

THIS IS CS4084!

GCR:wzj3vua

IF YOU DON'T TALK TO YOUR KIDS
ABOUT QUANTUM COMPUTING...

SOMEONE ELSE WILL.

Quantum computing and
consciousness are both weird
and therefore equivalent.

MULTI QUBIT SYSTEM

CONTENT

We are covering chapter 4 “Multiple Quantum Bits” from the book `Introduction to Classical and Quantum Computing By Thomas G Wong`.

4.2

4.3

4.4.1 , 4.4.2 , 4.4.3

Practise book exercise for these sections.

TENSOR PRODUCT

This is pronounced “zero tensor zero.” $|0\rangle \otimes |0\rangle$

Often, we compress the notation and leave out the tensor product in both writing and speech:

$$|0\rangle|0\rangle \quad |00\rangle$$

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, \quad |1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}.$$

TWO QUBIT

With two qubits, the Z-basis is $\{|00\rangle, |01\rangle, |10\rangle, |11\rangle\}$.

A general state is a superposition of these basis states:

$$c_0|00\rangle + c_1|01\rangle + c_2|10\rangle + c_3|11\rangle$$

KRONECKER PRODUCT

$$|00\rangle = |0\rangle|0\rangle = |0\rangle \otimes |0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ 0 \begin{pmatrix} 1 \\ 0 \end{pmatrix} \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}.$$

$$|01\rangle = |0\rangle|1\rangle = |0\rangle \otimes |1\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ 0 \begin{pmatrix} 0 \\ 1 \end{pmatrix} \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}.$$

$$|10\rangle = |1\rangle|0\rangle = |1\rangle \otimes |0\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ 1 \begin{pmatrix} 1 \\ 0 \end{pmatrix} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}.$$

$$|11\rangle = |1\rangle|1\rangle = |1\rangle \otimes |1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \otimes \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ 1 \begin{pmatrix} 0 \\ 1 \end{pmatrix} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}.$$

TWO QUBITS

$$c_0|00\rangle + c_1|01\rangle + c_2|10\rangle + c_3|11\rangle = \begin{pmatrix} c_0 \\ c_1 \\ c_2 \\ c_3 \end{pmatrix}.$$

Exercise 4.4. Verify that

$$|1\rangle \otimes |1\rangle \otimes |0\rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}.$$

Exercise 4.5. Consider a two-qubit state

$$|\psi\rangle = \frac{1}{2}|00\rangle + \frac{i}{\sqrt{2}}|10\rangle + \frac{\sqrt{3}+i}{4}|11\rangle.$$

(a) What is $|\psi\rangle$ as a (column) vector?

MEASURING INDIVIDUAL QUBIT

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

What is the probability?

MEASURING INDIVIDUAL QUBIT

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

What is the probability if we measure only 1 qubit?

$|0\rangle$ with some probability, and the state collapses to something,

$|1\rangle$ with some probability, and the state collapses to something.

MEASURING INDIVIDUAL QUBIT

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

The probability of getting $|0\rangle$ when measuring the left qubit is given by the sum of the norm-squares of the amplitudes of $|00\rangle$ and $|01\rangle$, since those both have the left qubit as $|0\rangle$.

$$\left|\frac{1}{\sqrt{2}}\right|^2 + \left|\frac{1}{2}\right|^2 = \frac{3}{4}.$$

MEASURING INDIVIDUAL QUBIT

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

What is the probability if we measure only 1 qubit?

$|0\rangle$ with probability $\frac{3}{4}$, and the state collapses to something,
 $|1\rangle$ with probability $\frac{1}{4}$, and the state collapses to something.

MEASURING INDIVIDUAL QUBIT - LEFT QUBIT

State collapses to

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

$$A \left(\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle \right)$$

$$B \left(\frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle \right)$$

MEASURING INDIVIDUAL QUBIT - LEFT QUBIT

State collapses to

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

$|0\rangle$ with probability $\frac{3}{4}$, and the state collapses to $\sqrt{\frac{2}{3}}|00\rangle + \frac{1}{\sqrt{3}}|01\rangle$,

$|1\rangle$ with probability $\frac{1}{4}$, and the state collapses to $\frac{\sqrt{3}}{2}|10\rangle + \frac{1}{2}|11\rangle$.

MEASURING 3 QUBIT STATE

We can apply these ideas to any number of qubits. For example, if we have three qubits in the state.

$$c_0|000\rangle + c_1|001\rangle + c_2|010\rangle + c_3|011\rangle + c_4|100\rangle + c_5|101\rangle + c_6|110\rangle + c_7|111\rangle.$$

MEASURING 3 QUBIT STATE

If we measure the left and middle qubits

$$c_0|000\rangle + c_1|001\rangle + c_2|010\rangle + c_3|011\rangle + c_4|100\rangle + c_5|101\rangle + c_6|110\rangle + c_7|111\rangle.$$

$$|00\rangle \text{ with probability } |c_0|^2 + |c_1|^2, \text{ collapses to } \frac{c_0|000\rangle + c_1|001\rangle}{\sqrt{|c_0|^2 + |c_1|^2}},$$

$$|01\rangle \text{ with probability } |c_2|^2 + |c_3|^2, \text{ collapses to } \frac{c_2|010\rangle + c_3|011\rangle}{\sqrt{|c_2|^2 + |c_3|^2}},$$

$$|10\rangle \text{ with probability } |c_4|^2 + |c_5|^2, \text{ collapses to } \frac{c_4|100\rangle + c_5|101\rangle}{\sqrt{|c_4|^2 + |c_5|^2}},$$

$$|11\rangle \text{ with probability } |c_6|^2 + |c_7|^2, \text{ collapses to } \frac{c_6|110\rangle + c_7|111\rangle}{\sqrt{|c_6|^2 + |c_7|^2}}.$$

Exercise 4.7. Two qubits are in the state

$$\frac{i}{\sqrt{10}}|00\rangle + \frac{1-2i}{\sqrt{10}}|01\rangle + \frac{e^{i\pi/100}}{\sqrt{10}}|10\rangle + \frac{\sqrt{3}}{\sqrt{10}}|11\rangle.$$

If we measure the qubits in the Z-basis $\{|00\rangle, |01\rangle, |10\rangle, |11\rangle\}$, what are the possible outcomes and with what probabilities?

Exercise 4.8. Normalize the following quantum state:

$$A \left(\frac{1}{2} |00\rangle + i |01\rangle + \sqrt{2} |10\rangle - |11\rangle \right).$$

SEQUENTIAL SINGLE-QUBIT MEASUREMENTS

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

If we first measure the left qubit, we get

$|0\rangle$ with probability $\frac{3}{4}$, and the state collapses to $\sqrt{\frac{2}{3}}|00\rangle + \frac{1}{\sqrt{3}}|01\rangle$,

$|1\rangle$ with probability $\frac{1}{4}$, and the state collapses to $\frac{\sqrt{3}}{2}|10\rangle + \frac{1}{2}|11\rangle$.

If we measure right qubit now

$$\text{Prob}(|00\rangle) = \text{Prob}(\text{first left } |0\rangle) \text{Prob}(\text{then right } |0\rangle) = \frac{3}{4} \frac{2}{3} = \frac{1}{2},$$

$$\text{Prob}(|01\rangle) = \text{Prob}(\text{first left } |0\rangle) \text{Prob}(\text{then right } |1\rangle) = \frac{3}{4} \frac{1}{3} = \frac{1}{4},$$

$$\text{Prob}(|10\rangle) = \text{Prob}(\text{first left } |1\rangle) \text{Prob}(\text{then right } |0\rangle) = \frac{1}{4} \frac{3}{4} = \frac{3}{16},$$

$$\text{Prob}(|11\rangle) = \text{Prob}(\text{first left } |1\rangle) \text{Prob}(\text{then right } |1\rangle) = \frac{1}{4} \frac{1}{4} = \frac{1}{16}.$$

Exercise 4.9. Consider the two-qubit state

$$\frac{1}{4}|00\rangle + \frac{1}{2}|01\rangle + \frac{1}{\sqrt{2}}|10\rangle + \frac{\sqrt{3}}{4}|11\rangle.$$

If you measure only the left qubit, what are the resulting states, and with what probabilities?

Exercise 4.10. Consider the three-qubit state

$$\frac{1}{6}|000\rangle + \frac{1}{3\sqrt{2}}|001\rangle + \frac{1}{\sqrt{6}}|010\rangle + \frac{1}{2}|011\rangle + \frac{1}{6}|100\rangle + \frac{1}{3}|101\rangle + \frac{1}{6}|110\rangle + \frac{1}{\sqrt{3}}|111\rangle.$$

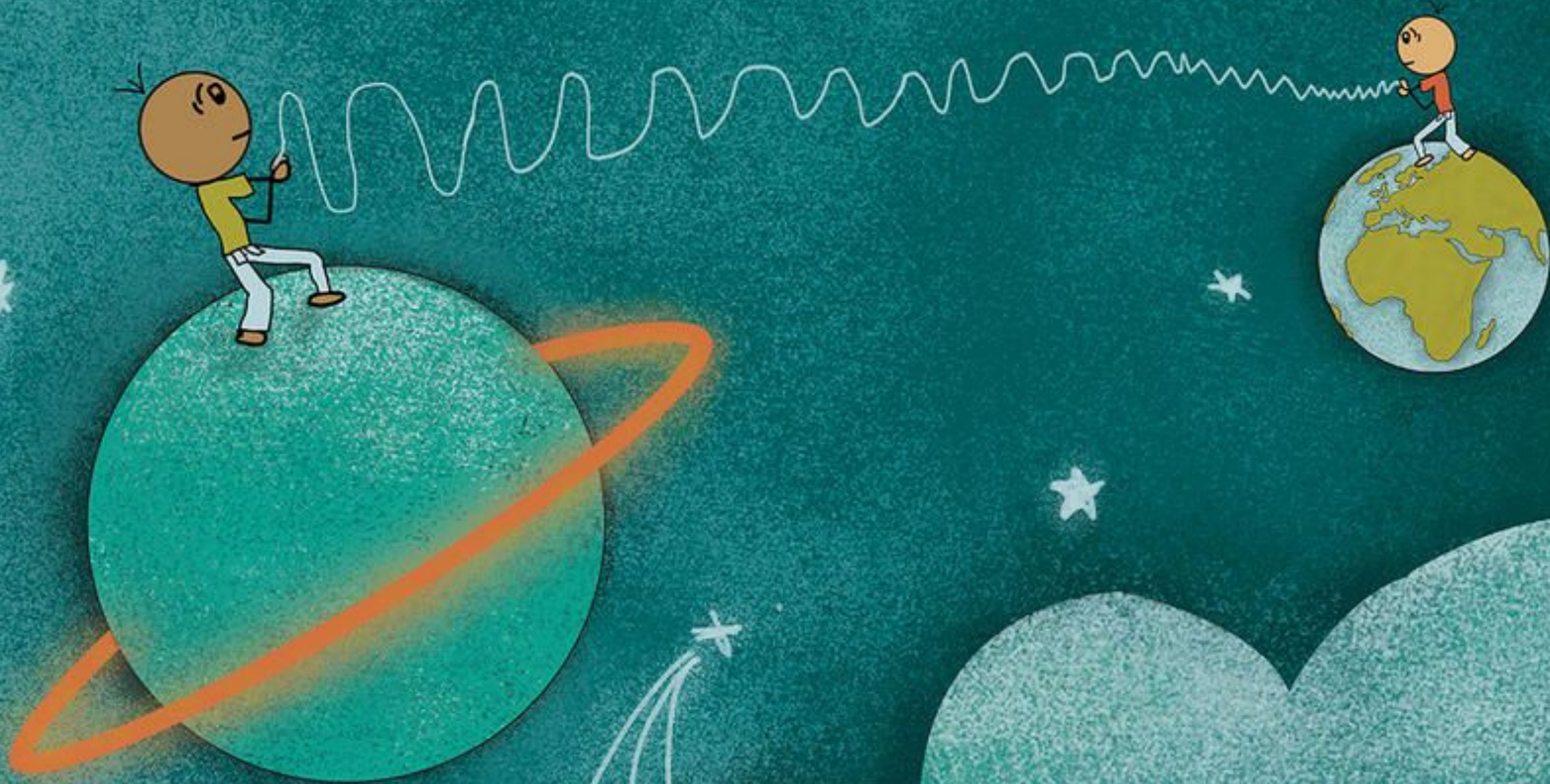
If you measure only the left and right qubits, but not the middle qubit, what are the resulting states, and with what probabilities?

Quantum
Entanglement

Spooky action
at a distance



ENTANGLEMENT



Separable State

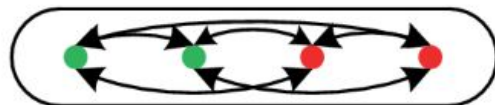


$$|\psi\rangle_{AB} = |\psi\rangle_A \otimes |\psi\rangle_B$$



(a)

Entangled State



$$|\psi\rangle_{AB} \neq |\psi\rangle_A \otimes |\psi\rangle_B$$



(b)

PRODUCT STATES

Some quantum states can be factored into (the tensor product of) individual qubit states. For example,

$$\begin{aligned}\frac{1}{2}(|00\rangle - |01\rangle + |10\rangle - |11\rangle) &= \underbrace{\frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)}_{|+\rangle} \otimes \underbrace{\frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)}_{|-\rangle} \\ &= |+\rangle \otimes |-\rangle \\ &= |+\rangle|-\rangle.\end{aligned}$$

PRODUCT STATES

$$\frac{1}{2\sqrt{2}} \left(\sqrt{3}|00\rangle - \sqrt{3}|01\rangle + |10\rangle - |11\rangle \right).$$

We want to write this as the product of two single-qubit states,

$$|\psi_1\rangle|\psi_0\rangle,$$

where

$$|\psi_1\rangle = \alpha_1|0\rangle + \beta_1|1\rangle, \quad |\psi_0\rangle = \alpha_0|0\rangle + \beta_0|1\rangle.$$

$$\begin{aligned} |\psi_1\rangle|\psi_0\rangle &= (\alpha_1|0\rangle + \beta_1|1\rangle)(\alpha_0|0\rangle + \beta_0|1\rangle) \\ &= \alpha_1\alpha_0|00\rangle + \alpha_1\beta_0|01\rangle + \beta_1\alpha_0|10\rangle + \beta_1\beta_0|11\rangle. \end{aligned}$$

Matching up the coefficients with our original state,

$$\alpha_1\alpha_0 = \frac{\sqrt{3}}{2\sqrt{2}}, \quad \alpha_1\beta_0 = \frac{-\sqrt{3}}{2\sqrt{2}}, \quad \beta_1\alpha_0 = \frac{1}{2\sqrt{2}}, \quad \beta_1\beta_0 = \frac{-1}{2\sqrt{2}}.$$

PRODUCT STATES

$$\begin{aligned} |\psi_1\rangle|\psi_0\rangle &= (\alpha_1|0\rangle + \beta_1|1\rangle)(\alpha_0|0\rangle + \beta_0|1\rangle) \\ &= \left(\frac{\sqrt{3}}{2\sqrt{2}\alpha_0}|0\rangle + \frac{1}{2\sqrt{2}}\frac{1}{\alpha_0}|1\rangle \right) (\alpha_0|0\rangle - \alpha_0|1\rangle). \end{aligned}$$

We see that α_0 cancels, yielding

$$|\psi_1\rangle|\psi_0\rangle = \left(\frac{\sqrt{3}}{2\sqrt{2}}|0\rangle + \frac{1}{2\sqrt{2}}|1\rangle \right) (|0\rangle - |1\rangle).$$

Moving the factor of $1/\sqrt{2}$ to the right qubit so that both qubits are normalized,

$$|\psi_1\rangle|\psi_0\rangle = \left(\frac{\sqrt{3}}{2}|0\rangle + \frac{1}{2}|1\rangle \right) \left(\frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle \right).$$

ENTANGLED STATES

There exist quantum states that cannot be factored into product states. These are called *entangled states*. For example, with two qubits,

$$|\Phi^+\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$$

cannot be written as $|\psi_1\rangle|\psi_0\rangle$. As a proof, let us try writing it as a product state using the procedure from the last section:

$$\begin{aligned} |\psi_1\rangle|\psi_0\rangle &= (\alpha_1|0\rangle + \beta_1|1\rangle)(\alpha_0|0\rangle + \beta_0|1\rangle) \\ &= \alpha_1\alpha_0|00\rangle + \alpha_1\beta_0|01\rangle + \beta_1\alpha_0|10\rangle + \beta_1\beta_0|11\rangle. \end{aligned}$$

Matching the coefficients, we get

$$\alpha_1\alpha_0 = \frac{1}{\sqrt{2}}, \quad \alpha_1\beta_0 = 0, \quad \beta_1\alpha_0 = 0, \quad \beta_1\beta_0 = \frac{1}{\sqrt{2}}.$$

TWO QUBIT GATES

CNOT

The CNOT gate or controlled-NOT gate inverts the right qubit if the left qubit is 1

The left qubit is called the control qubit, and the right qubit is called the target qubit.

Control qubit is unchanged by CNOT

Target qubit becomes the XOR of the inputs

$$\text{CNOT}|00\rangle = |00\rangle,$$

$$\text{CNOT}|01\rangle = |01\rangle,$$

$$\text{CNOT}|10\rangle = |11\rangle,$$

$$\text{CNOT}|11\rangle = |10\rangle.$$

CNOT - CX - CONTROLLED X

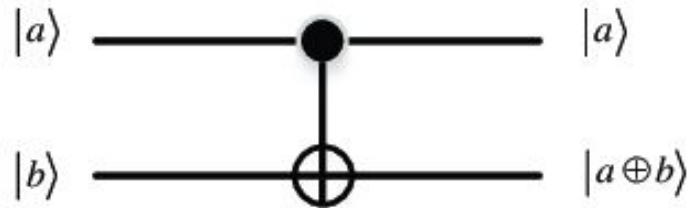
$$\text{CNOT}|00\rangle = |00\rangle,$$

$$\text{CNOT}|01\rangle = |01\rangle,$$

$$\text{CNOT}|10\rangle = |11\rangle,$$

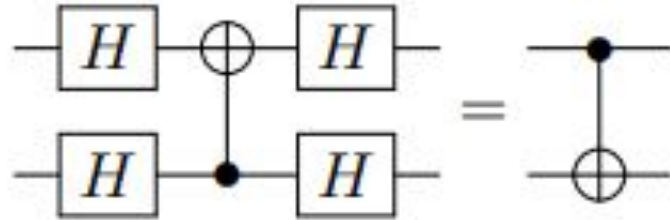
$$\text{CNOT}|11\rangle = |10\rangle.$$

$$\text{CNOT} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$



$\text{CNOT}_{ij} = \text{CNOT}$ with qubit i as the control and qubit j as the target.

WE DID THE CALCULATIONS IN CLASS



$$(H \otimes H)\text{CNOT}(H \otimes H) = \text{CNOT}_{01}$$

$$H \otimes H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \otimes \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{pmatrix}.$$

$$= \frac{1}{2} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \frac{1}{2} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{pmatrix}$$

$$= \frac{1}{4} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{pmatrix} \begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & 1 & -1 & -1 \end{pmatrix}$$

$$= \frac{1}{4} \begin{pmatrix} 4 & 0 & 0 & 0 \\ 0 & 0 & 0 & 4 \\ 0 & 0 & 4 & 0 \\ 0 & 4 & 0 & 0 \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}.$$

BELL STATES

Bell states are quantum states of two qubits that represent simple examples of quantum entanglement.

When one of the two qubits is measured, it takes on a specific value, and the second qubit is forced to also take on a specific value, as the entangled state collapses.

BELL STATES

Bell states are also known as EPR states or EPR pairs.

$$|\beta_{00}\rangle = \frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

$$|\beta_{01}\rangle = \frac{|01\rangle + |10\rangle}{\sqrt{2}}$$

$$|\beta_{10}\rangle = \frac{|00\rangle - |11\rangle}{\sqrt{2}}$$

$$|\beta_{11}\rangle = \frac{|01\rangle - |10\rangle}{\sqrt{2}}$$

BELL STATES

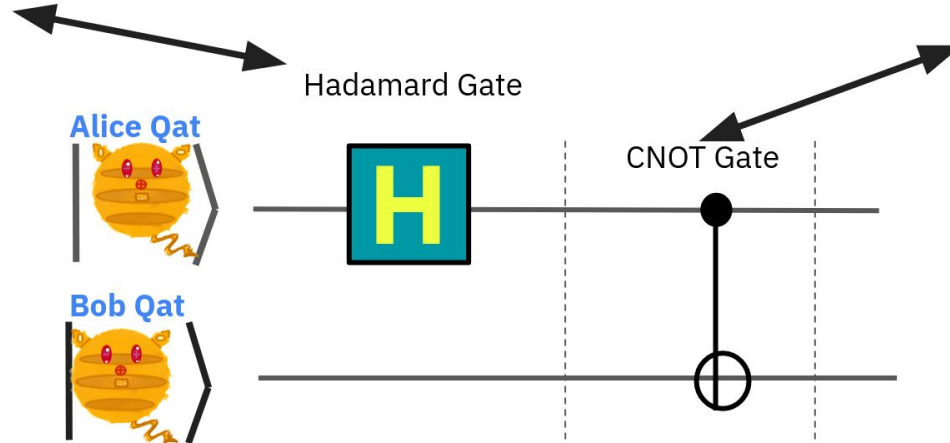
Bell states are quantum states of two qubits that represent simple examples of quantum entanglement.

When one of the two qubits is measured, it takes on a specific value, and the second qubit is forced to also take on a specific value, as the entangled state collapses.

quantum entanglement

$$\begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{bmatrix}$$

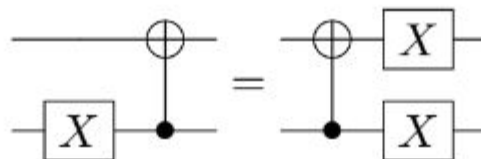
$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$



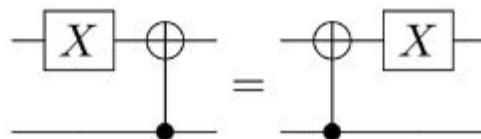
$$|\text{red qat}\rangle = \sqrt{\frac{1}{2}} |\text{yellow qat}\rangle + \sqrt{\frac{1}{2}} |\text{pink qats}\rangle$$

Exercise 4.15. Prove the following circuit identities, such as by finding the matrix representation of each circuit.

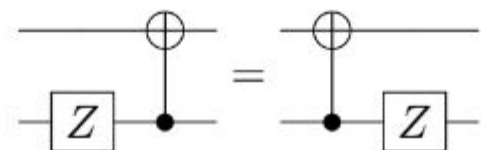
(a) $\text{CNOT}(X \otimes I) = (X \otimes X)\text{CNOT}.$



(b) $\text{CNOT}(I \otimes X) = (I \otimes X)\text{CNOT}.$



(c) $\text{CNOT}(Z \otimes I) = (Z \otimes I)\text{CNOT}.$



(d) $\text{CNOT}(I \otimes Z) = (Z \otimes Z)\text{CNOT}.$

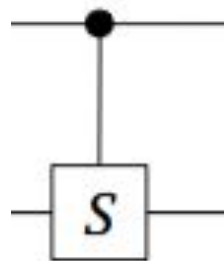
CONTROLLED Z GATE



$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

CONTROLLED S GATE

$$CS = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & i \end{pmatrix}$$



SWAP GATE

$$\text{SWAP} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}.$$

$$\text{SWAP}|00\rangle = |00\rangle,$$

$$\text{SWAP}|01\rangle = |10\rangle,$$

$$\text{SWAP}|10\rangle = |01\rangle,$$

$$\text{SWAP}|11\rangle = |11\rangle.$$

$|a\rangle$ \times $|b\rangle$

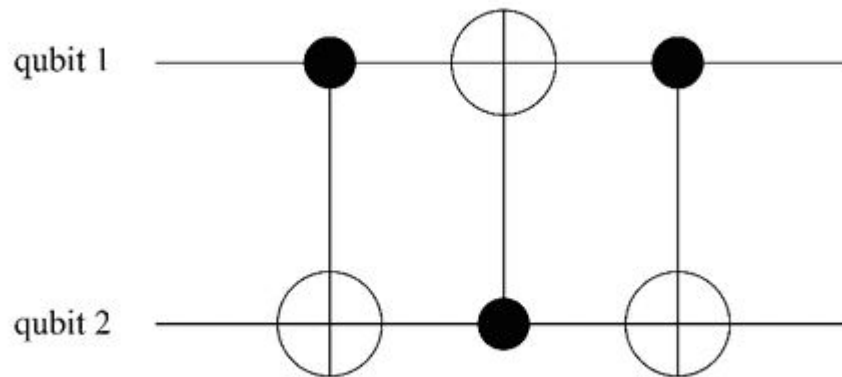
$|b\rangle$ \times $|a\rangle$

or

$|a\rangle$ ——— $|b\rangle$

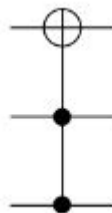
$|b\rangle$ ——— $|a\rangle$

SWAP GATE USING CNOT ONLY



TOFFOLI GATE

$$\text{Toffoli} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}.$$



$$\text{Toffoli}|000\rangle = |000\rangle,$$

$$\text{Toffoli}|001\rangle = |001\rangle,$$

$$\text{Toffoli}|010\rangle = |010\rangle,$$

$$\text{Toffoli}|011\rangle = |011\rangle,$$

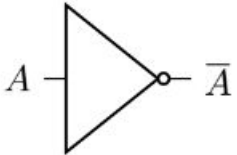

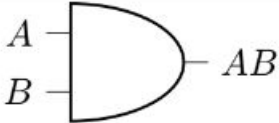
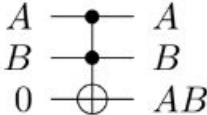
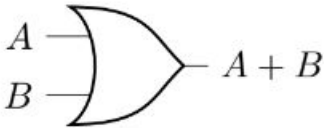
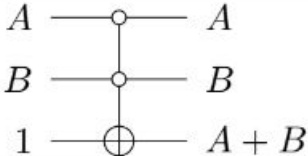
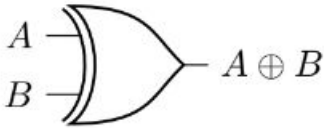
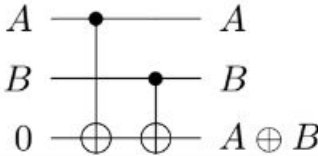
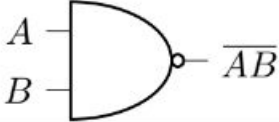
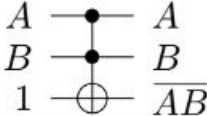
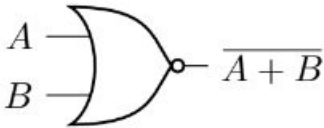
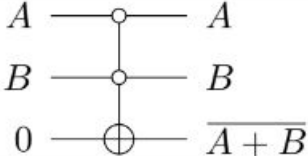
$$\text{Toffoli}|100\rangle = |100\rangle,$$

$$\text{Toffoli}|101\rangle = |101\rangle,$$

$$\text{Toffoli}|110\rangle = |111\rangle,$$

$$\text{Toffoli}|111\rangle = |110\rangle.$$

$$\text{Toffoli}|a\rangle|b\rangle|c\rangle = |a\rangle|b\rangle|ab \oplus c\rangle.$$

Classical		Reversible/Quantum	
NOT		X-Gate	
AND		Toffoli	
OR		anti-Toffoli	
XOR		CNOTs	
NAND		Toffoli	
NOR		anti-Toffoli	

TWO QUBIT GATES



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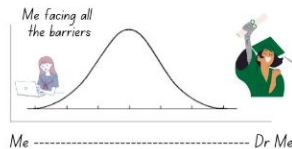
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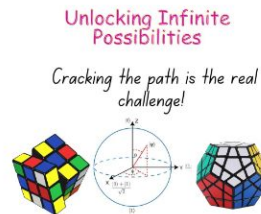
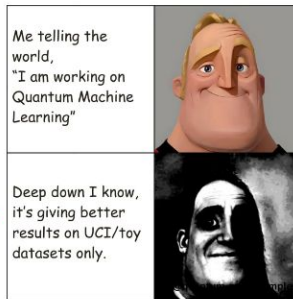
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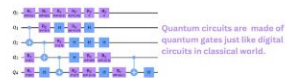


CONNA QUANTUM TUNNEL RIGHT THROUGH IT!

@quantum_made_simple



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Quantum Neural Networks

Fun fact: Quantum circuits are the superheroes of quantum neural networks. They can tackle all sorts of problems in classical ML with just some right combination of gates.

IN A PARALLEL WORLD



**SUPERPOSITION STATE
OF ALL CHANDLER'S CLOTHS**

REFERENCES

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