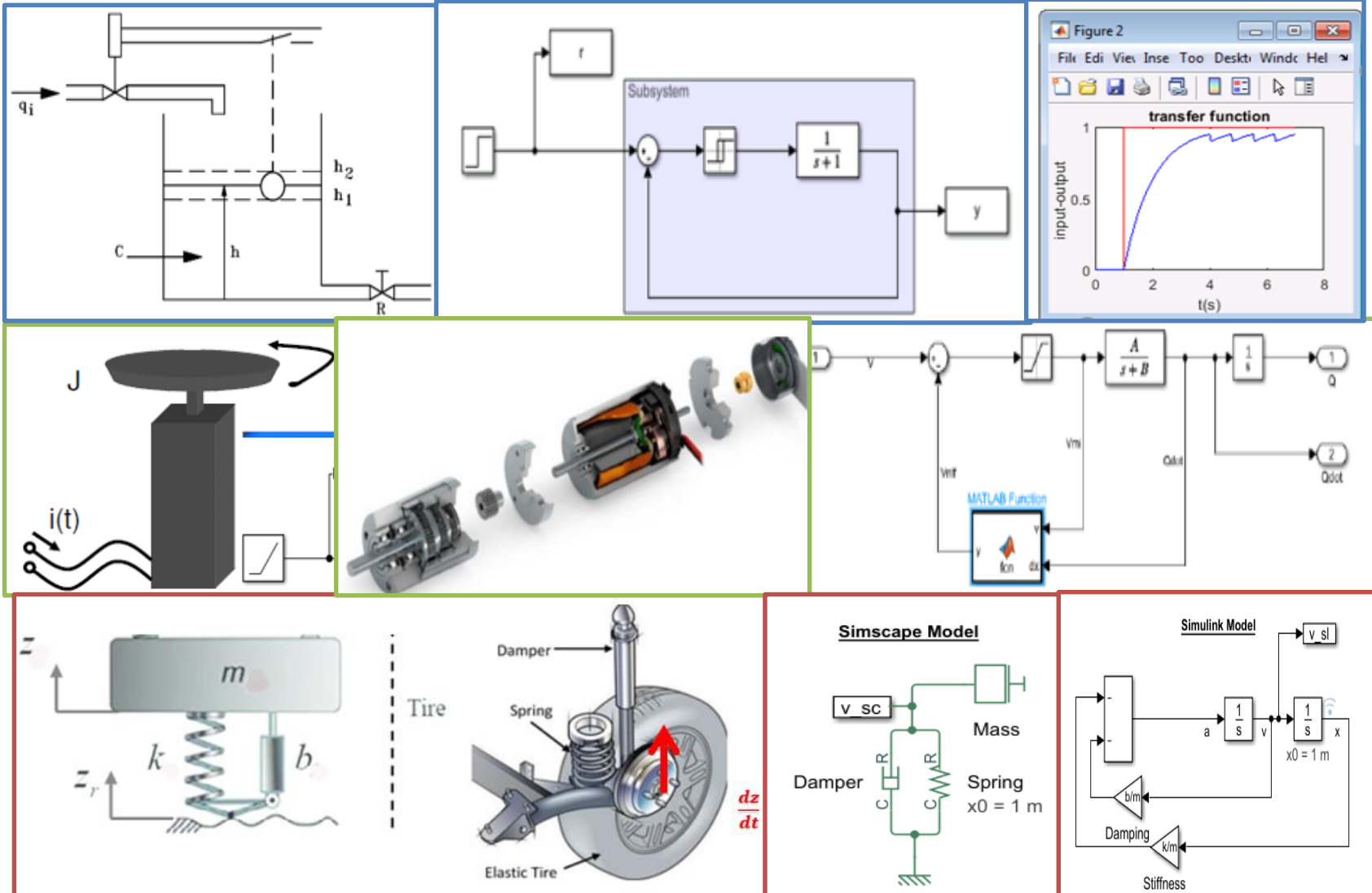


Modeling & Simulation of Dynamic Systems (MSDS)

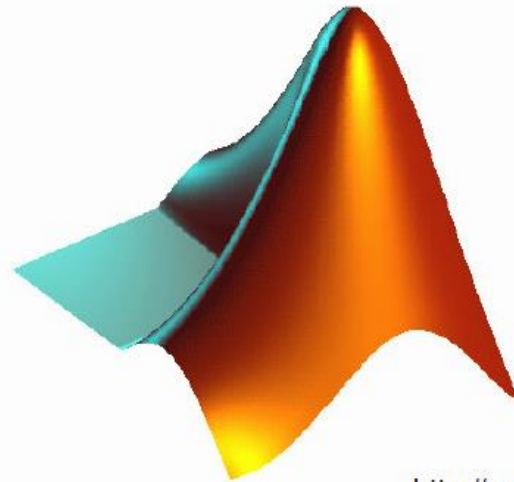
Simulation and Model Based Design

Introduction to System Modeling with MATLAB and Simulink and the Use of the Live Editor



In this course on system modeling with MATLAB and Simulink, you'll learn the basics of Simulink and Simscape, two powerful tools for simulating dynamic systems. We'll cover everything from connecting blocks to modeling complex mechanical systems, giving you practical experience in system analysis. Let's dive in and explore together!

MATLAB SIMULINK® - Simulation and Model Based Design

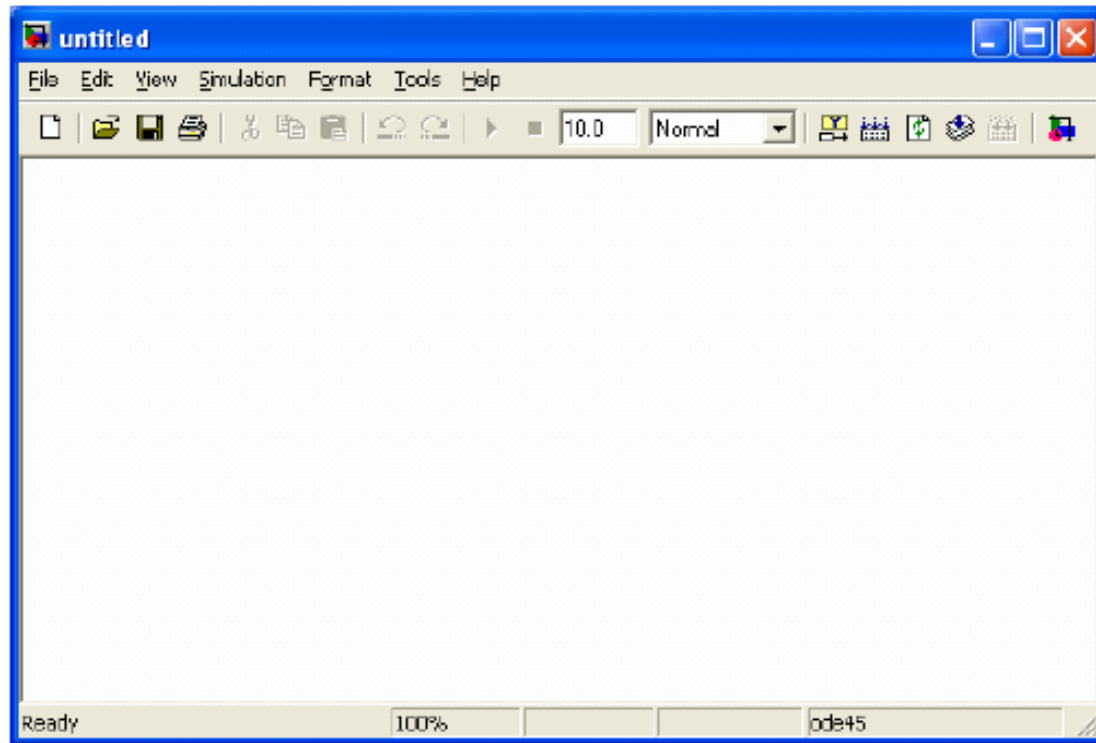


<http://www.mathworks.com>

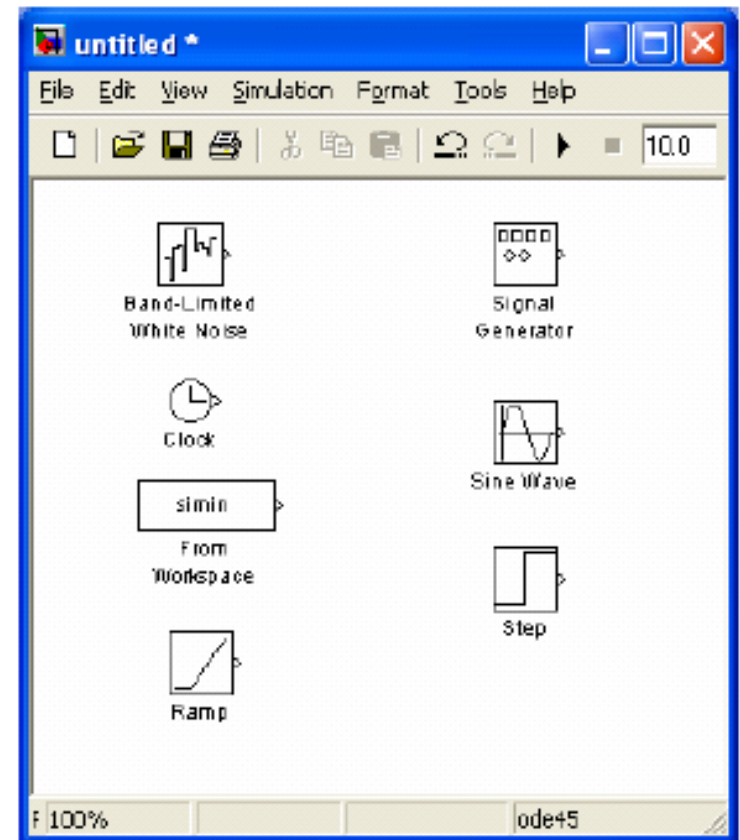
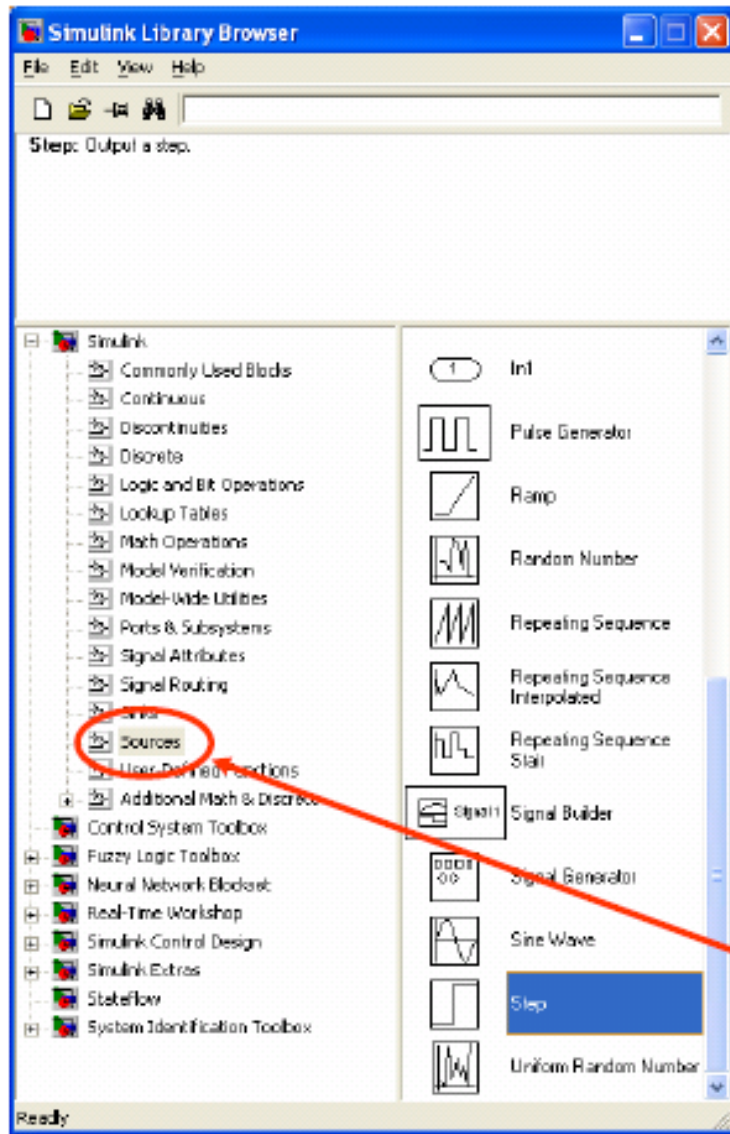
What is Simulink good for?

- Modeling/designing dynamic systems (including nonlinear dynamics)
- Modeling/designing control systems (including nonlinear controllers and plants)
- Signal processing design/simulation

A Simulink model is a block diagram. Click “File|New|Model” in the Library Browser. An empty block diagram will pop up. You can drag blocks into the diagram from the library.

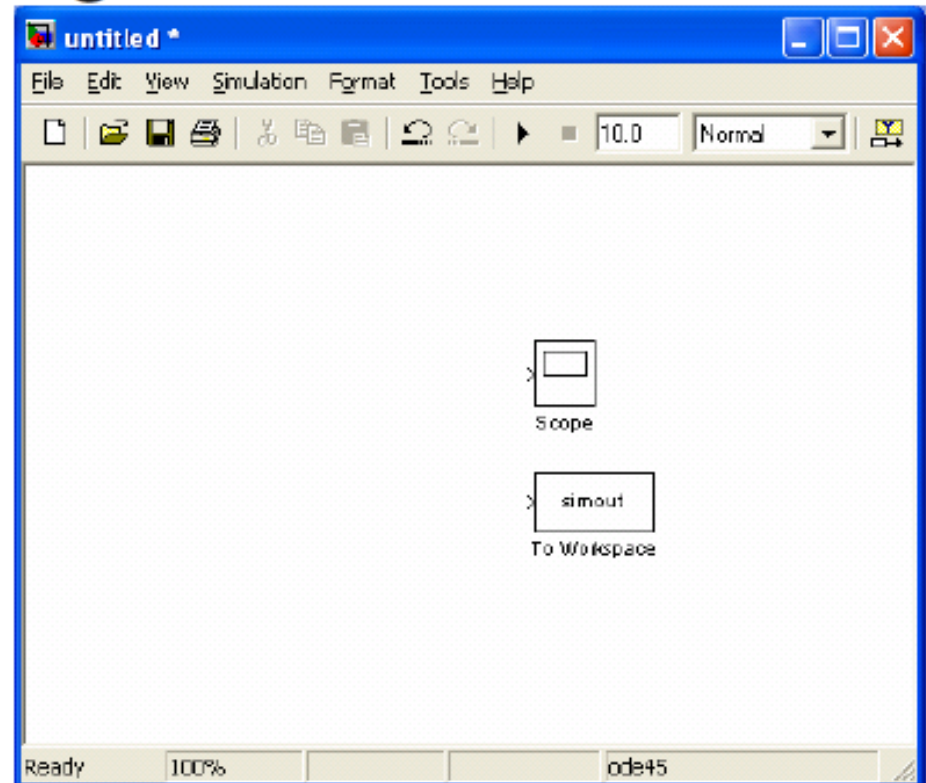
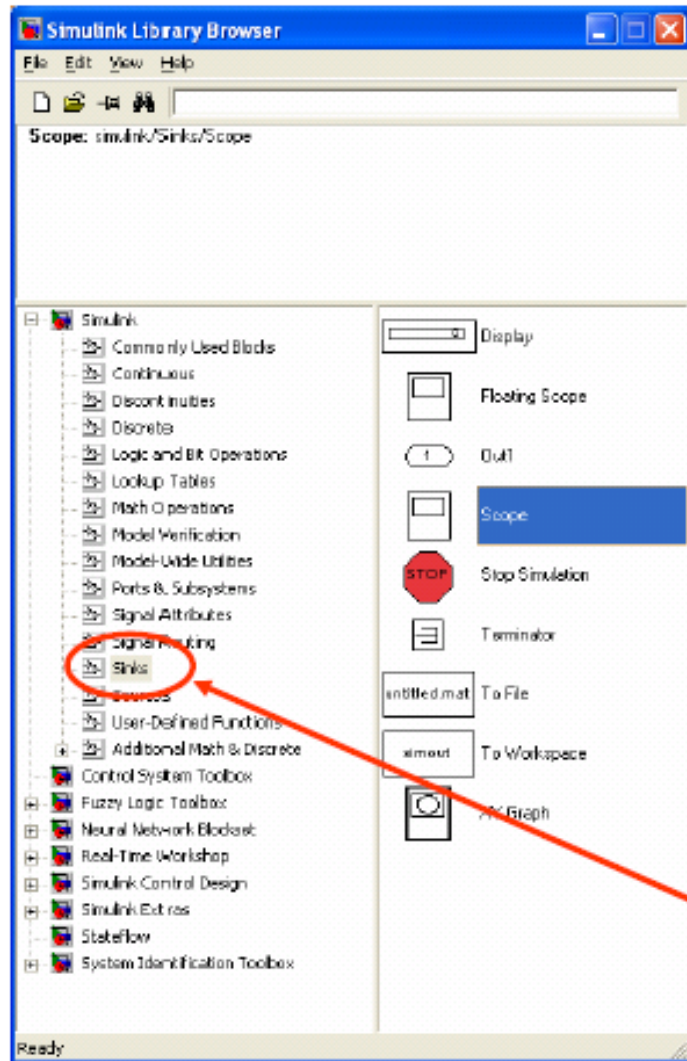


Sources: Produce Signals



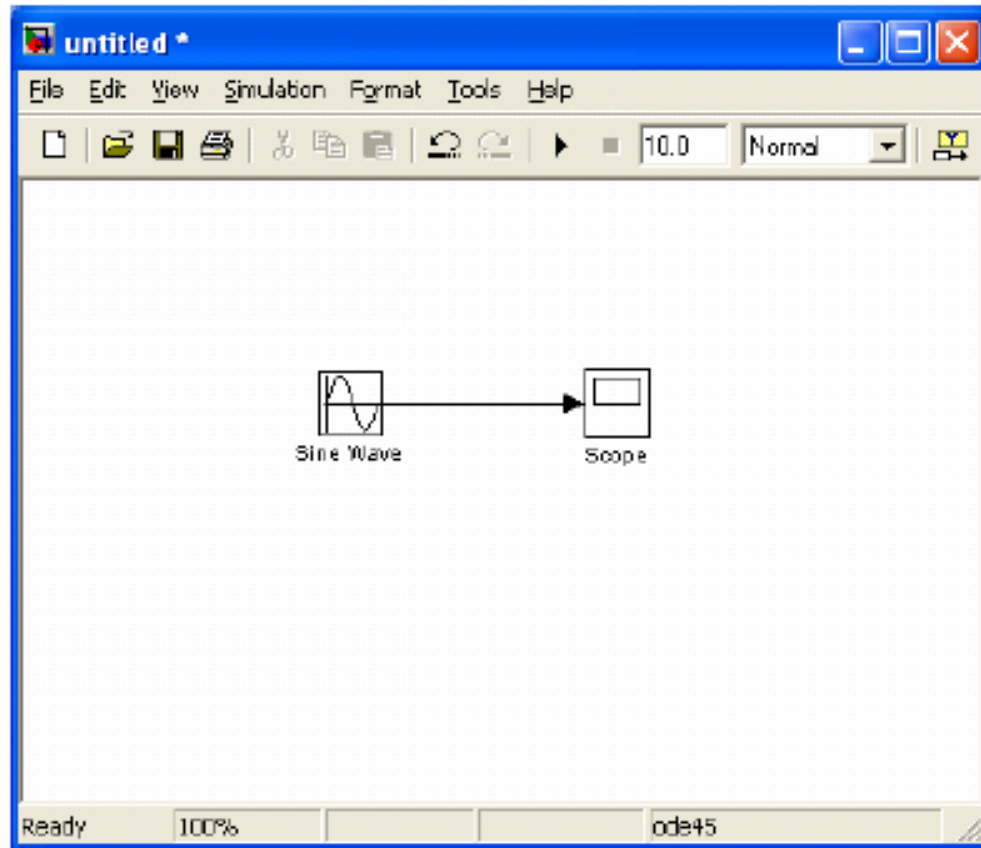
Select "sources" from the library.
Drag any block you want to use
into the model.

Sinks: Terminate Signals



Select "sinks" from the library.
Drag any block you want to use
into the model.

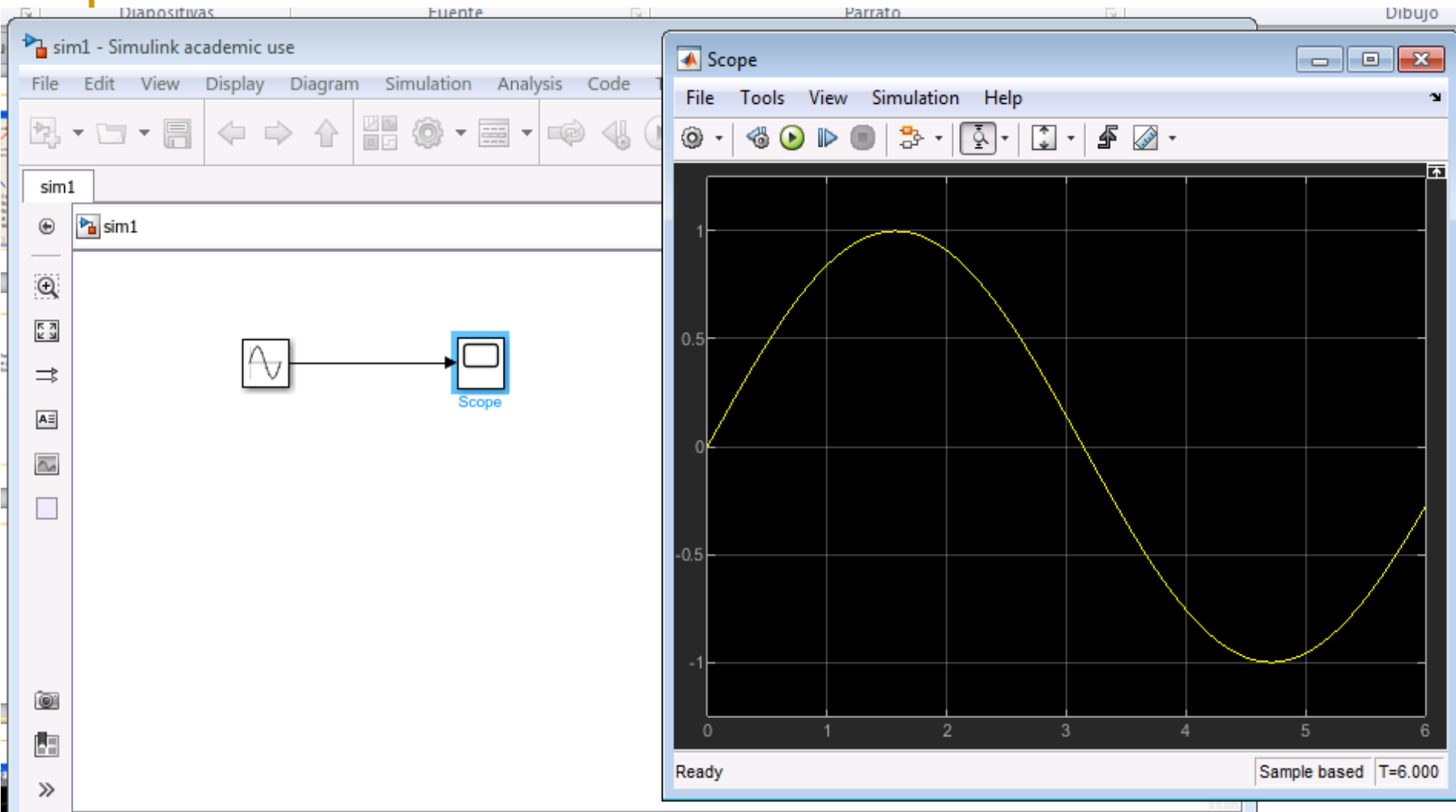
Connecting Blocks



Drag a signal line from the output of a block to the input of another block.

Ctrl-Click will automatically connect.

Viewing Results: Scope



Running the Simulation

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%%% FIRST PROGRAM
```

```
%%%
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%% 1. PARAMETERS
```

```
t_s = 10;
```

```
h = 0.001;
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%% 2. VALUES
```

```
% Sin Input
```

```
A=1;
```

```
f=3; %(rad)
```

```
% 3. SIMULATION AND PLOTS
```

```
sim sin_w
```

```
%%% plots
```

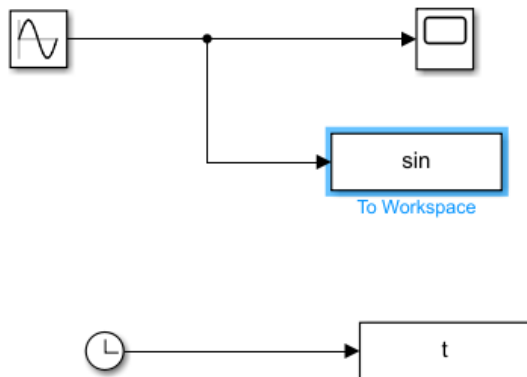
```
figure;
```

```
plot(t,sin_w);
```

```
xlabel('Time(s)');
```

```
ylabel('sin (rad.)');
```

```
title('Simula sin');
```



Block Parameters: To Workspace

To Workspace

Write input to specified timeseries, array, or structure in a workspace. For menu-based simulation, data is written in the MATLAB base workspace. Data is not available until the simulation is stopped or paused.

To log a bus signal, use "Timeseries" save format.

Parameters

Variable name:

Limit data points to last:

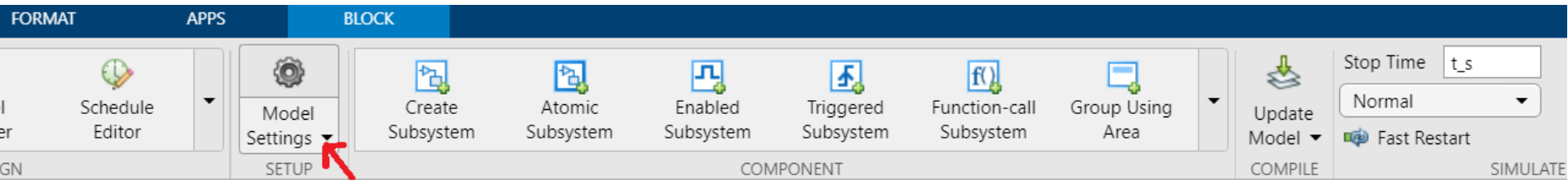
Decimation:

Save format:

Save 2-D signals as:

☒ Log fixed-point data as a fi object

Sample time (-1 for inherited):



Configuration Parameters: sin_in/Configuration (Active)

Search

Solver

Data Import/Export
Math and Data Types

- ▶ Diagnostics
- Hardware Implementation
- Model Referencing
- Simulation Target
- ▶ Code Generation
- ▶ Coverage
- ▶ HDL Code Generation

Simulation time

Start time: 0.0

Stop time: t_s

Solver selection

Type: Fixed-step

Solver: ode5 (Dormand-Prince)

▼ Solver details

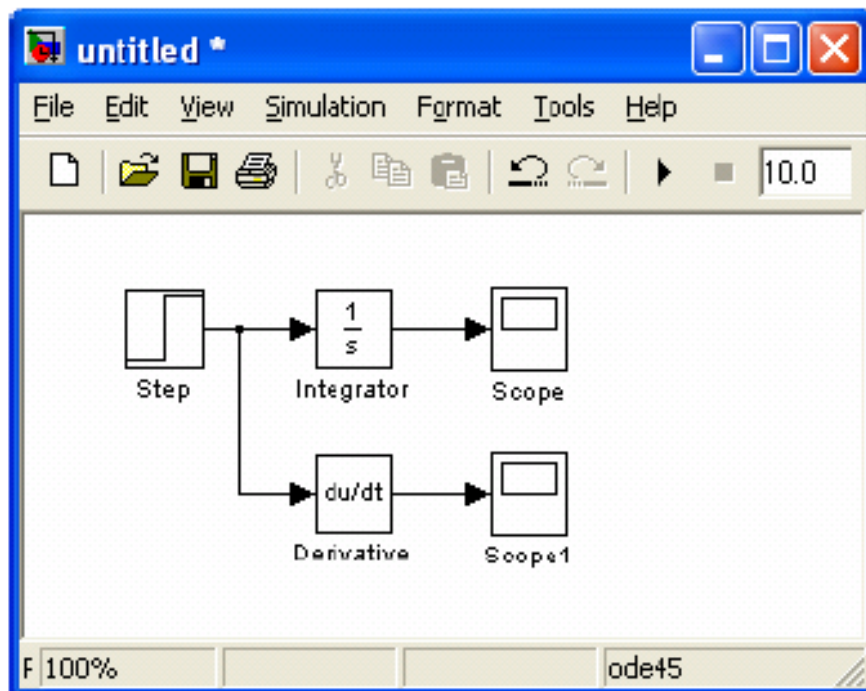
Fixed-step size (fundamental sample time): h

Tasking and sample time options

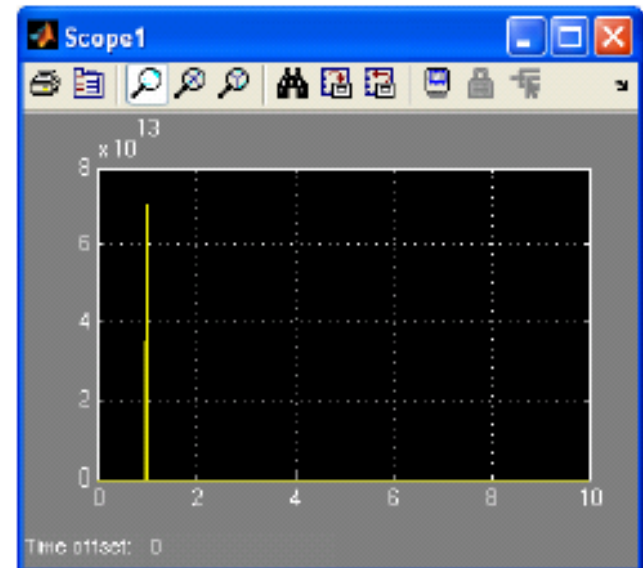
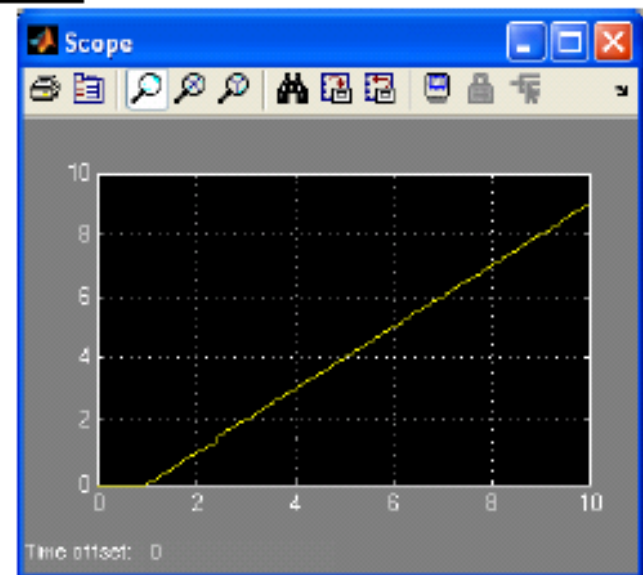
Periodic sample time constraint: Unconstrained

- ☐ Treat each discrete rate as a separate task
- ☐ Allow tasks to execute concurrently on target
- ☐ Automatically handle rate transition for data transfer
- ☐ Higher priority value indicates higher task priority

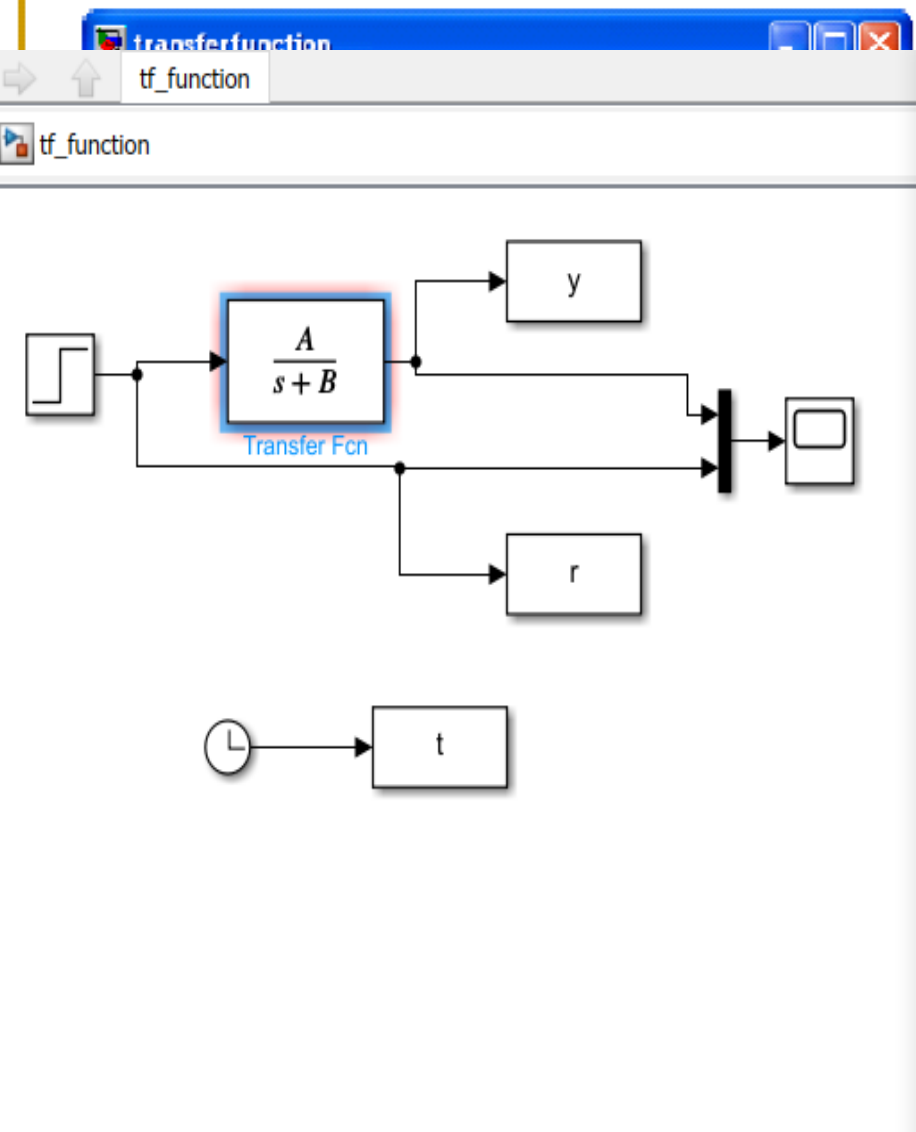
Integrators and Derivatives



Integrators and derivatives are available in the “continuous” library.



Transfer Functions



Block Parameters: Transfer Fcn

Transfer Fcn

The numerator coefficient can be a vector or matrix expression. The denominator coefficient must be a vector. The output width equals the number of rows in the numerator coefficient. You should specify the coefficients in descending order of powers of s .

Parameters

Numerator coefficients:

[A]

Denominator coefficients:

[1 B]

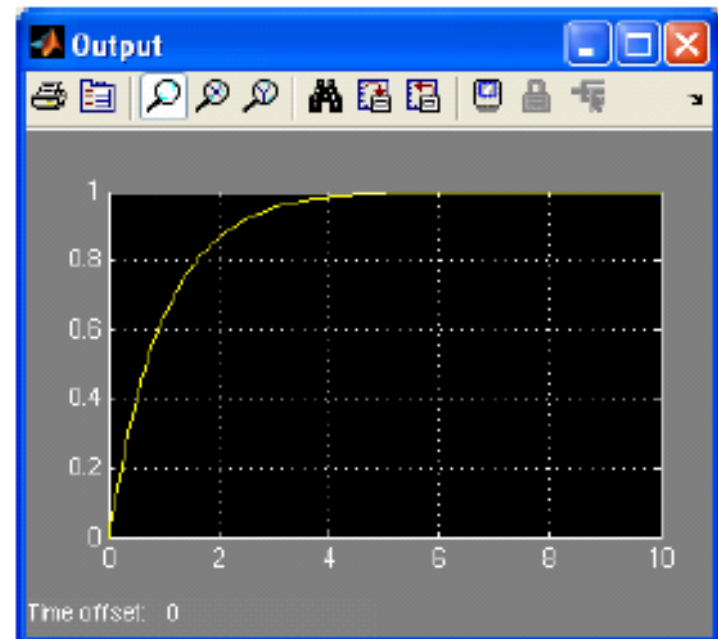
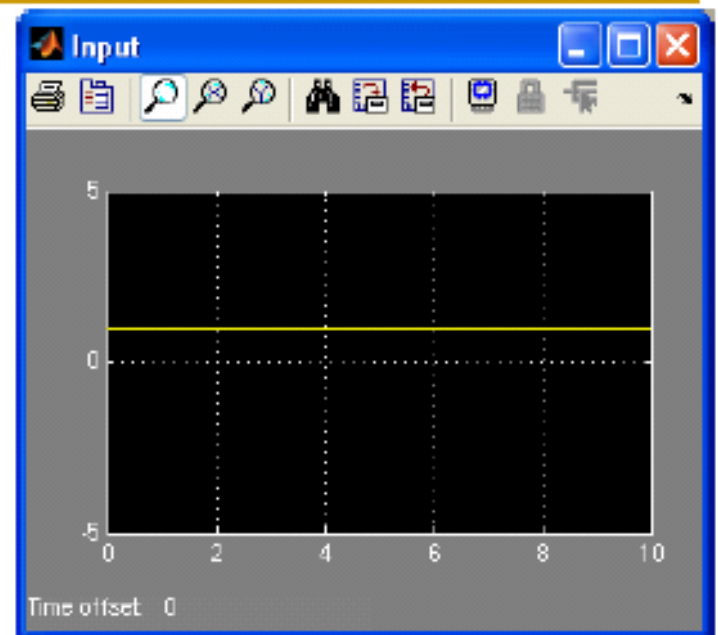
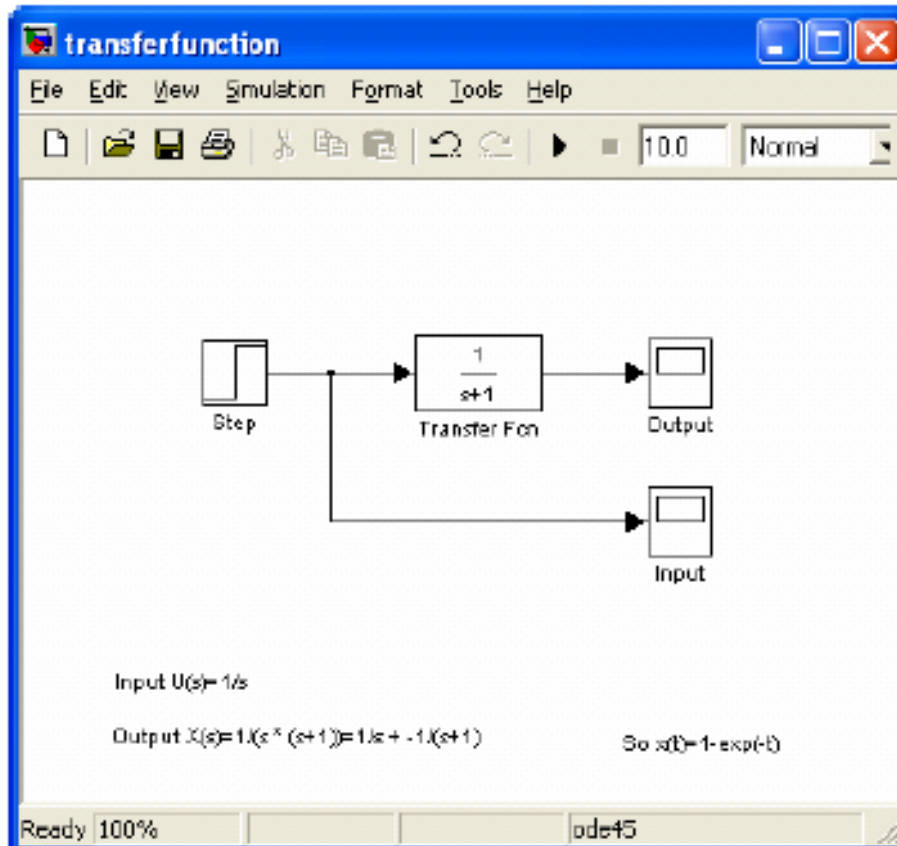
Absolute tolerance:

auto

State Name: (e.g., 'position')

"

Transfer Functions



$$U(s) = 1/s$$

$$X(s) = 1/(s(s+1)) = 1/s - 1/(s+1)$$

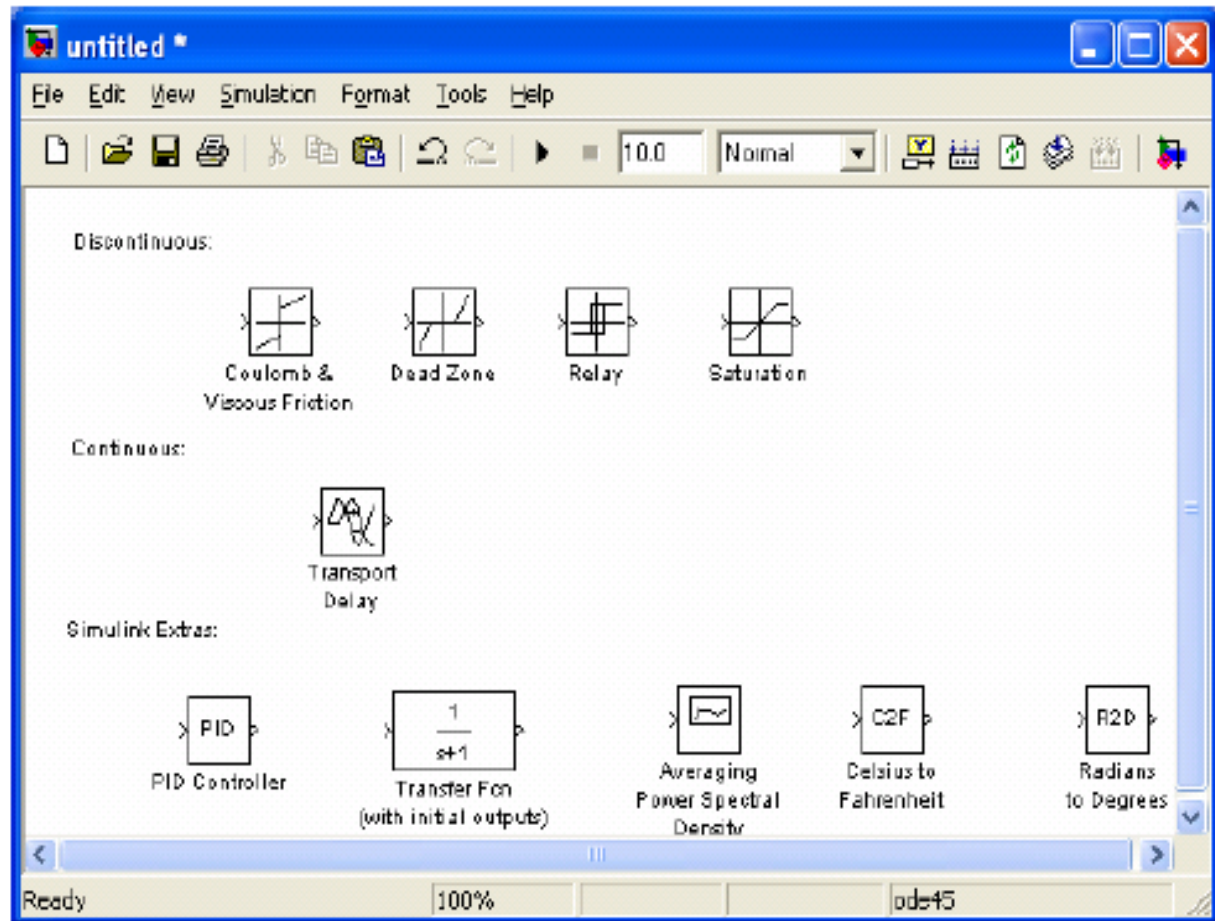
$$\text{So } x(t) = 1 - \exp(-t)$$

Other Useful Blocks

Under “Discontinuous” you will find coulomb friction, dead zone, saturation, and relay.

Under “Continuous” there is a delay block.

Under “Simulink Extras” there is a PID controller, transfer function with non-zero initial conditions, some useful sinks (such as power spectral density), and radians-to-degrees and Fahrenheit-to-Celsius converters.

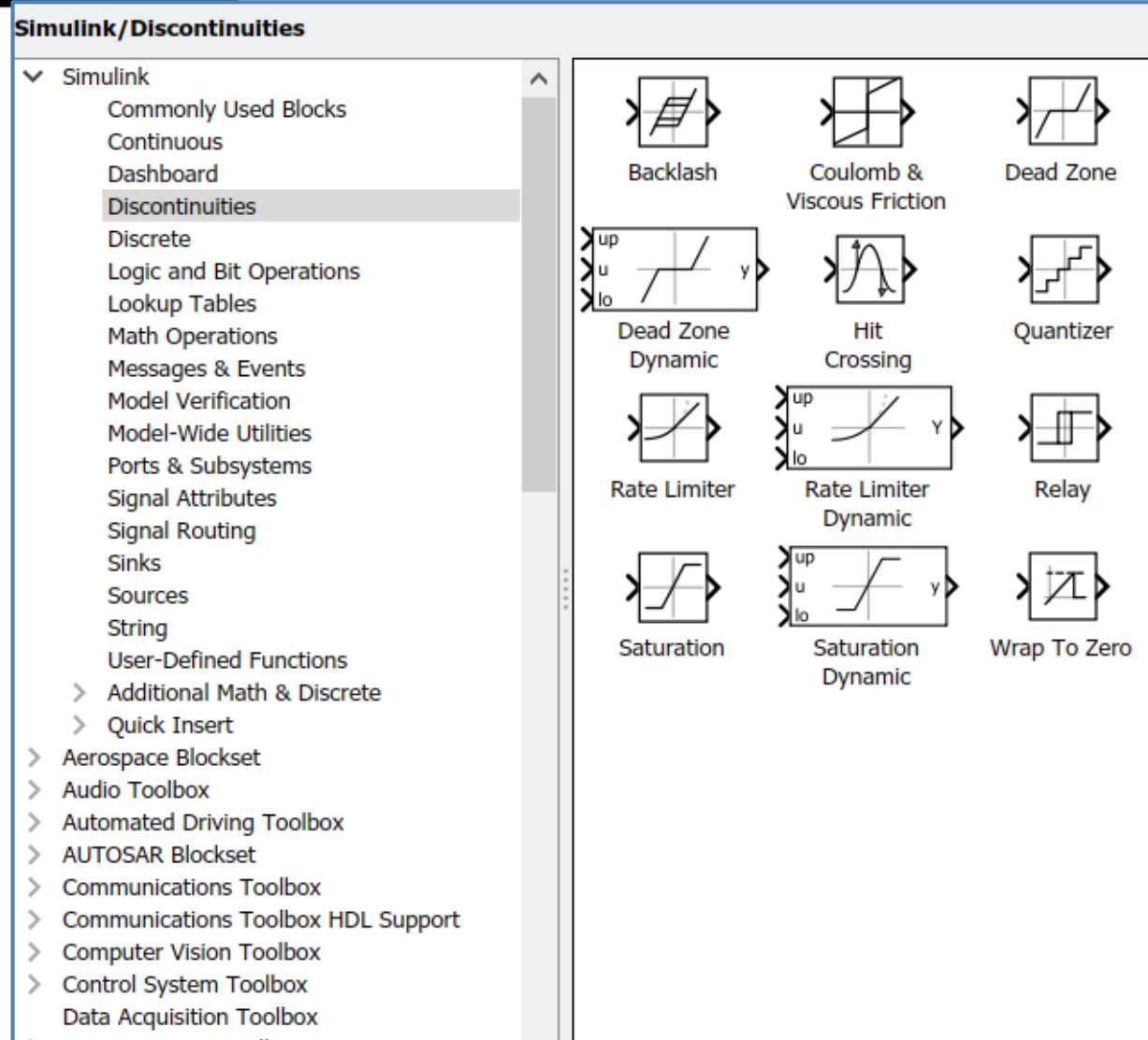


Other Useful Blocks

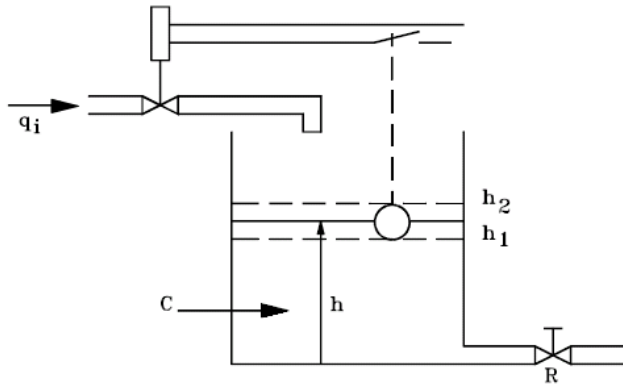
Under “Discontinuous” you will find coulomb friction, dead zone, saturation, and relay.

Under “Continuous” there is a delay block.

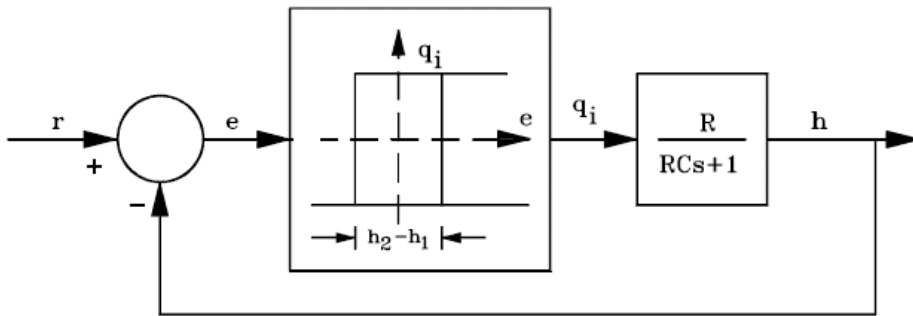
Under “Simulink Extras” there is a PID controller, transfer function with non-zero initial conditions, some useful sinks (such as power spectral density), and radians-to-degrees and Fahrenheit-to-Celsius converters.



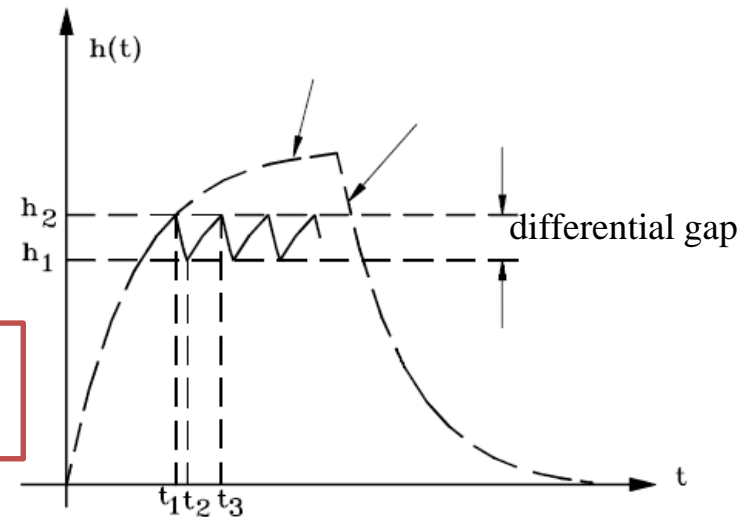
Modelling the tank



$$C \frac{dh}{dt} + \frac{h}{R} = q_i(t)$$

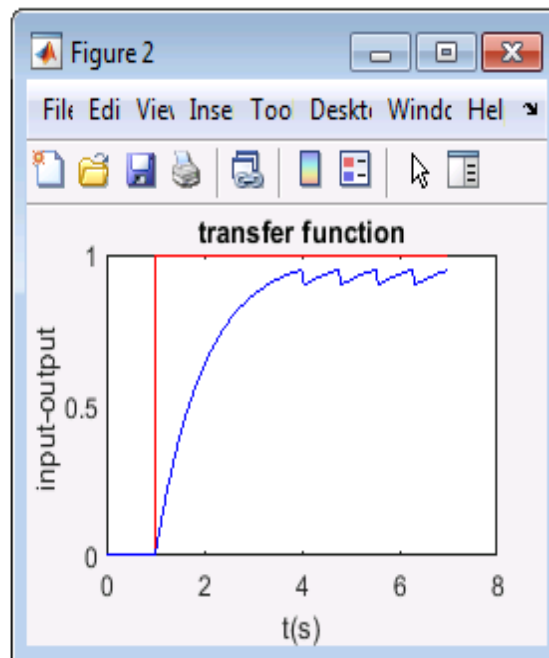
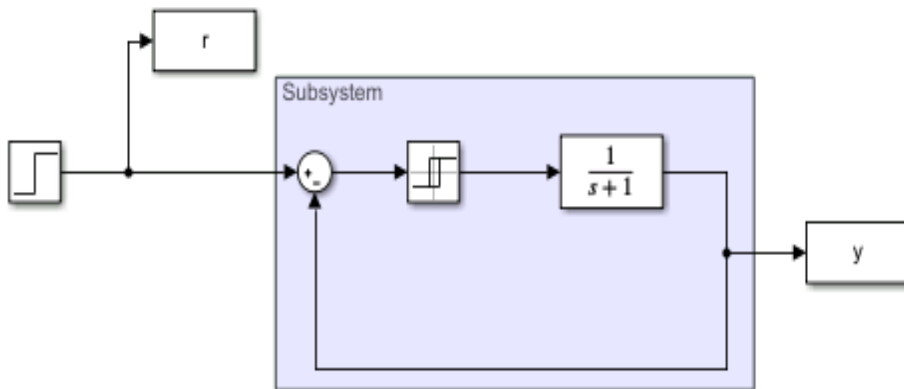


Response of the level of a tank with ON-OFF control and a differential gap



Closed Loop Control System:

Output



Block Parameters: Relay

Relay

Output the specified 'on' or 'off' value by comparing the input to the specified thresholds. The on/off state of the relay is not affected by input between the upper and lower limits.

Main Signal Attributes

Switch on point: 0.1

Switch off point: 0.05

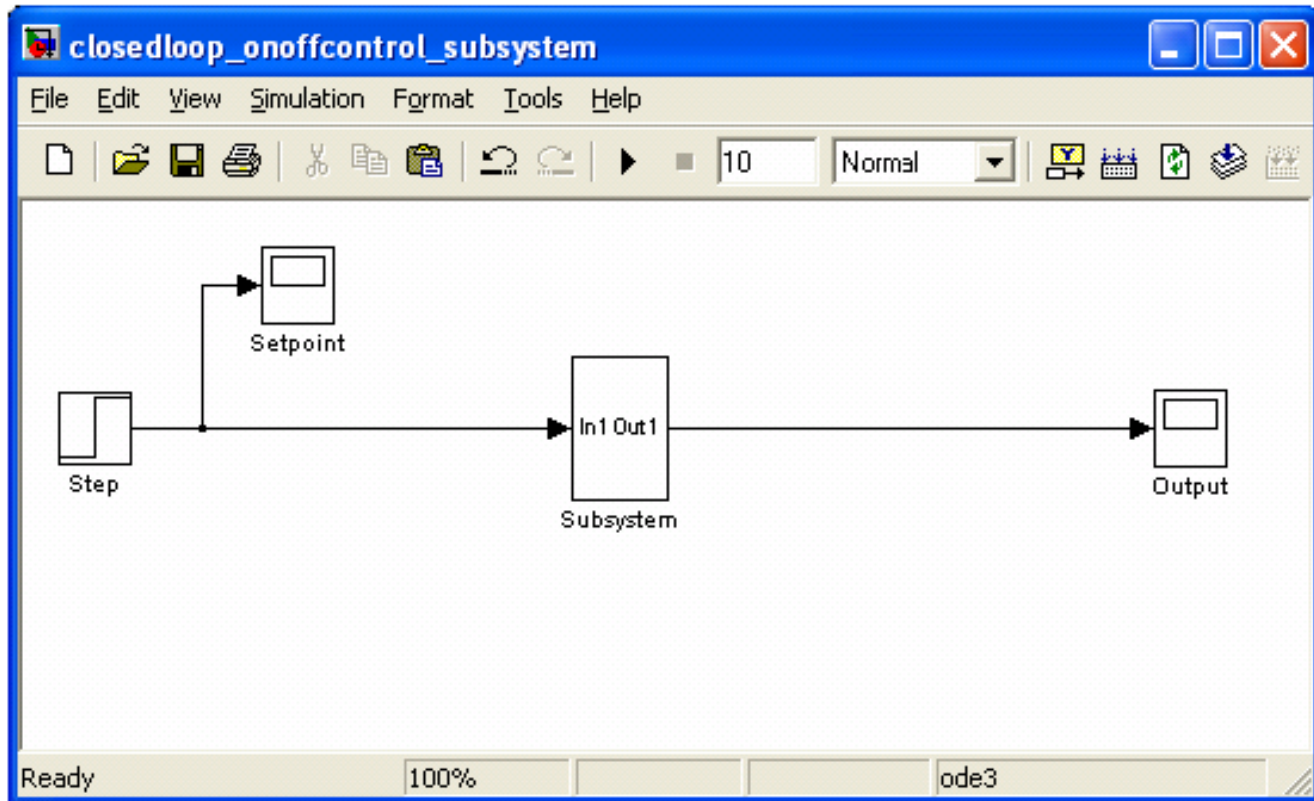
Output when on: 1

Output when off: 0

Input processing: Elements as channels (sample based)

OK Cancel Help Apply

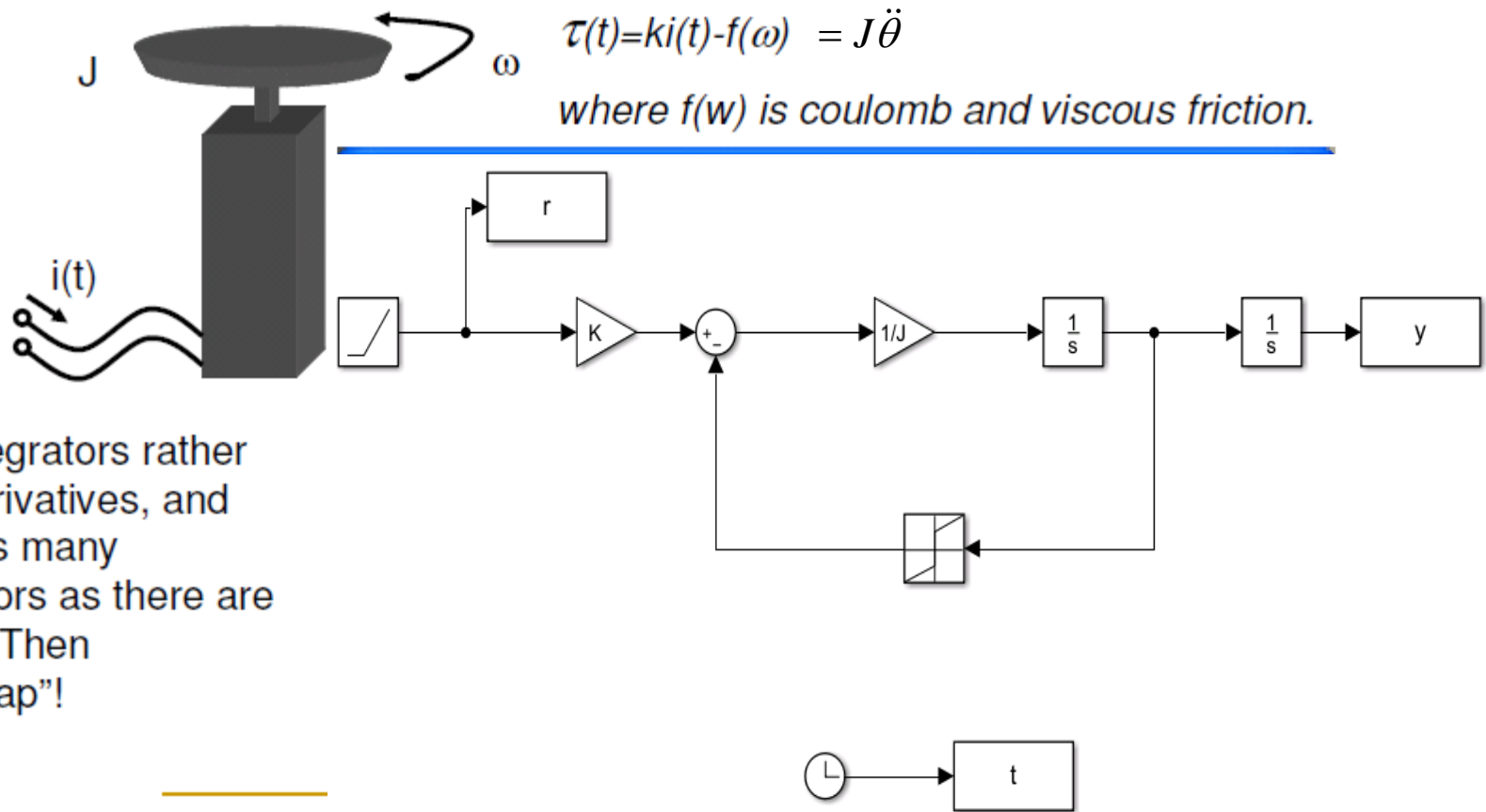
Subsystems



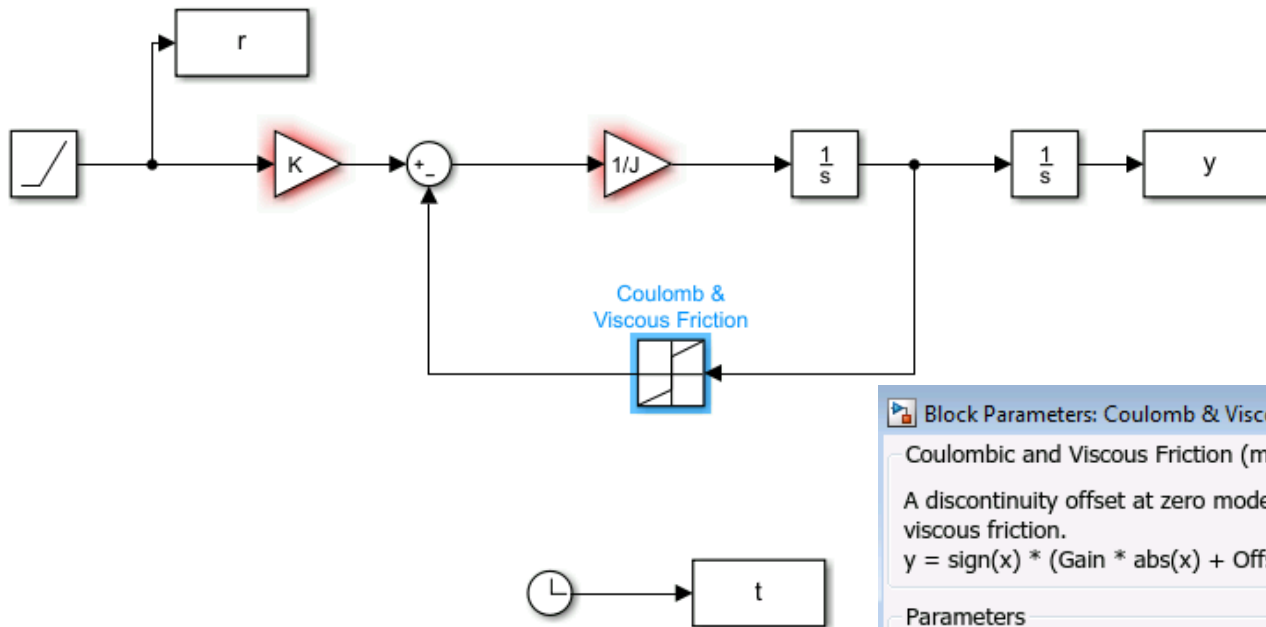
You can group a set of blocks together into a subsystem, by selecting them and right clicking and saying "Create Subsystem". They will all go under a single block. If you double click the subsystem, you can see what is under the "mask".

Setting Up Systems with Integrators

If you have a nonlinear equation system, you can't describe it with a transfer function. One option is to put all of the operations in as individual blocks:



Use integrators rather than derivatives, and put in as many integrators as there are states. Then “bootstrap”!



Block Parameters: Coulomb & Viscous Friction

Coulombic and Viscous Friction (mask) (link)

A discontinuity offset at zero models coulomb friction. Linear gain models viscous friction.
 $y = \text{sign}(x) * (\text{Gain} * \text{abs}(x) + \text{Offset})$

Parameters

Coulomb friction value (Offset):

Coefficient of viscous friction (Gain):

Buttons: ? OK Cancel Help Apply

User Defined Functions

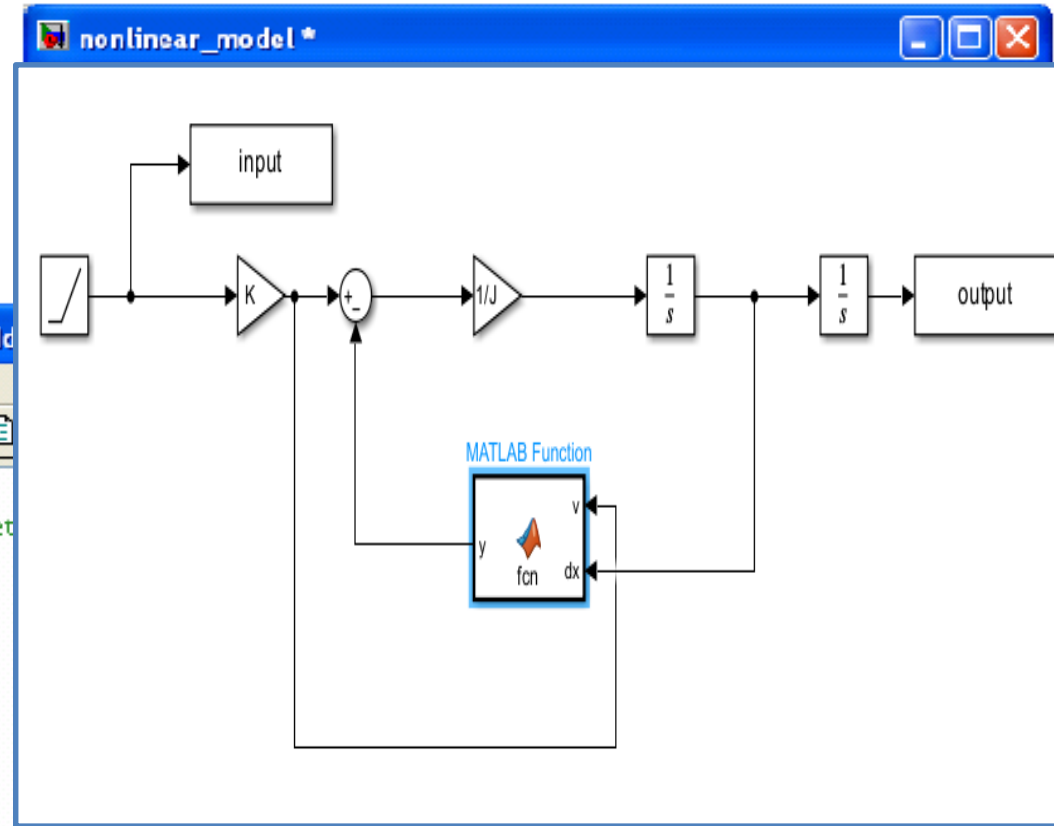
You can embed user-defined m-files using the “Embedded MATLAB Function” block under the “user-defined functions” library.

Embedded MATLAB Editor - Block: nonlinear_model/Embedd

File Edit Text Debug Tools Window Help

```
1 function y = fcn(u1,u2)
2 % This block supports an embeddable subset
3 % See the help menu for details.
4
5 - StickTorque=1;
6 - c=1;
7
8 - if u2>StickTorque || u2<-StickTorque
9 -     y=c*u1;
10 else
11 -     y=u2;
12 end
```

Ready | Ln 1 | Col 1



DC motor dynamics

The plant: a DC motor

$$\Gamma = kV = \underbrace{Js^2\theta + \gamma s\theta + \Gamma^{nlf}}_{\text{plant}}$$

Laplace tf

$$V(s) \rightarrow \boxed{G(s)} \rightarrow \theta(s)$$

Γ : motor torques

k : motor constant

γ : viscous friction

J : motor inertia

Γ^{nlf} = static Coulomb friction

V = input

$$kV(s) = Js^2\theta(s) + \gamma s\theta(s)$$

$$kV(s) = s(Js + \gamma)\theta(s)$$

$$G(s) = \frac{\theta(s)}{V(s)} = \frac{k}{s(Js + \gamma)}$$

$$\rightarrow \frac{\theta(s)}{V(s)} = \frac{k/J}{s(s + \gamma/J)} = \frac{A}{s(s+B)}$$

$$\Gamma^{nlf} \rightarrow \frac{\Gamma^{nlf}}{k} \rightarrow V^{nlf}$$



$$A =$$

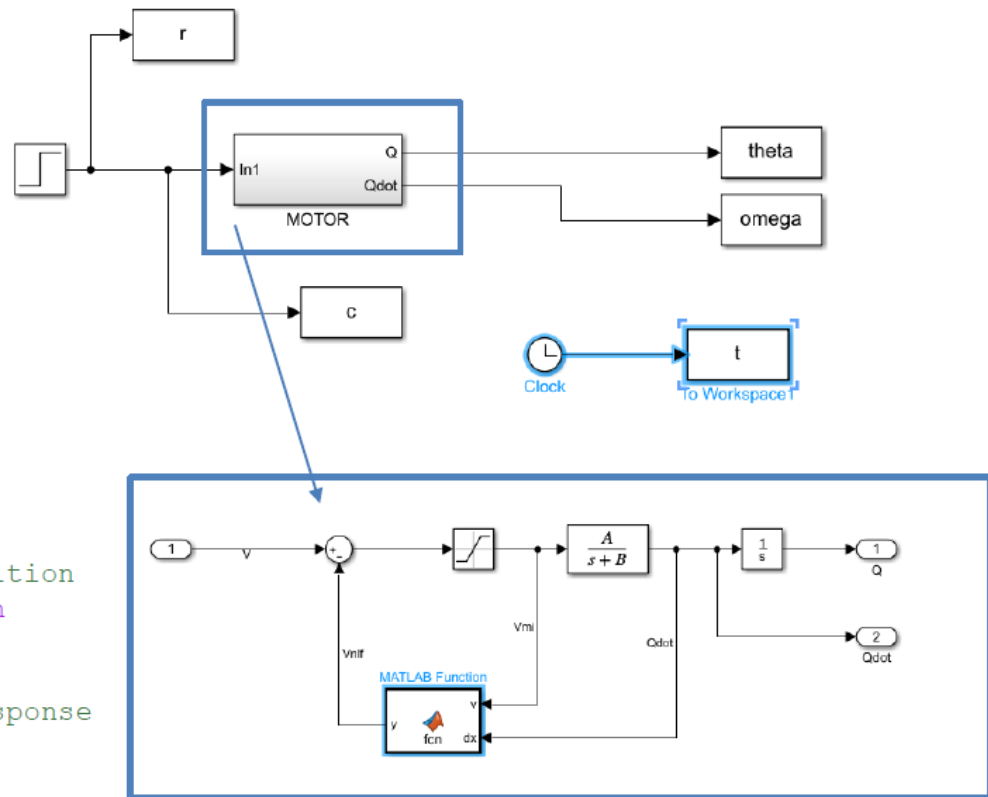
$$B =$$

DC motor dynamics

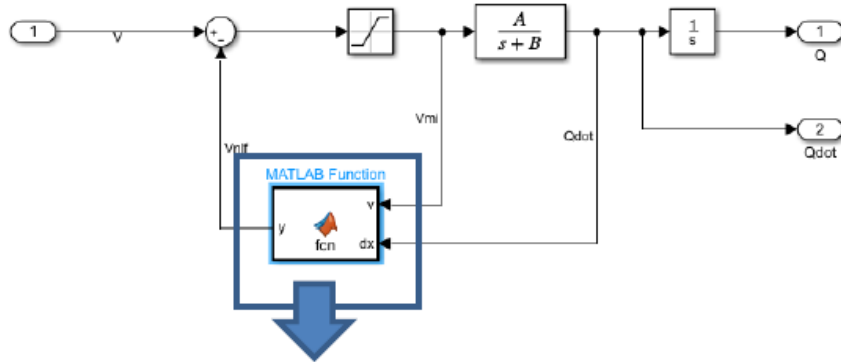
```

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%% MOTOR SIMULATION
%%% System configuration
t_s=10;
h=0.001;
%Motor and simulation parameters
ref=1;
K1=0.00302;
J1=2.97E-07;
v1=8.23E-06;
A=K1/J1;
B=v1/J1;
sat1=1.0;
%%% Simulation and plots
sim motor_sim;
figure;
plot(t,theta,'b',t,r,'r'); %motor position
xlabel('t(s)'); ylabel('Motor position
(rad)');title('DC Motor');
figure;
plot(t,omega,'b',t,r,'r'); %system response
xlabel('t(s)'); ylabel('Motor speed
(rad/s)');title('DC Motor');

```



DC motor dynamics

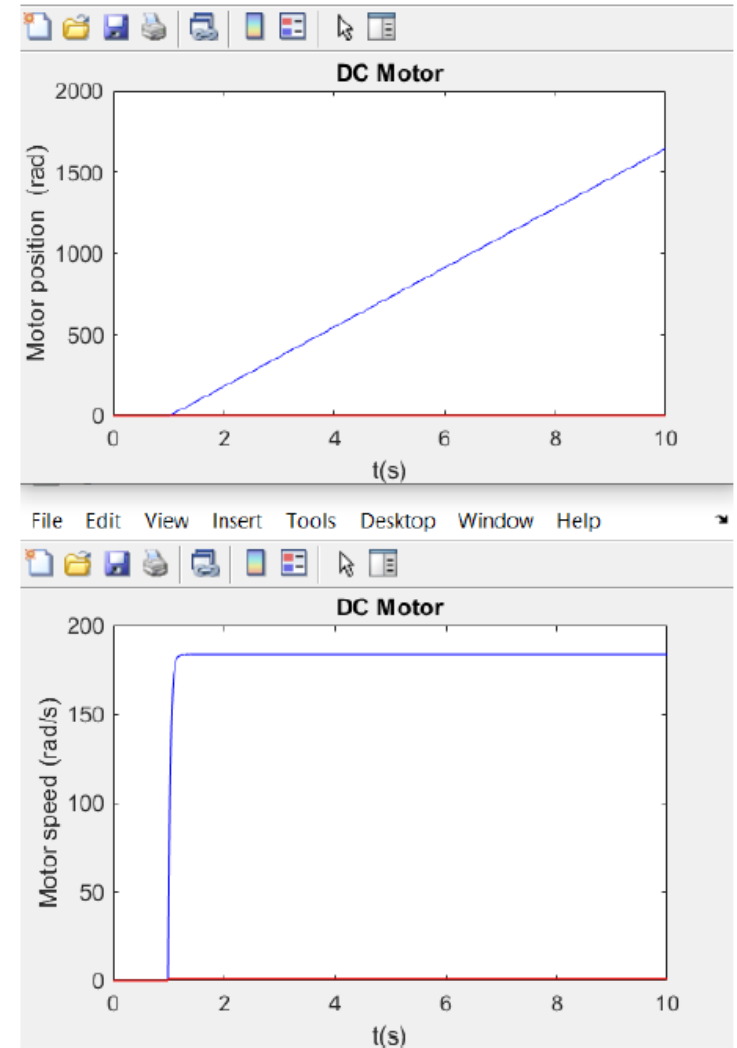


```
function y = fcn(v, dx)
%#codegen
Vie=0.15;
if dx==0
    if abs(v)<=Vie
        y=v;
    else
        y=sign(v)*Vie;
    end
else
    y=Vie*sign(dx);
end
```

$$f\dot{\theta}=0;$$

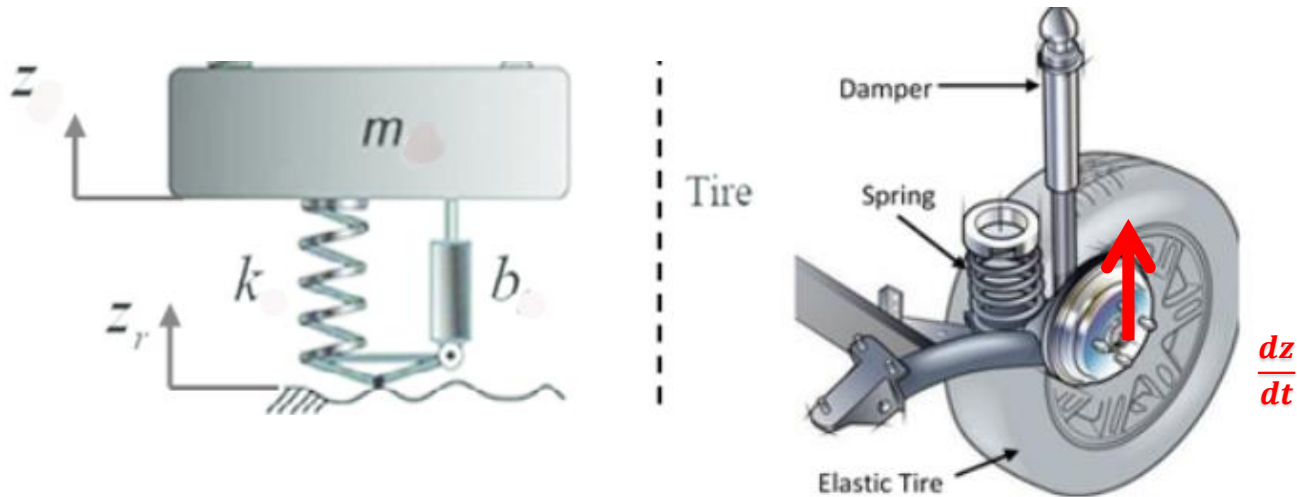
$$v^{nlf} = \begin{cases} |v_{mi}| \leq v_{ie}^{nlf}; V_{mi} \\ |v_{mi}| > v_{ie}^{nlf}; \text{sgn}(V_{mi}) \cdot v_{ie}^{nlf} \end{cases}$$

$$\text{if } \dot{\theta} \neq 0; v^{nlf} = v_{ie}^{nlf} \cdot \text{sgn}(\dot{\theta})$$

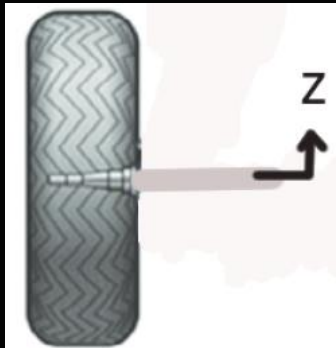
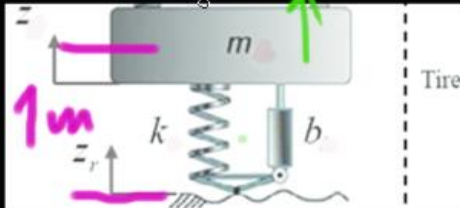


Suspension system

A suspension system has to be modelled and simulated. Here, z is the vertical displacement of the wheel center. We are interested in obtaining how the speed of mass m changes by time $\frac{dz}{dt}$.



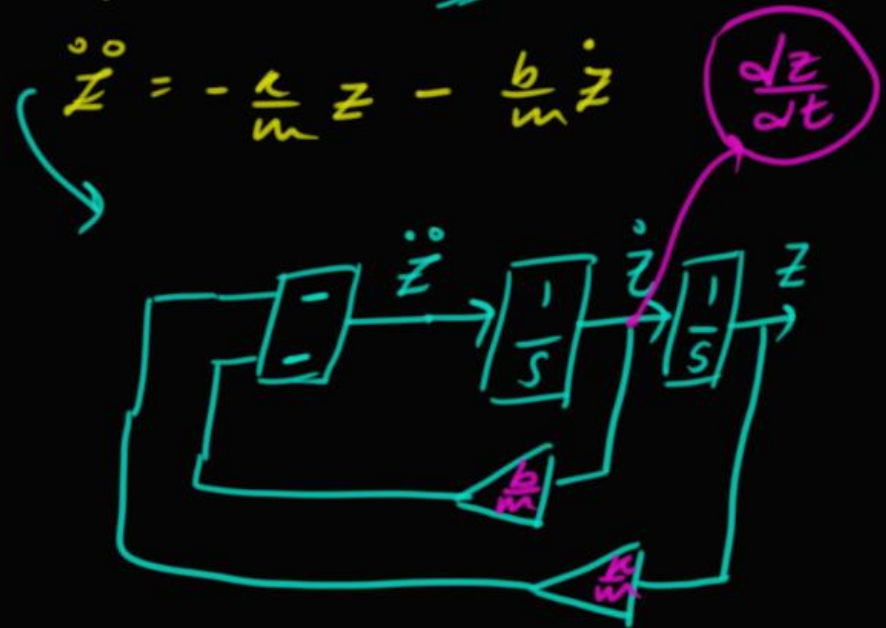
Suspension



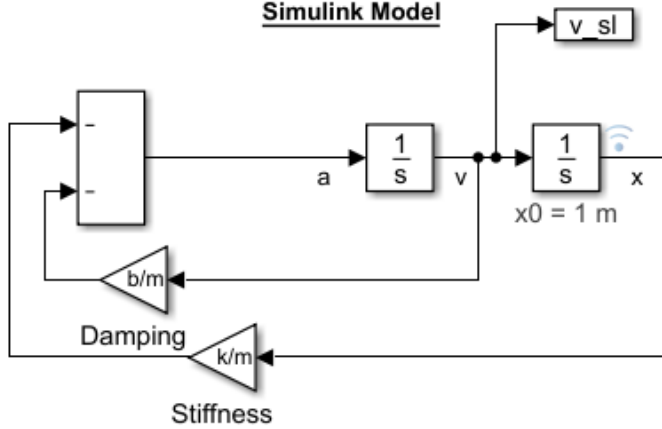
$$\sum F = ma = m\ddot{z}$$

$$m\ddot{z} = -kz - b\dot{z}$$

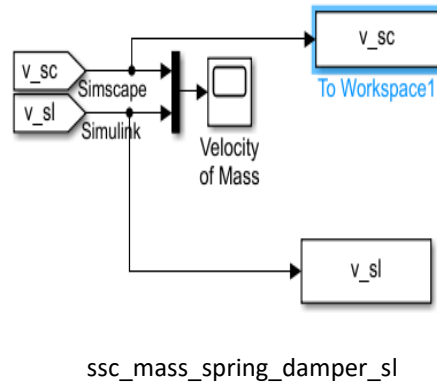
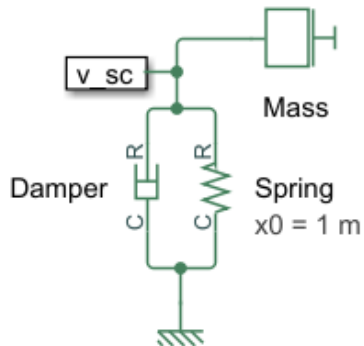
$$\ddot{z} = -\frac{k}{m}z - \frac{b}{m}\dot{z}$$



Simulink Model



Simscape Model



▼ Simscape

▼ Foundation Library

▼ Electrical

Electrical Elements
Electrical Sensors
Electrical Sources

> Gas

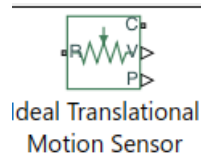
> Hydraulic

> Isothermal Liquid

> Magnetic

▼ Mechanical

Mechanical Sensors



```

%%%%%  MASS SPRING DAMPER
%%%%%  SIMULINK AND SIMSCAPE
%%%%%

```

% 1. SIMULATION PARAMETERS

```
b=10;%N/(m/s)
```

```
k=400;% N/m
```

```
m=3.6;%kg
```

```
x0=1;%m
```

% 2. SIMULATION AND PLOTS

```
%
```

```
Sim ssc_mass_spring_damper_sl_2022;
```

```
figure;
```

```
plot(v_sc,'g','LineWidth',2);
```

```
hold on
```









```
plot(v_sl,'--r','LineWidth',2);
```

```
xlabel('Time(s)');
```

```
ylabel('Velocity (m/s)');
```

```
title('Velocity of Mass');
```


- Electrical Elements
 - Electrical Sensors
 - Electrical Sources
 - Gas
 - Hydraulic
 - Isothermal Liquid
 - Magnetic
 - Mechanical Sensors
 - Mechanical Sources
 - Mechanisms
 - Multibody Interfaces
 - Rotational Elements
 - Translational Elements

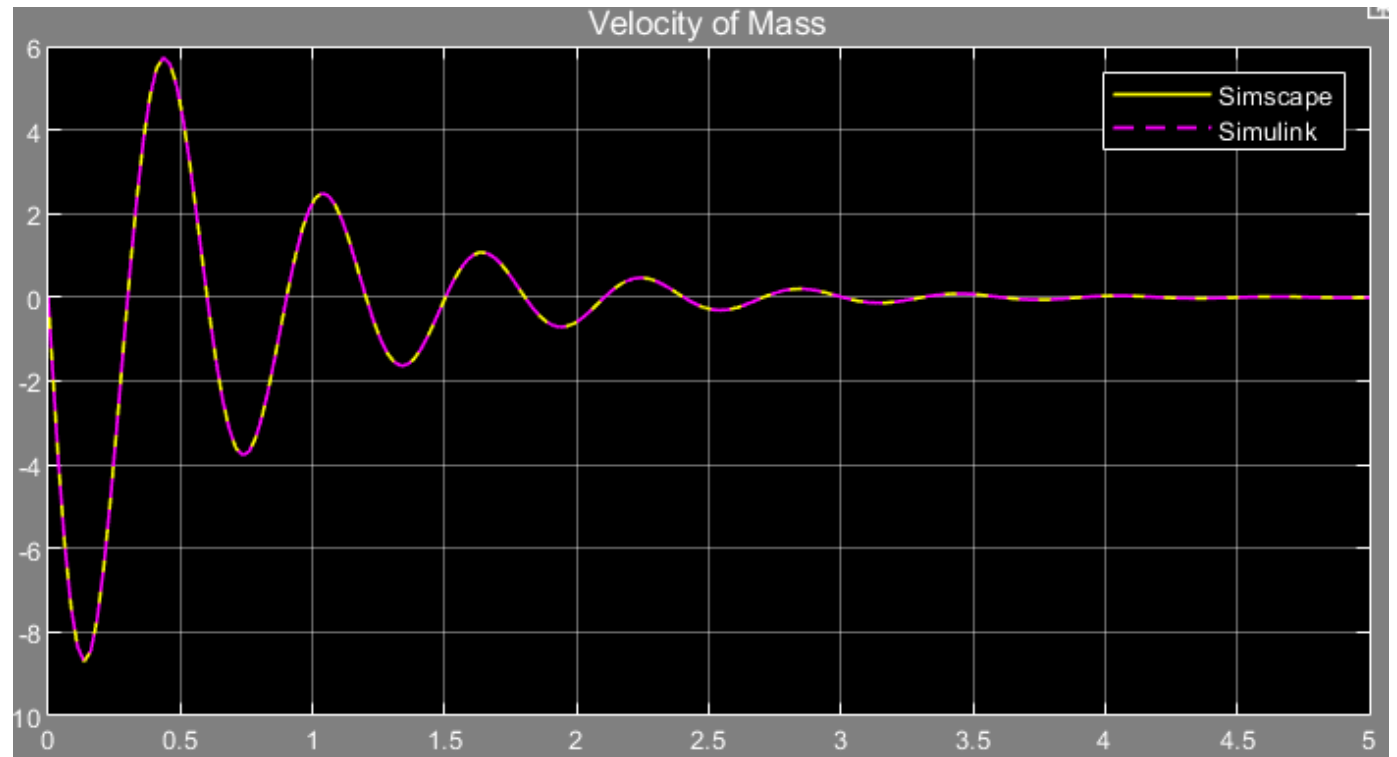
							
Mass	Mechanical Translational Reference	Translational Damper	Translational Free End	Translational Hard Stop	Translational Spring	Translational Friction	Translational Inerter

- Electrical Elements
 - Electrical Sensors
 - Electrical Sources
 - Gas
 - Hydraulic
 - Isothermal Liquid
 - Magnetic
 - Mechanical Sensors

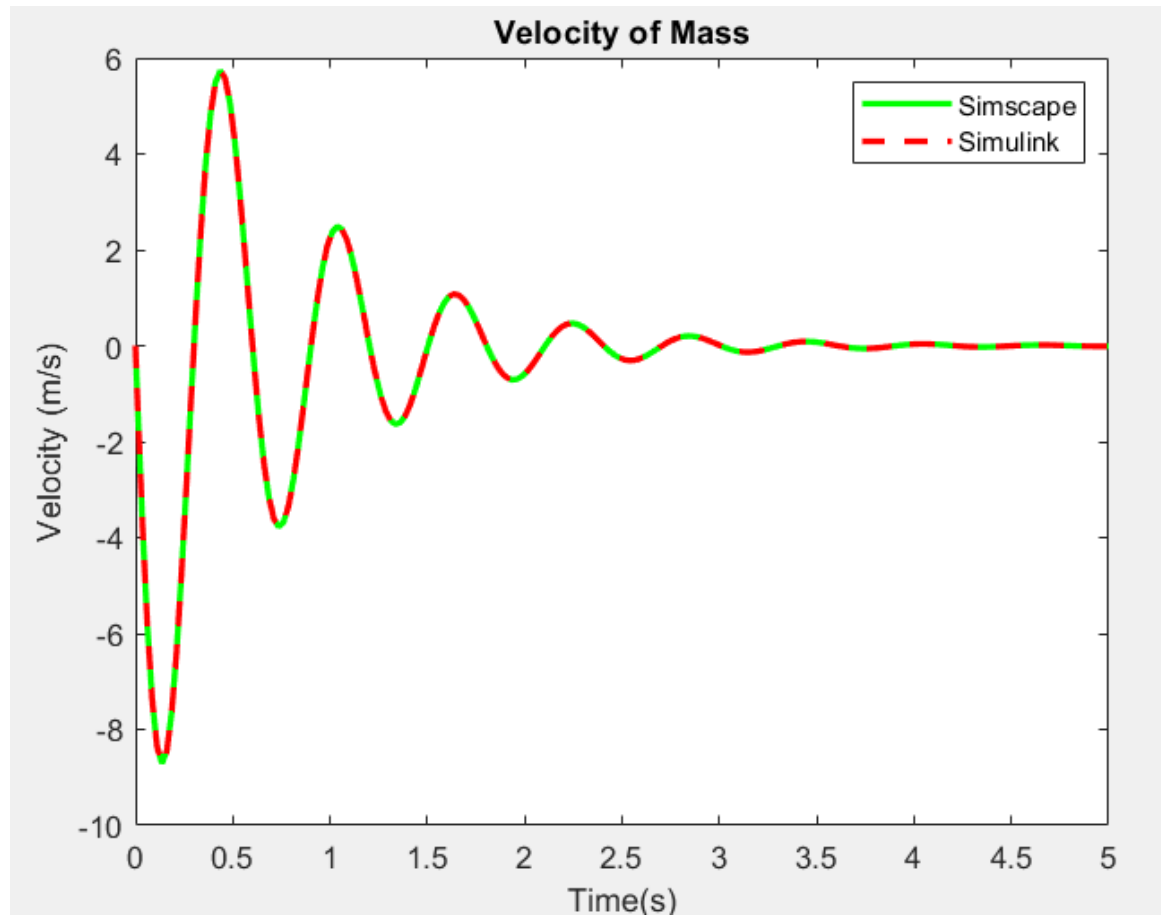


Ideal Translational Motion Sensor

Velocity of
mass (m/s)

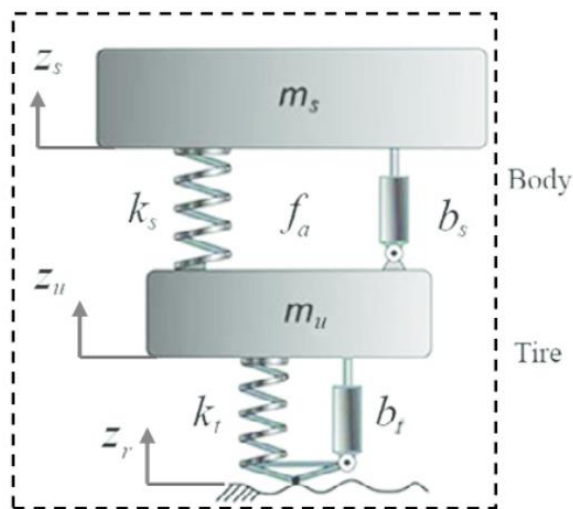


Time (s)

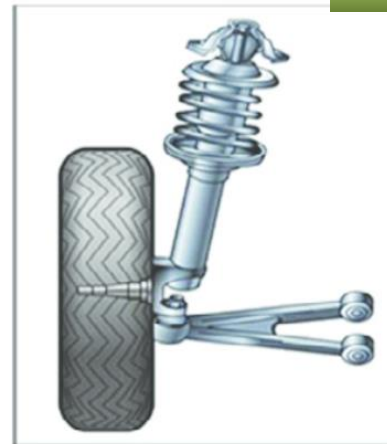


Suspension system

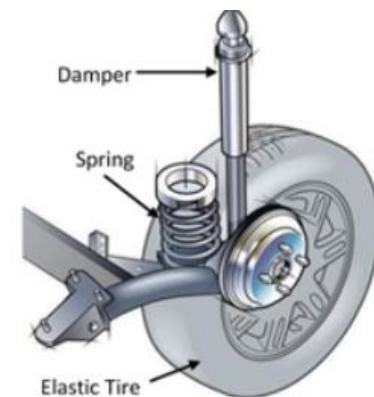
A quarter-car and its suspension system has to be modelled and simulated. Here, z_u is the vertical displacement of the wheel center and z_s is the vertical displacement of vehicle chassis. We are interested in obtaining how the speed of masses m_s and m_u change by time.



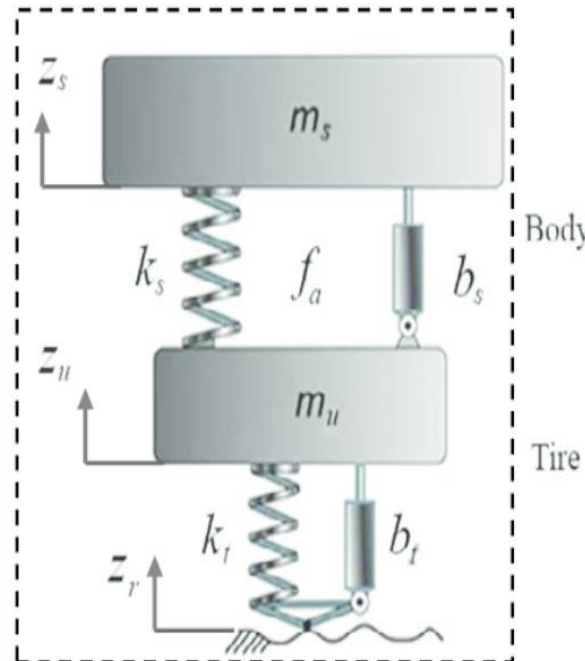
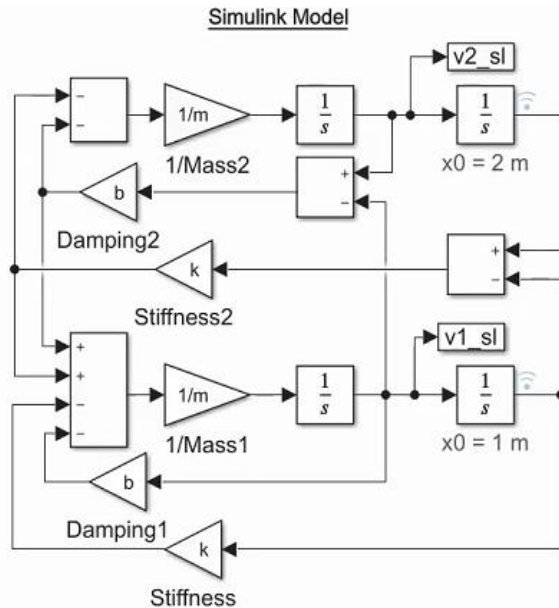
A quarter-car model of suspension system



Quarter-car



Mass-Spring-Damper Simulink

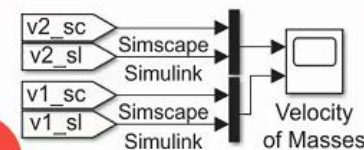


<https://www.mathworks.com/help/physmod/simscape/ug/double-mass-spring-damper-in-simulink-and-simscape.html>

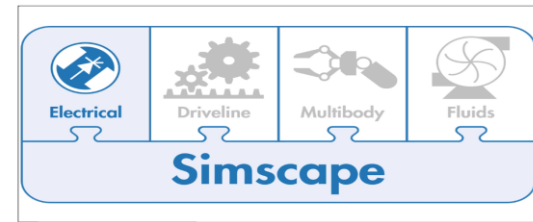
<https://ctms.engin.umich.edu/CTMS/index.php?example=Suspension§ion=SimulinkControl>

Double Mass-Spring-Damper in Simulink and Simscape

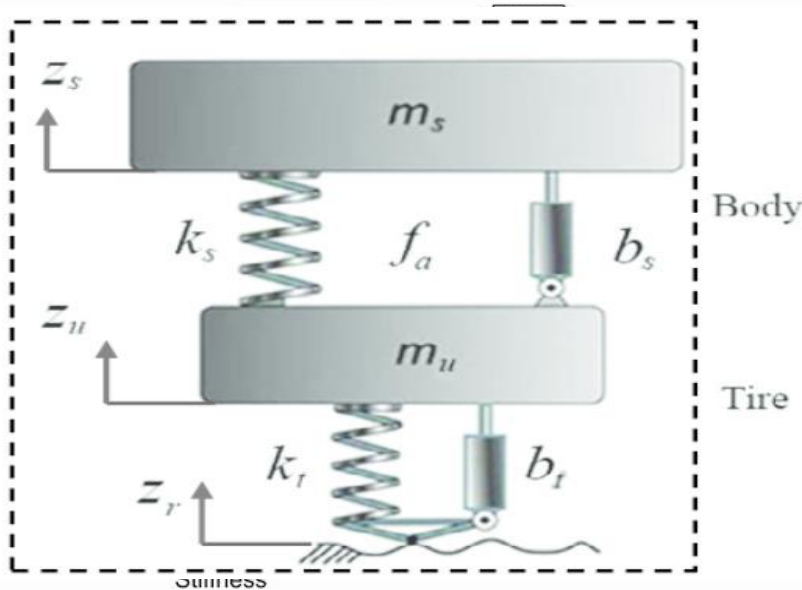
1. [Plot position of masses \(see code\)](#)
2. [Explore simulation results](#) using [sscexplore](#)
3. [Learn more](#) about this example
4. [Open model](#) of single mass-spring-damper
5. Learn more about [modeling physical networks](#)



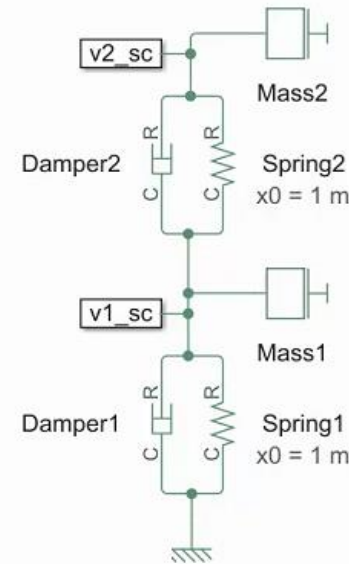
Mass-Spring-Damper Simscape



Simulink Model



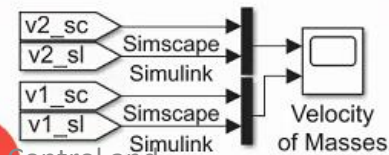
Simscape Model



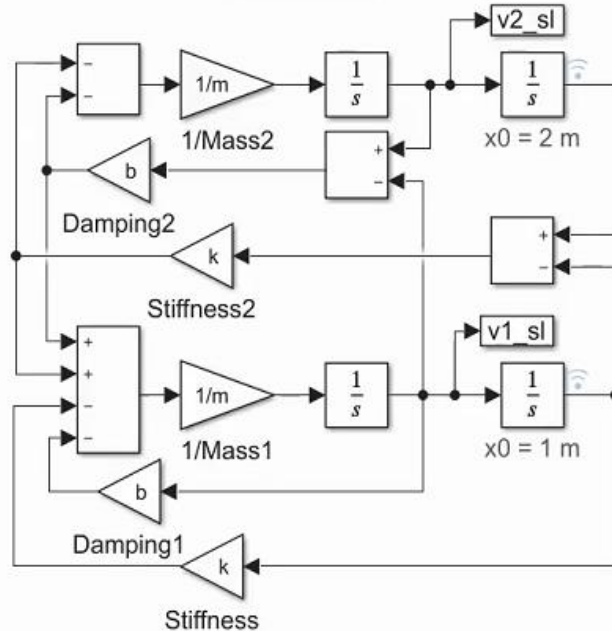
https://www.mathworks.com/services/training.html?s_tid=gn_trg_ov

Double Mass-Spring-Damper in Simulink and Simscape

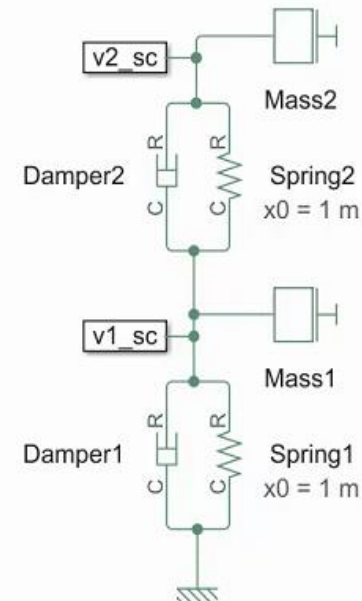
1. [Plot position of masses \(see code\)](#)
2. [Explore simulation results](#) using `sscexplore`
3. [Learn more](#) about this example
4. [Open model](#) of single mass-spring-damper
5. Learn more about [modeling physical networks](#)



Simulink Model



Simscape Model



Double Mass-Spring-Damper in Simulink and Simscape

1. [Plot position of masses \(see code\)](#)
2. [Explore simulation results using sscexplore](#)
3. [Learn more](#) about this example
4. [Open model](#) of single mass-spring-damper
5. Learn more about [modeling physical networks](#)

