$$

$$L_l \sim \mu$$

$$G_l \sim \sigma$$

$$C_l \sim \varepsilon$$

$R_l \sim$ Nu are correspondent, la linii e legat de conductorul care ghideaza

α si β se pot calcula in functie de parametrii lineici si de frecventa:

$$\alpha = \sqrt{\frac{1}{2} \left[R_l G_l - \omega^2 L_l C_l + \sqrt{(R_l G_l - \omega^2 L_l C_l)^2 + \omega^2 (L_l G_l + R_l C_l)^2} \right]}$$

$$\beta = \sqrt{\frac{1}{2} \left[-R_l G_l + \omega^2 L_l C_l + \sqrt{(R_l G_l - \omega^2 L_l C_l)^2 + \omega^2 (L_l G_l + R_l C_l)^2} \right]}$$

OBS: daca $R_l = 0$ si $G_l = 0$ atunci $\alpha = 0$

Intr-un mediu fara pierderi, undele se propaga fara atenuare.

1. Concepte utile

1.1. a) Propagare neghidata

- **Unda plana** = unda care depinde de o singura coordonata spatiala (de exemplu z) si de timp.

Obs: 1) Coordonata spatiala este cea de-a lungul careia are loc propagarea; 2) Intr-un plan perpendicular pe coordonata spatiala de care depinde, unda are aceeasi valoare la un moment de timp fixat.)

Undele plane nu exista in realitate (ar trebui generate de plane infinit extinse parcurse de curenti). Ele sunt importante pentru ca sunt simple si pot fi folosite ca aproximatii ale undelor reale la distante sufficient de departate de sursele care le genereaza - antene.

$$\vec{E}(x, y, z, t) = \vec{E}_x(x, y, z, t)\vec{i} + \vec{E}_y(x, y, z, t)\vec{j} + \vec{E}_z(x, y, z, t)\vec{k}$$

Unda plana: $\vec{E}(z, t) = \vec{E}_x(z, t)\vec{i} + \vec{E}_y(z, t)\vec{j} + \vec{E}_z(z, t)\vec{k}$

Unda plana in r.a.p – reprezentare in complex: $\underline{\vec{E}}(z) = \underline{E}_x(z)\vec{i} + \underline{E}_y(z)\vec{j} + \underline{E}_z(z)\vec{k}$

Sa presupunem ca unda are doar componenta dupa directia Ox: $\underline{\vec{E}}(z) = \underline{E}_x(z)\vec{i}$

- **Polarizarea unei unde EM** = are legatura cu directia campului electric.

Unda polarizata liniar dupa Ox.

Unda plana
polarizata
dupa Ox:

$$\Delta \vec{E} - \gamma^2 \vec{E} = 0$$

$$\frac{d^2 \underline{E}_x(z)}{dz^2} \vec{i} - \gamma^2 \underline{E}_x(z) \vec{i} = 0$$

$$\Delta \vec{E} = \Delta \underline{E}_x(z) \vec{i} = \left(\frac{\partial^2 \underline{E}_x(z)}{\partial x^2} + \frac{\partial^2 \underline{E}_x(z)}{\partial y^2} + \frac{\partial^2 \underline{E}_x(z)}{\partial z^2} \right) \vec{i} = \frac{d^2 \underline{E}_x(z)}{dz^2} \vec{i}$$

$$\frac{d^2 \underline{E}_x(z)}{dz^2} - \gamma^2 \underline{E}_x(z) = 0$$

$$\underline{E}_x(z) = \underline{C}_1 e^{-\gamma z} + \underline{C}_2 e^{+\gamma z}$$

$$\underline{E}_x(z) = \underline{E}_d(z) + \underline{E}_i(z)$$

Ec. Helmholtz scalara complexa

\underline{C}_1 si \underline{C}_2 sunt constante de
integrare care se determina din
datele problemei

Si campul magnetic se determina din rel. de ord. I

$$\nabla \times \vec{E} = -j\omega\mu \vec{H} \rightarrow \vec{H}(z) = \underline{H}_y(z) \vec{j}$$

Unda plana este TEM (transversal electromagnetica)!

$$\underline{H}_y(z) = \frac{1}{\underline{Z}_c} (\underline{E}_d(z) - \underline{E}_i(z))$$

$$\underline{Z}_c = \sqrt{\frac{j\omega\mu}{\sigma + j\omega\epsilon}}$$

Impedanța
caracteristică
complexă a mediului

$$\underline{Z}_c = \frac{\underline{E}_d}{\underline{H}_d} = -\frac{\underline{E}_i}{\underline{H}_i}$$

Raport de
componente
directe!

$$\underline{Z}_c = \frac{\underline{U}_d}{\underline{I}_d} = -\frac{\underline{U}_i}{\underline{I}_i}$$

Impedanța
caracteristică
complexă a liniei

$$\underline{Z}_c = \sqrt{\frac{R_l + j\omega L_l}{G_l + j\omega C_l}}$$

1. Concepte utile

1.1. a) Propagare neghidata

$$\vec{E}(z) = \underline{E}_x(z) \vec{i}$$

La linii am rezolvat
ecuatia de gradul II

$$\frac{d^2 \underline{U}(z)}{dz^2} = \gamma^2 \underline{U}(z)$$

$$\underline{U}(z) = \underline{C}_1 e^{-\gamma z} + \underline{C}_2 e^{+\gamma z}$$

$$\underline{U}(z) = \underline{U}_d(z) + \underline{U}_i(z)$$

unda
elementara
directa de
tensiune = $\underline{U}_d(z)$

unda
elementara
inversa de
tensiune = $\underline{U}_i(z)$

Si curentul a fost determinat din rel. de ord. I

$$-\frac{d\underline{U}(z)}{dz} = (R_l + j\omega L_l) \underline{I}(z)$$

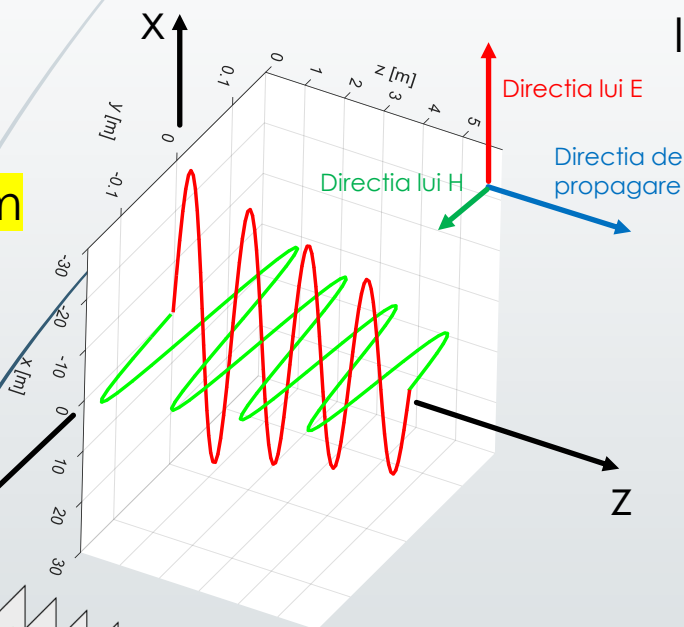
$$\underline{I}(z) = \frac{1}{\underline{Z}_c} (\underline{U}_d(z) - \underline{U}_i(z))$$

1. Concepte utile

1.1. a) Propagare neghidata

$$E_x(z, t) = E_0 e^{-\alpha z} \sqrt{2} \sin(\omega t - \beta z + \varphi_0)$$

demo2.m



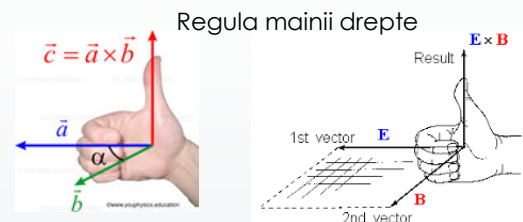
In general, pentru o unda plana

$$\vec{u}_E \times \vec{u}_H = \vec{u}_{\text{propagare}}$$

directia
campului
electric

directia
campului
magnetic

directia de
propagare



La T. energiei am definit

$$\vec{E} \times \vec{H} = \vec{S}$$

**Directia vectorului
Poynting indica
directia de
propagare a undei.**

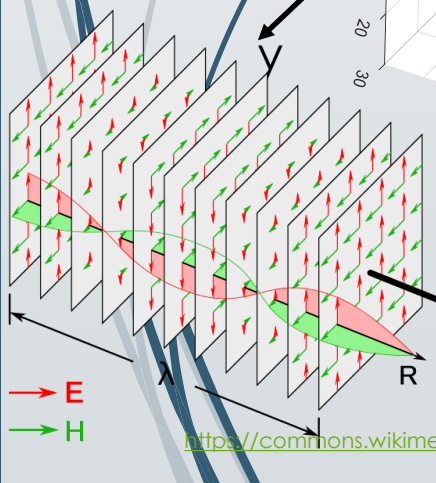
Modul de propagare a unei plane este **TEM – transversal electromagnetic.**

Unda plana

in plane perpendiculara pe directia de propagare, **campurile sunt uniforme!**

TEM

campul electric este perpendicular pe directia de propagare $\vec{u}_E \perp \vec{u}_{\text{propagare}}$
si
campul magnetic este perpendicular pe directia de propagare $\vec{u}_H \perp \vec{u}_{\text{propagare}}$



1. Concepte utile


1.1. a) Propagare neghidata

Cazuri particulare:

a1) **In medii fara pierderi:** $\sigma = 0, \varepsilon = \varepsilon_0 \varepsilon_r, \mu = \mu_0 \mu_r$

$$\underline{\gamma} = \sqrt{(j\omega\mu)(\sigma + j\omega\varepsilon)} = \sqrt{-\omega^2\mu\varepsilon} = j\omega\sqrt{\mu\varepsilon}$$

$$\underline{\gamma} = \alpha + j\beta$$

 $\alpha = 0$ Nu exista atenuare

$$\beta = \omega\sqrt{\mu\varepsilon}$$

$$v = \frac{\omega}{\beta} = \frac{1}{\sqrt{\mu\varepsilon}}$$

Daca parametrii mediului nu depind de frecventa, atunci viteza de propagare nu depinde de frecventa. => Semnalele se propaga fara distorsiuni (toate armonicile se propaga cu aceeasi frecventa).

$$\underline{Z}_c = \sqrt{\frac{j\omega\mu}{\sigma + j\omega\varepsilon}} = \sqrt{\frac{\mu}{\varepsilon}} \in \mathbb{R}; \underline{Z}_c \stackrel{\text{not}}{=} Z_0 \quad \theta = 0$$

Impedanta caracteristica este un numar real.

Campul magnetic e in faza cu campul electric.

a) **Linia fara pierderi** ($R_l = 0; G_l = 0$)

$$\underline{\gamma} = \sqrt{(R_l + j\omega L_l)(G_l + j\omega C_l)} = \sqrt{-\omega^2 L_l C_l} = j\omega\sqrt{L_l C_l}$$

$$\underline{\gamma} = \alpha + j\beta$$

 $\alpha = 0$ Nu exista atenuare

$$\beta = \omega\sqrt{L_l C_l}$$

$$v = \frac{\omega}{\beta} = \frac{1}{\sqrt{L_l C_l}}$$

Daca parametrii lineici nu depind de frecventa, atunci viteza de propagare nu depinde de frecventa. => Semnalele se propaga fara distorsiuni (toate armonicile se propaga cu aceeasi frecventa).

$$\underline{Z}_c = \sqrt{\frac{L_l}{C_l}} \in \mathbb{R}; \underline{Z}_c \stackrel{\text{not}}{=} Z_0$$

Impedanta caracteristica este un numar real.

1. Concepte utile

1.1. a) Propagare neghidata

Cazuri particulare:

α2) In vid: $\sigma = 0, \varepsilon = \varepsilon_0, \mu = \mu_0$

$$c = \frac{1}{4\pi \cdot 10^{-7} \cdot 8.854 \cdot 10^{-12}} = 2.9979 \cdot 10^8 \approx 3 \cdot 10^8 \text{ m/s}$$

In cazul anterior $\varepsilon_r = 1, \mu_r = 1$

Viteza de propagare a luminii in vid.

Lumina este o unda electromagnetica.



$\alpha = 0$ Nu exista atenuare

$$\beta = \omega \sqrt{\mu_0 \varepsilon_0}$$

$$v = \frac{\omega}{\beta} = \frac{1}{\sqrt{\mu_0 \varepsilon_0}} \triangleq c$$

$$\underline{Z}_c = \sqrt{\frac{\mu_0}{\varepsilon_0}} \in \mathbb{R}; \underline{Z}_c \stackrel{\text{not}}{=} Z_0$$

Impedanta caracteristica este un numar real.

Campul magnetic e in faza cu campul electric.

$$Z_0 = \sqrt{\frac{4\pi \cdot 10^{-7}}{8.854 \cdot 10^{-12}}} \approx 377 \Omega$$

Impedanta vidului.

50 Ω

Impedanta tipica a cablurilor.

Obs: in dielectrici fara pierderi

$$v = \frac{1}{\sqrt{\mu\varepsilon}} = \frac{c}{\sqrt{\mu_r \varepsilon_r}} < c$$

$\mu_r = 1$ (medii nemagnetice)
 $\varepsilon_r > 1$ (medii dielectrice, nu vid)

$$\frac{c}{v} \stackrel{\text{def}}{=} n = \sqrt{\mu_r \varepsilon_r}$$

Indicele de refractie al unui mediu.

1. Concepte utile

1.1. a) Propagare neghidata

Cazuri particulare:

b) **In conductoare foarte bune:** $\sigma \neq 0, \sigma \gg \omega \varepsilon$

$$\alpha = \omega \sqrt{\frac{\mu \varepsilon}{2} \left[-1 + \sqrt{1 + \left(\frac{\sigma}{\omega \varepsilon} \right)^2} \right]} \approx \omega \sqrt{\frac{\mu \varepsilon}{2} \left[-1 + \sqrt{\left(\frac{\sigma}{\omega \varepsilon} \right)^2} \right]} \approx \omega \sqrt{\frac{\mu \varepsilon}{2} \left[-1 + \frac{\sigma}{\omega \varepsilon} \right]} \approx \omega \sqrt{\frac{\mu \varepsilon}{2} \frac{\sigma}{\omega \varepsilon}} = \sqrt{\frac{\omega \mu \sigma}{2}}$$

$$\beta = \omega \sqrt{\frac{\mu \varepsilon}{2} \left[1 + \sqrt{1 + \left(\frac{\sigma}{\omega \varepsilon} \right)^2} \right]} \approx \sqrt{\frac{\omega \mu \sigma}{2}}$$

$$\underline{Z}_c = \sqrt{\frac{j \omega \mu}{\sigma + j \omega \varepsilon}} \quad Z_c = |\underline{Z}_c| = \sqrt{\frac{\omega \mu}{\sqrt{\sigma^2 + (\omega \varepsilon)^2}}} \approx \sqrt{\frac{\omega \mu}{\sigma}}$$

$$2\theta = \frac{\pi}{2} - \operatorname{atan} \frac{\omega \varepsilon}{\sigma} \approx \frac{\pi}{2} \quad \Rightarrow \quad \theta = \frac{\pi}{4}$$

Campul magnetic e defazat in urma campului electric cu $\pi/4$.

$$\alpha = \beta = \sqrt{\frac{\omega \mu \sigma}{2}}$$

$$v = \frac{\omega}{\beta} = \sqrt{\frac{2 \omega}{\mu \sigma}}$$

Depinde de frecventa

Adancimea de patrundere in conductoare foarte bune:

$$\delta = \frac{1}{\alpha} = \sqrt{\frac{2}{\omega \mu \sigma}}$$

1. Concepte utile

1.1. a) Propagare neghidata

Important!

Comportarea unui material in camp electromagnetic nu depinde numai de proprietatile lui electrice (ϵ), magnetice (μ) sau de conductie (σ) ci si de frecventa la care este folosit (ω).

$$\operatorname{tg} \delta = \frac{\sigma}{\omega \epsilon} \gg 1$$

Materialul este un conductor foarte bun

$$\operatorname{tg} \delta = \frac{\sigma}{\omega \epsilon} \ll 1$$

Materialul poate fi considerat fara pierderi.

1. Concepte utile

1.1. a) Propagare neghidata

- **Polarizarea unei unde plane** = se refera la modul de variatie in timp a directiei campului electric, mai precis la locul geometric al varfului vectorului $\vec{E}(z, t)$, vazut pe un plan perpendicular pe directia de propagare (front de unda).

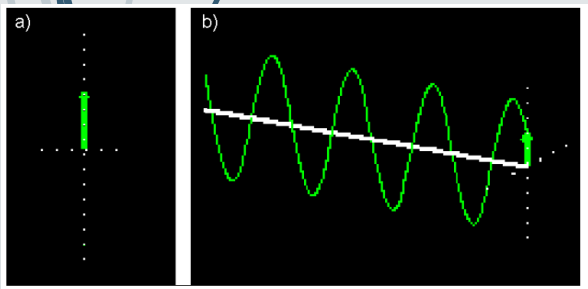
Poate fi: **liniara**, **circulara**, **eliptica**

- varful vectorului \vec{E} descrie (in timp) un segment/cerc/elipsa intr-un plan perpendicular pe directia de propagare (frontul undei).

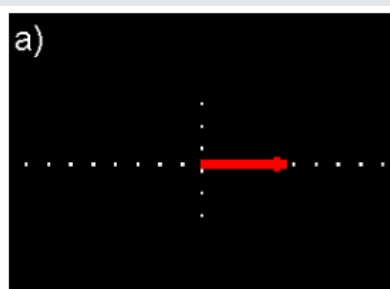
Pentru a putea comunica, doua antene trebuie sa produca unde polarizate similar.

radio AM (Vpol), radio FM (Vpol, Cpol, sau Epol), WiFi (Vpol), GPS (RHCP).

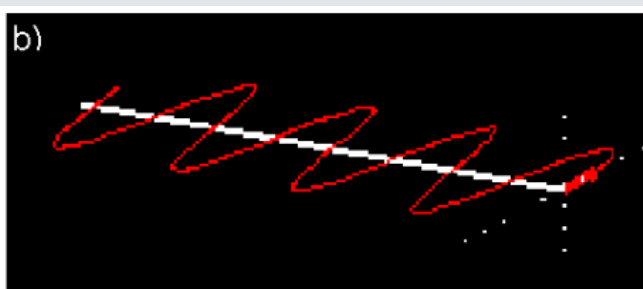
Polarizare liniara



Polarizare liniara - verticala
(folosita in radio AM si in WiFi)



Polarizare liniara - orizontala
(folosita la TV)



Polarizare liniara - oblica

Aici obtinuta din superpozitia a doua unde polarizate liniar (una verticala si una orizontala), **de aceeasi frecventa**, care **sunt in faza** si au aceeaasi amplitudine (=> unghi de 45 de grade)

1. Concepte utile

1.1. a) Propagare neghidata

$$\vec{E}(z, t) = E_1 \sin(\omega t - \beta z) \vec{i} + E_2 \sin(\omega t - \beta z + \Phi) \vec{j}$$

daca $\Phi = 0$ sau $\Phi = \pi$ **atunci**

\vec{E} este polarizata liniar

altfel

daca $\Phi = \pm \frac{\pi}{2}$ si $E_1 = E_2$ **atunci**

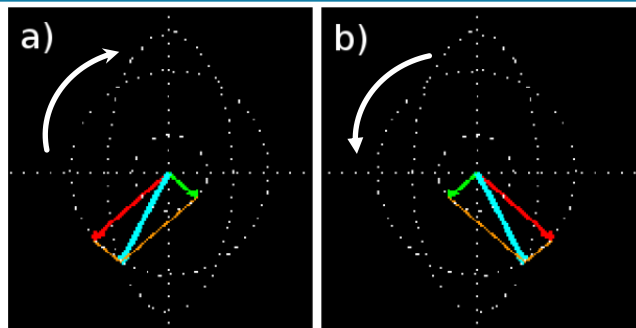
\vec{E} este polarizata circular

altfel

\vec{E} este polarizata eliptic

Polarizare eliptica

(folosita des in radio FM)

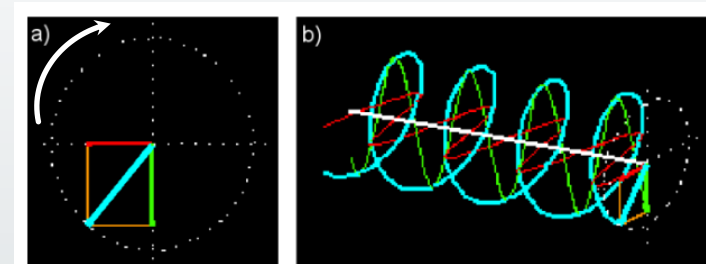


Left handed

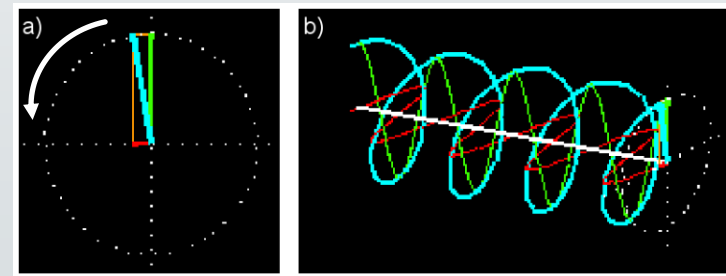
Right handed

Daca cele doua unde sunt in faza, polarizarea este liniara, verticala pentru $E_2=0$, orizontala cand $E_1=0$ si oblica atunci cand $E_1>0$, si $E_2>0$, diferite. In cazul general, eliptic, defazajul este nenul, polarizarea devine circulara cand $E_1=E_2$ si defazajul este de 90 grade (cele doua unde polarizate liniar de amplitudine egala sunt in cuadratura atat spatial cat si temporal).

Polarizare circulara



Left handed circular polarized (LHCP)



Right handed circular polarized (RHCP)

(folosite in GPS)

In figurile 2D - directia de propagare iese din foaie.

Luati mana dreapta astfel incat degetul mare deschis la 90 de grade (fata de celelalte degete intinse) sa indice directia de propagare (indreptat spre dvs). Indoiti celelalte 4 degete, varful lor indica directia de rotatie pentru cazul RHCP (trigonometric).

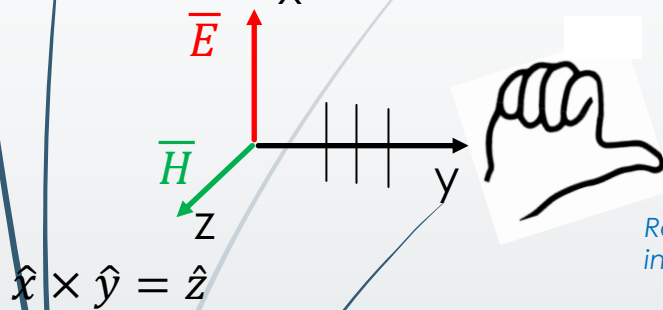
Vedeti animatii la

https://shopdelta.eu/wave-polarisation_l2_aid893.html

1. Concepte utile

1.1. a) Propagare neghidata - puteri

Unda plană polarizată liniar care se propaga după direcția pozitivă a axei Oz (e o undă directă):



Regula mainii drepte poate fi folosită pentru a indica direcția de transfer a puterii.

$$\vec{E}(z, t) = E_{xd}(z, t) \hat{x}$$

$$\vec{H}(z, t) = H_{xd}(z, t) \hat{y}$$

Vectorul Poynting

$$\vec{S}(z, t) = \vec{E} \times \vec{H} = E_{xd}(z, t) H_{xd}(z, t) \hat{z} = S(z, t) \hat{z}$$

Indica sensul transferului de energie.

Modulul lui reprezintă puterea transmisă de unda pe unitatea de arie, este deci o **densitate de putere**. [W/m²]

Intr-un mediu fara pierderi.

Campul electric si campul magnetic sunt in faza.

Nu exista atenuare. (In realitate, undele EM se atenuaza datorita raspandirii lor in spatiu, ele avand un front sferic si nu plan).

Impedanta caracteristica este un numar real.

Viteza de propagare a undei este

$$v = \frac{1}{\sqrt{\mu\epsilon}}$$

$$Z_0 = \sqrt{\frac{\mu}{\epsilon}}$$

$$Z_0 = \frac{E_{xd}(z, t)}{H_{xd}(z, t)} \quad \forall z, \forall t$$

$$S(z, t) = \frac{E_{xd}^2(z, t)}{Z_0} = Z_0 H_{xd}^2(z, t) = \sqrt{\frac{\epsilon}{\mu}} E_{xd}^2(z, t) = \sqrt{\frac{\mu}{\epsilon}} H_{xd}^2(z, t) = \frac{2}{\sqrt{\mu\epsilon}} \frac{\epsilon E_{xd}^2(z, t)}{2} = \frac{2}{\sqrt{\mu\epsilon}} \frac{\mu H_{xd}^2(z, t)}{2} = 2 v w_e = 2 v w_m$$

$$w_e(z, t) = w_m(z, t)$$

$$w(z, t) = 2w_e(z, t) = 2w_m(z, t)$$

$$S(z, t) = v w(z, t)$$

Unda plană, într-un mediu fără pierderi, e tot timpul la rezonanță.

Densitatea de energie totală.

1. Concepte utile

1.1. a) Propagare neghidata - puteri

Intr-un mediu cu pierderi.

Rationamentul se face in r.a.p.

$$\underline{\bar{S}} = \underline{\bar{E}} \times \underline{\bar{H}}^*$$

Marimile depind de z .

$$\underline{\bar{E}}(z) = \underline{E}_0 e^{-\underline{\gamma}z} \hat{x} = \underline{Z}_c \underline{H}_0 e^{-\underline{\gamma}z} \hat{x}$$

$$\underline{\bar{H}}(z) = \frac{\underline{E}_0}{\underline{Z}_c} e^{-\underline{\gamma}z} \hat{y} \quad \longrightarrow \quad \underline{\bar{H}}^*(z) = \frac{\underline{E}_0^*}{\underline{Z}_c^*} e^{-\underline{\gamma}^*z} \hat{y} = \underline{H}_0^* e^{-\underline{\gamma}^*z} \hat{y}$$

$$\underline{\bar{S}} = \underline{\bar{E}} \times \underline{\bar{H}}^* = \underline{E}_0 e^{-\underline{\gamma}z} \frac{\underline{E}_0^*}{\underline{Z}_c^*} e^{-\underline{\gamma}^*z} \hat{k} = \underline{S} \hat{k}$$

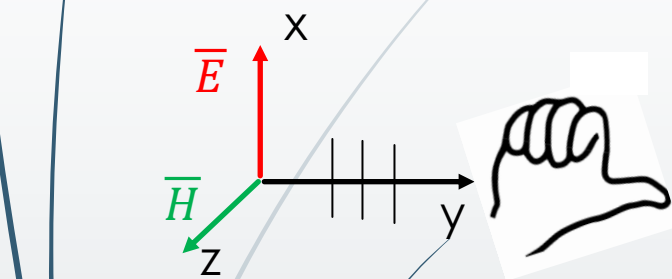
$$\underline{\bar{S}} = \underline{\bar{E}} \times \underline{\bar{H}}^* = \underline{Z}_c \underline{H}_0 e^{-\underline{\gamma}z} \underline{H}_0^* e^{-\underline{\gamma}^*z} \hat{k} = \underline{S} \hat{k}$$

$$\underline{S}(z) = \frac{\underline{E}_0 \underline{E}_0^*}{\underline{Z}_c^*} e^{-(\underline{\gamma} + \underline{\gamma}^*)z} = \frac{E_0^2}{\underline{Z}_c^*} e^{-2\alpha z}$$

$$\underline{S}(z) = \underline{Z}_c \underline{H}_0 \underline{H}_0^* e^{-(\underline{\gamma} + \underline{\gamma}^*)z} = \underline{Z}_c H_0^2 e^{-2\alpha z}$$

Pentru a afla media pe o perioada a densitatii de putere transmise:

$$\widetilde{S(z, t)}^T = \frac{1}{T} \int_0^T S(z, t) dt = \text{Real}(\underline{S}(z))$$



$$\hat{x} \times \hat{y} = \hat{z}$$

Regula mainii drepte poate fi folosita pentru a indica directia de transfer a puterii.

1. Concepte utile

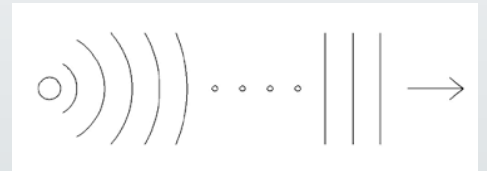
1.1. a) Propagare neghidata - ex.1

1) Campul electric (unda sferica) produs de o statie de baza dintr-o retea de telefonie mobila.

Sa presupunem ca o statie de baza dintr-o retea de telefonie mobila are o putere de emisie de $P=10$ kW. Vom estima valoarea maxima a intensitatii campului electric la o distanta de 1 metru de antena (de fapt valoarea medie a acestei marimi pe sfera de raza 1 metru).

Pp. ca mediul este vid (fara pierderi, de impedanta $Z_0 = 377 \Omega$) si presupunem ca sursa emite izotrop (la fel in toate directiile), produce o unda sferica. In aceste conditii puterea transmisa de antena trebuie sa se regaseasca pe o sfera de raza r , centrata in antena. Fiind unda sferica, directia de propagare este radiala, si datorita simetriei, valoarea densitatii de putere este aceeaasi pe sfera.

$$P = P(r) = - \oint_{\Sigma} \vec{S} \cdot \vec{n} dA = S_{\text{mediu}}(r) 4 \pi r^2 \quad \Rightarrow \quad S_{\text{mediu}}(r) = S(r) = \frac{P}{4 \pi r^2} \quad \left[\frac{W}{m^2} \right]$$



Aproximand local unda sferica cu o unda plana, putem estima modulul intensitatii campului electric

Atunci

$$S = \frac{E^2}{Z_0}$$

unde E este valoare efectiva

$$\Rightarrow S(r) = \frac{E_{\text{max}}^2(r)}{2 Z_0} \quad \Rightarrow \quad E_{\text{max}}(r) = \sqrt{2 Z_0 S(r)} = \sqrt{Z_0 \frac{P}{2 \pi r^2}}$$

$$E_{\text{max}}(1) = \sqrt{377 \frac{10^4}{2 \pi}} = 775 \text{ [V/m]}$$

$$E_{\text{max}}(1000) = \sqrt{377 \frac{10^4}{2 \pi 10^6}} = 775 \text{ [mV/m]}$$

1. Concepte utile

1.1. a) Propagare neghidata-ex.2

2) Campul electric produs de un telefon mobil.

Sa presupunem ca un telefon mobil are o putere de emisie de $P = 1\text{ W}$. Vom estima valoarea maxima a intensitatii campului electric la o distanta de 10 cm de telefon (de fapt valoarea medie a acestei marimi pe sfera de raza 10 cm).

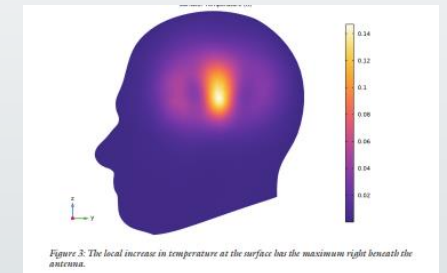
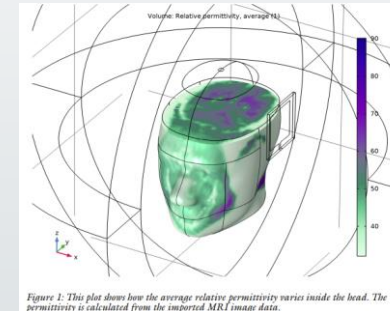
Am putea sa reluam ipotezele si calculul din exemplu anterior. Rezultatul ar fi

$$E_{\max}(r) = \sqrt{2 Z_0 S(r)} = \sqrt{Z_0 \frac{P}{2 \pi r^2}}$$

$$E_{\max}(0.1) = \sqrt{377 \frac{1}{2 \pi 0.01}} = 77.5 \quad [\text{V/m}]$$

In realitate un astfel de model nu este potrivit la o distanta mica de antena, nu putem presupune mediul omogen si fara pierderi, nici aproximatia de unda plana nu este potrivita.

Pentru a calcula campul EM intr-un astfel de scenario, trebuie folosite model numerice care sa include tipul de radiatie al antenei si forma si proprietatile EM ale capului.



https://www.comsol.com/model/download/1093691/models.rf.sar_in_human_head.pdf

1. Concepte utile

1.1. a) Propagare neghidata-ex.3

3) Comunicarea dintre un vapor si un submarin.

Sa presupunem ca un submarin se afla scufundat la 100 m fata de un vapor aflat pe mare. Personalul aflat pe vapor doreste sa comunice cu submarinul, folosind frecventa $f = 3 \text{ kHz}$. Sa se calculeze puterea (densitatea pe unitatea de suprafata) necesara emitatorului (pe vapor) astfel incat receptorul (submarin) sa primeasca un semnal cu o amplitudine de minimum $E_{\min} = 1 \mu\text{V/m}$.

Este necesara folosirea unor frecvente mici pentru comunicare deoarece apa marii este conductoare. Tangenta unghiului de pierderi este

$$\tan \delta_c = \frac{\sigma}{\omega \epsilon} \approx 10^5 \gg 1$$

Apa marii poate fi considerate foarte bun conductor, chiar si la aceasta frecventa foarte mica.

Vom folosi formulele demonstrate la conductoarele foarte bune (sectiunea 5.3.).

$$\alpha = \beta = \sqrt{\frac{\omega \mu \sigma}{2}} \approx 0.2$$

$$\lambda = \frac{2\pi}{\beta} = 29 \text{ m}$$

$$\delta = \frac{1}{\alpha} = 4.6 \text{ m}$$

$$Z_c = \sqrt{\frac{\omega \mu}{\sigma}} \approx 0.08 \Omega \quad \theta = 45^\circ$$

$$E(z, t) = E_0 \sqrt{2} e^{-\alpha z} \sin(\omega t - \beta z)$$

$$H(z, t) = \frac{E_0}{Z_c} \sqrt{2} e^{-\alpha z} \sin(\omega t - \beta z - \theta)$$

La receptor: $E_0 e^{-\alpha d} \sqrt{2} \geq E_{\min} \quad E_0 \geq \frac{E_{\min}}{\sqrt{2}} e^{\alpha d}$

La sursa: $\underline{S}(0) = \frac{E_0^2}{Z_c^*} = \frac{E_0^2}{Z_c} e^{j\theta}$

$$P(0) = \text{Real}(\underline{S}(0)) \geq \frac{E_{\min}^2 e^{2\alpha d} \cos \theta}{2 Z_c} = 37 \frac{\text{MW}}{\text{m}^2}$$

La receptor densitatea de putere este $\underline{S}(d) = \frac{E_0^2}{Z_c^*} e^{-2\alpha d}$

$$P(d) = \text{Real}(\underline{S}(d)) = P(0) e^{-2\alpha d} = 4.5 \cdot 10^{-12} \frac{\text{W}}{\text{m}^2} = 4.5 \frac{\text{pW}}{\text{m}^2}$$

La $d = 10 \text{ m}$, $P(0) = 0.35 \frac{\text{nW}}{\text{m}^2}$, $P(d) = 4.5 \frac{\text{pW}}{\text{m}^2}$

Proprietatile apei de mare

$$\sigma = 4 \text{ S/m}, \epsilon_r = 81, \mu_r = 1$$

Cod matlab disponibil

1. Concepte utile

1.1. b) Radiatie

Ipoteze de studiu: 1) mediu **liniar electric si magnetic**, afin dpdv al conductiei, **omogen** din pdv electric si magnetic, **izotrop**

$$\bar{D} = \varepsilon \bar{E}$$

$$\bar{B} = \mu \bar{H}$$

$$\bar{J} = \sigma \bar{E} + \bar{J}_i \approx \bar{J}_i$$

In conductoare vom neglija curentii indusi.
Dielectricii ii vom presupune fara pierderi.

Materiale liniare din punct de vedere si electric (ϵ), magnetic (μ), dpdv ak conductiei, relatia este afina, exista si un current imprimat (impus, de valoare cunoscuta)

Proprietatile de material electric si magnetic nu depind de punctul din spatiu, sunt aceleasi in toate punctele domeniului de studiu.

Proprietatile de material nu depend de directia campului.
Constantele de material sunt scalari, nu tensori.

2) Vom presupune un regim armonic permanent (r.a.p), de pulsatie ω

Ecuatii de ordinul I

$$\begin{aligned} \nabla \cdot \underline{\vec{E}} &= \frac{\rho}{\epsilon} = 0 \\ \nabla \cdot \underline{\vec{H}} &= 0 \end{aligned} \quad \text{In ipoteza } \nabla \cdot \underline{\vec{j}}_i = 0.$$

$$\nabla \times \underline{\vec{E}} = -j\omega\mu\underline{\vec{H}}$$

$$\nabla \times \underline{\underline{\vec{H}}} = (j\omega\varepsilon)\underline{\underline{\vec{E}}} + \underline{\underline{\vec{J}_i}}$$

F3-EM, 2022-2023

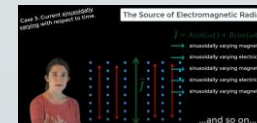
Ecuatii de ordinul II – in E sau H

$$\begin{aligned}\Delta \underline{\vec{E}} - j \omega \mu(j\omega\varepsilon)\underline{\vec{E}} &= j\omega\mu \underline{\vec{J}}_i \\ \Delta \underline{\vec{H}} - j \omega \mu(j\omega\varepsilon)\underline{\vec{H}} &= -\nabla \times \underline{\vec{J}}_i\end{aligned}$$

(ambele sunt de tip Helmholtz complex)

$$\begin{aligned}\Delta \bar{E} - \varepsilon\mu \frac{d^2 \bar{E}}{dt^2} &= \mu \frac{d\bar{J}_i}{dt} \\ \Delta \bar{H} - \varepsilon\mu \frac{d^2 \bar{H}}{dt^2} &= -\nabla \times \bar{J}_i\end{aligned}$$

→ Unde EM



1. Concepte utile

1.1. c) Antene

Antena = dispozitiv electromagnetic (EM) folosit pentru a trimite si receptiona unde EM.

(In ecuatiile anterioare, antena de emisie corespunde curentului fixat, sursa de camp.

In mod tipic ele sunt dispozitive care au un singur port. Un ghid de unda sau o linie de transmisie este conectat la antena intr-un singur punct.

Antenna As A Transition/Transducer Device

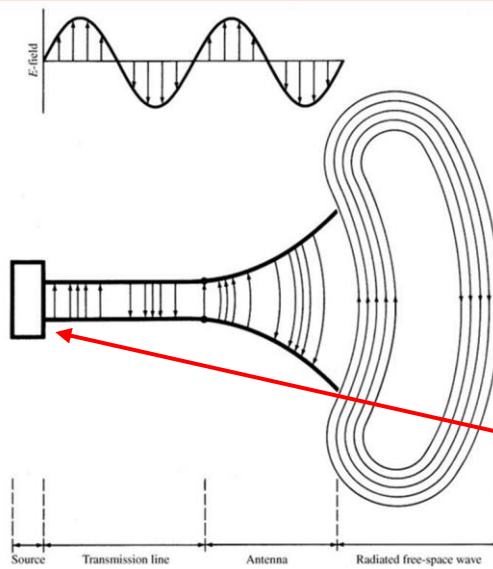


Fig. 1.1

Copyright © 2016 by Constantine A. Balanis
All right reserved

Chapter 1
Antennas

Antenna System

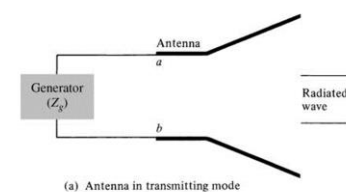


Fig. 2.27a

Copyright © 2016 by Constantine A. Balanis
All rights reserved

Chapter 2
Fundamental Parameters

Antena in
mod de
emisie (TX)

Antenna In Receiving Mode

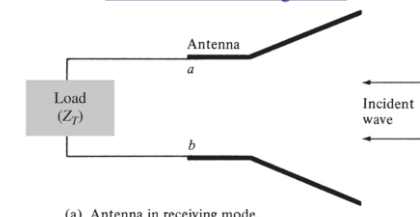


Fig. 2.28a

Copyright © 2016 by Constantine A. Balanis
All rights reserved

Chapter 2
Fundamental Parameters

Antena in
mod de
receptie (RX)

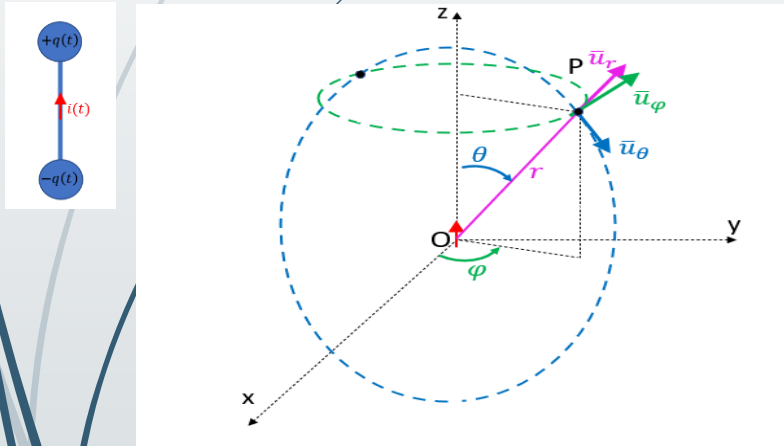
12/20/2022

Portul antenei: a-b

1. Concepte utile

1.1. c) Antene

Dipolul electric elementar = sistem radiant ideal, alcatuit din doua sarcini opuse, care variaza in timp $+q(t)$ si $-q(t)$, intre care exista un curent de conductie $i(t)$, astfel incat la orice moment de timp sa fie satisfacuta TCS (teorema conservarii sarcinii). Sistemul este plasat intr-un mediu dielectric liniar, omogen, izotrop.



$$\bar{p}(t) = \lim_{\substack{|q| \rightarrow \infty \\ l \rightarrow 0}} q(t) \bar{l}$$

$$i(t) \bar{l} = \frac{d \bar{p}(t)}{dt}$$

$$-i(t) = -\frac{dq(t)}{dt}$$

F3-EM, 2022-2023

$$E_r(\bar{r}, t) = \frac{1}{4\pi\epsilon} \left(\frac{2}{c} \frac{[\dot{p}]}{r^2} + \frac{2}{r^3} [p] \right) \cos \theta$$

$$E_\theta(\bar{r}, t) = \frac{1}{4\pi\epsilon} \left(\frac{[\ddot{p}]}{c^2 r} + \frac{[\dot{p}]}{c r^2} + \frac{[p]}{r^3} \right) \sin \theta$$

$$E_\phi(\bar{r}, t) = 0$$

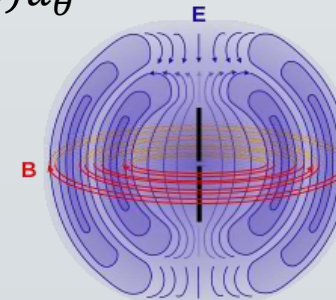
$$\bar{E}(\bar{r}, t) = E_r(\bar{r}, t) \bar{u}_r + E_\theta(\bar{r}, t) \bar{u}_\theta$$

$$H_r(\bar{r}, t) = 0$$

$$H_\theta(\bar{r}, t) = 0$$

$$H_\phi(\bar{r}, t) = \frac{1}{4\pi} \left(\frac{[\ddot{p}]}{c r} + \frac{[\dot{p}]}{r^2} \right) \sin \theta$$

$$\bar{H}(\bar{r}, t) = H_\phi(\bar{r}, t) \bar{u}_\phi$$



1. Concepte utile

1.1. c) Antene

Relatiile anterioare arata ca vectorul \vec{E} este situat in plane meridian ($E_\phi(\vec{r}, t) = 0$), iar vectorul \vec{H} in plane perpendicular pe axa oscilatorului ($H_r(\vec{r}, t) = 0, H_\theta(\vec{r}, t) = 0$).

Analizam doua zona importante:

a) **Zona apropiata** de oscilator, in care $r \ll \lambda$

Se pot retine numai termenii care il au pe r la puterea cea mai mare, iar campul se stabileste practice instantaneu (deoarce $\frac{r}{c} \ll t$):

$$E_r(\vec{r}, t) = \frac{2 p(t)}{4\pi\epsilon r^3} \cos \theta$$

$$E_\theta(\vec{r}, t) = \frac{p(t)}{4\pi\epsilon r^3} \sin \theta$$

$$H_\phi(\vec{r}, t) = \frac{\dot{p}(t)}{4\pi r^2} \sin \theta$$

$$p(t) = Iq(t) \quad \dot{p}(t) = Ii(t)$$

$$\underline{E}_r(\vec{r}) = \frac{2 P}{4\pi\epsilon r^3} \cos \theta$$

$$\underline{E}_\theta(\vec{r}) = \frac{P}{4\pi\epsilon r^3} \sin \theta$$

$$\underline{H}_\phi(\vec{r}) = \frac{j\omega P}{4\pi r^2} \sin \theta$$

(*)

b) **Zona indepartata** de oscilator (**a undelor**), in care $r \gg \lambda$

Se pot retine numai termenii care il au pe r la puterea cea mai mica, campul se propaga (deoarce $\frac{r}{c} \gg t$):

$$E_r(\vec{r}, t) = 0$$

$$E_\theta(\vec{r}, t) = \frac{1}{4\pi\epsilon} \frac{[\ddot{p}]}{c^2 r} \sin \theta$$

$$H_\phi(\vec{r}, t) = \frac{1}{4\pi} \frac{[\ddot{p}]}{c r} \sin \theta$$

$$\underline{E}_r(\vec{r}) = 0 \quad (**)$$

$$\underline{E}_\theta(\vec{r}) = \frac{1}{4\pi\epsilon} \frac{I I j \omega}{c^2 r} e^{j(-\frac{\omega r}{c})} \sin \theta$$

$$\underline{H}_\phi(\vec{r}) = \frac{1}{4\pi} \frac{I I j \omega}{c r} e^{j(-\frac{\omega r}{c})} \sin \theta$$

Campurile au cate o singura componenta, sunt ortogonali si perpendicular pe directia de propagare de versor \vec{u}_r .

1. Concepte utile

1.1. c) Antene

Concluzii – dipolul electric elementar

- ▶ Spre deosebire de cazul undelor plane, amplitudinile campurilor radiate de dipolul electric elementar, pentru zona undelor, nu mai sunt constante ci variaza invers proportional cu distanta r , conform (**).
- ▶ In zona undelor, amplitudinile campurilor radiate sunt proportionale cu frecventa (**), de aceea in radiocomunicatii se lucreaza la frecvente inalte.
- ▶ Facand raportul modulelor in relatia (**) se obtine $\frac{E_\theta}{H_\varphi} = \frac{1}{\epsilon c} = Z$, adica impedanta de unda a mediului (ca la unda plana). In cazul vidului aceasta impedanta este $120\pi = 377 \Omega$.
- ▶ In zona undelor, componentele electrice si magnetice ale campului radiat sunt in faza, conform (**). In zona apropiata, fazele campurilor sunt in cuadratura, conform (*).
- ▶ In zona undelor, la un moment de timp fixat, componentele de faza egala au acelasi $\omega t - \frac{\omega r}{c}$, de unde componentele de faza egala au acelasi r . Undele radiate de dipolul electric elementar sunt unde sferice.
- ▶ Undele radiate de dipolul electric elementar sunt polarizate liniar, campul electric fiind orientat exclusiv dupa axa de coordonata θ .
- ▶ Intr-un punct in zona undelor, aflat la distanta r de dipolul plasat in origine si orientat dupa z , \vec{E} are doar componenta dupa θ , \vec{H} are doar componenta dupa φ , ambii vectori sunt tangenti la suprafata sferei de raza r , sistemul de vectori $(\vec{E}, \vec{H}, \vec{r})$ formeaza un triedru ortogonal drept.
- ▶ Din (**) se observa ca E_θ si H_φ sunt proportionale cu $\sin \theta$. Se spune ca dipolul electric elementar are **directivitate**. Valoarea maxima are loc in planul ecuatorial (definit de $\theta = \frac{\pi}{2}$). Dipolul nu radiaza dupa axa Oz ($\theta = 0$).

1. Concepte utile

1.1. c) Antene

$$\theta \in [0, \pi]$$

Parametri

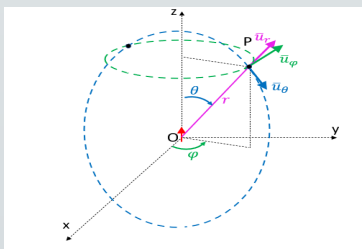
$$\underline{E}_\theta(\vec{r}) = \frac{1}{4\pi\epsilon} \frac{-\omega^2 P}{c^2 r} e^{j(-\frac{\omega r}{c})} \sin \theta = \underline{E}_{\theta, \max}(\vec{r}) \sin \theta$$

Raportul

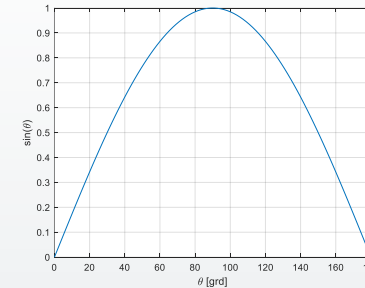
$$\frac{|\underline{E}_\theta(\vec{r})|}{|\underline{E}_{\theta, \max}(\vec{r})|} = \sin \theta = f(\theta)$$

Se numeste **caracteristica/rofilul de radiație al campului** (*field radiation pattern*)

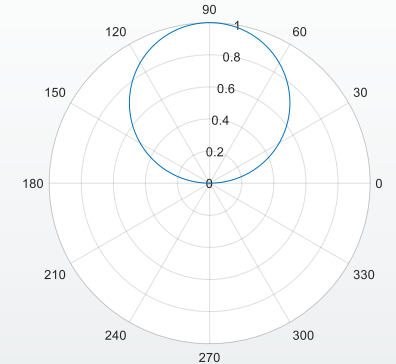
Se deseneaza de obicei intr-un sistem polar 2D, sau 3D.



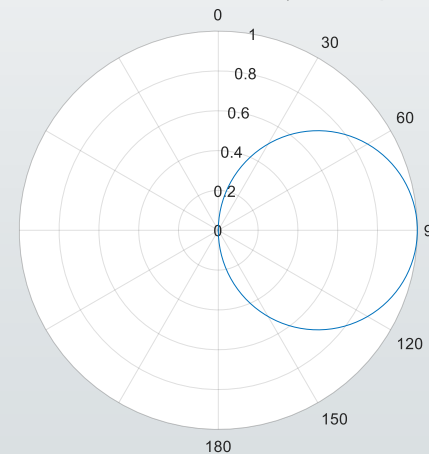
$$\theta \in [0, \pi]$$



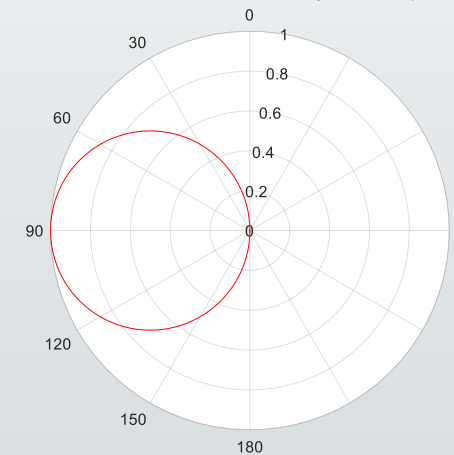
Polar plot, with θ - measured from the Ox axis (usual math representation)



Polar plot, with θ - measured from the Oz axis (antenna representation, $\phi = 0$)



Polar plot, with θ - measured from the Oz axis (antenna representation, $\phi = \pi$)



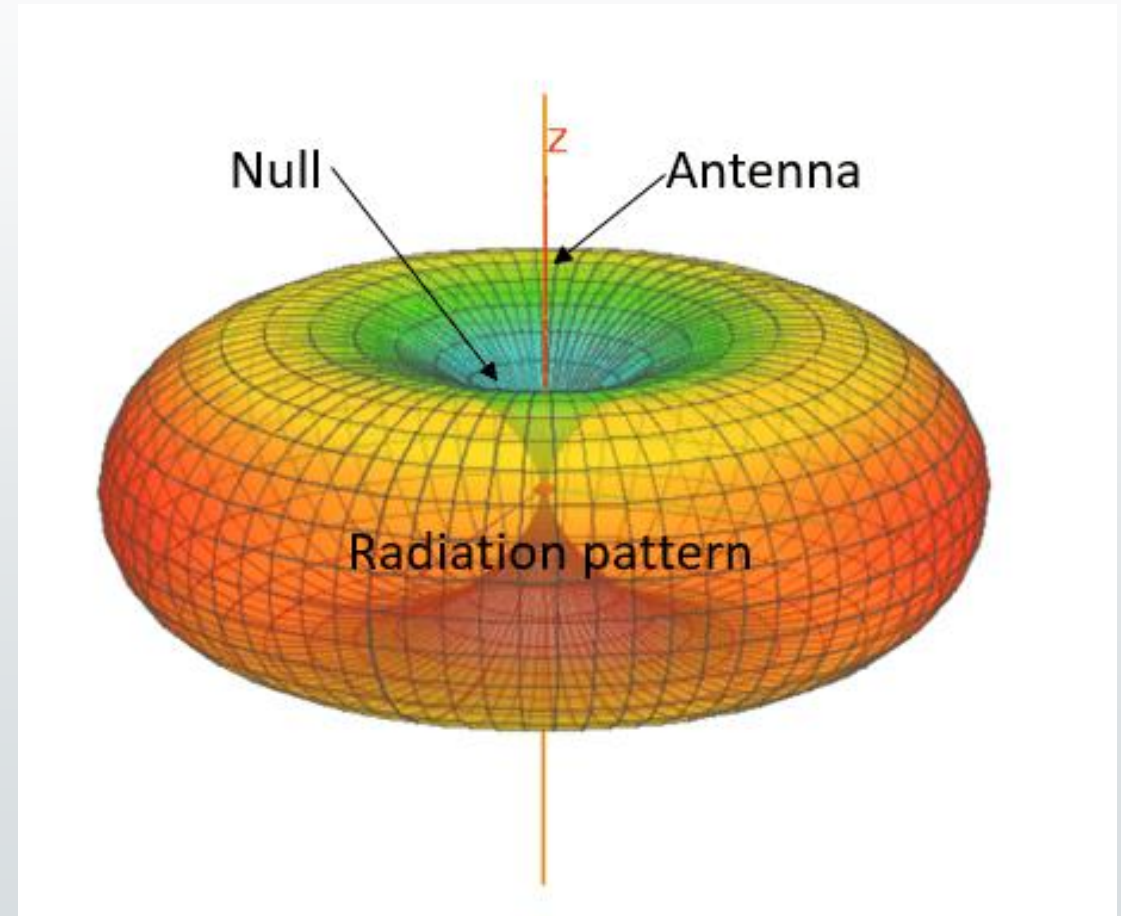
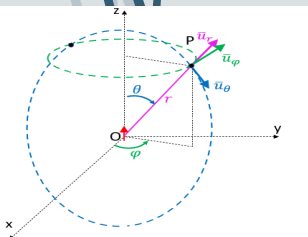
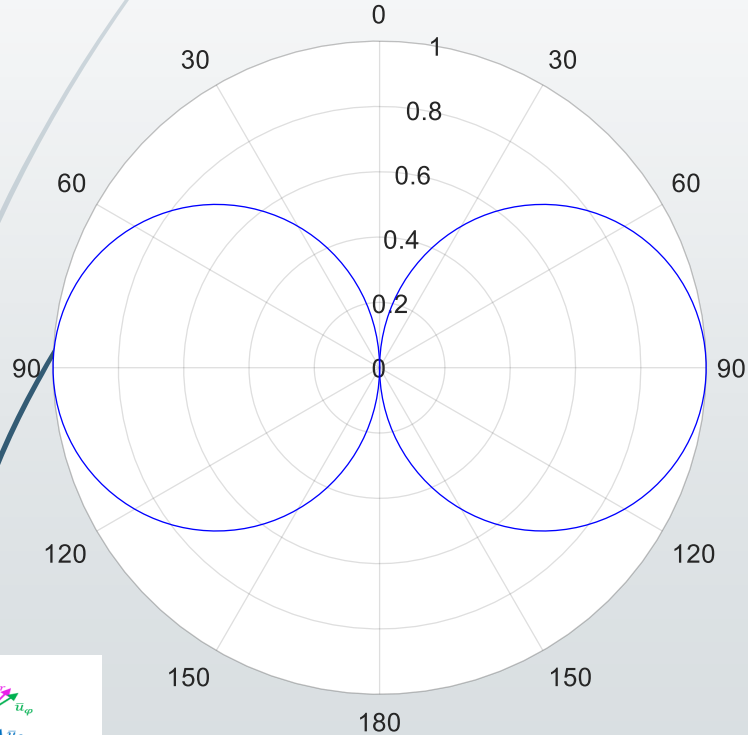
θ - unghiul de elevatie din sistemul sferic

1. Concepte utile

1.1. c) Antene

Parametri – profilul de radiatie al campului

Dipole 2D pattern (E field pattern)



1. Concepte utile

1.1. c) Antene

Parametri – puterea radiată

Se calculează în zona undelor.

Se folosește vectorul lui Poynting – care este o densitate superficială de putere, mărime locală și instantanee.

$$\bar{S}(\bar{r}, t) = \bar{E}_\theta(\bar{r}, t) \times \bar{H}_\varphi(\bar{r}, t) = E_\theta(\bar{r}, t) H_\varphi(\bar{r}, t) \bar{u}_r = S_r(\bar{r}, t) \bar{u}_r$$

$$E_\theta(\bar{r}, t) = \frac{1}{4\pi\epsilon} \frac{[\ddot{p}]}{c^2 r} \sin \theta$$

$$H_\varphi(\bar{r}, t) = \frac{1}{4\pi} \frac{[\dot{p}]}{cr} \sin \theta$$

$$\Rightarrow S_r(\bar{r}, t) = \frac{1}{(4\pi)^2 \epsilon c^3} \frac{[\ddot{p}]^2}{r^2} \sin^2 \theta$$

Vectorul Poynting este radial, în sensul propagării unde.

Modulul Poynting depinde de unghiul θ , radiația se face directiv, fiind maximă în planul perpendicular pe dipol și nulă pe axa dipolului. Densitatea de putere este invers proporțională cu pătratul distanței.

Să presupunem variații armonice în timp

$$\underline{E}_\theta(\bar{r}) = \frac{1}{4\pi\epsilon} \frac{I l j \omega}{c^2 r} e^{j(-\frac{\omega r}{c})} \sin \theta$$

$$\underline{H}_\varphi(\bar{r}) = \frac{1}{4\pi} \frac{I l j \omega}{cr} e^{j(-\frac{\omega r}{c})} \sin \theta$$

$$\Rightarrow \bar{S}(\bar{r}) = \underline{E}_\theta(\bar{r}) \times \underline{H}_\varphi(\bar{r})^* = \frac{1}{(4\pi)^2 \epsilon c^3} \frac{I^2 l \omega^2}{r^2} \sin^2 \theta \bar{u}_r$$

(are doar componenta reală)

1. Concepte utile

1.1. c) Antene

$$\underline{S}(r) = \frac{1}{(4\pi)^2 \epsilon c^3} \frac{I^2 l \omega^2}{r^2} \sin^2 \theta = \underline{S}_{\max}(r) \sin^2 \theta$$

(***)

Raportul $\frac{|\underline{S}(\vec{r})|}{|\underline{S}_{\max}(r)|} = \sin^2 \theta$

Se numeste **caracteristica de radiatie de putere** (profil de radiatie, *power radiation pattern*).

Se deseneaza de obicei intr-un sistem polar 2D, sau 3D.

Dipole 2D pattern (power polar pattern - linear scale)

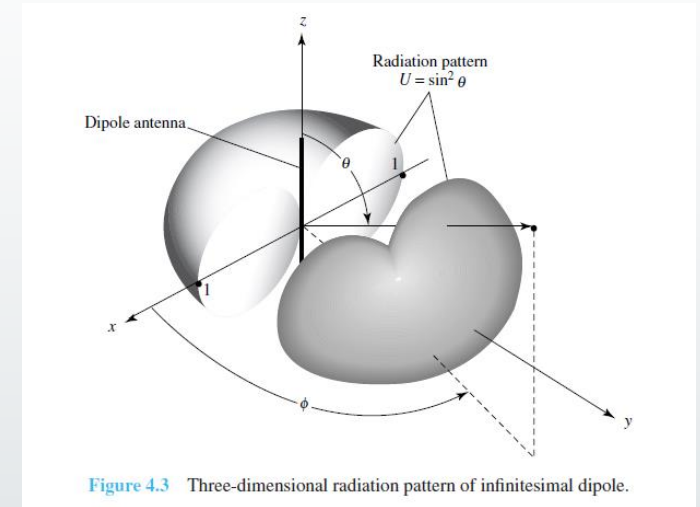
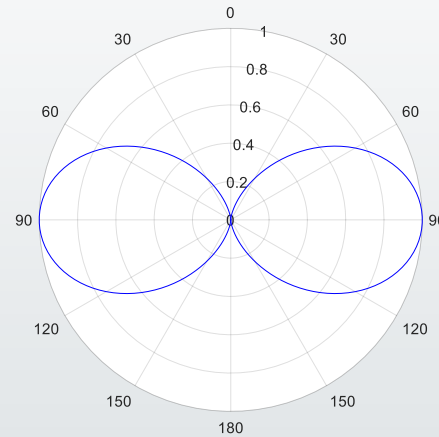
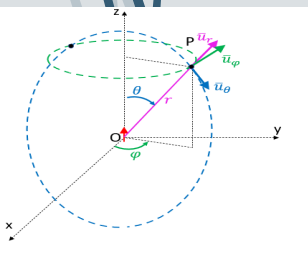


Figure 4.3 Three-dimensional radiation pattern of infinitesimal dipole.

Constantine Balanis, Antenna Theory. Analysis and Design, Wiley 2016

Caracteristicile de radiatie pentru putere se deseneaza uneori pentru valorile in decibel.



$$\theta \in [0, \pi]$$

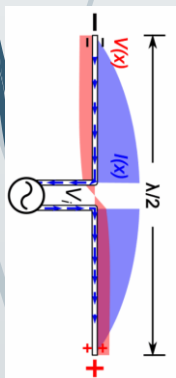
1. Concepte utile

1.1. c) Antene

Dipolul electric = antena liniara, subtire, simetrica, alimentata central

Notam cu l – lungimea antenei

Obs: numai daca $l \ll \lambda$, dipolul electric este elementar. Studiul lui este foarte util pentru analiza unor sisteme radiante mai complexe, care pot fi considerate ca o infinitate de dipoli elementari, si solutia se poate calcula prin **superpozitie**. Este cazul antenelor liniare subtiri (diametrul lor $d < \frac{\lambda}{100}$), formate din doua conductoare, de lungime $\frac{l}{2}$ fiecare. Se pp. ca alimentarea se face in partea centrala, printr-o linie de transmisie bifilara. Se pp. ca distributia de current este sinusoidala, aceasta aproximand destul de bine distributiile din antenele subtiri.



https://en.wikipedia.org/wiki/Dipole_antenna#/media/File:Standing_waves_animation_6_-_5fps.gif

Current Distributions Along
the Length of a Linear Wire Antenna

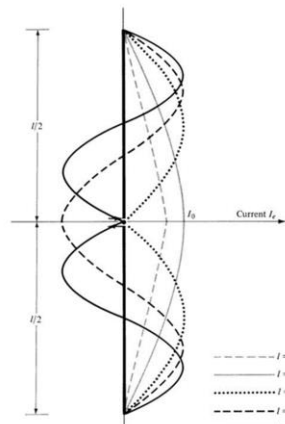


Fig. 4.8

Copyright©2016 by Constantine A. Balanis
All rights reserved

Chapter 4
Linear Wire Antennas

Se poate demonstra ca functia de directivitate de amplitudine pentru aceste antene este

$$f(\theta) = \frac{\cos\left(\pi \frac{l}{\lambda} \cos \theta\right) - \cos\left(\pi \frac{l}{\lambda}\right)}{\sin \theta}$$

Pentru a putea compara directivitatea diferitor antene se normalizeaza aceasta valoare.

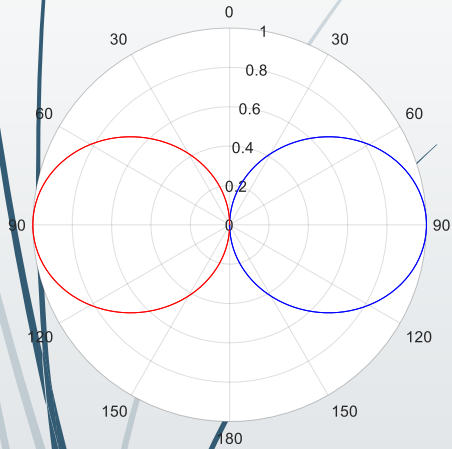
$$f_{\text{normal}}(\theta) = \frac{f(\theta)}{\max(|f(\theta)|)}$$

1. Concepte utile

1.1. c) Antene

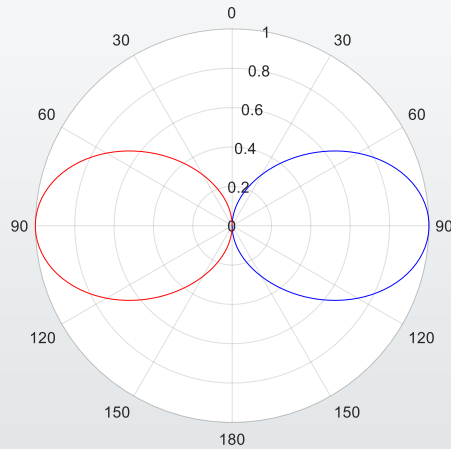
$$l = \frac{\lambda}{2}$$

Dipole 2D pattern (normalized field pattern)



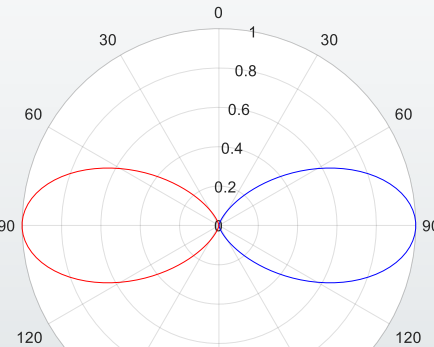
$$l = \frac{3}{4}\lambda$$

Dipole 2D pattern (normalized field pattern)

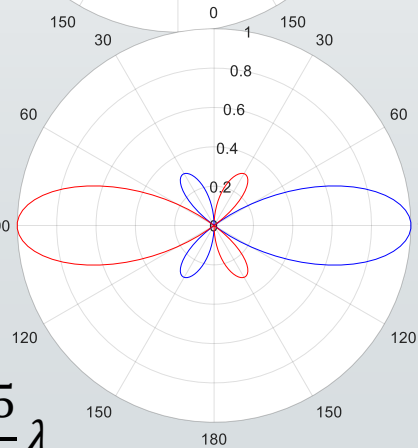


$$l = \lambda$$

Dipole 2D pattern (normalized field pattern)

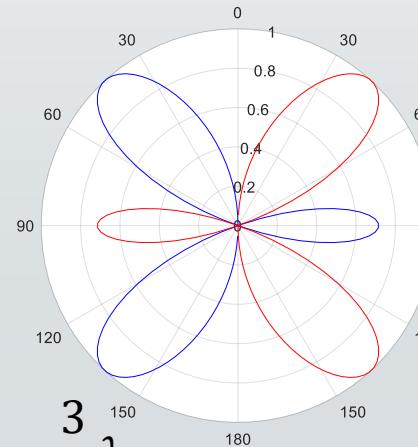


Dipole 2D pattern (normalized field pattern)



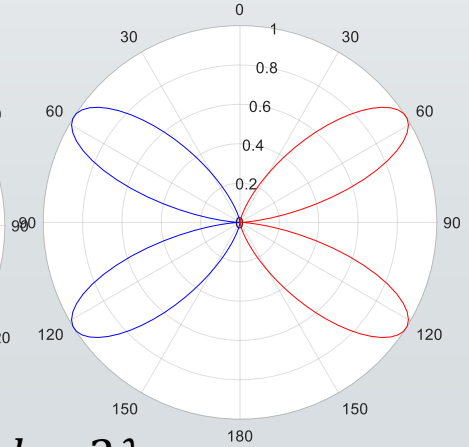
$$l = \frac{5}{4}\lambda$$

Dipole 2D pattern (normalized field pattern)



$$l = \frac{3}{2}\lambda$$

Dipole 2D pattern (normalized field pattern)



$$l = 2\lambda$$

$$f_{\text{normal}}(\theta) = \frac{f(\theta)}{\max(|f(\theta)|)}$$

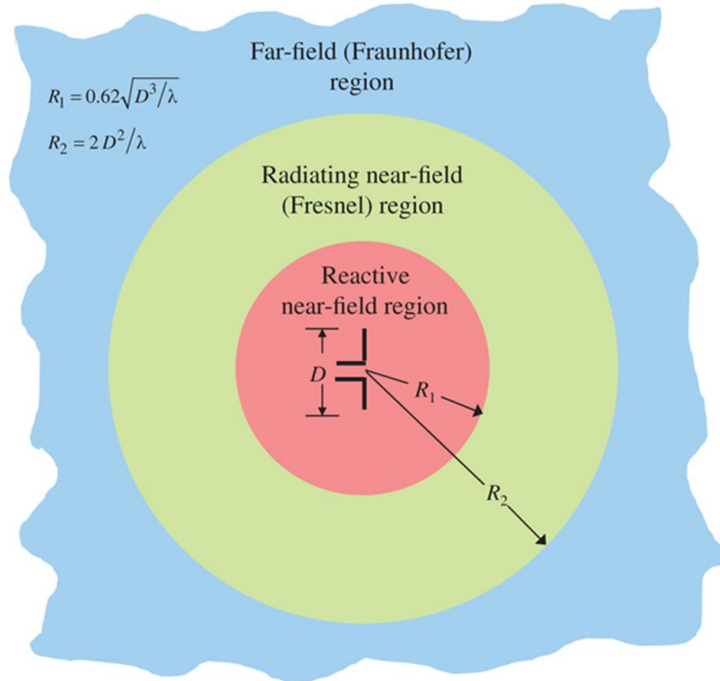
Profilul de radiatie
normalat, al campului.

Cod Matlab disponibil

1. Concepte utile

1.1. c) Antene

Field Regions



Zona apropiata (reactive near-field) = la distante mici de antenna

- Fazele campurilor electrice si magnetice sunt in cuadratura (defazate la 90 de grade). De aceea in aceasta zona impedanta undei este puternic reactiva. O mare parte din energia acumulata in aceasta zona nu contribuie la propagare.

Zona intermediara (radiating near-field, Fresnel) = la distante medii fata de antenna

- Campurile sunt predominant in faza, dar nu au inca un front sferic. De aceea campul variaza cu distanta fata de antenna. Este regiunea unde se fac masuratorile de camp apropiat (near-field measurements).

Zona departata (zona undelor, far-field, Fraunhofer) = la distante mari de antenna

Fig. 2.7

Campurile au front de unda sferic. In mod ideal campul nu depinde de distanta fata de antenna. Campurile electrice si magnetice sunt in faza. Impedanta de unda este, in mod ideal, reala. Puterea este predominant activa (reala), energia acumulata in aceasta zona contribuie la propagare.

1. Concepte utile

1.1. c) Antene

Parametrii antenelor sunt acele marimi care permit alegerea unui tip de antena pentru o aplicatie (vedeti si 6.8). Cei mai importanti parametri de performanta ai unei antene sunt:

- **Frecventa de operare**
- **Caracteristica de radiatie (camp/putere).**
 - **Intensitate maxima a campului electric** in puncte semnificative ale sistemului radiant, importanta mai ales in instalatiile radiante de mare putere, unde ar putea fi induse fenomene corona sau strapungerea dielectricilor din vecinatate.
 - **Putere totala radiata** P_{rad} = atunci cand sistemul radiant este excitat de o distributie de current sau de sarcina cunoscuta.
 - **Intensitatea radiatiei** U
 - **Directivitate** D
- **Impedanta de intrare** a sistemului radiant Z_{in} = importanta mai ales in problemele de adaptare a sistemului radiant la sistemul de alimentare al acestuia.
 - **Caracteristica de frecventa** – parametrii S
- **Eficienta (randament)** sistemului radiant e_{cd} = puterea radiata/puterea totala primita de la sistemul de alimentare (care este suma dintre puterea radiata si cea disipata in sistem). **Castig.**
- **Largime de banda**

Nu toti acesti parametri sunt independenti. Pentru a descrie complet performantele unei antene, numai unii dintre acesti parametri sunt suficienti.

1. Concepte utile

1.1. c) Antene

Caracteristica de radiatie (*radiation pattern*)

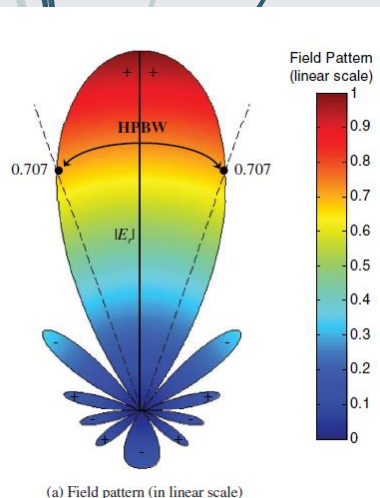
= o functie matematica sau o reprezentare grafica a proprietatilor de radiatie a antenei, ca o functie de coordonatele spatiale. In majoritatea cazurilor se determina in zona undelor si este o functie de coordonatele θ si φ .

Cea mai importanta proprietate legata de radiatie este distributia spatiala (2D sau 3D) a energiei radiate, in functie de pozitia unui observator aflat pe o suprafata sferica, de raza constanta, cu centrul in antena.

Ea se poate referi la :

- Amplitudinea campului (electric sau magnetic) => caracteristica de radiatie a campului (*field radiation pattern*)
- Densitatea de putere (de obicei amplitudinea la patrat a campului electric sau magnetic) => caracteristica de radiatie a puterii (*power radiation pattern*). Se reprezinta si in dB, pentru a pune in evidenta mai bine lobii minori (secundari).

De obicei aceste marimi sunt normate => *normalized field/power radiation pattern*

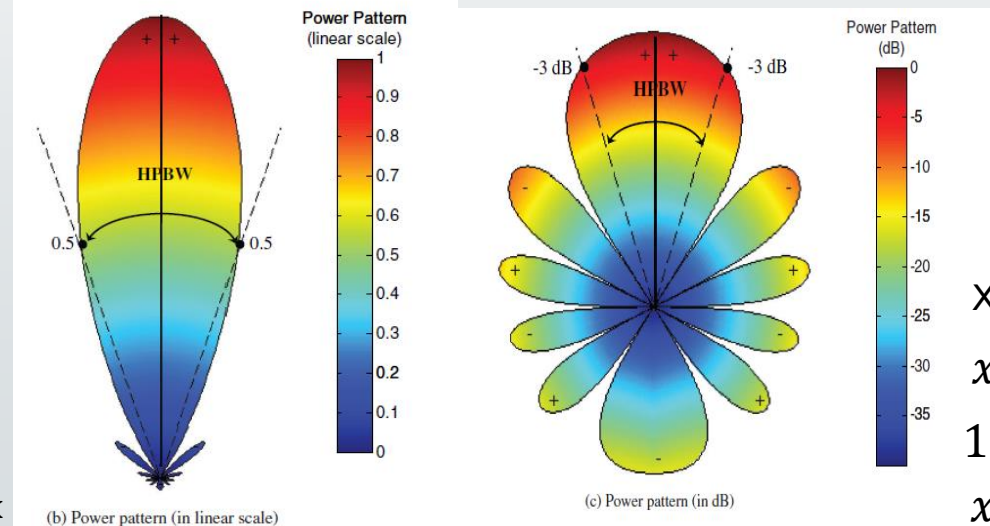


$$p \sim E^2$$

$$p_{\max} = C E_{\max}^2$$

$$0.5 p_{\max} = C E_{0.5p_{\max}}^2$$

$$E_{0.5p_{\max}} = \frac{E_{\max}}{\sqrt{2}} = 0.707 E_{\max}$$



Two-dimensional normalized *field pattern (linear scale)*, *power pattern (linear scale)*, and *power pattern (in dB)* of a 10-element linear array with a spacing of $d = 0.25\lambda$.

$$x_{\text{dB}} = 10 \cdot \log_{10}(x)$$

$$x = 1$$

$$10 \log_{10} 1 = 0 \text{ dB}$$

$$x = 0.5$$

$$10 \log_{10} 0.5 = -3 \text{ dB}$$

1. Concepte utile

1.1. c) Antene

Puterea radiata = puterea activa calculata prin integrarea vectorului Poynting pe o sfera centrata in antenna.

$$P_{rad} = \int_{\Sigma} \operatorname{Re} (\underline{\bar{E}} \times \underline{\bar{H}}^*) \cdot d\bar{A} = \int_{\Sigma} \underline{\bar{W}}_{rad} \cdot d\bar{A}$$

Unde am notat densitatea de putere cu

$$\underline{\bar{W}}_{rad} = \operatorname{Re} (\underline{\bar{E}} \times \underline{\bar{H}}^*) = W_{rad} \bar{u}_r$$

Deoarece in zona undelor, radiatia este dupa directia radiala. In aceasta zona, puterea reactiva e nula.

O antenna ideala, ar radia izotrop, la fel in toate directiile, caz in care densitatea de putere nu depinde decat de raza $W_{rad}(r)$. Rezulta ca

$$P_{rad} = 4 \pi r^2 W_{rad}(r) \quad W_{rad}(r) = \frac{P_{rad}}{4 \pi r^2}$$

Aceasta marime, desi nu corespunde unei situatii reale, e folosita pentru normare.

Intensitatea radiatiei = puterea radiata de o antenna pe unitatea de unghi solid

Se defineste pentru zona undelor

$$U = r^2 W_{rad}$$

[W/unitate de unghi solid]

$$U(\theta, \varphi) = B_0 F(\theta, \varphi) \approx \frac{1}{Z} |E(\theta, \varphi)|^2$$

Pentru ca in zona undelor componenta radiala a campului se poate neglija.

unde B_0 este o constanta

Pentru rezonatorul ideal $U = \frac{P_{rad}}{4 \pi} \triangleq U_0$

Valoarea maxima $U_{max} = B_0 F_{max}(\theta, \varphi)$

Puterea totala radiata devine

$$P_{rad} = B_0 \int_0^{2\pi} \int_0^{\pi} F(\theta, \varphi) \sin \theta d\theta d\varphi$$

1. Concepte utile

1.1. c) Antene

La dipolul electric, caracteristica de radiatie (camp sau putere) depinde numai de unghiul θ .

Directia (φ_0, θ_0) in care caract. de radiatie are cea mai mare valoare = **directie de radiatie maxima**.

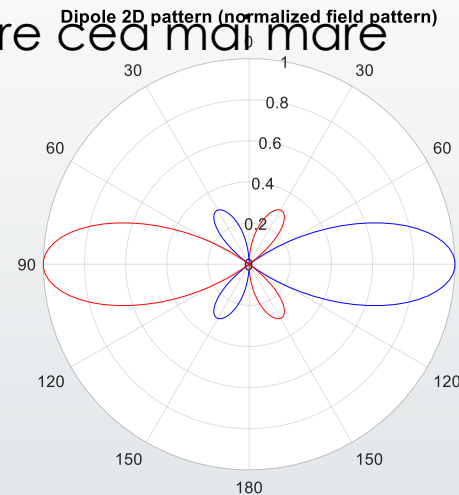
Directiile in care nu exista radiatie = **directii de radiatie nula**.

Totalitatea valorilor caracteristicii de directivitate cuprinse intre doua directii de radiatie nula = **lob**.

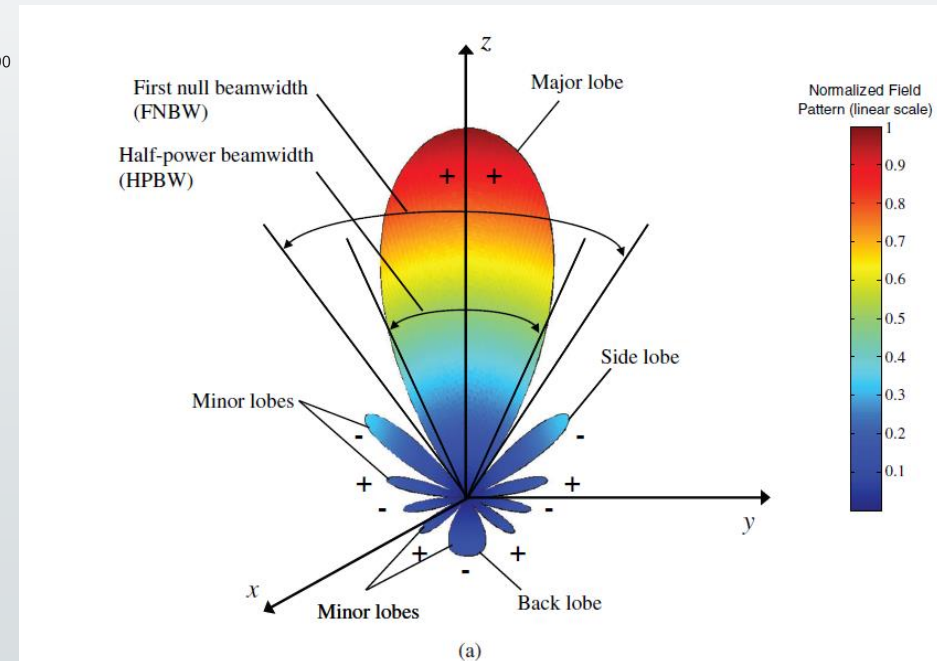
Lobul a carui maxim se suprapune pe directia de radiatie maxima = **lob principal**.

Ceilalti – **secundari (minori)**

Cu cat lobul principal este mai ingust, cu atat antenna este mai directiva. (La aceesi putere, distanta de actiune e mai mare – util pentru radar).



$$l = \frac{5}{4}\lambda$$



1. Concepte utile

1.1. c) Antene

Directivitate = raportul dintre intensitatea de radiatie intr-o directie data si intensitatea de radiatie mediata dupa toate directiile. Aceasta din urma este puterea totala radiata de antenna impartita la 4π . Daca nu se specifica nicio directie, implicit se considera directia de radiatie maxima.

$$D = \frac{U}{U_0} = \frac{4\pi U}{P_{rad}}$$

$$D(\varphi, \theta) = 4\pi \frac{F(\theta, \varphi)}{\int_0^{2\pi} \int_0^\pi F(\theta, \varphi) \sin \theta \, d\theta \, d\varphi}$$

$$D_{max} = D_0 = \frac{4\pi U_{max}}{P_{rad}}$$

$$D_0 = 4\pi \frac{F(\theta, \varphi)|_{max}}{\int_0^{2\pi} \int_0^\pi F(\theta, \varphi) \sin \theta \, d\theta \, d\varphi}$$

D -directivitate [adimensionala]

D_0 -directivitate maxima

U -intensitatea radiatiei [W/unitate de unghi solid]

U_{max} -valoarea maxima a intensitatii radiatiei

U_0 -intensitatea radiatiei unei surse care radiaza izotrop

P_{rad} -puterea totala radiata [W]

O directivitate mai mare inseamna o antenna mai directiva. De exemplu $D = 2$ inseamna ca antenna transmite de 2 ori mai multa putere in directia de radiatie maxima decat o antenna ideala (numita si izotropa).

Antenele telefoanelor mobile trebuie sa aiba o directivitate mica, deoarece semnalul poate veni din orice directie, si antenna trebuie sa il receptioneze.

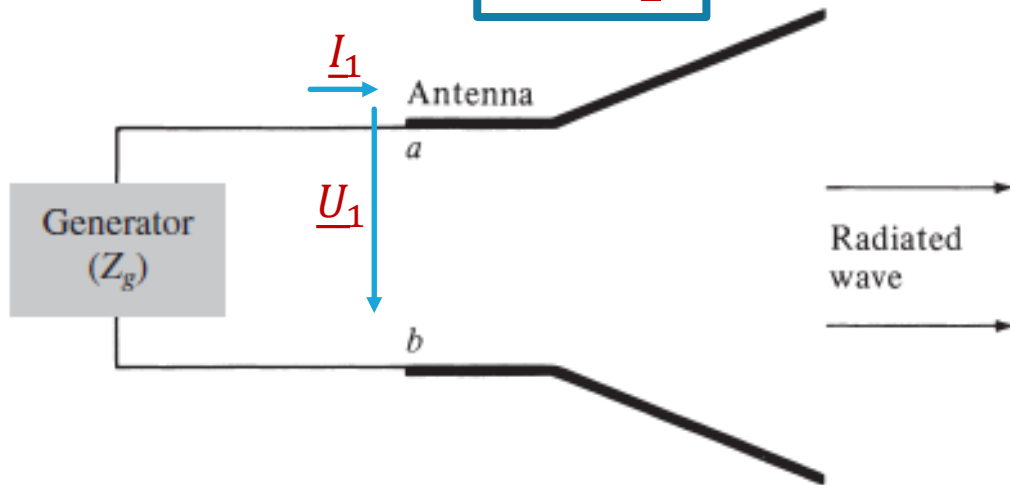
O antenna de satelit trebuie sa aiba o directivitate mare, pentru ca ea receptioneaza semnalele dintr-o directie fixa. De regula, antenele care au o dimensiune mai mica decat lungimea de unda au o directivitate mica.

1. Concepte utile

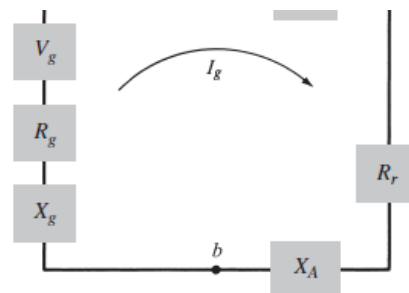
1.1. c) Antene

Impedanta de intrare

$$\underline{Z}_{in} = \frac{\underline{U}_1}{\underline{I}_1}$$



(a) Antenna in transmitting mode



(b) Thevenin equivalent

$$\underline{Z}_{in} = R_A + j X_A$$

Impedanta
antenei la
terminalele a-b

Rezistenta

Reactanta

In general, rezistenta antenei are doua componente

$$R_A = R_L + R_{rad}$$

Rezistenta de
pierderi (loss)

$R_{rad} = R_r$ Rezistenta de
radiatie

1. Concepte utile

1.1. c) Antene

Adaptarea antenelor la liniile de alimentare

$\lambda_0/4$ Transformer

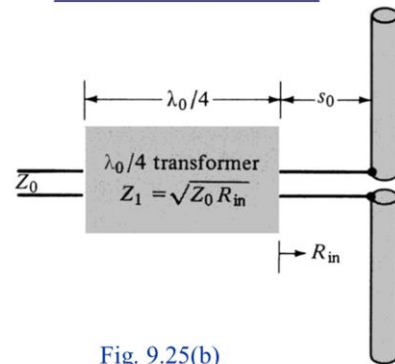


Fig. 9.25(b)

Copyright©2016 by Constantine A. Balanis
All rights reserved

Chapter 9
Broadband Dipoles and Matching Techniques

Shunt Matching

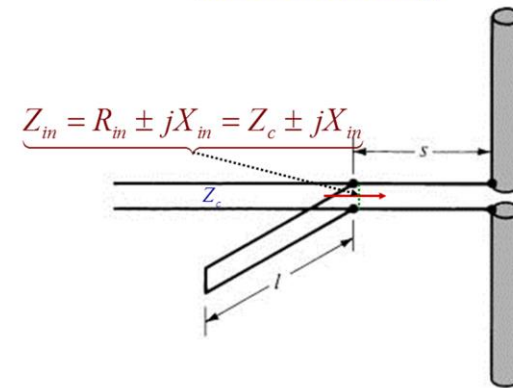


Fig. 9.25(a)

Copyright©2016 by Constantine A. Balanis
All rights reserved

Chapter 9
Broadband Dipoles and Matching Techniques

1. Concepte utile

1.1. c) Antene

Eficiența (randamentul)

E o masura a cat de bine o antenna primeste puterea primita in putere radiata.

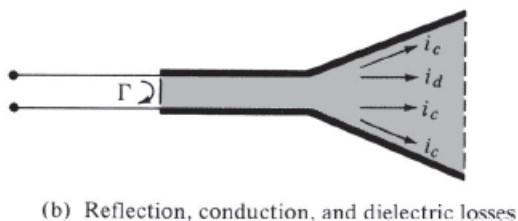
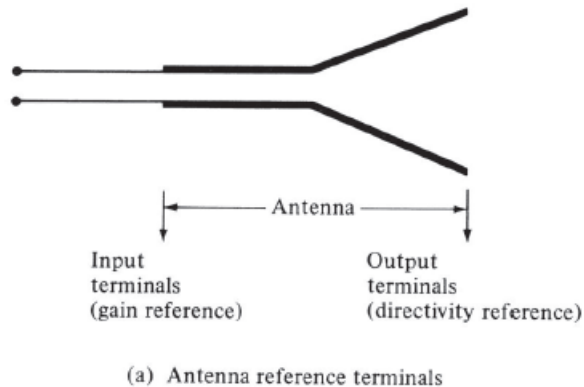


Figure 2.22 Reference terminals and losses of an antenna.

$$e_0 = e_r e_{cd}$$

e_0 - eficiența (randamentul) totală [adimensională]

e_r - eficiența datorată reflexiei $e_r = 1 - |\underline{\Gamma}|^2$

$$\underline{\Gamma} = \frac{Z_{in} - Z_0}{Z_{in} + Z_0}$$

e_{cd} - eficiența de radiație, include fenomenele de conducție-c și fenomenele în dielectrici-d

Dacă notăm P_p - puterea furnizată antenei de către generator.

$$e_r = \frac{P_{in}}{P_p}$$

Dacă antenna este adaptată: $P_{in} = P_p, e_r = 1$.

Dacă antenna nu este adaptată: $P_{in} < P_p, e_r < 1$.

$$e_{cd} = \frac{P_{rad}}{P_{in}} = \frac{P_{rad}}{P_{rad} + P_L}$$

P_L = putere disipată prin conducție în antenna

1. Concepte utile

1.1. c) Antene

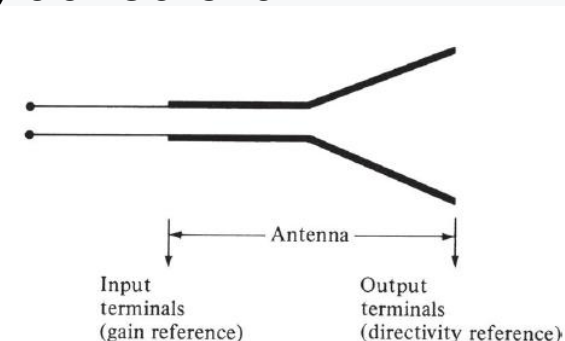
Castigul antenei

Este un numar de performanta (*figure of merit*) strans legat de directivitate, dar care ia in considerare si eficienta antenei (e_{cd}).

$$G(\theta, \varphi) = e_{cd} D(\theta, \varphi)$$

Considerand valoarea maxima

$$G_0 = e_{cd} D_0$$

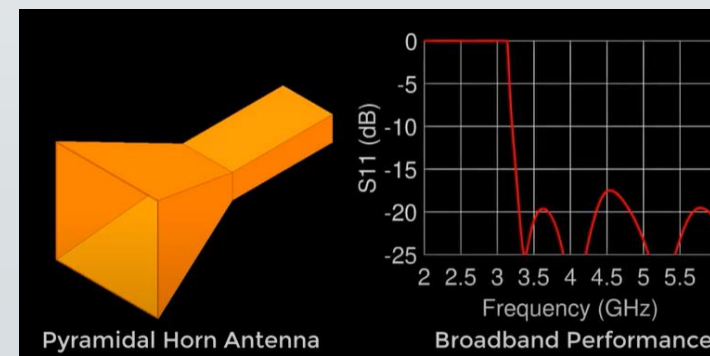
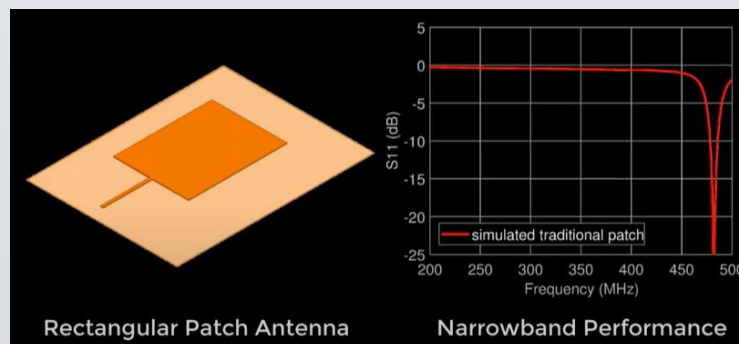


Lartimea de banda – gama de frecvente in care performantele antenei, in raport anumite caracteristici (de exemplu, impedanta de intrare, profilul de ratiatie, latimea lobului principal (beamwidth), polarizarea, latimea lobilor secundari, castigul, directia fascicolului, eficienta de radiatie) sunt conforme cu specificatiile dorite.

<https://www.youtube.com/watch?v=WuVv4tWVd8&list=PL2fRCJxWQiS916POeW3xkF5AU0H7ImNis&index=3>

Ex:

$$BW = \frac{f_{\max, -10dB} - f_{\min, -10dB}}{f_{\text{rez}}}$$



Se considera acceptabil

$$S_{11}(\text{dB}) \leq -10 \text{ dB}$$

1. Concepte utile

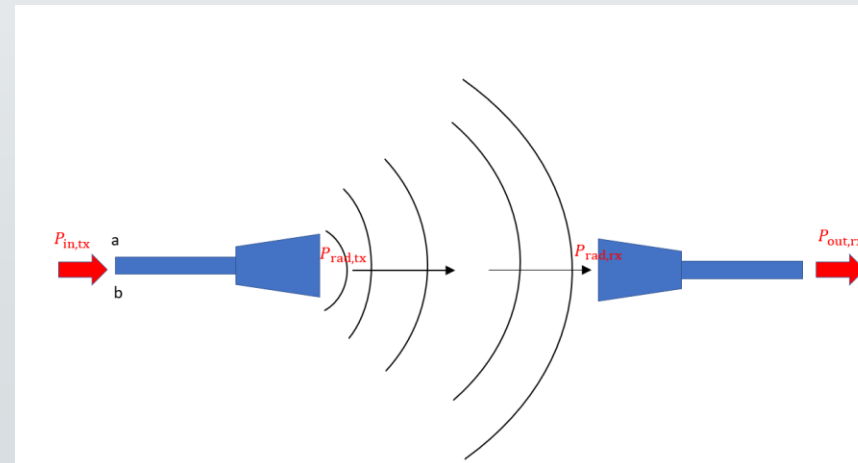
1.2. Sistem de 2 antene

Sistemele de comunicatie fara fir (*wireless*) transmit informatia dintre doua antene:

- O antenna care emite (transmitator – Tx)
- O antenna care receptioneaza (receptor – Rx)

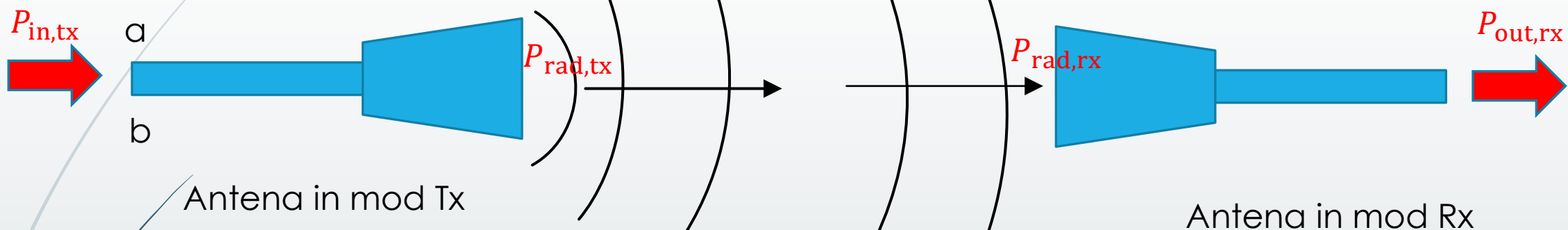
Puterea receptionata de antenna Rx depinde de:

- Puterea trimisa de antenna Tx
- Tipul antenelor (geometrie, materiale) – determina parametrii lor de performanta (e.g. castigul, largimea de banda)
- Pozitia relativa a antenelor
- Mediul prin care se propaga
- Compatibilitatea dintre cele 2 antene



1. Concepte utile

1.2. Sistem de 2 antene



Castigul sistemului $G_S = \frac{P_{out,Rx}}{P_{in,Tx}}$

A nu se confuda cu castigul antenei!

$P_{out,Rx}$

Puterea generata de portul antenei Rx

$P_{out,Tx}$

Puterea primita de portul antenei Tx

F3-EM, 2022-2023

Formula Friis

$$G_S = G_{Tx}(\theta_{Tx}, \varphi_{Tx}) G_{Rx}(\theta_{Rx}, \varphi_{Rx}) \left(\frac{\lambda}{4\pi r} \right)^2$$

Castigul antenei Tx

Castigul antenei Rx

(dep. de orientarea antenelor, care trebuie orientate corespunzator pentru un transfer maxim)

λ – lungimea de unda a semnalului

r – distanta dintre cele 2 antene

11/20/2022

1. Concepte utile

1.2. Sistem de 2 antene

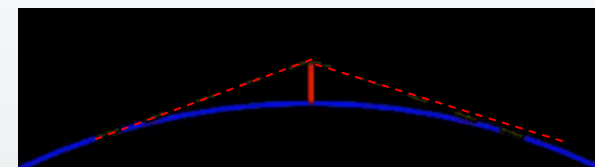
Formula Friis este valabila in urmatoarele ipoteze:

1. Se neglijeaza neadaptarea datorata unor **polarizari diferite**, se pp. ca antenele au acelasi fel de polarizare;
2. Se neglijeaza posibilele obstructii (mediul dintre cele doua antene se pp. omogen);
3. Se pp. ca intre cele 2 antene exista o linie dreapta (de exemplu semnalul nu s-ar putea transmite direct daca antena receptoare este dincolo de linia orizontului);
4. Se pp. mediul fara pierderi (nu exista atenuare datorata unor proprietati conductoare ale mediului);
5. Se pp. ca ambele antene sunt **perfect adaptate** circuitelor la care sunt conectate.

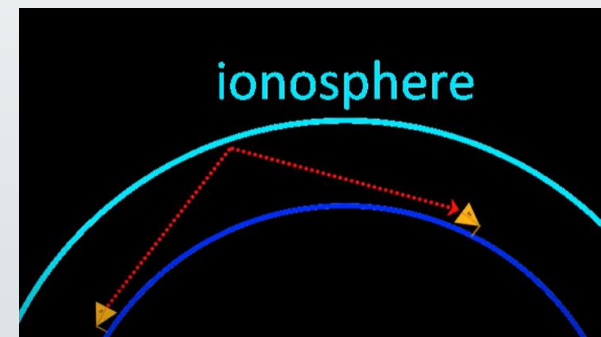
Chiar daca sunt multe ipoteze, formula Friis este utila pentru ca ea permite calculul puterii maxime care poate fi transmisa, datorata limitarilor fizice ale sistemului (2,3,4). Ipotezele 1 si 5 sunt la indemana proiectantilor de antene.

F3-EM, 2022-2023

Antena plasata la inaltimea de 2 m => transmite pana la 5 km
30 m => 21 km



Remediu



La frecventa mari, ionosfera se comporta ca un reflector.

<https://www.youtube.com/watch?v=EdvbgZo2MNg&list=PL2fRCJxWQis8AbtAcDF1AoB3q3qhZ57c&index=2>

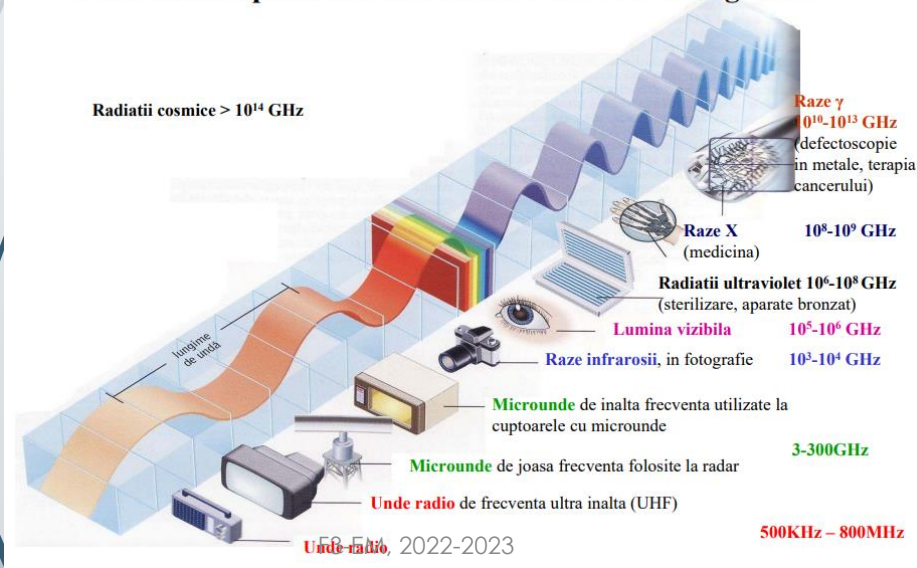
12/20/2022

1. Concepte utile

1.3. Principiul unui sistem de comunicatie RF (radio-frequency)

RF = frecventele cele mai joase ale spectrului EM, folosite in sistemele de comunicatii analoge si digitale. Cuprinde gama de frecvente dintre 3 kHz and 300 GHz. Aplicatii: radio analog, sistemele de navigatie ale aeronavelor, navelor maritime, radio de amatori, transmisii TV, retele mobile si sisteme de sateliti.

Clasificarea aplicatiilor ce folosesc unde electromagnetice



Radio Frequency Spectrum: Ranges

Designation	Abbreviation	Frequencies	Wavelengths
Very Low Frequency	VLF	3 kHz - 30 kHz	100 km - 10 km
Low Frequency	LF	30 kHz - 300 kHz	10 km - 1 km
Medium Frequency	MF	300 kHz - 3 MHz	1 km - 100 m
High Frequency	HF	3 MHz - 30 MHz	100 m - 10 m
Very High Frequency	VHF	30 MHz - 300 MHz	10 m - 1 m
Ultra High Frequency	UHF	300 MHz - 3 GHz	1 m - 100 mm
Super High Frequency	SHF	3 GHz - 30 GHz	100 mm - 10 mm
Extremely High Frequency	EHF	30 GHz - 300 GHz	10 mm - 1 mm

1. Concepte utile

1.3. Principiul unui sistem de comunicatie RF (radio-frequency)

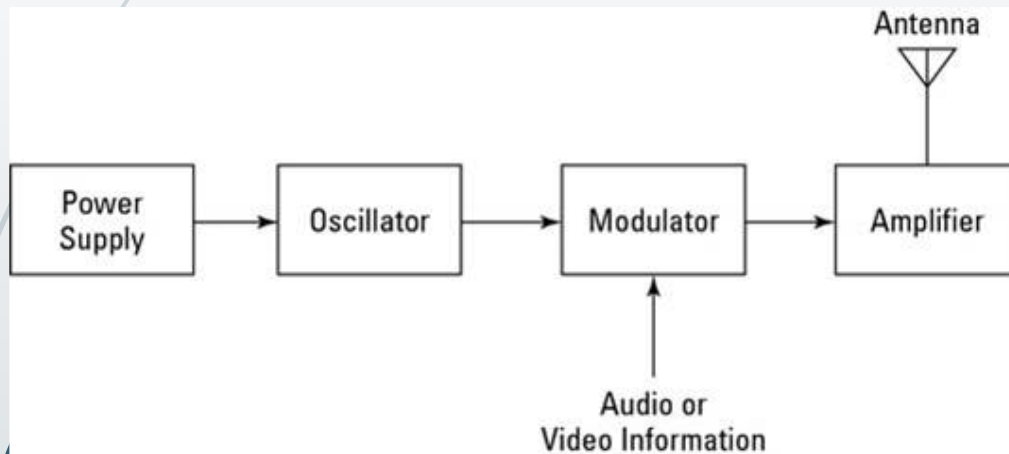


Diagrama bloc a unui sistem de emisie (Tx)

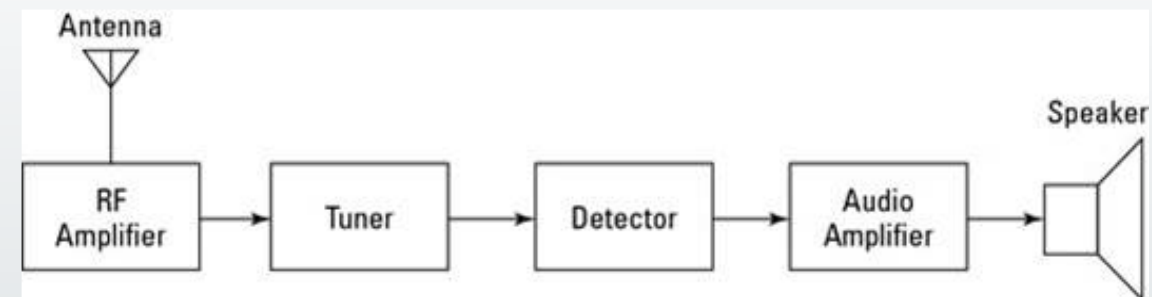


Diagrama bloc a unui sistem de receptie (Rx)

1. Concepte utile

1.3. Principiul unui sistem de comunicatie RF (radio-frequency)

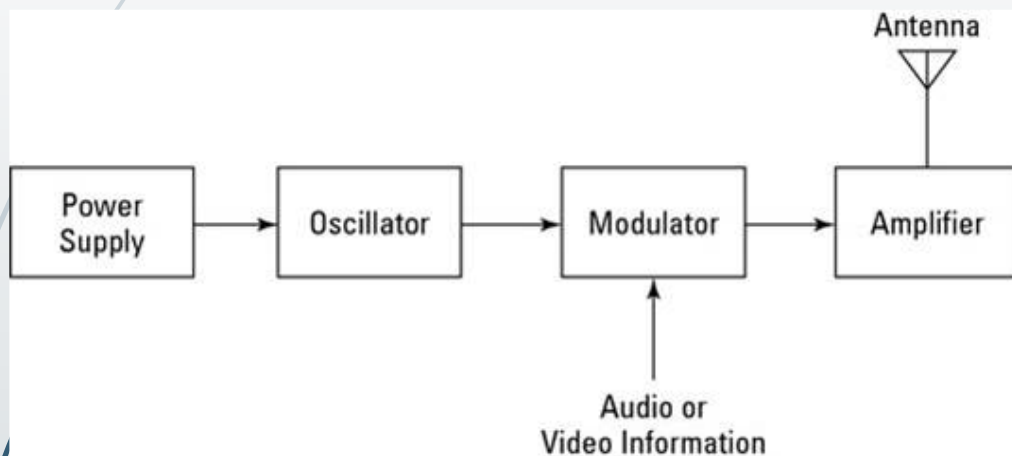


Diagrama bloc a unui sistem de emisie (Tx)

Semnalul util (de exemplu audio sau video) va fi combinat cu un semnal de frecventa inalta (semnal purtator) generat de un oscilator. Modulatorul este blocul care realizeaza aceasta combinatie a semnalelor. De exemplu, in cazul modulatiei in amplitudine (AM- amplitude modulation), invasuratoarea (anvelopa) semnalului modulat va fi proportionala cu semnalul util, de transmis. Semnalul rezultat este amplificat, el alimenteaza antenna de emisie, care genereaza undele EM.

1. Concepte utile

1.3. Principiul unui sistem de comunicatie RF (radio-frequency)

Sistemul de receptie incepe cu antenna care receptioneaza undele EM, la portul ei se induce un semnal, care este apoi preluat de un filtru (tuner) care extrage semnalul de frecventa dorita, din combinatia de semnale receptionate. Detectorul este blocul care separa semnalul purtator de semnalul util. Semnalul rezultat este amplificat si redat.

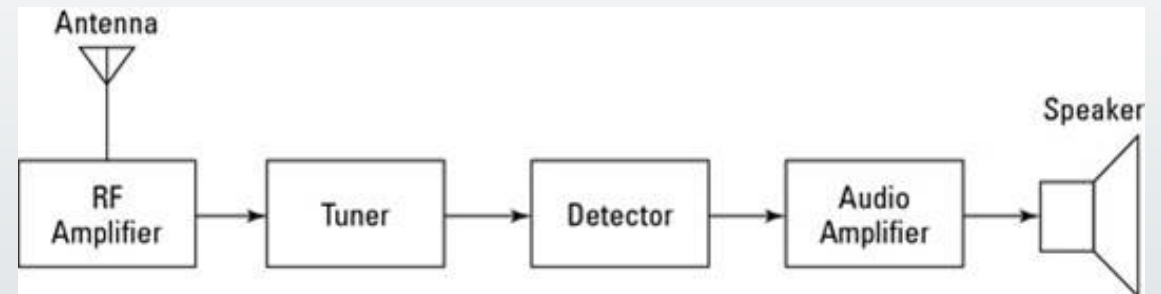


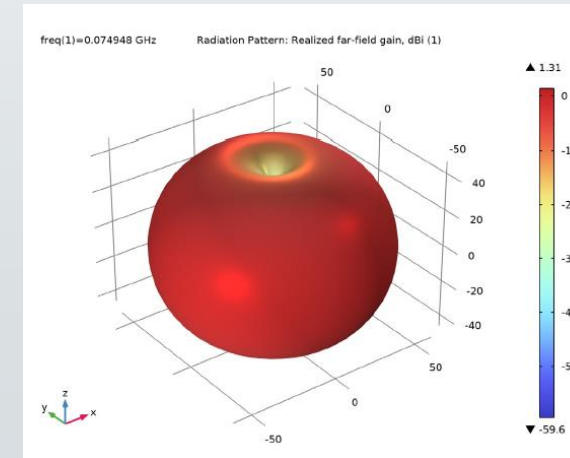
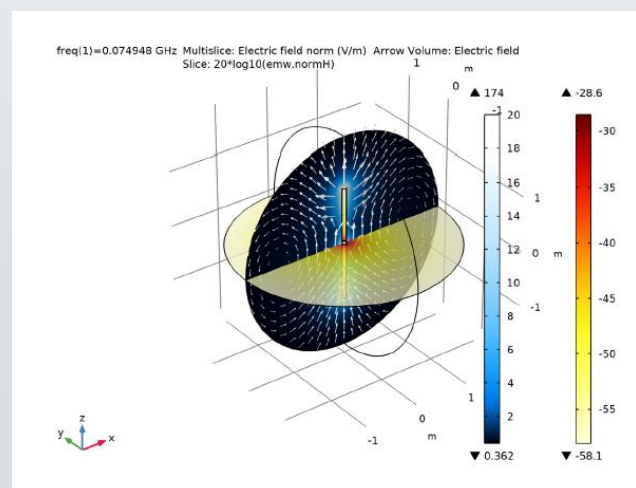
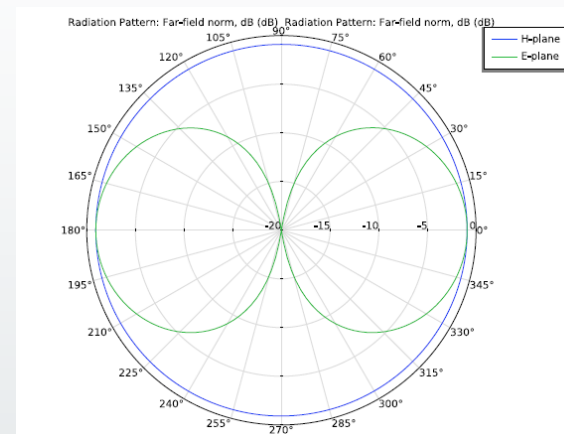
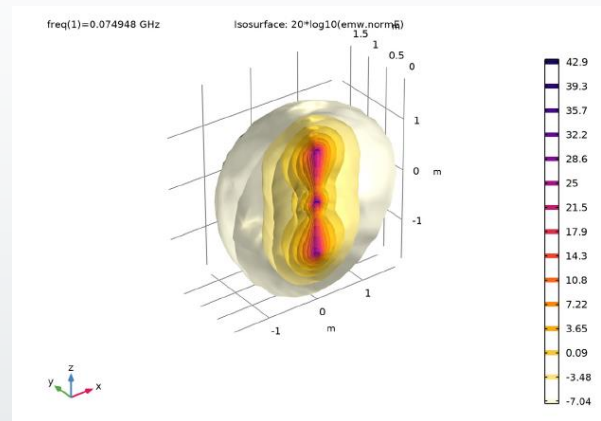
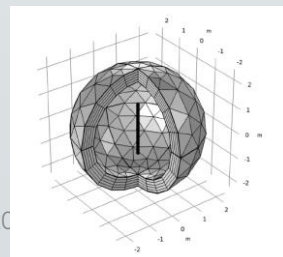
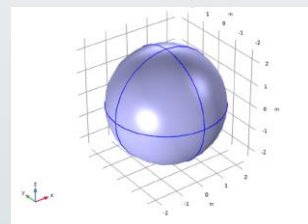
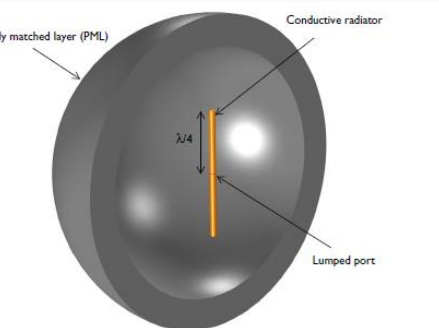
Diagrama bloc a unui sistem de receptie (Tx)

2. Esperimento virtuale

<https://www.comsol.com/model/dipole-antenna-8715>

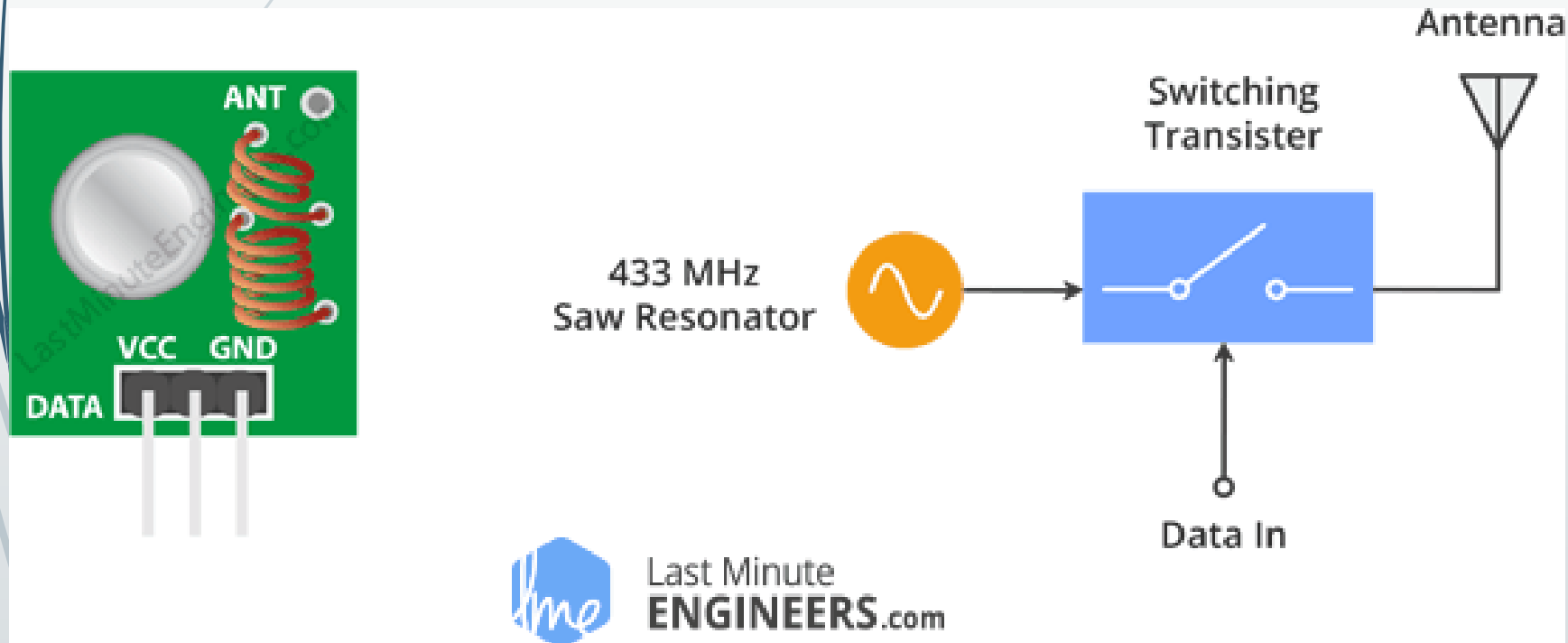
The length of the rods is chosen such that they are quarter wavelength elements at the operating frequency. The free space wavelength at the antenna's operating frequency is 4 m. Thus, each of the antenna arms is 1 m long and aligned with the z-axis. The arm radius is chosen to be 0.05 m. A small cylindrical gap of size 0.01 m between the antenna arms represents the voltage source. The power supply and feed structure are not modeled explicitly, and it is assumed that a uniform voltage difference is applied across these faces. This source induces electromagnetic fields and surface currents on the adjacent conductive faces. The air domain around the antenna is modeled as sphere of free space of radius 2 m, which is approximately the boundary between the near-field and the far-field. This sphere of air is truncated with a perfectly matched layer (PML) that acts as an absorber of outgoing radiation. The far-field pattern is computed on the boundary between the air and the PML domains. The mesh is manually adjusted such that there are five elements per free space wavelength and that the boundaries of the antenna are meshed more finely. The PML is swept with a total of five elements along the radial direction. The real part of the impedance as seen by the port is evaluated to be about $120 \, \Omega$ which agrees reasonably with expectations. With further tuning of the antenna length, radius and gap height to have the resonance at which the reactance is zero, the result approaches the well known value for a half-wave ($0.48 \lambda_0$) dipole antenna, which is $73 \, \Omega$.

$$f = \frac{c}{\lambda} = \frac{3 \cdot 10^8 \text{ m/s}}{4 \text{ m}} = 75 \text{ MHz}$$



3. Experiment real - Modulul RF Tx-Rx 433MHz

Diagrama bloc a sistem de emisie (Tx)

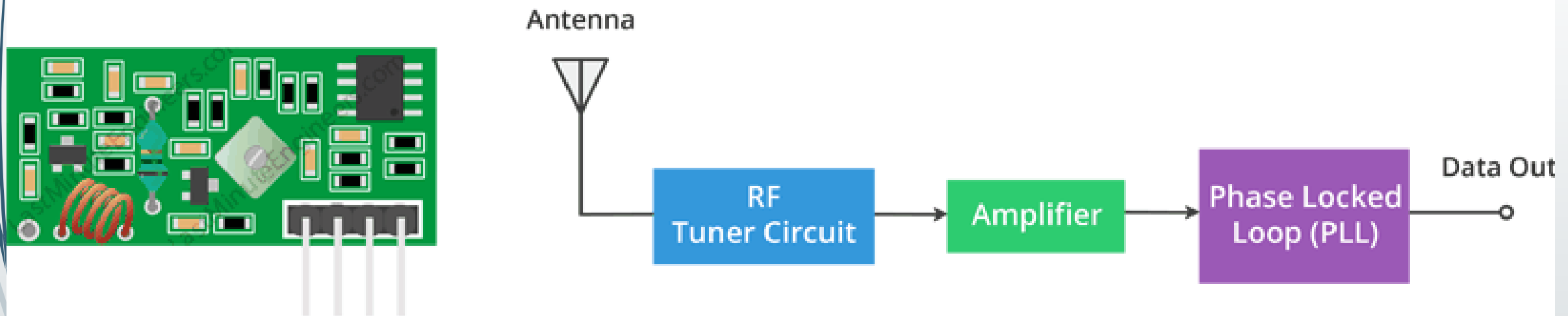


Specificatii:

- Launch distance :20-200 meters (different voltage - different results)
- Operating voltage :3.5-12V
- Dimensions: 19 * 19mm
- Operating mode: AM
- Transfer rate: 4KB / S
- Transmitting power: 10mW
- Transmitting frequency: 433M

3. Experiment real - Modulul RF Tx-Rx 433MHz

Diagrama bloc a sistem de receptie (Rx)



<https://lastminuteengineers.com/433mhz-rf-wireless-arduino-tutorial/>

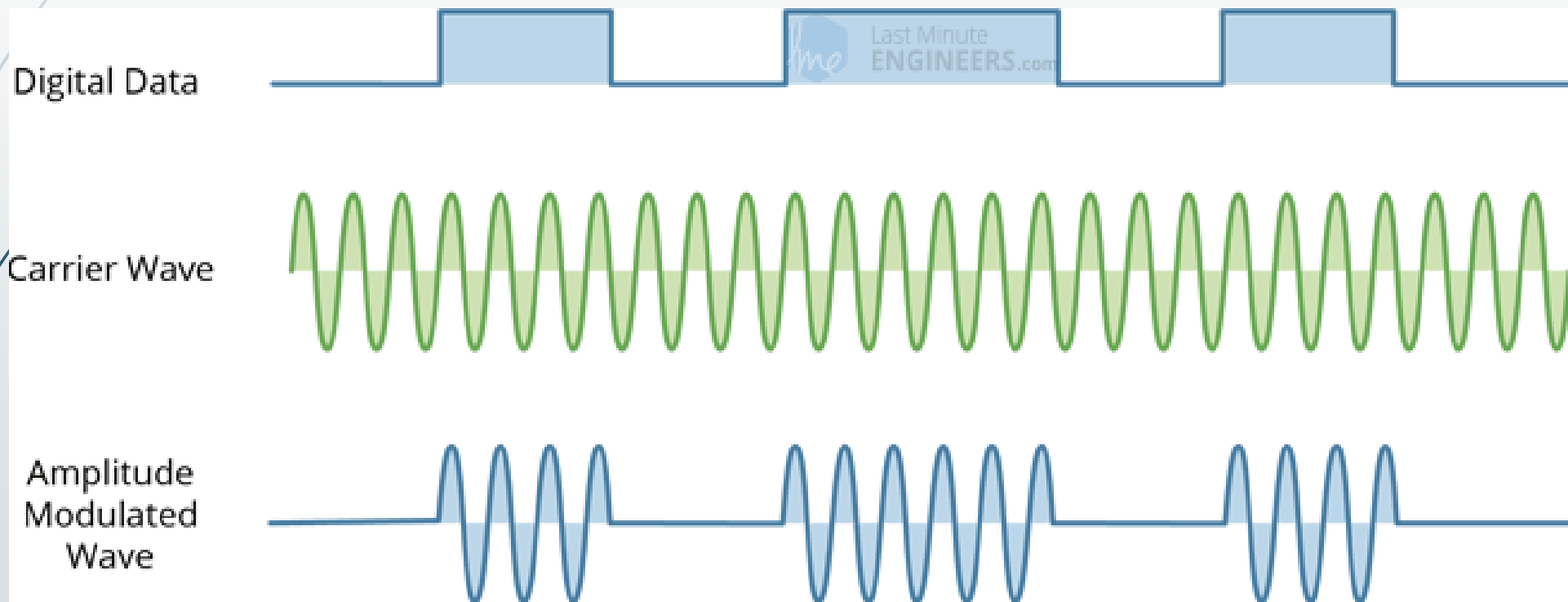
Specificatii:

- Operating mode: AM
- Operating voltage: DC5V
- Quiescent Current: 4mA
- Receiver sensitivity:-105DB
- Receiveng frequency: 433M
- Size: 30 * 14 * 7mm

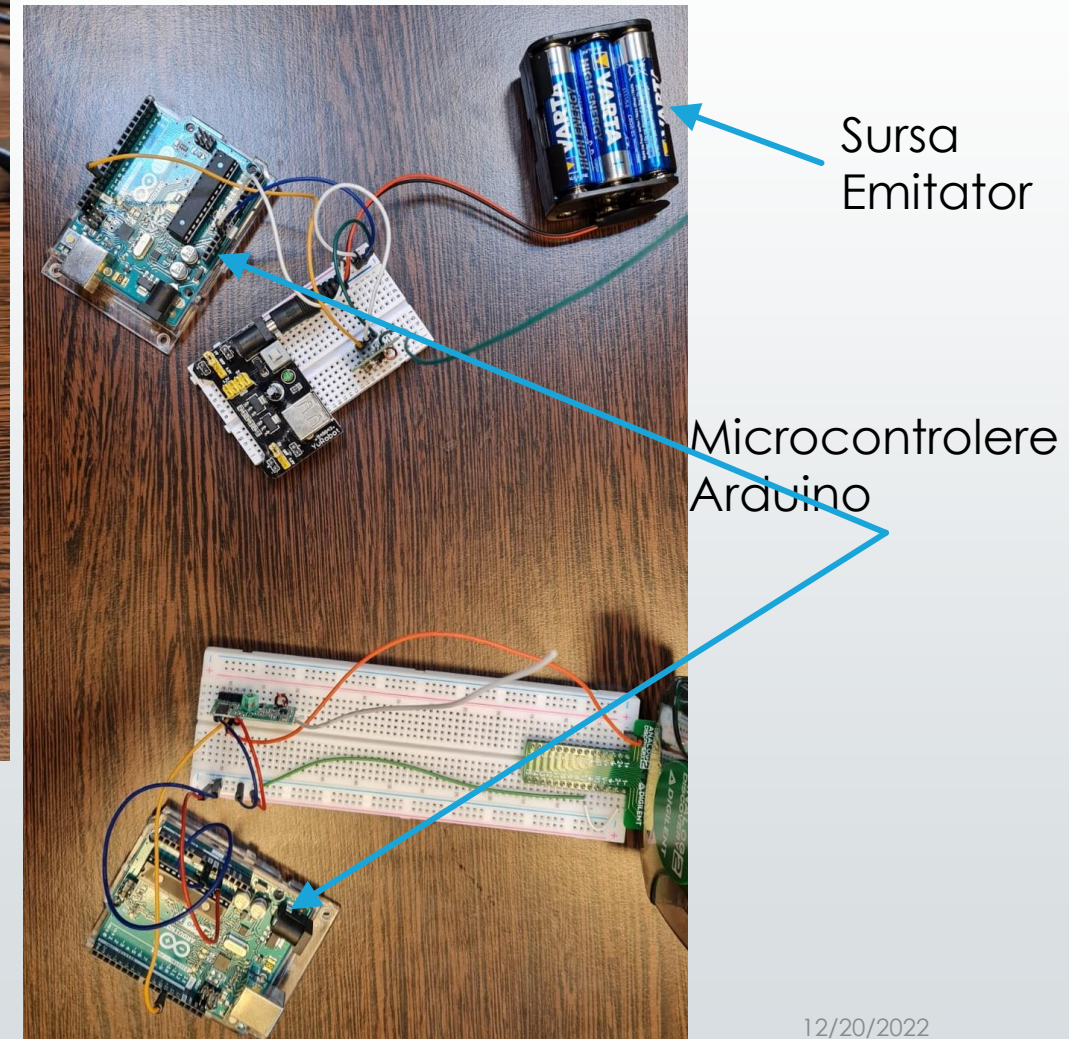
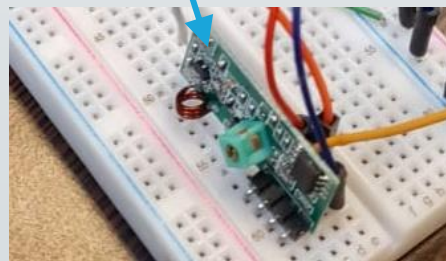
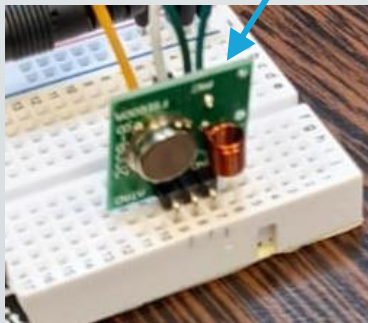
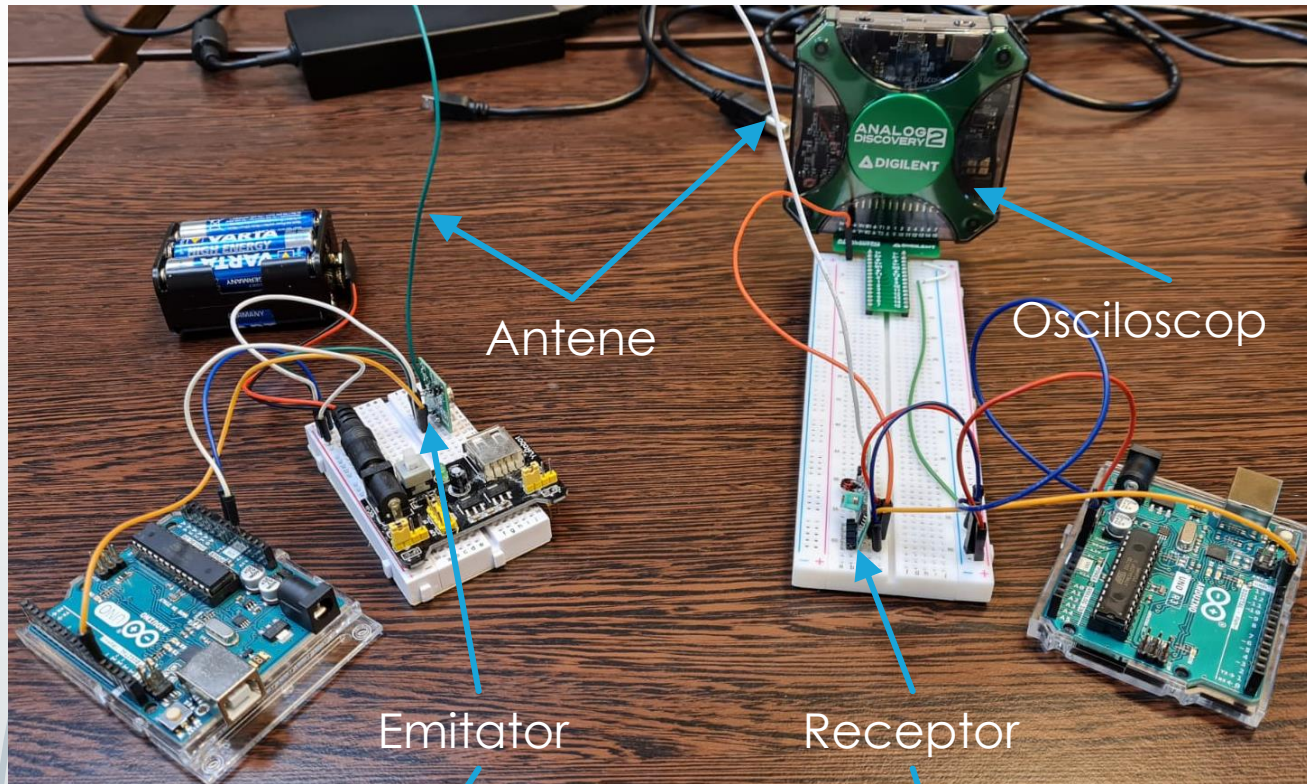
3. Experiment real - Modulul RF Tx-Rx 433MHz

Mod de functionare

- Utilizeaza tehnici de modulatie digitala – ASK (Amplitude-shift keying) pentru a transimite de date



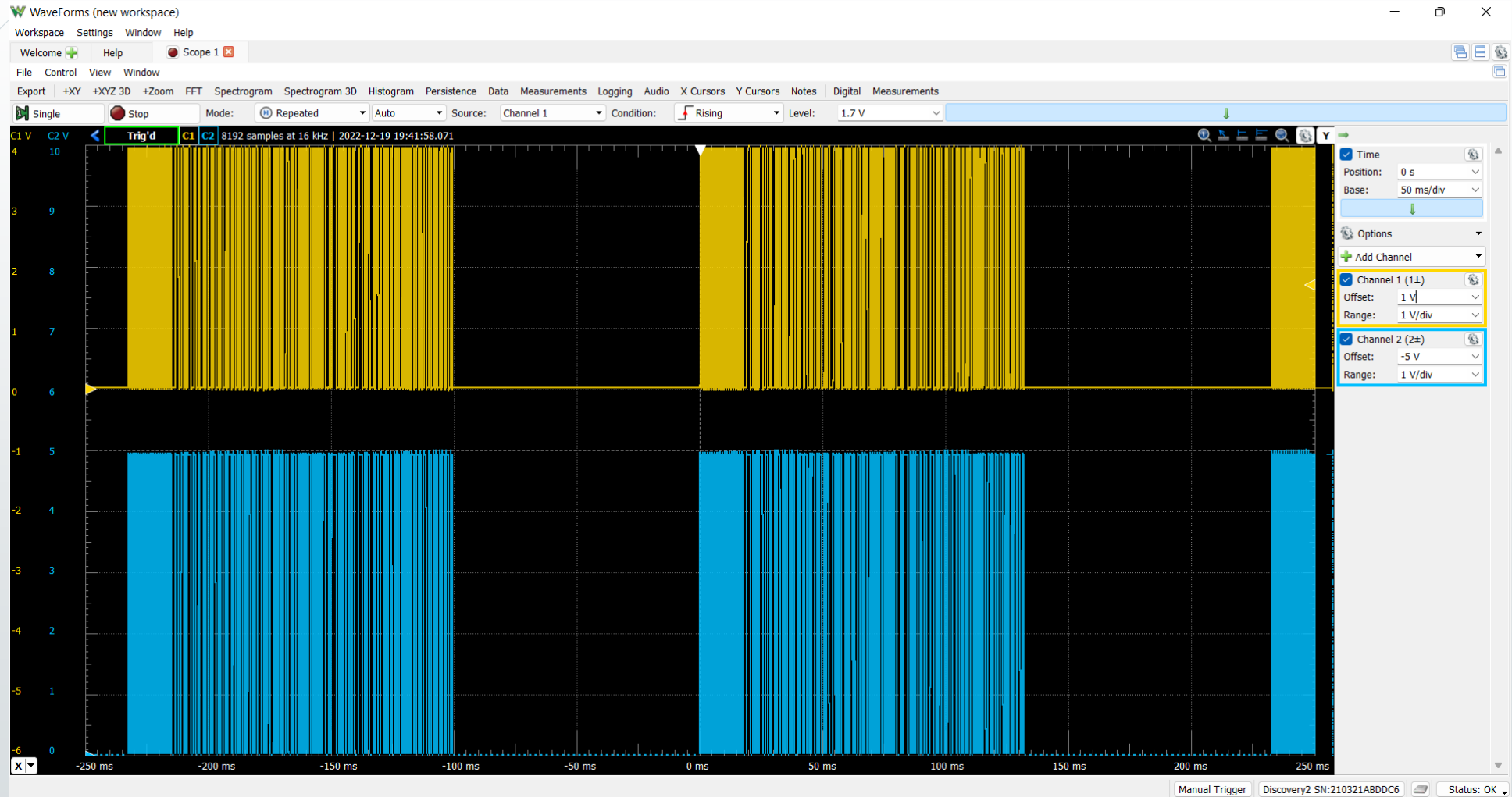
3. Experiment real – montaj experimental



3. Experiment real - rezultate

Semnal receptat

Semnal emis



Folosirea tehnologiei wireless in locul cablurilor:

- Avantaje: costul mai redus, mobilitatea, instalarea mai simpla, robustetea (se defecteaza mai greu decat reseau de cabluri), poate fi folosita si dupa dezastre (cutremure, inundatii, incendii).
- Dezavantaje,: interferente nedorite cu alte sisteme wireless, securitate mai slaba decat cea oferita de cabluri, ingrijorarile privind efectul undelor (mai ales cele de mare putere) asupra sanatatii.

In secolul XXI, comunicatiile bazate pe unde electromagnetice au avut o dezvoltare exploziva, care a generat profunde modificari sociale si culturale: posta electronica (email, prin Gmail sau alte servere), telefonie celulara, retelele de calculatoare, in general internetul (Chrome), cu multiplele sale aplicatii. Smartphonurile au tot mai multa putere de calcul, memorie, dar si de comunicatii (au nu numai functii GSM, ci si Wi-Fi, Bluetooth si RFID), la fel si laptopurile. Criza pandemica a contribuit si ea la folosirea tot mai intensiva a telemuncii si a scolii online, ambele bazate pe comunicatii fara fir. Infrastructura hardware, retele de calculatoare si solutii software dedicate, cum sunt Team, Moodle, sau alte tehnici digitale colaborative.

Toate acestea ar fi fost imposibile fara telecomunicatiile prin unde electromagnetice. Si revolutia nu se termina aici.

Notare

- Rezolvati quiz-ul P6.

- Pentru bonus (pana in saptamana 14)
 - – crearea unor figuri/animatii proprii ilustrative pentru cursul de EM, folosind coduri proprii si instrumente software mai performante, de exemplu <https://vtk.org/>, <https://www.paraview.org/>
 - - realizarea unor experimente virtuale/reale care sa ilustreze conceptele discutate.