Regressão Linear - TE2

April 29, 2025

```
[2]: import numpy as np
     import pandas as pd
     import seaborn as sns
     import matplotlib.pyplot as plt
[3]: casas = pd.read_csv('USA_Housing.csv')
[4]: casas.head()
[4]:
                                                Avg. Area Number of Rooms
        Avg. Area Income
                           Avg. Area House Age
     0
            79545.458574
                                      5.682861
                                                                  7.009188
     1
            79248.642455
                                      6.002900
                                                                  6.730821
     2
            61287.067179
                                      5.865890
                                                                  8.512727
     3
            63345.240046
                                      7.188236
                                                                  5.586729
     4
            59982.197226
                                      5.040555
                                                                  7.839388
        Avg. Area Number of Bedrooms
                                       Area Population
                                                                Price
     0
                                          23086.800503
                                                         1.059034e+06
                                 4.09
     1
                                 3.09
                                          40173.072174 1.505891e+06
     2
                                 5.13
                                          36882.159400
                                                        1.058988e+06
     3
                                 3.26
                                          34310.242831
                                                        1.260617e+06
                                          26354.109472
     4
                                 4.23
                                                         6.309435e+05
                                                    Address
        208 Michael Ferry Apt. 674\nLaurabury, NE 3701...
       188 Johnson Views Suite 079\nLake Kathleen, CA...
       9127 Elizabeth Stravenue\nDanieltown, WI 06482...
     2
     3
                                 USS Barnett\nFPO AP 44820
     4
                                USNS Raymond\nFPO AE 09386
```

0.0.1 Modelo supervisionado

• separação entre base de treino e base de teste

0.0.2 Modelo não supervisionado

• não existe a separação entre base de treino e teste

```
[5]: casas.info()
```

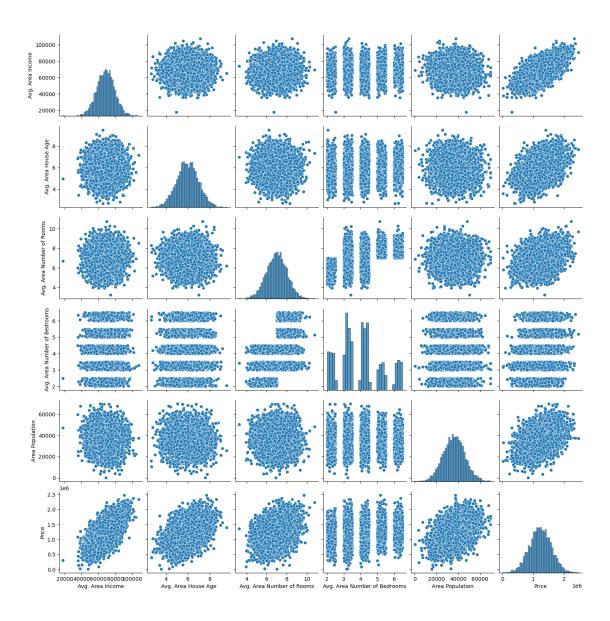
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 5000 entries, 0 to 4999
Data columns (total 7 columns):

#	Column	Non-Null Count	Dtype
0	Avg. Area Income	5000 non-null	float64
1	Avg. Area House Age	5000 non-null	float64
2	Avg. Area Number of Rooms	5000 non-null	float64
3	Avg. Area Number of Bedrooms	5000 non-null	float64
4	Area Population	5000 non-null	float64
5	Price	5000 non-null	float64
6	Address	5000 non-null	object

dtypes: float64(6), object(1)
memory usage: 273.6+ KB

[6]: sns.pairplot(casas)

[6]: <seaborn.axisgrid.PairGrid at 0x7fa925e78c50>



[7]: casas.corr()

/tmp/ipykernel_253299/2249505781.py:1: FutureWarning: The default value of numeric_only in DataFrame.corr is deprecated. In a future version, it will default to False. Select only valid columns or specify the value of numeric_only to silence this warning.

casas.corr()

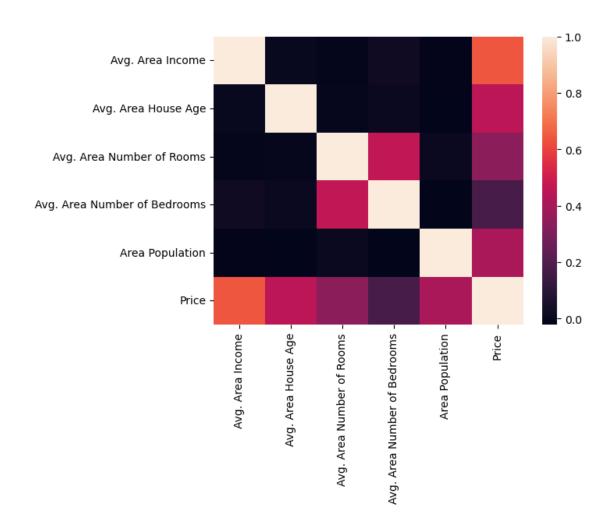
[7]:	A	vg. Area Income Av	√g. Area House Age \
Avg. Area Income		1.000000	-0.002007
Avg. Area House A	Age	-0.002007	1.000000
Avg. Area Number	of Rooms	-0.011032	-0.009428
Avg. Area Number	of Bedrooms	0.019788	0.006149

Area Population Price	-0.016234 0.639734	-0.018743 0.452543				
11100						
	Avg. Area Number of Rooms \					
Avg. Area Income	-0.011032					
Avg. Area House Age	-0.009428					
Avg. Area Number of Rooms	1.000000					
Avg. Area Number of Bedrooms	0.462695					
Area Population	0.002040					
Price	0.335664					
	Avg. Area Number of Bedrooms	Area Population \				
Avg. Area Income	0.019788	-				
Avg. Area House Age	0.006149	-0.018743				
Avg. Area Number of Rooms	0.462695	0.002040				
Avg. Area Number of Bedrooms	1.000000	-0.022168				
Area Population	-0.022168	1.000000				
Price	0.171071	0.408556				
	Price					
Avg. Area Income	0.639734					
Avg. Area House Age	0.452543					
Avg. Area Number of Rooms	0.335664					
Avg. Area Number of Bedrooms	0.171071					
Area Population	0.408556					
Price	1.000000					
sns.heatmap(casas.corr())						

/tmp/ipykernel_253299/254642754.py:1: FutureWarning: The default value of numeric_only in DataFrame.corr is deprecated. In a future version, it will default to False. Select only valid columns or specify the value of numeric_only to silence this warning.

sns.heatmap(casas.corr())

[8]: <AxesSubplot: >



```
[9]: casas.columns
```

[10]: casas[['Avg. Area Income', 'Avg. Area House Age', 'Avg. Area Number of Rooms', 'Avg. Area Number of Bedrooms', 'Area Population', 'Price']].corr()

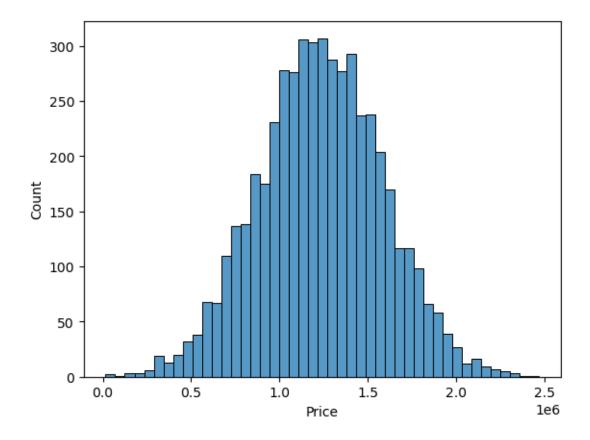
```
[10]:
                                     Avg. Area Income Avg. Area House Age
      Avg. Area Income
                                             1.000000
                                                                  -0.002007
      Avg. Area House Age
                                            -0.002007
                                                                   1.000000
      Avg. Area Number of Rooms
                                            -0.011032
                                                                  -0.009428
      Avg. Area Number of Bedrooms
                                             0.019788
                                                                   0.006149
      Area Population
                                            -0.016234
                                                                  -0.018743
     Price
                                             0.639734
                                                                   0.452543
```

```
Avg. Area Number of Rooms \
                                                    -0.011032
      Avg. Area Income
      Avg. Area House Age
                                                    -0.009428
      Avg. Area Number of Rooms
                                                     1.000000
      Avg. Area Number of Bedrooms
                                                     0.462695
     Area Population
                                                     0.002040
     Price
                                                     0.335664
                                    Avg. Area Number of Bedrooms Area Population \
     Avg. Area Income
                                                        0.019788
                                                                         -0.016234
     Avg. Area House Age
                                                                         -0.018743
                                                        0.006149
      Avg. Area Number of Rooms
                                                        0.462695
                                                                          0.002040
      Avg. Area Number of Bedrooms
                                                        1.000000
                                                                         -0.022168
      Area Population
                                                       -0.022168
                                                                          1.000000
     Price
                                                        0.171071
                                                                          0.408556
                                       Price
      Avg. Area Income
                                    0.639734
      Avg. Area House Age
                                    0.452543
      Avg. Area Number of Rooms
                                    0.335664
      Avg. Area Number of Bedrooms 0.171071
      Area Population
                                    0.408556
     Price
                                    1.000000
[12]: sns.heatmap(casas[['Avg. Area Income', 'Avg. Area House Age', 'Avg. Area Number_
       ⇔of Rooms',
             'Avg. Area Number of Bedrooms', 'Area Population', 'Price']].corr(),
       →annot=True)
[12]: <AxesSubplot: >
```



[13]: sns.histplot(casas['Price'])

[13]: <AxesSubplot: xlabel='Price', ylabel='Count'>



Modelo de regressão

- X -> VARIÁVEIS PREDITORAS
- Y -> VARIÁVEL QUE QUERO PREDIZER (DESCOBRIR) ALVO

[14]: casas.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 5000 entries, 0 to 4999
Data columns (total 7 columns):

#	Column	Non-Null Count	Dtype
0	Avg. Area Income	5000 non-null	float64
1	Avg. Area House Age	5000 non-null	float64
2	Avg. Area Number of Rooms	5000 non-null	float64
3	Avg. Area Number of Bedrooms	5000 non-null	float64
4	Area Population	5000 non-null	float64
5	Price	5000 non-null	float64
6	Address	5000 non-null	object

dtypes: float64(6), object(1)
memory usage: 273.6+ KB

```
[15]: casas.columns
[15]: Index(['Avg. Area Income', 'Avg. Area House Age', 'Avg. Area Number of Rooms',
             'Avg. Area Number of Bedrooms', 'Area Population', 'Price', 'Address'],
            dtype='object')
[16]: X = casas[['Avg. Area Income', 'Avg. Area House Age', 'Avg. Area Number of
       ⇔Rooms',
             'Avg. Area Number of Bedrooms', 'Area Population']]
      Y = casas['Price']
[17]: X
[17]:
            Avg. Area Income
                               Avg. Area House Age Avg. Area Number of Rooms
                79545.458574
                                          5.682861
                                                                       7.009188
      1
                79248.642455
                                          6.002900
                                                                       6.730821
      2
                61287.067179
                                          5.865890
                                                                       8.512727
      3
                63345.240046
                                          7.188236
                                                                       5.586729
      4
                59982.197226
                                                                       7.839388
                                          5.040555
      4995
                60567.944140
                                          7.830362
                                                                       6.137356
      4996
                78491.275435
                                          6.999135
                                                                       6.576763
      4997
                63390.686886
                                          7.250591
                                                                       4.805081
      4998
                68001.331235
                                          5.534388
                                                                       7.130144
      4999
                65510.581804
                                          5.992305
                                                                       6.792336
            Avg. Area Number of Bedrooms
                                          Area Population
      0
                                     4.09
                                               23086.800503
      1
                                     3.09
                                               40173.072174
      2
                                     5.13
                                               36882.159400
      3
                                     3.26
                                               34310.242831
      4
                                     4.23
                                               26354.109472
                                               22837.361035
      4995
                                     3.46
      4996
                                     4.02
                                               25616.115489
      4997
                                     2.13
                                               33266.145490
      4998
                                     5.44
                                               42625.620156
      4999
                                     4.07
                                               46501.283803
      [5000 rows x 5 columns]
[18]: Y
[18]: 0
              1.059034e+06
      1
              1.505891e+06
      2
              1.058988e+06
      3
              1.260617e+06
```

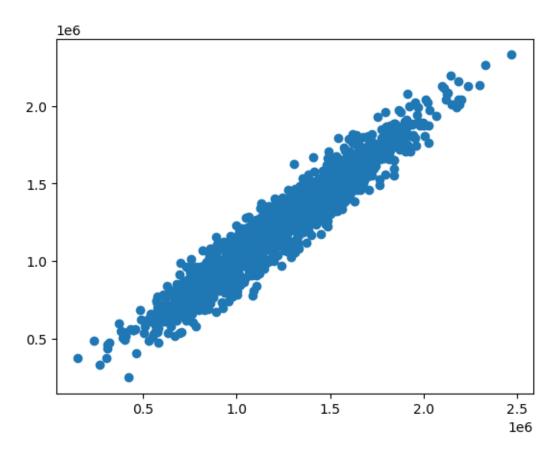
```
4995
              1.060194e+06
      4996
              1.482618e+06
      4997
              1.030730e+06
      4998
              1.198657e+06
      4999
              1.298950e+06
      Name: Price, Length: 5000, dtype: float64
     0.0.3 Divisão do conjunto de dados
     0.0.4 %pip install scikit-learn
[19]: from sklearn.model_selection import train_test_split
[20]: X_treino, X_teste, Y_treino, Y_teste = train_test_split(X,Y,
                                                                 train_size=0.7,
       →random_state=46)
[21]: X_treino
[21]:
            Avg. Area Income
                              Avg. Area House Age Avg. Area Number of Rooms
      456
                62653.092462
                                           6.543984
                                                                       7.884326
      4480
                71481.034926
                                           5.188492
                                                                       7.152361
      3564
                63889.411593
                                           5.548089
                                                                       6.357831
      587
                51918.546873
                                           5.892497
                                                                       6.708809
      2634
                42814.993038
                                                                       6.080981
                                           5.247613
      3933
                71229.357964
                                          4.850191
                                                                       6.978128
      3787
                50362.538095
                                           5.582574
                                                                       4.608843
      658
                73829.777741
                                          6.130263
                                                                       6.182843
      2451
                63421.903955
                                          7.594954
                                                                       8.777735
      2490
                65010.553474
                                           6.299952
                                                                       7.529846
            Avg. Area Number of Bedrooms Area Population
      456
                                     3.28
                                               41467.867658
      4480
                                     4.32
                                               45246.174103
      3564
                                     2.11
                                               34442.099648
      587
                                     3.37
                                               24734.406520
      2634
                                     4.02
                                               41426.389765
      3933
                                     4.15
                                               27168.842194
                                     2.40
      3787
                                               23611.056225
      658
                                     3.50
                                               51385.523241
      2451
                                     3.09
                                               11511.387050
      2490
                                     6.32
                                               34706.866627
      [3500 rows x 5 columns]
```

4

6.309435e+05

```
[22]: Y_treino
[22]: 456
              1.382110e+06
      4480
              1.530013e+06
      3564
              1.134126e+06
      587
              6.610434e+05
      2634
              4.525302e+05
      3933
              6.997873e+05
      3787
              3.141678e+05
      658
              1.376493e+06
      2451
              1.432318e+06
      2490
              1.305186e+06
      Name: Price, Length: 3500, dtype: float64
[23]: X_treino.shape[0]
[23]: 3500
[24]: X_teste.shape[0]
[24]: 1500
[25]: Y_treino.shape
[25]: (3500,)
[26]: Y_teste.shape
[26]: (1500,)
     Criando o modelo de treino
[27]: | from sklearn.linear_model import LinearRegression
[28]: LR=LinearRegression()
[29]: LR.fit(X_treino,Y_treino )
[29]: LinearRegression()
[30]: y_predicao = LR.predict(X_teste)
[31]: y_predicao
[31]: array([1176591.88192438, 997847.03239798, 1179674.83216237, ...,
              934885.47457475, 1497530.06928932, 866365.31013406])
[32]: plt.scatter(Y_teste, y_predicao)
```

[32]: <matplotlib.collections.PathCollection at 0x7fa913c68590>

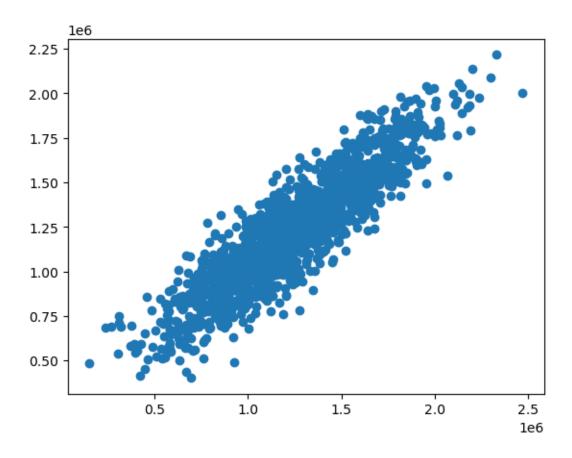


```
[33]: from sklearn import metrics
[34]: metrics.mean_absolute_error(Y_teste, y_predicao)
[34]: 79806.83254169731
        Y_teste
        y_predicao
        ((Y_teste - y_predicao)^2)1/2
[35]: metrics.mean_squared_error(Y_teste, y_predicao)
[35]: 9993926845.480902
        Y_teste
        y_predicao
        ((Y_teste - y_predicao)^2)
```

Atividade

Com base na regressão linear vista em aula, remova um dos preditores e compare o resultado obtido com esse modelo.

[42]: <matplotlib.collections.PathCollection at 0x7fa911a6d750>



```
[43]: metrics.mean_absolute_error(Y2_teste, Y2_predicao)

[43]: 127067.82406794395

[]:
```