## Lab 10

## Direct methods for solving linear systems

## Gauss's method with partial pivoting

Consider the linear system Ax = b, with  $A = (a(i, j))_{i,j=\overline{1,n}}$  and b = (b(1), ..., b(n))'.

Algorithm:

Input: n-order of the system; A-matrix of coefficients; b-vector of free terms;

Output: x-vector of the solutions or a message in case of incompatibility of the system

1. For p = 1, ..., n - 1

Let  $abs(a(q, p)) = \max(abs(a(p : n, p))).$ 

If a(q, p) = 0 then "Message"; Exit

If  $q \neq p$  interchange the lines p and q from A and b.

Perform the necessary operations for obtaining zeros on the column p, below a(p,p).

Apply the transformations also to the vector b.

- 2. If a(n,n) = 0 then "Message"; Exit
- 3. For i = n : -1 : 1 do

Compute x(i).

4. Display x.

## Problem:

1. Implement the Gauss method for solving linear systems, using partial elimination. Solve the following system of equations:

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 2 & 3 & 1 & 5 \\ -1 & 1 & -5 & 3 \\ 3 & 1 & 7 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 10 \\ 31 \\ -2 \\ 18 \end{bmatrix}.$$