

$$y = \frac{1}{\sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma}$$

$$\begin{aligned}\mu &= \text{Mean} \\ \sigma &= \text{Standard Deviation} \\ \pi &\approx 3.14159 \\ e &\approx 2.71828\end{aligned}$$

Gaussian (G)

$$\text{Lorentzian (L)} \quad f(x; x_0, \gamma) = \frac{1}{\pi \gamma \left[1 + \left(\frac{x - x_0}{\gamma} \right)^2 \right]} = \frac{1}{\pi} \left[\frac{\gamma}{(x - x_0)^2 + \gamma^2} \right]$$

γ is the scale parameter which specifies the half-width at half-maximum (HWHM), alternatively 2γ is full width at half

Intermediate
Lorentzian (IL)

Modified
Lorentzian (ML)

Pearson VII (PVII)

Voigt (V)

pseudo-Voigt

$$I_{i,k} = \frac{2 \sqrt{\ln(2)}}{H_k} \exp \left[\frac{-4 \ln(2)}{H_k^2} (2\theta_i - 2\theta_k)^2 \right]$$

$$I_{i,k} = \frac{\sqrt{4}}{\pi H_k} \left[1 + \frac{4(\sqrt{2}-1)}{H_k^2} (2\theta_i - 2\theta_k)^2 \right]^{-1}$$

$$I_{i,k} = \frac{\sqrt{4(2^{3/2}-1)}}{2 \pi H_k} \left[1 + \frac{4(2^{2/3}-1)}{H_k^2} (2\theta_i - 2\theta_k)^2 \right]^{-1.5}$$

$$I_{i,k} = \frac{2 \sqrt{4(\sqrt{2}-1)}}{\pi H_k} \left[1 + \frac{4(\sqrt{2}-1)}{H_k^2} (2\theta_i - 2\theta_k)^2 \right]^{-2}$$

$$I_{i,k} = \frac{2 \sqrt{m} \Gamma(2^{1/m}-1)}{\pi \Gamma(m-0.5) H_k} \left[1 + \frac{4(2^{1/m}-1)}{H_k^2} (2\theta_i - 2\theta_k)^2 \right]^{-m}$$

$$I_{i,k} = \beta_g^{-1} \operatorname{Re} \left\{ \Omega \left[\frac{\sqrt{\pi}}{\beta} |2\theta_i - 2\theta_k| + i \frac{\beta_c^2}{\beta_g^2 \pi} \right] \right\}$$

$$I_{i,k} = \eta L_{i,k} + (1-\eta) G_{i,k}$$

Key: $I_{i,k}$, intensity at i^{th} point in pattern due to k^{th} line; $2\theta_k$, Bragg angle; H_k , full-width at half-maximum intensity; β_c & β_g , integral-breadths of Lorentzian and Gaussian components, respectively; η , mixing parameter; Ω , complex error function; Re, real part of function.