```
# Install packages
!pip install pennylane pennylane-lightning pennylane-lightning[gpu] cotengra quimb --upgr
!pip install tifffile
!pip install -U "jax[cuda12_pip]" -f https://storage.googleapis.com/jax-releases/jax_cuda
# !pip install --upgrade "jax[cuda11_pip]" -f https://storage.googleapis.com/jax-releases

→ Collecting pennylane

       Downloading PennyLane-0.39.0-py3-none-any.whl.metadata (9.2 kB)
     Collecting pennylane-lightning
       Downloading PennyLane_Lightning-0.39.0-cp310-cp310-manylinux_2_28_x86_64.whl.metada
     Collecting cotengra
       Downloading cotengra-0.6.2-py3-none-any.whl.metadata (4.5 kB)
     Collecting quimb
       Downloading quimb-1.9.0-py3-none-any.whl.metadata (5.5 kB)
     Requirement already satisfied: numpy<2.1 in /usr/local/lib/python3.10/dist-packages (
     Requirement already satisfied: scipy in /usr/local/lib/python3.10/dist-packages (from
     Requirement already satisfied: networkx in /usr/local/lib/python3.10/dist-packages (f
     Collecting rustworkx>=0.14.0 (from pennylane)
       Downloading rustworkx-0.15.1-cp38-abi3-manylinux_2_17_x86_64.manylinux2014_x86_64.w
     Requirement already satisfied: autograd in /usr/local/lib/python3.10/dist-packages (f
     Requirement already satisfied: toml in /usr/local/lib/python3.10/dist-packages (from
     Collecting appdirs (from pennylane)
       Downloading appdirs-1.4.4-py2.py3-none-any.whl.metadata (9.0 kB)
     Collecting autoray>=0.6.11 (from pennylane)
       Downloading autoray-0.7.0-py3-none-any.whl.metadata (5.8 kB)
     Requirement already satisfied: cachetools in /usr/local/lib/python3.10/dist-packages
     Requirement already satisfied: requests in /usr/local/lib/python3.10/dist-packages (f
     Requirement already satisfied: typing-extensions in /usr/local/lib/python3.10/dist-pa
     Requirement already satisfied: packaging in /usr/local/lib/python3.10/dist-packages (
     Collecting pennylane-lightning-gpu (from pennylane-lightning[gpu])
       Downloading PennyLane_Lightning_GPU-0.39.0-cp310-cp310-manylinux_2_28_x86_64.whl.me
     Collecting cytoolz>=0.8.0 (from quimb)
       Downloading cytoolz-1.0.0-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
     Requirement already satisfied: numba>=0.39 in /usr/local/lib/python3.10/dist-packages
     Requirement already satisfied: psutil>=4.3.1 in /usr/local/lib/python3.10/dist-packag
     Requirement already satisfied: tqdm>=4 in /usr/local/lib/python3.10/dist-packages (fr
     Requirement already satisfied: toolz>=0.8.0 in /usr/local/lib/python3.10/dist-package
     Requirement already satisfied: llvmlite<0.44,>=0.43.0dev0 in /usr/local/lib/python3.1
     Requirement already satisfied: charset-normalizer<4,>=2 in /usr/local/lib/python3.10/
     Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.10/dist-package
     Requirement already satisfied: urllib3<3,>=1.21.1 in /usr/local/lib/python3.10/dist-p
     Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.10/dist-p
     Downloading PennyLane-0.39.0-py3-none-any.whl (1.9 MB)
                                             --- 1.9/1.9 MB 36.4 MB/s eta 0:00:00
     Downloading PennyLane_Lightning-0.39.0-cp310-cp310-manylinux_2_28_x86_64.whl (1.7 MB)
                                               - 1.7/1.7 MB 62.1 MB/s eta 0:00:00
    Downloading cotengra-0.6.2-py3-none-any.whl (177 kB)
                                             --- 177.8/177.8 kB 16.3 MB/s eta 0:00:00
     Downloading quimb-1.9.0-py3-none-any.whl (1.7 MB)
                                              — 1.7/1.7 MB 51.3 MB/s eta 0:00:00
     Downloading autoray-0.7.0-py3-none-any.whl (930 kB)
                                               - 930.0/930.0 kB 48.8 MB/s eta 0:00:00
     Downloading cytoolz-1.0.0-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.whl
```

```
- 2.0/2.0 MB 62.4 MB/s eta 0:00:00
     Downloading rustworkx-0.15.1-cp38-abi3-manylinux_2_17_x86_64.manylinux2014_x86_64.whl
                                                 - 2.0/2.0 MB 73.3 MB/s eta 0:00:00
     Downloading appdirs-1.4.4-py2.py3-none-any.whl (9.6 kB)
     Downloading PennyLane_Lightning_GPU-0.39.0-cp310-cp310-manylinux_2_28_x86_64.whl (776
                                                  - 776.7/776.7 kB 38.7 MB/s eta 0:00:00
     Installing collected packages: appdirs, rustworkx, cytoolz, autoray, cotengra, quimb,
     Successfully installed appdirs-1.4.4 autoray-0.7.0 cotengra-0.6.2 cytoolz-1.0.0 penny
     Requirement already satisfied: tifffile in /usr/local/lib/python3.10/dist-packages (2
     Requirement already satisfied: numpy in /usr/local/lib/python3.10/dist-packages (from
     Looking in links: <a href="https://storage.googleapis.com/jax-releases/jax_cuda_releases.html">https://storage.googleapis.com/jax-releases/jax_cuda_releases.html</a>
import jax
import jax.numpy as jnp
x = jnp.ones((1000, 1000))
y = jnp.dot(x, x)
print(jax.devices())
     [CudaDevice(id=0)]
# Import packages
import matplotlib as mpl
import matplotlib.pyplot as plt
import sys
import numpy as np
#np.set printoptions(threshold=sys.maxsize)
import pandas as pd
from sklearn import datasets
import seaborn as sns
import jax
import time
from tifffile import tifffile
import functools
from typing import List, Union, Tuple, Dict, Optional, Any
from typing import Callable
jax.config.update("jax enable x64", True)
#jax.config.update("jax_debug_nans", True)
import jax.numpy as jnp
import optax # optimization using jax
import torch # https://pytorch.org
import torchvision # https://pytorch.org
#torch.set_printoptions(profile="full")
import pennylane as qml
import pennylane.numpy as pnp
```

```
import os, cv2, itertools # cv2 -- OpenCV
import shutil
import zipfile
%matplotlib inline
from jax.lib import xla_bridge
def set_jax_platform():
    # Check if TPU is available
   try:
        tpu_backend = xla_bridge.get_backend('tpu')
        if tpu_backend and tpu_backend.device_count() > 0:
            # Set platform to TPU
            jax.config.update('jax_platform_name', 'tpu')
            print("Set platform to TPU")
            return
    except RuntimeError:
        pass # No TPU found, move on to check for GPU
   # Check if GPU is available
   try:
      gpu_backend = xla_bridge.get_backend('gpu')
      if gpu_backend and gpu_backend.device_count() > 0:
          # Set platform to CUDA (GPU)
          jax.config.update('jax_platform_name', 'gpu')
          print("Set platform to GPU")
    except RuntimeError:
          # Set platform to CPU
          jax.config.update('jax_platform_name', 'cpu')
          print("Set platform to CPU")
# Call the function to set the platform
set_jax_platform()
sns.set()
seed = 1701
rng = np.random.default_rng(seed=seed)
prng = pnp.random.default_rng(seed=seed)
jrng_key = jax.random.PRNGKey(seed)
     Set platform to GPU
     <ipython-input-3-18305dd46f60>:40: DeprecationWarning: jax.lib.xla_bridge.get_backenc
       tpu_backend = xla_bridge.get_backend('tpu')
     <ipython-input-3-18305dd46f60>:51: DeprecationWarning: jax.lib.xla_bridge.get_backenc
       gpu_backend = xla_bridge.get_backend('gpu')
from google.colab import drive
drive.mount('/content/drive')
```

Mounted at /content/drive

```
ROWS, COLS = 32, 32

# Extract data from https://www.kaggle.com/datasets/kmader/siim-medical-images
data_zip = '/content/drive/MyDrive/Datasets/CTMedicalImages/archive.zip'

# extract the file
with zipfile.ZipFile(data_zip, 'r') as zip_ref:
    zip_ref.extractall(os.getcwd())
from google.colab.patches import cv2_imshow
```

from google.colab.patches import cv2_imshow
 overview_df = pd.read_csv('overview.csv')
 overview_df.columns = ['id']+list(overview_df.columns[1:])
 overview_df['Contrast'] = overview_df['Contrast'].map(lambda x: 1 if x else 0) #1 for con
 dummy_img = tifffile.imread(os.path.join('tiff_images', overview_df['tiff_name'][0]))
 cv2_imshow(dummy_img)



resized = cv2.resize(dummy_img, (ROWS, COLS),interpolation=cv2.INTER_CUBIC)
cv2 imshow(resized)



```
def read tiff and resize(filepath, resize row = 32, resize col = 32):
  img = tifffile.imread(filepath)
  return cv2.resize(img, (resize_row, resize_col),interpolation=cv2.INTER_CUBIC)
class CTImgHerm(torch.utils.data.Dataset):
    def __init__(self, overview_csv='overview.csv', tiff_img_folder='tiff_images', resize
        self.overview_df = pd.read_csv('overview.csv')
        self.overview_df.columns = ['idx']+list(overview_df.columns[1:])
        self.overview_df['Contrast'] = overview_df['Contrast'].map(lambda x: 1 if x else
        self.resize_col = resize_col
        self.resize_row = resize_row
        self.data = []
        for i in range(len(self.overview_df)):
          img = read_tiff_and_resize(os.path.join(tiff_img_folder, overview_df['tiff_name
          img = cv2.normalize(img, None, 0, 1.0,cv2.NORM_MINMAX, dtype=cv2.CV_32F)
          label = self.overview_df['Contrast'][i]
          self.data.append((img, label))
    def __len__(self):
        return len(self.data)
    def __getitem__(self, idx):
        img, label = self.data[idx]
        img = (img + np.transpose(img))/2
        return img, label
dummy_dataset = CTImgHerm()
dummy_dataset[0]
     (array([[0.00067681, 0.00067681, 0.00067681, ..., 0.00067681, 0.00067681,
              0.00067681],
             [0.00067681, 0.00067681, 0.00067681, ..., 0.00858719, 0.00069783,
              0.00067681],
             [0.00067681, 0.00067681, 0.00067681, ..., 0.05319135, 0.00705113,
              0.00054893],
             [0.00067681, 0.00858719, 0.05319135, ..., 0.07699811, 0.0740454,
              0.04863514],
             [0.00067681, 0.00069783, 0.00705113, ..., 0.0740454, 0.41830966,
              0.02946547],
             [0.00067681, 0.00067681, 0.00054893, ..., 0.04863514, 0.02946547,
              0.00067681]], dtype=float32),
```

```
1)
def img_hermitian_evolve(
    img:jnp.ndarray,
   t:float
)->jnp.ndarray:
  assert img.shape[-1]==32 and img.shape[-2] == 32, f"The shape of the image must be 32 by
  return jax.scipy.linalg.expm(img*( -0.5j*t))
print(
    img_hermitian_evolve(
        dummy_dataset[0][0],
        )[16]
    )
     [ 0.03316834+0.10185403j
                               0.03990275+0.01448904j -0.01340654-0.11395637j
      -0.09734283-0.04602238j -0.02874839-0.10615511j 0.03417724-0.0231277j
       0.31355855-0.00824658j -0.02404667+0.14984643j -0.20052674-0.04882964j
       0.14395793+0.08981129j 0.1990049 -0.210869j -0.27399263+0.07857375j
      -0.06780967-0.25949493j 0.26647484-0.00677687j 0.05676082-0.0082445j
      -0.06779608-0.04115491j 0.11816131-0.20410226j -0.08650953-0.03623072j
      -0.04554248+0.09426466j 0.15362452+0.02755849j 0.07865272-0.17987852j
      -0.07149893+0.21788627j 0.08791468-0.09473701j 0.01336784+0.02959449j
       0.23885594-0.01219563j 0.15551719-0.15525931j 0.0274305 -0.07152441j
       0.18937154+0.15392612j -0.07521366+0.0550395j -0.04855048-0.09508036j
      -0.04012334-0.05201115j 0.05081468-0.17594492j]
ket = {
    '0':jnp.array([1,0]),
    '1':jnp.array([0,1]),
    '+':(jnp.array([1,0]) + jnp.array([0,1]))/jnp.sqrt(2),
    '-':(jnp.array([1,0]) - jnp.array([0,1]))/jnp.sqrt(2)
}
pauli = {
    'I':jnp.array([[1,0],[0,1]]),
    'X':jnp.array([[0,1],[1,0]]),
    'Y':jnp.array([[0, -1j],[1j, 0]]),
    'Z':jnp.array([[1,0],[0,-1]])
}
def tensor_product(*args):
  input_list = [a for a in args]
  return functools.reduce(jnp.kron, input_list)
def multi_qubit_identity(n_qubits:int)->jnp.ndarray:
  assert n_qubits>0
  if n_qubits == 1:
    return pauli['I']
```

```
erse:
    return tensor_product(*[pauli['I'] for _ in range(n_qubits)])
pauli_words_su4 = {}
for key1 in pauli.keys():
  for key2 in pauli.keys():
    if not (key1==key2 and key1=='I' and key2=='I'):
      pauli_words_su4[key1+key2] = tensor_product(pauli[key1], pauli[key2])
pauli_words_su8 = {}
for key1 in pauli.keys():
  for key2 in pauli.keys():
    for key3 in pauli.keys():
      if not key1+key2+key3 == 'III':
        pauli_words_su8[key1+key2+key3] = tensor_product(pauli[key1], pauli[key2], pauli[
pauli_words_su16 = {}
for key1 in pauli.keys():
  for key2 in pauli.keys():
    for key3 in pauli.keys():
      for key4 in pauli.keys():
        if not key1+key2+key3+key4 == 'IIII':
          pauli_words_su16[key1+key2+key3+key4] = tensor_product(
              pauli[key1],
              pauli[key2],
              pauli[key3],
              pauli[key4]
          )
pauli_words_su32 = {}
for key1 in pauli.keys():
  for key2 in pauli.keys():
    for key3 in pauli.keys():
      for key4 in pauli.keys():
        for key5 in pauli.keys():
          if not key1+key2+key3+key4+key5 == 'IIIII':
            pauli_words_su32[key1+key2+key3+key4+key5] = tensor_product(
                pauli[key1],
                pauli[key2],
                pauli[key3],
                pauli[key4],
                pauli[key5]
            )
observables_2_cls_5q = [0]*2
for i in ['0', '1']:
      idx = int(i, 2)
      basis_state =ket[i]
      single_qubit_obs = jnp.outer(basis_state, basis_state)
      observables_2_cls_5q[idx] = tensor_product(single_qubit_obs, multi_qubit_identity(4
```

```
print(observables_2_cls_5q)
     [Array([[1, 0, 0, ..., 0, 0, 0],
            [0, 1, 0, \ldots, 0, 0, 0],
            [0, 0, 1, \ldots, 0, 0, 0],
            . . . ,
            [0, 0, 0, \ldots, 0, 0, 0],
            [0, 0, 0, \ldots, 0, 0, 0],
            [0, 0, 0, ..., 0, 0, 0]], dtype=int64), Array([[0, 0, 0, ..., 0, 0, 0],
            [0, 0, 0, \ldots, 0, 0, 0],
            [0, 0, 0, \ldots, 0, 0, 0],
            [0, 0, 0, \ldots, 1, 0, 0],
            [0, 0, 0, \ldots, 0, 1, 0],
            [0, 0, 0, ..., 0, 0, 1]], dtype=int64)]
def su4 op(
    params:jnp.ndarray
):
  generator = jnp.einsum("i, ijk -> jk", params, jnp.asarray(list(pauli_words_su4.values(
  return jax.scipy.linalg.expm(1j*generator)
def brickwall_su4_5q_single_layer(
    params:jnp.ndarray
):
  A brickwall layer of su4 gates on 5 qubits.
  Second stack is three su4 on qubit pairs (1,2), (3,4)
  First stack is two su4 on qubit pairs (2,3), (4,5)
  .....
  second_stack = tensor_product(
      su4 op(params[:15]),
      su4_op(params[15:30]),
      multi_qubit_identity(1)
  first_stack = tensor_product(
      multi qubit identity(1),
      su4_op(params[30:45]),
      su4_op(params[45:60]),
  )
  return jnp.dot(second_stack, first_stack)
def su32_op(
    params:jnp.ndarray
):
  generator = jnp.einsum("i, ijk - >jk", params, jnp.asarray(list(pauli_words_su32.values
  return jax.scipy.linalg.expm(1j*generator)
test_params = jax.random.normal(shape=[60], key=jrng_key)
print(brickwall_su4_5q_single_layer(test_params).shape)
```

```
(32, 32)
def measure_sv(
    state:jnp.ndarray,
   observable:jnp.ndarray
   ):
  .....
 Measure a statevector with a Hermitian observable.
 Note: No checking Hermitianicity of the observable or whether the observable
  has all real eigenvalues or not
  expectation_value = jnp.dot(jnp.conj(state.T), jnp.dot(observable, state))
  return jnp.real(expectation_value)
def measure_dm(
    rho: jnp.ndarray,
   observable:jnp.ndarray
):
 Measure a density matrix with a Hermitian observable.
  Note: No checking Hermitianicity of the observable or whether the observable
  has all real eigenvalues or not.
  product = jnp.dot(rho, observable)
 # Calculate the trace, which is the sum of diagonal elements
 trace = jnp.trace(product)
 # The expectation value should be real for physical observables
 return jnp.real(trace)
vmap_measure_sv = jax.vmap(measure_sv, in_axes=(None, 0), out_axes=0)
vmap_measure_dm = jax.vmap(measure_dm, in_axes=(None, 0), out_axes=0)
def bitstring_to_state(bitstring:str):
 Convert a bit string, like '0101001' or '+-+-101'
 to a statevector. Each character in the bitstring must be among
  0, 1, + and -
 assert len(bitstring)>0
  for c in bitstring:
    assert c in ['0', '1', '+', '-']
  single_qubit_states = [ket[c] for c in bitstring]
  return tensor_product(*single_qubit_states)
def qnn_hamevo(
    params:jnp.ndarray,
    t:jnp.ndarray,
```

```
img:jnp.ndarray
)->jnp.ndarray:
 A QNN that takes (M+M^T)/2
 as input, where M is the (rescaled) original image,
 as well as a trainable parameter t,
  and parameters for the trainable layers
  and output an array of 2 elements representing classification logits
  single op params = 60 \#4**5-1
 n_outer_layers = len(t)
  n_inner_layers = (len(params)//single_op_params)//n_outer_layers
  state = tensor_product(ket['+'], ket['+'], ket['+'], ket['+'])
  for i in range(n_outer_layers):
    state = jnp.dot(
      img_hermitian_evolve(img, t[i]),
      state
      )
    inner_layer_params = params[i*(single_op_params*n_inner_layers):(i+1)*(single_op_para
    for j in range(n_inner_layers):
      state = jnp.dot(
          brickwall_su4_5q_single_layer(inner_layer_params[j*single_op_params:(j+1)*singl
      )
  return vmap_measure_sv(state, jnp.asarray(observables_2_cls_5q))
print(
    qnn_hamevo(
        jax.random.normal(shape=[60*15], key=jrng_key),
        jax.random.normal(shape=[15], key=jrng_key),
        dummy_dataset[0][0]
    )
)
     [0.44247169 0.55752831]
@jax.jit
def compute_out(weight,t, features, labels):
    """Computes the output of the corresponding label in the qcnn"""
   out = lambda weight,t, feature, label: qnn_hamevo(weight,t, feature)
    return jax.vmap(out, in axes=(None, None, 0, 0), out axes=0)(
        weight,t, features, labels
    )
def compute accuracy(weight,t, features, labels):
    """Computes the accuracy over the provided features and labels"""
```

```
out = compute_out(weight,t, features, labels)
    pred = jnp.argmax(out, axis = 1)
    return jnp.sum(jnp.array(pred == labels).astype(int)) / len(out)
def compute cost(weight,t, features, labels):
    """Computes the cost over the provided features and labels"""
    logits = compute_out(weight,t, features, labels)
    return jnp.nanmean(optax.softmax cross entropy with integer labels(logits, labels))
value_and_grad = jax.jit(jax.value_and_grad(compute_cost, argnums=[0,1]))
N_OUTER_LAYERS = 2
N INNER LAYERS = 1
N_LAYERS = N_OUTER_LAYERS*N_INNER_LAYERS
SINGLE OP PARAMS = 60 \#4**5-1
def init_weights_random():
    print("Random Init")
    return jax.random.normal(shape=[SINGLE_OP_PARAMS*N_LAYERS], key=jrng_key),jax.random.
def init weights beta(alpha=0.5, beta=2.0):
   # Initialize weights with a Beta distribution skewed towards 0
   weights = jax.random.beta(jrng key, alpha, beta, shape=[SINGLE OP PARAMS*N LAYERS])
    biases = jax.random.beta(jrng_key, alpha, beta, shape=[N_OUTER_LAYERS])
    return weights, biases
import pandas as pd
import os
def save_weights_to_csv(weights, biases, epoch, file_name='weights.csv'):
    """Saves the weights and biases to a CSV file."""
    # Convert weights and biases to a flat list
   weight_list = weights.flatten().tolist()
    bias_list = biases.flatten().tolist()
   # Create a dictionary to store the weights and biases with epoch
    data = {'epoch': [epoch], 'weights': [weight_list], 'biases': [bias_list]}
   # Convert to DataFrame
   df = pd.DataFrame(data)
   # Check if the file exists before appending
    if not os.path.isfile(file_name):
        # If the file does not exist, create it with a header
        df.to_csv(file_name, mode='w', header=True, index=False)
    else:
        # If the file exists, append the new data without a header
```

dt.to_csv(tile_name, mode='a', header=False, index=False)

```
# def train_vqc(batchsize:int, n_epochs:int, seed:int=1701):
    start = time.time()
#
   pnp.random.seed(seed)
#
   np.random.seed(seed)
#
   # load data
#
   full_dataset = CTImgHerm()
#
   train_size = int(0.8 * len(full_dataset))
#
   test_size = len(full_dataset) - train_size
#
   train dataset, test dataset = torch.utils.data.random split(full dataset, [train size
#
   trainloader = torch.utils.data.DataLoader(
#
      train_dataset, batch_size=batchsize, shuffle=True
#
    )
#
   testloader = torch.utils.data.DataLoader(
#
      test dataset, batch size=batchsize, shuffle=True
#
#
   # Exponential decay of the learning rate.
#
    scheduler = optax.exponential_decay(
#
      init_value=0.01,
#
      transition_steps=n_epochs,
#
      decay_rate=0.99)
#
   # Combining gradient transforms using `optax.chain`.
#
    gradient_transform = optax.chain(
#
      optax.clip(1.0),
      optax.scale_by_adam(), # Use the updates from adam.
#
#
      optax.scale_by_schedule(scheduler), # Use the learning rate from the scheduler.
#
      # Scale updates by -1 since optax.apply_updates is additive and we want to descend
      optax.scale(-1.0)
#
#
    )
#
   # init weights and optimizer
#
   weights, weights_last = init_weights()
#
   opt_state = gradient_transform.init((weights, weights_last))
#
   #data containers
#
   train_cost_epochs, test_cost_epochs, train_acc_epochs, test_acc_epochs = [], [], [],
#
   for step in range(n_epochs):
#
          train_cost_batches = []
#
          train_acc_batches = []
#
          test_cost_batches = []
#
          test_acc_batches = []
#
          epoch_start = time.time()
#
          print(f"Training at Epoch {step+1}/{n_epochs}, Train batches {len(trainloader)}
#
          for batch, (x_train, y_train) in enumerate(trainloader):
#
            batch_start = time.time()
#
            # Training step with (adam) optimizer
#
            x_train, y_train = jnp.asarray(x_train.numpy()), jnp.asarray(y_train.numpy())
            train_cost, grad_circuit = value_and_grad(weights, weights_last, x_train, y_t
#
            updates, opt_state = gradient_transform.update(grad_circuit, opt_state)
```

```
#
            weights, weights_last = optax.apply_updates((weights, weights_last), updates)
#
            train_acc = compute_accuracy(weights, weights_last, x_train, y_train)
#
            train_cost_batches.append(train_cost)
#
            train acc batches.append(train acc)
#
            if len(trainloader)<= 5 or (batch+1)%5==0:</pre>
#
              print(f"Training at Epoch {step+1}/{n_epochs}, Batch {batch+1}, Cost {train
#
          train cost epochs.append(np.mean(train cost batches))
#
          train_acc_epochs.append(np.mean(train_acc_batches))
          # load test data
#
          for batch, (x_test, y_test) in enumerate(testloader):
#
#
            batch_start = time.time()
#
            x_test, y_test = jnp.asarray(x_test.numpy()), jnp.asarray(y_test.numpy())
            # compute accuracy and cost on testing data
#
#
            test_out = compute_out(weights, weights_last, x_test, y_test)
#
            test_pred = jnp.argmax(test_out, axis=1)
            test_acc = jnp.sum(jnp.array(test_pred == y_test).astype(int)) / len(test_out
#
#
            test_cost = jnp.nanmean(optax.softmax_cross_entropy_with_integer_labels(test_
#
            test_cost_batches.append(test_cost)
#
            test_acc_batches.append(test_acc)
            if len(testloader)<= 5 or (batch+1)%5==0:</pre>
#
              print(f"Testing at Epoch {step+1}/{n_epochs}, Batch {batch+1}, Cost {test_c
#
#
          test_acc_epochs.append(np.mean(test_acc_batches))
#
          test_cost = np.mean(test_cost_batches)
          test_cost_epochs.append(test_cost)
#
#
          print("....")
          print(f"Epoch {step+1}/{n_epochs}, Train: Cost {np.mean(train_cost_batches)}, A
#
          print(f"Epoch {step+1}/{n_epochs}, Test: Cost {test_cost}, Acc {test_acc}. Time
#
#
          print("=-="*10)
#
    return dict(
#
          n_train=[train_size] * n_epochs,
#
          step=np.arange(1, n_epochs + 1, dtype=int).tolist(),
          train_cost=[c.astype(float) for c in train_cost_epochs],
#
#
          train_acc=[c.astype(float) for c in train_acc_epochs],
#
          test_cost=[c.astype(float) for c in test_cost_epochs],
          test_acc=[c.astype(float) for c in test_acc_epochs],
#
#
      )
import numpy as np
import pandas as pd
import time
import torch
import optax
import jax.numpy as jnp
```

```
def train_vqc(batchsize: int, n_epochs: int, seed: int = 1701):
    start = time.time()
    np.random.seed(seed)
   # Load data once
    full_dataset = CTImgHerm()
   train size = int(0.75 * len(full dataset))
    val_size = int(0.05 * len(full_dataset))
   test_size = len(full_dataset) - train_size - val_size
   # Split dataset into train, validation, and test sets (fixed split for both initializ
   train_dataset, val_test_dataset = torch.utils.data.random_split(
        full_dataset, [train_size, val_size + test_size]
    )
   val_dataset, test_dataset = torch.utils.data.random_split(
        val_test_dataset, [val_size, test_size]
    )
   # Create data loaders
    trainloader = torch.utils.data.DataLoader(
        train_dataset, batch_size=batchsize, shuffle=True
    valloader = torch.utils.data.DataLoader(
        val_dataset, batch_size=batchsize, shuffle=True
    testloader = torch.utils.data.DataLoader(
        test_dataset, batch_size=batchsize, shuffle=False
    )
   # Exponential decay of the learning rate
    scheduler = optax.exponential_decay(
        init value=0.01,
        transition_steps=n_epochs,
        decay_rate=0.99
    )
    gradient_transform = optax.chain(
        optax.clip(1.0),
        optax.scale_by_adam(),
        optax.scale_by_schedule(scheduler),
        optax.scale(-1.0)
    )
    def run_training(init_weights_func, file_name):
        """Run the training loop for a given initialization function."""
        weights, weights_last = init_weights_func()
        opt_state = gradient_transform.init((weights, weights_last))
        train_cost_epochs, val_cost_epochs = [], []
        train_acc_epochs, val_acc_epochs = [], []
        # Training and validation loop
```

```
for step in range(n_epochs):
    train_cost_batches, train_acc_batches = [], []
    val_cost_batches, val_acc_batches = [], []
    print(f"Epoch {step+1}/{n_epochs} - Training...")
    # Training loop
    for x_train, y_train in trainloader:
        x_train, y_train = jnp.asarray(x_train.numpy()), jnp.asarray(y_train.nump
        train_cost, grad_circuit = value_and_grad(weights, weights_last, x_train,
        updates, opt_state = gradient_transform.update(grad_circuit, opt_state)
        weights, weights_last = optax.apply_updates((weights, weights_last), upda
        train_acc = compute_accuracy(weights, weights_last, x_train, y_train)
        print(f"Training at Epoch {step+1}/{n_epochs}, Cost {train_cost}, Acc {tr
        train_cost_batches.append(train_cost)
        train_acc_batches.append(train_acc)
    train_cost_epochs.append(np.mean(train_cost_batches))
    train_acc_epochs.append(np.mean(train_acc_batches))
    # Validation loop
    for x_val, y_val in valloader:
        x_val, y_val = jnp.asarray(x_val.numpy()), jnp.asarray(y_val.numpy())
        val_out = compute_out(weights, weights_last, x_val, y_val)
        val_pred = jnp.argmax(val_out, axis=1)
        val_acc = jnp.sum(val_pred == y_val) / len(val_out)
        val_cost = jnp.nanmean(optax.softmax_cross_entropy_with_integer_labels(va
        val_cost_batches.append(val_cost)
        val_acc_batches.append(val_acc)
    val_cost_epochs.append(np.mean(val_cost_batches))
    val_acc_epochs.append(np.mean(val_acc_batches))
# Testing loop
test_cost_batches, test_acc_batches = [], []
for x_test, y_test in testloader:
    x_test, y_test = jnp.asarray(x_test.numpy()), jnp.asarray(y_test.numpy())
    test_out = compute_out(weights, weights_last, x_test, y_test)
    test_pred = jnp.argmax(test_out, axis=1)
    test_acc = jnp.sum(test_pred == y_test) / len(test_out)
    test_cost = jnp.nanmean(optax.softmax_cross_entropy_with_integer_labels(test_
    print('TEST ACC:', test_acc,'TEST COST:', test_cost)
    test_cost_batches.append(test_cost)
    test_acc_batches.append(test_acc)
final_test_cost = np.mean(test_cost_batches)
final_test_acc = np.mean(test_acc_batches)
```

```
# Save weights to CSV
        save_weights_to_csv(weights, weights_last,n_epochs, file_name=file_name)
        return dict(
            n_train=[train_size] * n_epochs,
            n_val=[val_size] * n_epochs,
            n_test=[test_size] * n_epochs,
            step=np.arange(1, n_epochs + 1, dtype=int).tolist(),
            train_cost=[c.astype(float) for c in train_cost_epochs],
            train_acc=[c.astype(float) for c in train_acc_epochs],
            val_cost=[c.astype(float) for c in val_cost_epochs],
            val_acc=[c.astype(float) for c in val_acc_epochs],
            test_cost=final_test_cost.astype(float),
            test acc=final test acc.astype(float)
        )
    # Run Loop 1: Random Initialization
    results_random = run_training(init_weights_random, file_name='random_weights.csv')
    # Run Loop 2: Beta Initialization
    results_beta = run_training(init_weights_beta, file_name='beta_weights.csv')
    # Return results for both initializations along with the testloader
    return results_random, results_beta, testloader
\# n_epochs = 500
\# n_{reps} = 20
# batch size = 5000
# train_sizes = [int(0.8 * len(CTImgHerm()))]
# def run_iterations():
      results df = pd.DataFrame(
#
          columns=["train_acc", "train_cost", "test_acc", "test_cost", "step", "n_train"]
#
      )
      for _ in range(n_reps):
#
          results = train_vqc(n_epochs=n_epochs, batchsize=batch_size)
          results_df = pd.concat(
              [results_df, pd.DataFrame.from_dict(results)], axis=0, ignore_index=True
#
          )
      return results df
# results df = run iterations()
n = 500
n rens = 20
```

```
11_1 CP3 - 20
batch_size = 5000
# train_sizes = [int(0.8 * len(CTImgHerm()))] # 80% train size
def run iterations():
   results_random_df = pd.DataFrame(
       columns=["train_acc", "train_cost", "val_acc", "val_cost",
                "test_acc", "test_cost", "step", "n_train"]
   )
   results_beta_df = pd.DataFrame(
       columns=["train_acc", "train_cost", "val_acc", "val_cost",
                "test_acc", "test_cost", "step", "n_train"]
   )
   for _ in range(n_reps):
       # Train the model and get results
       # results = train_vqc_r(n_epochs=n_epochs, batchsize=batch_size)
       results_random, results_beta, testloader = train_vqc(batchsize=batch_size, n_epoc
       # Convert results to DataFrame and append to the results DataFrame
       results random df = pd.concat(
           [results_random_df, pd.DataFrame.from_dict(results_random)],
           axis=0, ignore index=True
       )
       results beta df = pd.concat(
           [results_beta_df, pd.DataFrame.from_dict(results_beta)],
           axis=0, ignore index=True
       )
   return results random df, results beta df, testloader
# Run the iterations and store the results
results_random_df,results_beta_df,testloader = run_iterations()
    Random Init
    Epoch 1/500 - Training...
    /usr/local/lib/python3.10/dist-packages/jax/_src/lax/lax.py:3373: ComplexWarning: Cas
      x_bar = _convert_element_type(x_bar, x.aval.dtype, x.aval.weak_type)
    Training at Epoch 1/500, Cost 0.683920462217599, Acc 0.6
    Epoch 2/500 - Training...
    Training at Epoch 2/500, Cost 0.6786253168212966, Acc 0.5866666666666667
    Epoch 3/500 - Training...
    Epoch 4/500 - Training...
    Epoch 5/500 - Training...
    Training at Epoch 5/500, Cost 0.6693050508313451, Acc 0.65333333333333333
    Epoch 6/500 - Training...
    Training at Epoch 6/500, Cost 0.6673731910754609, Acc 0.6533333333333333
    Enach 7/500 - Insining
```

```
באמכ / וויaדוודווצייי - באמכ / באחרוו
    Epoch 8/500 - Training...
    Training at Epoch 8/500, Cost 0.6634034329329047, Acc 0.64
    Epoch 9/500 - Training...
    Training at Epoch 9/500, Cost 0.6614985112357895, Acc 0.69333333333333334
    Epoch 10/500 - Training...
    Training at Epoch 10/500, Cost 0.6599028823394565, Acc 0.706666666666666667
    Epoch 11/500 - Training...
    Training at Epoch 11/500, Cost 0.6587146879823255, Acc 0.70666666666666667
    Epoch 12/500 - Training...
    Training at Epoch 12/500, Cost 0.6578767070025507, Acc 0.74666666666666667
    Epoch 13/500 - Training...
    Training at Epoch 13/500, Cost 0.6572242904610075, Acc 0.74666666666666667
    Epoch 14/500 - Training...
    Epoch 15/500 - Training...
    Training at Epoch 15/500, Cost 0.6558476461873717, Acc 0.746666666666666667
    Epoch 16/500 - Training...
    Training at Epoch 16/500, Cost 0.6549970181361655, Acc 0.746666666666666667
    Epoch 17/500 - Training...
    Training at Epoch 17/500, Cost 0.6540767420968209, Acc 0.73333333333333333
    Epoch 18/500 - Training...
    Training at Epoch 18/500, Cost 0.653148383947802, Acc 0.73333333333333333
    Epoch 19/500 - Training...
    Training at Epoch 19/500, Cost 0.6522468461643489, Acc 0.72
    Epoch 20/500 - Training...
    Training at Epoch 20/500, Cost 0.6513625026089405, Acc 0.70666666666666667
    Epoch 21/500 - Training...
    Training at Epoch 21/500, Cost 0.6504531313444936, Acc 0.69333333333333334
    Epoch 22/500 - Training...
    Training at Epoch 22/500, Cost 0.6494772214136342, Acc 0.6933333333333333
    Epoch 23/500 - Training...
    Training at Epoch 23/500, Cost 0.64842340431054, Acc 0.7066666666666666667
    Epoch 24/500 - Training...
    Training at Epoch 24/500, Cost 0.6473160568682821, Acc 0.6933333333333334
    Epoch 25/500 - Training...
    Training at Epoch 25/500, Cost 0.6461974473038606, Acc 0.69333333333333334
    Epoch 26/500 - Training...
    Training at Epoch 26/500, Cost 0.6451008040543521, Acc 0.7066666666666666667
    Epoch 27/500 - Training...
    Training at Epoch 27/500, Cost 0.6440309005119483, Acc 0.72
    Epoch 28/500 - Training...
print('last epoch results')
print("RANDOM")
print(results_random_df.iloc[-1])
print("BETA")
print(results beta df.iloc[-1])
    last epoch results
    RANDOM
    train acc
                0.826667
    train_cost 0.55343
    val_acc
                       0.8
```

```
val_cost
               0.65327
    test_acc 0.65
test_cost 0.613101
                      500
    step
    n_train
                       75
    n_val
                      5.0
                     20.0
    n test
    Name: 9999, dtype: object
    BETA
    val_acc
                      0.4
    500
    step
                       75
    n_train
                      5.0
    n_val
    n_test
                     20.0
    Name: 9999, dtype: object
from google.colab import files
results_beta_df.to_csv('CT-beta-df.csv',index=False)
results_random_df.to_csv('CT-random-df.csv',index=False)
files.download('CT-beta-df.csv')
files.download('CT-random-df.csv')
import pandas as pd
def load_weights_and_biases_from_csv(file_name):
   # Load the weights DataFrame
   weights_data = pd.read_csv(file_name)
   # Get the last epoch's weights and biases
   last_epoch = weights_data.iloc[-1] # Get the last row
   weights = np.array(eval(last_epoch['weights'])) # Convert string representation back
   biases = np.array(eval(last_epoch['biases'])) # Convert string representation back t
   return weights, biases
import pandas as pd
import ast
import jax.numpy as jnp
import torch
import optax
```

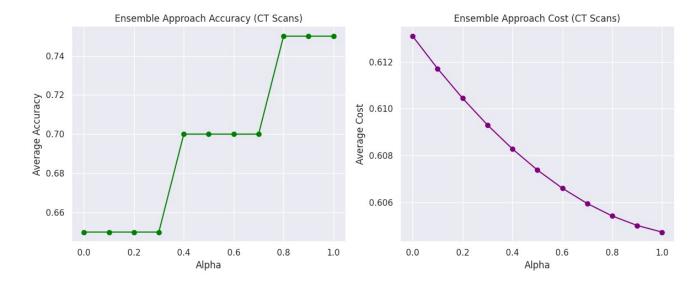
```
def ensemble_test_model(testloader, weights1, weights_last1, weights2, weights_last2, alp
    """Test the ensemble model using weights from two models and a given alpha."""
    total_cost = 0
    correct_predictions = 0
    total samples = 0
    for x_{\text{test}}, y_{\text{test}} in testloader:
        x_test, y_test = jnp.asarray(x_test.numpy()), jnp.asarray(y_test.numpy())
        test_out1 = compute_out(weights1, weights_last1, x_test, y_test)
        test_out2 = compute_out(weights2, weights_last2, x_test, y_test)
        # Weighted ensemble output
        ensemble_out = alpha * test_out1 + (1 - alpha) * test_out2
        ensemble_pred = jnp.argmax(ensemble_out, axis=1)
        correct_predictions += jnp.sum(jnp.array(ensemble_pred == y_test).astype(int))
        total_samples += len(y_test)
        test_cost = jnp.nanmean(optax.softmax_cross_entropy_with_integer_labels(ensemble_
        total_cost += test_cost * len(y_test)
    avg_test_cost = total_cost / total_samples
    avg_test_acc = correct_predictions / total_samples
    return avg_test_cost, avg_test_acc
# Load weights for both models
weights1, weights_last1 = load_weights_and_biases_from_csv('beta_weights.csv')
weights2, weights_last2 = load_weights_and_biases_from_csv('random_weights.csv')
for x_test, y_test in testloader:
  x_test, y_test = jnp.asarray(x_test.numpy()), jnp.asarray(y_test.numpy())
  myout2 = compute_out(weights2, weights_last2, x_test, y_test)
  my2pred = jnp.argmax(myout2, axis=1)
  myacc = jnp.sum(my2pred == y_test) / len(myout2)
# Alpha values from 0.0 to 1.0 in steps of 0.1
alpha_values = [i / 10 for i in range(11)]
# Store results for each alpha
results = []
# Perform ensemble testing for each alpha (one run per alpha)
for alpha in alpha_values:
    print(f"Testing with alpha={alpha}")
    # Run the ensemble test model with the current alnha
```

```
# NOTE CITE CITECHIOTIC CCEC HOUCE WITH CHE COLLICITE OIPHO
    avg_cost, avg_acc = ensemble_test_model(testloader, weights1, weights_last1, weights2
    # Store the result for each alpha
    results.append([alpha, avg_cost, avg_acc])
# Create a DataFrame to display results in table format
results_df = pd.DataFrame(results, columns=['Alpha', 'Average Cost', 'Average Accuracy'])
# Display the final table of results
print("\nEnsemble Test Results by Alpha:")
print(results_df)
# Save the results to a CSV file
results_df.to_csv('ensemble_test_results_by_alpha.csv', index=False)
     Testing with alpha=0.0
     Testing with alpha=0.1
     Testing with alpha=0.2
     Testing with alpha=0.3
     Testing with alpha=0.4
     Testing with alpha=0.5
     Testing with alpha=0.6
     Testing with alpha=0.7
     Testing with alpha=0.8
     Testing with alpha=0.9
     Testing with alpha=1.0
     Ensemble Test Results by Alpha:
                     Average Cost Average Accuracy
     0
           0.0 0.6131014909065542
                                               0.65
     1
           0.1 0.6117167292880316
                                               0.65
           0.2 0.6104518410481592
                                               0.65
     3
           0.3 0.6093076126287471
                                               0.65
           0.4 0.6082847787208743
                                                0.7
     4
           0.5 0.6073840203418356
     5
                                                0.7
           0.6 0.606605963017278
                                                0.7
     6
           0.7 0.6059511750792497
     7
                                                0.7
           0.8 0.6054201660904043
                                               0.75
     8
           0.9 0.6050133854040143
                                               0.75
     9
           1.0 0.6047312208687539
                                               0.75
     10
import matplotlib.pyplot as plt
# Data from the new table
alpha_ct = results_df['Alpha']
accuracy_ct = results_df['Average Accuracy']
cost ct = results df['Average Cost']
# Plot Accuracy vs Alpha
plt.figure(figsize=(12, 5))
plt.subplot(1, 2, 1)
nlt.nlot(alnha ct. accuracy ct. marker='o'. linestyle='-'. color='green')
```

```
plt.title('Ensemble Approach Accuracy (CT Scans)')
plt.xlabel('Alpha')
plt.ylabel('Average Accuracy')
plt.grid(True)

# Plot Cost vs Alpha
plt.subplot(1, 2, 2)
plt.plot(alpha_ct, cost_ct, marker='o', linestyle='-', color='purple')
plt.title('Ensemble Approach Cost (CT Scans)')
plt.xlabel('Alpha')
plt.ylabel('Average Cost')
plt.grid(True)

# Show the plots
plt.tight_layout()
plt.show()
```



```
import matplotlib.pyplot as plt
import seaborn as sns

# Aggregate data for plotting (mean and std per epoch)
df_random_agg = results_random_df.groupby(["step"]).agg(["mean", "std"]).reset_index()
df_beta_agg = results_beta_df.groupby(["step"]).agg(["mean", "std"]).reset_index()
```

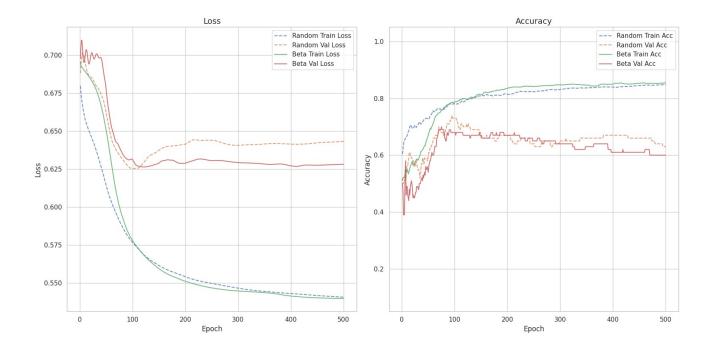
22 of 25 11/21/2024, 7:10 PM

```
sns.set_style("whitegrid")
colors = sns.color_palette()
fig, axes = plt.subplots(nrows=1, ncols=2, figsize=(16, 8)) # 1 row, 2 columns for 2 graph
axes = axes.flatten() # Flatten for easy indexing
# Titles and axis labels
titles = ["Loss", "Accuracy"]
ylabels = ["Loss", "Accuracy"]
# Plot metrics
for i, (df, label) in enumerate([
    (df_random_agg, "Random"),
    (df_beta_agg, "Beta"),
1):
    # Loss: Train and Validation
   train_loss = df.train_cost["mean"]
   val_loss = df.val_cost["mean"]
   # Accuracy: Train and Validation
   train_acc = df.train_acc["mean"]
   val_acc = df.val_acc["mean"]
   # Loss plot
    axes[0].plot(
        df.step, train_loss,
        label=f"{label} Train Loss",
        linestyle="--" if label == "Random" else "-",
        color=colors[2 * i], # Unique color
        alpha=0.8
    )
    axes[0].plot(
        df.step, val_loss,
        label=f"{label} Val Loss",
        linestyle="--" if label == "Random" else "-",
        color=colors[2 * i + 1], # Unique color
        alpha=0.8
    )
   # Accuracy plot
    axes[1].plot(
        df.step, train_acc,
        label=f"{label} Train Acc",
        linestyle="--" if label == "Random" else "-",
        color=colors[2 * i], # Unique color
        alpha=0.8
    )
    axes[1].plot(
        df.step, val_acc,
        label=f"{label} Val Acc",
        linestyle="--" if label == "Random" else "-",
        color=colors[2 * i + 1], # Unique color
```

```
alpha=0.8
)

# Format each subplot
for idx, ax in enumerate(axes):
    ax.set_title(titles[idx], fontsize=14)
    ax.set_xlabel("Epoch")
    ax.set_ylabel(ylabels[idx])
    if idx == 1: # Accuracy plot
        ax.set_ylim(0.05, 1.05) # Accuracy typically ranges between 0 and 1
    ax.legend()

plt.tight_layout()
plt.show()
```



24 of 25 11/21/2024, 7:10 PM