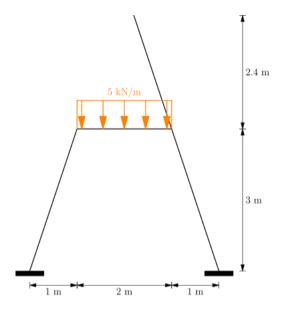
Introducción a elementos finitos Tarea 3 I-2016

Resolver mediante matriz de rigidez, $E=2.1\times 10^6~\mathrm{kN/m^2}$



Numeración

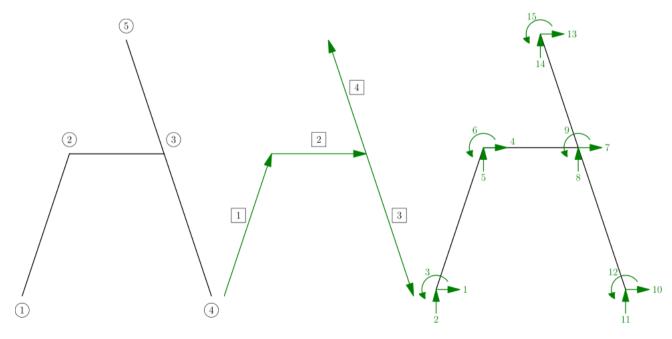


Figura 1: Numeración de la estructura

Coordenadas de los nodos

$$(1) = [0, 0]$$

$$(2) = [1, 3]$$

$$(3) = [3, 3]$$

$$(4) = [4, 0]$$

$$(5) = [2.2, 5.4]$$

Elemento $\boxed{1}$, tiene la dirección $\boxed{1}$ - $\boxed{2}$

Elemento $\boxed{2}$, tiene la dirección $\boxed{2}$ - $\boxed{3}$

Elemento $\boxed{3}$, tiene la dirección $\boxed{3}$ - $\boxed{4}$

$$A = 0.3 \cdot 0.4 = 0.12 \text{ m}^2$$

$$I = \frac{0.3 \cdot 0.4^3}{12} = 0.0016 \text{m}^4$$

$$L = \sqrt{(1 - 0)^2 + (3 - 0)^2} = 3.162 \text{ m}$$

$$\lambda_x = \frac{1 - 0}{3.162} = 0.316$$

$$\lambda_y = \frac{3 - 0}{3.162} = 0.949$$

$$A = 0.25 \cdot 0.4 = 0.1 \text{ m}^2$$

$$I = \frac{0.25 \cdot 0.4^3}{12} = 0.0013 \text{m}^4$$

$$L = \sqrt{(3-1)^2 + (3-.)^2} = 2 \text{ m}$$

$$\lambda_x = \frac{3-1}{2} = 1$$

$$\lambda_y = \frac{3-3}{2} = 0$$

$$A = 0.3 \cdot 0.4 = 0.12 \text{ m}^2$$

$$I = \frac{0.3 \cdot 0.4^3}{12} = 0.0016 \text{m}^4$$

$$L = \sqrt{(4-3)^2 + (0-3)^2} = 3.162 \text{ m}$$

$$\lambda_x = \frac{4-3}{3.162} = 0.316$$

$$\lambda_y = \frac{0-3}{3.162} = -0.949$$

Elemento 4, tiene la dirección 3 - 5

$$A = 0.3 \cdot 0.4 = 0.12 \text{ m}^2$$

$$I = \frac{0.3 \cdot 0.4^3}{12} = 0.0016 \text{m}^4$$

$$L = \sqrt{(2.2 - 3)^2 + (5.4 - 3)^2} = 2.53 \text{ m}$$

$$\lambda_x = \frac{2.2 - 3}{2.53} = -0.316$$

$$\lambda_y = \frac{5.4 - 3}{2.53} = 0.949$$

Matriz de rigidez local de cada elemento

Elemento 1

	1	2	3	4	5	6	
	79696.39	0	0	-79696.39	0	0	1
k' =	0	1275.37	2016.35	0	-1275.37	2016.35	2
	0	2016.35	4250.47	0	-2016.35	2125.24	3
	-79696.39	0	0	79696.39	0	0	4
	0	-1275.37	-2016.35	0	1275.37	-2016.35	5
	0	2016.35	2125.24	0	-2016.35	4250.47	6

Elemento 2

$$k' = \begin{bmatrix} 105000 & 0 & 0 & -105000 & 0 & 0 \\ 0 & 4095 & 4095 & 0 & -4095 & 4095 \\ 0 & 4095 & 5460 & 0 & -4095 & 2730 \\ -105000 & 0 & 0 & 105000 & 0 & 0 \\ 0 & -4095 & -4095 & 0 & 4095 & -4095 \\ 0 & 4095 & 2730 & 0 & -4095 & 5460 \end{bmatrix}$$

 $0.949 \quad 0$

 $-0.949 \quad 0.316 \quad 0$

Matriz de rotación de cada elemento

Elemento 1

 $T = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$

Elemento 2

$$T = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} 0.316 & -0.949 & 0 & 0 & 0 & 0 \\ 0.949 & 0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & -0.949 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T = \begin{bmatrix} -0.316 & 0.949 & 0 & 0 & 0 & 0 \\ -0.949 & -0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Matriz de rigidez global de cada elemento

Elemento 1

$$k = T^T k'T = \begin{bmatrix} 0.316 & -0.949 & 0 & 0 & 0 & 0 \\ 0.949 & 0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & -0.949 & 0 \\ 0 & 0 & 0 & 0.316 & -0.949 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 79696.39 & 0 & 0 & -79696.39 & 0 & 0 \\ 0 & 2016.35 & 4250.47 & 0 & -2016.35 & 2125.24 \\ -79696.39 & 0 & 0 & 79696.39 & 0 & 0 \\ 0 & -1275.37 & -2016.35 & 0 & 1275.37 & -2016.35 \\ 0 & 2016.35 & 2125.24 & 0 & -2016.35 & 4250.47 \end{bmatrix} \begin{bmatrix} 0.316 & 0.949 & 0 & 0 & 0 & 0 \\ -0.949 & 0.316 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0.949 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0.949 & 0.949 & 0.949 & 0$$

Elemento 2

$$k = T^T k' T = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 105000 & 0 & 0 & -105000 & 0 & 0 \\ 0 & 4095 & 4095 & 0 & -4095 & 4095 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 105000 & 0 & 0 & -105000 & 0 & 0 \\ 0 & 4095 & 4095 & 0 & -4095 & 4095 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 105000 & 0 & -105000 & 0 & 0 \\ 0 & 4095 & 4095 & 0 & -4095 & 4095 \\ 0 & 4095 & 5460 & 0 & -4095 & 2730 \\ -105000 & 0 & 0 & 105000 & 0 & 0 \\ 0 & -4095 & -4095 & 0 & 4095 & -4095 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

$$k = T^T k'T = \begin{bmatrix} -0.316 & -0.949 & 0 & 0 & 0 & 0 & 0 \\ 0.949 & -0.316 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -0.316 & -0.949 & 0 \\ 0 & 0 & 0 & 0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & 0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 99604.74 & 0 & 0 & -99604.74 & 0 & 0 \\ 0 & 2489.77 & 3149.56 & 5312.25 & 0 & -3149.56 & 2656.13 \\ -99604.74 & 0 & 0 & 99604.74 & 0 & 0 \\ 0 & -2489.77 & -3149.56 & 0 & 2489.77 & -3149.56 \\ 0 & 0 & 3149.56 & 2656.13 & 0 & -3149.56 & 5312.25 \end{bmatrix} \begin{bmatrix} -0.316 & 0.949 & 0 & 0 & 0 & 0 \\ -0.949 & -0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & -0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Matriz de rigidez de la estructura

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
	9116.47	23524.31	-1912.55	-9116.47	-23524.31	-1912.55	0	0	0	0	0	0	0	0	0	1
	23524.31	71847.96	637.52	-23524.31	-71847.96	637.52	0	0	0	0	0	0	0	0	0	2
	-1912.55	637.52	4250.1	1912.55	-637.52	2125.05	0	0	0	0	0	0	0	0	0	3
	-9116.47	-23524.31	1912.55	114116.47	23524.31	1912.55	-105000	0	0	0	0	0	0	0	0	4
	-23524.31	-71847.96	-637.52	23524.31	75942.96	3457.48	0	-4095	4095	0	0	0	0	0	0	5
	-1912.55	637.52	2125.05	1912.55	3457.48	9710.1	0	-4095	2730	0	0	0	0	0	0	6
	0	0	0	-105000	0	0	126318.91	-52660.75	-1075.81	-9116.47	23524.31	1912.55	-12202.44	29136.44	-2988.35	7
K =	0	0	0	0	-4095	-4095	-52660.75	165842.56	-4453.6	23524.31	-71847.96	637.52	29136.44	-89899.6	-996.12	8
	0	0	0	0	4095	2730	-1075.81	-4453.6	15022.73	-1912.55	-637.52	2125.05	2988.35	996.12	2656.31	9
	0	0	0	0	0	0	-9116.47	23524.31	-1912.55	9116.47	-23524.31	-1912.55	0	0	0	10
	0	0	0	0	0	0	23524.31	-71847.96	-637.52	-23524.31	71847.96	-637.52	0	0	0	11
	0	0	0	0	0	0	1912.55	637.52	2125.05	-1912.55	-637.52	4250.1	0	0	0	12
	0	0	0	0	0	0	-12202.44	29136.44	2988.35	0	0	0	12202.44	-29136.44	2988.35	13
	0	0	0	0	0	0	29136.44	-89899.6	996.12	0	0	0	-29136.44	89899.6	996.12	14
	0	0	0	0	0	0	-2988.35	-996.12	2656.31	0	0	0	2988.35	996.12	5312.63	15

Cargas nodales

$$Q^T = \begin{bmatrix} Q_1 & Q_2 & Q_3 & 0 & -5 & -1.667 & 0 & -5 & 1.667 & Q_{10} & Q_{11} & Q_{12} & 0 & 0 & 0 \end{bmatrix}$$

Desplazamientos nodales

$$D^{T} = \begin{bmatrix} 0 & 0 & 0 & D_{4} & D_{5} & D_{6} & D_{7} & D_{8} & D_{9} & 0 & 0 & D_{13} & D_{14} & D_{15} \end{bmatrix}$$

Sistema de ecuaciones y solución

Γ	Q_1		9116.47	23524.31	-1912.55	-9116.47	-23524.31	-1912.55	0	0	0	0	0	0	0	0	0	
	Q_2		23524.31	71847.96	637.52	-23524.31	-71847.96	637.52	0	0	0	0	0	0	0	0	0	0
	Q_3		-1912.55	637.52	4250.1	1912.55	-637.52	2125.05	0	0	0	0	0	0	0	0	0	0
	0		-9116.47	-23524.31	1912.55	114116.47	23524.31	1912.55	-105000	0	0	0	0	0	0	0	0	D_4
	-5		-23524.31	-71847.96	-637.52	23524.31	75942.96	3457.48	0	-4095	4095	0	0	0	0	0	0	D_5
	-1.667		-1912.55	637.52	2125.05	1912.55	3457.48	9710.1	0	-4095	2730	0	0	0	0	0	0	D_6
	0		0	0	0	-105000	0	0	126318.91	-52660.75	-1075.81	-9116.47	23524.31	1912.55	-12202.44	29136.44	-2988.35	D_7
	-5	=	0	0	0	0	-4095	-4095	-52660.75	165842.56	-4453.6	23524.31	-71847.96	637.52	29136.44	-89899.6	-996.12	D_8
	1.667		0	0	0	0	4095	2730	-1075.81	-4453.6	15022.73	-1912.55	-637.52	2125.05	2988.35	996.12	2656.31	D_9
	Q_{10}		0	0	0	0	0	0	-9116.47	23524.31	-1912.55	9116.47	-23524.31	-1912.55	0	0	0	0
	Q_{11}		0	0	0	0	0	0	23524.31	-71847.96	-637.52	-23524.31	71847.96	-637.52	0	0	0	0
	Q_{12}		0	0	0	0	0	0	1912.55	637.52	2125.05	-1912.55	-637.52	4250.1	0	0	0	0
	0		0	0	0	0	0	0	-12202.44	29136.44	2988.35	0	0	0	12202.44	-29136.44	2988.35	D_{13}
	0		0	0	0	0	0	0	29136.44	-89899.6	996.12	0	0	0	-29136.44	89899.6	996.12	D_{14}
	0		0	0	0	0	0	0	-2988.35	-996.12	2656.31	0	0	0	2988.35	996.12	5312.63	D_{15}

Resolviendo

Diagrama de esfuerzos

$$A = k'TD = \begin{bmatrix} 79696.39 & 0 & 0 & -79696.39 & 0 & 0 \\ 0 & 1275.37 & 2016.35 & 0 & -1275.37 & 2016.35 \\ 0 & 2016.35 & 4250.47 & 0 & -2016.35 & 2125.24 \\ -79696.39 & 0 & 0 & 79696.39 & 0 & 0 \\ 0 & 2016.35 & 2125.24 & 0 & -2016.35 & 4250.47 \end{bmatrix} \begin{bmatrix} 0.316 & 0.949 & 0 & 0 & 0 & 0 \\ -0.949 & 0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0.949 & 0 \\ -7.51 \times 10^{-5} & -7.51 \times 10^{-5} \\ -2.48 \times 10^{-4} & -0.989 \end{bmatrix} = \begin{bmatrix} 5.423 \\ -0.458 \\ -0.460 \\ -5.423 \\ 0.458 \\ -0.989 \end{bmatrix}$$



Figura 2: Reacciones en el elemento

$$N = -5.423$$

 $V = -0.458$
 $M = 0.46 - 0.458x$

$$q = k'TD + q_0 = \begin{bmatrix} 105000 & 0 & 0 & -105000 & 0 & 0 \\ 0 & 4095 & 4095 & 0 & -4095 & 4095 \\ 0 & 4095 & 5460 & 0 & -4095 & 2730 \\ -105000 & 0 & 0 & 105000 & 0 & 0 \\ 0 & 4095 & 2730 & 0 & -4095 & 5460 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1.02 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ -2.48 \times 10^{-4} \\ -1.02 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ 2.48 \times 10^{-4} \end{bmatrix} + \begin{bmatrix} 0 \\ 5 \\ 1.667 \\ 0 \\ 5 \\ -1.667 \end{bmatrix} = \begin{bmatrix} 2.15 \\ 5 \\ 0.989 \\ -2.15 \\ 5 \\ -0.989 \end{bmatrix}$$

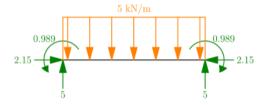


Figura 3: Reacciones en el elemento

$$N = -2.15$$

$$V = 5 - 5x$$

$$M = -0.989 + 5x - \frac{5}{2}x^{2}$$

$$q = k'TD = \begin{bmatrix} 79696.39 & 0 & 0 & -79696.39 & 0 & 0 \\ 0 & 1275.37 & 2016.35 & 0 & -1275.37 & 2016.35 \\ 0 & 2016.35 & 4250.47 & 0 & -2016.35 & 2125.24 \\ -79696.39 & 0 & 0 & 79696.39 & 0 & 0 \\ 0 & 2016.35 & 2125.24 & 0 & -2016.35 & 4250.47 \end{bmatrix} \begin{bmatrix} 0.316 & -0.949 & 0 & 0 & 0 & 0 \\ 0.949 & 0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.316 & -0.949 & 0 \\ 0 & 0 & 0 & 0.316 & 0 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0.949 & 0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} -1.02 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ 2.48 \times 10^{-4} \\ 0 \\ 0 \\ -5.423 \\ -0.458 \\ 0.461 \end{bmatrix}$$



Figura 4: Reacciones en el elemento

$$N = -5.423$$

 $V = 0.458$
 $M = -0.989 + 0.458x$

$$q = k'TD = \begin{bmatrix} 99604.74 & 0 & 0 & -99604.74 & 0 & 0 \\ 0 & 2489.77 & 3149.56 & 0 & -2489.77 & 3149.56 \\ 0 & 3149.56 & 5312.25 & 0 & -3149.56 & 2656.13 \\ -99604.74 & 0 & 0 & 99604.74 & 0 & 0 \\ 0 & -2489.77 & -3149.56 & 0 & 2489.77 & -3149.56 \\ 0 & 3149.56 & 2656.13 & 0 & -3149.56 & 5312.25 \end{bmatrix} \begin{bmatrix} -0.316 & 0.949 & 0 & 0 & 0 & 0 \\ -0.949 & -0.316 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -0.316 & 0.949 & 0 \\ 0 & 0 & 0 & -0.949 & -0.316 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} -1.02 \times 10^{-5} \\ -7.51 \times 10^{-5} \\ 2.48 \times 10^{-4} \\ -6.07 \times 10^{-4} \\ -2.74 \times 10^{-4} \\ 2.48 \times 10^{-4} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Figura 5: Reacciones en el elemento

$$N = 0$$
$$V = 0$$
$$M = 0$$