

RegresionNoLineal

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Cars

```
summary(cars)
```

```
##      speed      dist
##  Min.   : 4.0    Min.   :  2.00
##  1st Qu.:12.0    1st Qu.: 26.00
##  Median :15.0    Median : 36.00
##  Mean   :15.4    Mean   : 42.98
##  3rd Qu.:19.0    3rd Qu.: 56.00
##  Max.   :25.0    Max.   :120.00
```

```
data = cars
```

Parte 1: Análisis de normalidad

```
library(nortest)
```

```
ad.test(cars$speed)
```

```
##
##  Anderson-Darling normality test
##
## data:  cars$speed
## A = 0.26143, p-value = 0.6927
```

```
ad.test(cars$dist)
```

```
##
##  Anderson-Darling normality test
##
## data:  cars$dist
## A = 0.74067, p-value = 0.05021
```

```
library(e1071)
```

```
par(mfrow=c(1,2))
```

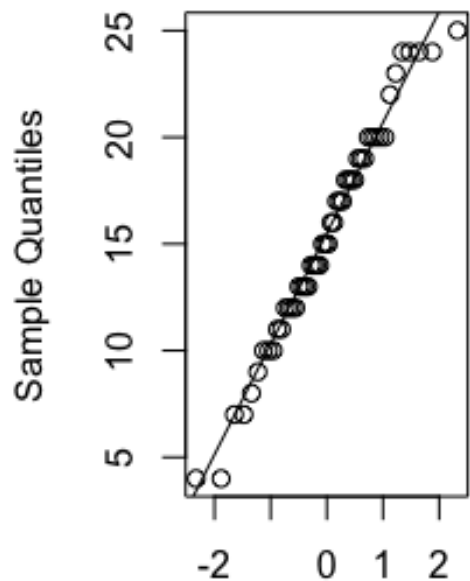
```
qqnorm(cars$speed, main = "QQ Plot - Speed")
```

```
qqline(cars$speed)
```

```
qqnorm(cars$dist, main = "QQ Plot - Distance")
```

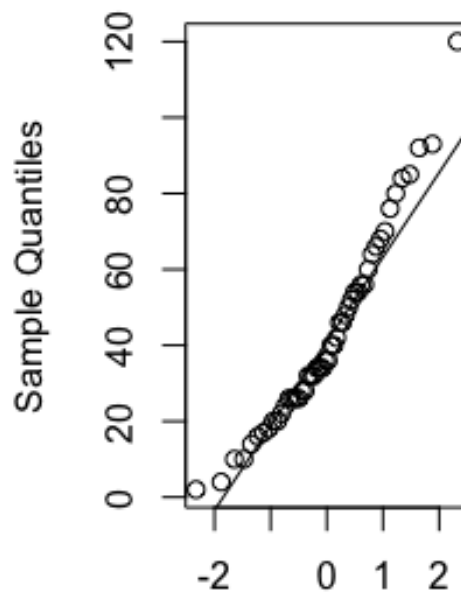
```
qqline(cars$dist)
```

QQ Plot - Speed



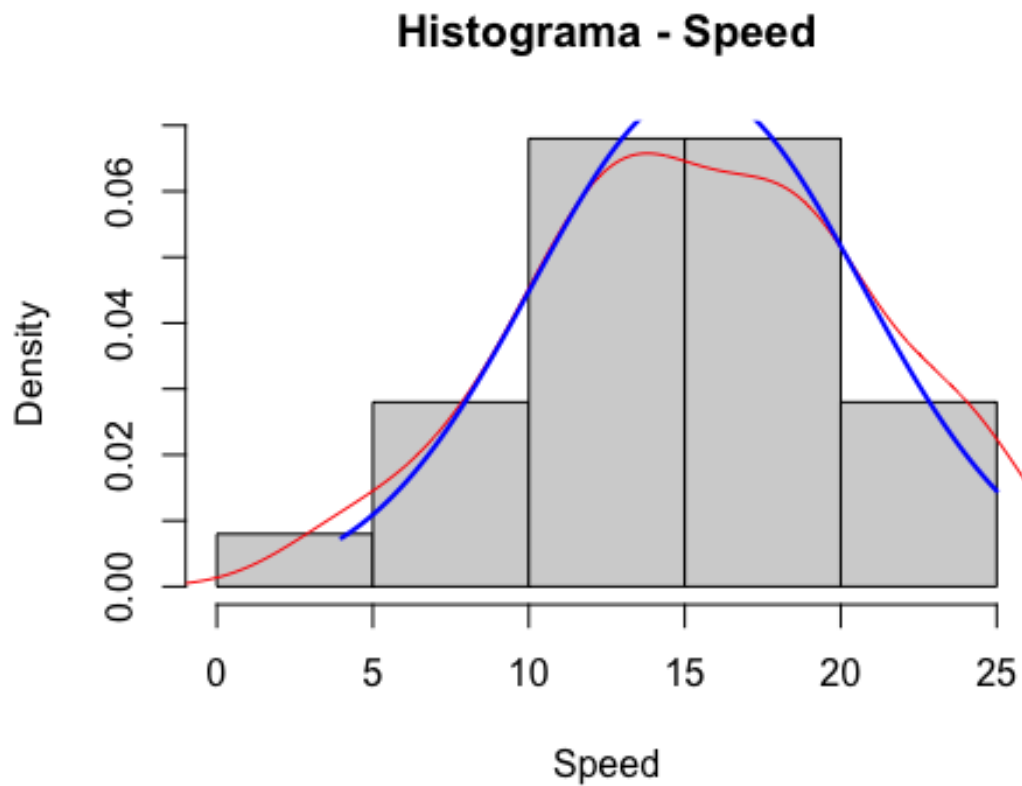
Theoretical Quantiles

QQ Plot - Distance



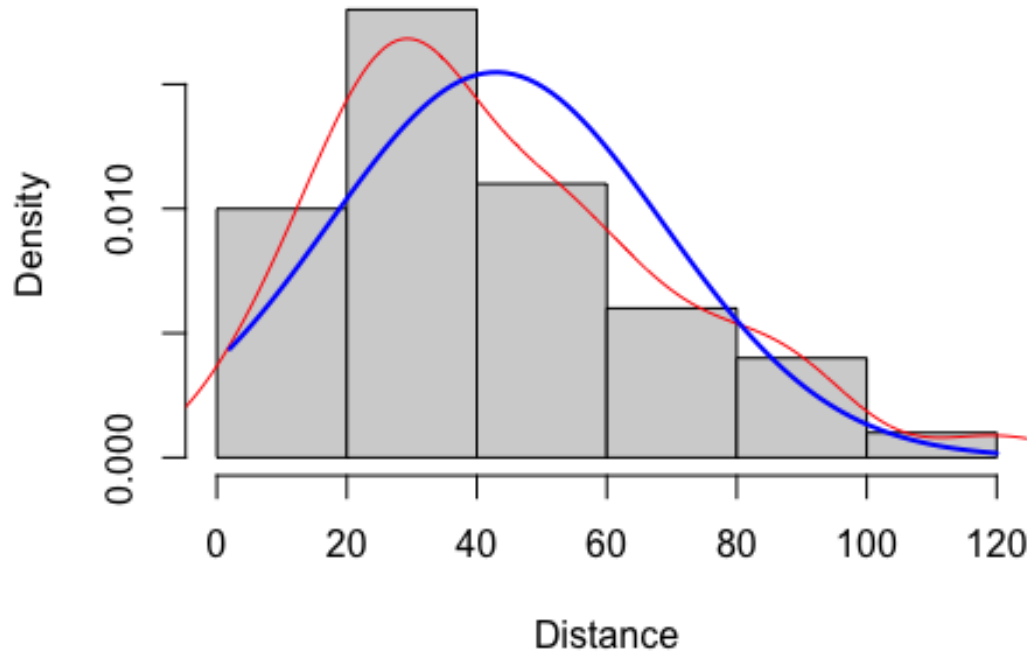
Theoretical Quantiles

```
hist(cars$speed, freq = FALSE, main = "Histograma - Speed", xlab = "Speed")
lines(density(cars$speed), col = "red") # Densidad observada
curve(dnorm(x, mean=mean(cars$speed), sd=sd(cars$speed)),
      from=min(cars$speed), to=max(cars$speed), add=TRUE, col="blue", lwd=2)
```



```
hist(cars$dist, freq = FALSE, main = "Histograma - Distance", xlab =  
"Distance")  
lines(density(cars$dist), col = "red") # Densidad observada  
curve(dnorm(x, mean=mean(cars$dist), sd=sd(cars$dist)),  
      from=min(cars$dist), to=max(cars$dist), add=TRUE, col="blue", lwd=2)
```

Histograma - Distance



```
speedske <- skewness(cars$speed)
speedske

## [1] -0.1105533

speedkur <- kurtosis(cars$speed)
speedkur

## [1] -0.6730924

distske <- skewness(cars$dist)
distske

## [1] 0.7591268

distkur <- kurtosis(cars$dist)
distkur

## [1] 0.1193971
```

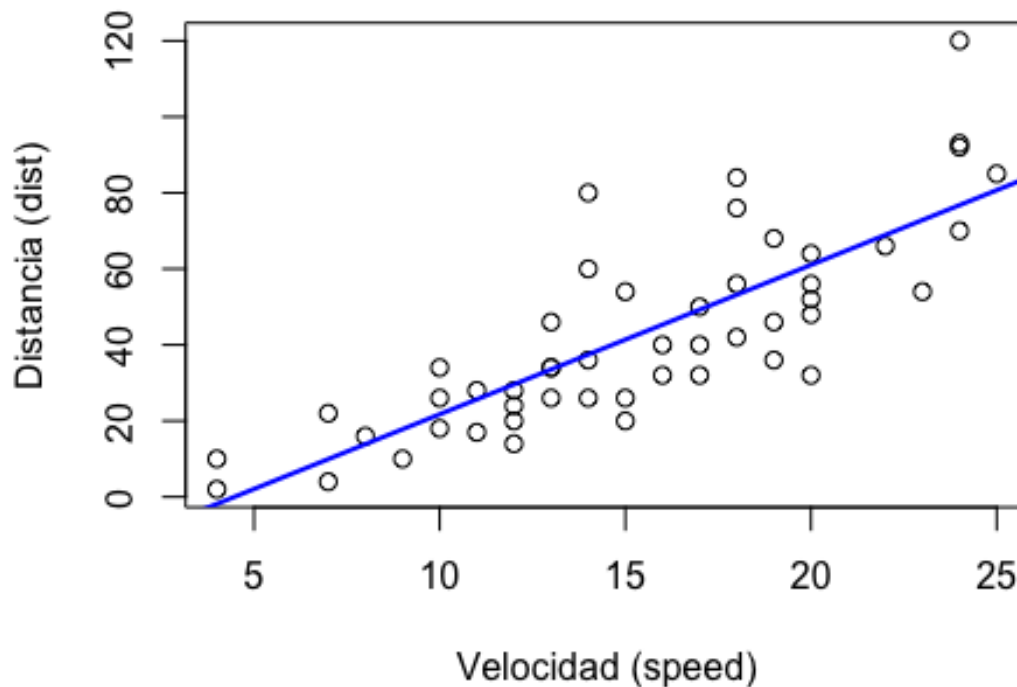
Parte 2: Regresión lineal

```
modelo1 = lm(dist ~ speed, data = cars)
summary(modelo1)
```

```
##
## Call:
## lm(formula = dist ~ speed, data = cars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -29.069  -9.525  -2.272   9.215  43.201
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -17.5791     6.7584  -2.601   0.0123 *
## speed        3.9324     0.4155   9.464 1.49e-12 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.38 on 48 degrees of freedom
## Multiple R-squared:  0.6511, Adjusted R-squared:  0.6438
## F-statistic: 89.57 on 1 and 48 DF,  p-value: 1.49e-12

plot(cars$speed, cars$dist, main="Distancia vs Velocidad", xlab="Velocidad
(speed)", ylab="Distancia (dist)")
abline(modelo1, col="blue", lwd=2)
```

Distancia vs Velocidad



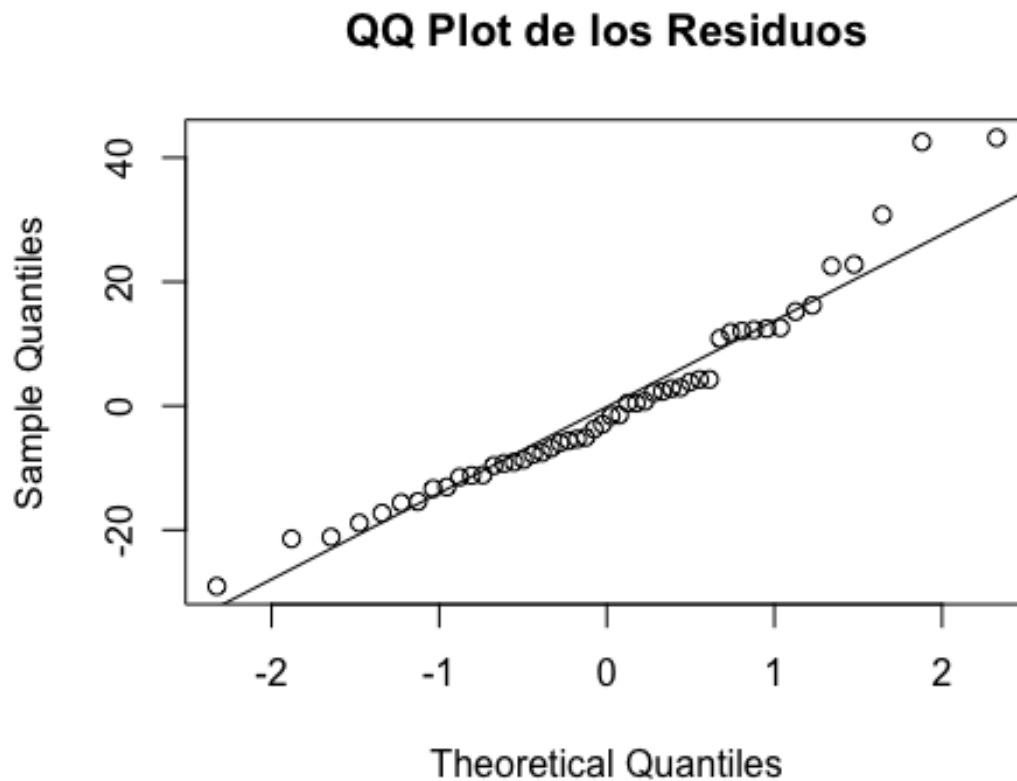
```

t.test(modelo1$residuals)

##
## One Sample t-test
##
## data: modelo1$residuals
## t = -2.0629e-16, df = 49, p-value = 1
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## -4.326 4.326
## sample estimates:
## mean of x
## -4.440892e-16

qqnorm(residuals(modelo1), main="QQ Plot de los Residuos")
qqline(residuals(modelo1))

```



```

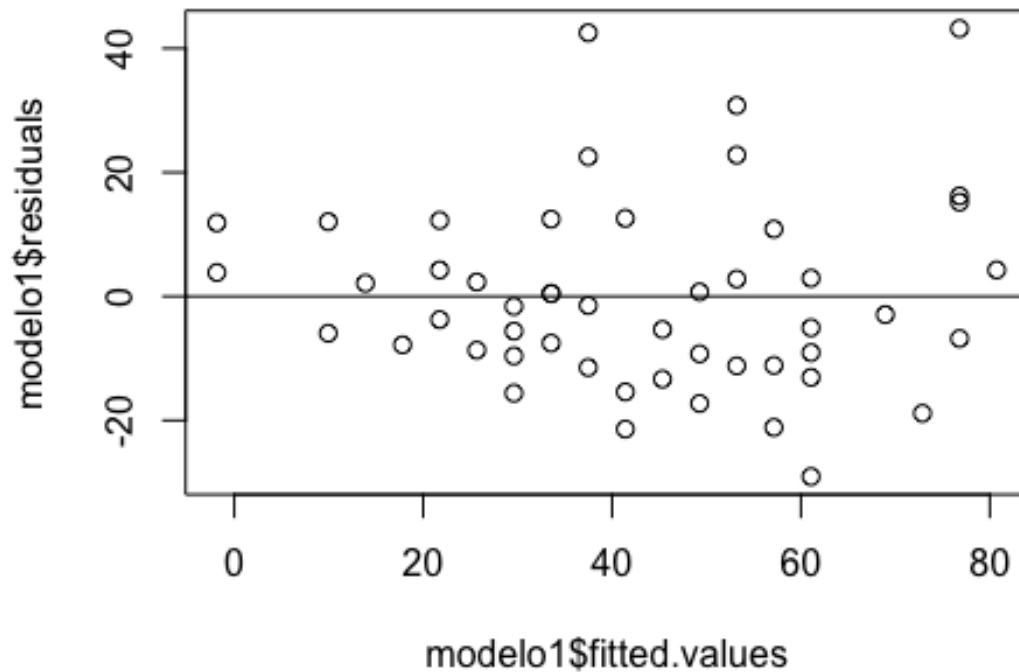
library(lmtest)

## Loading required package: zoo

##
## Attaching package: 'zoo'

```

```
## The following objects are masked from 'package:base':  
##  
##    as.Date, as.Date.numeric  
  
bptest(modelo1)  
  
##  
## studentized Breusch-Pagan test  
##  
## data:  modelo1  
## BP = 3.2149, df = 1, p-value = 0.07297  
  
gqtest(modelo1)  
  
##  
## Goldfeld-Quandt test  
##  
## data:  modelo1  
## GQ = 1.5512, df1 = 23, df2 = 23, p-value = 0.1498  
## alternative hypothesis: variance increases from segment 1 to 2  
  
plot(modelo1$fitted.values,modelo1$residuals)  
abline(h=0, color="blue")  
  
## Warning in int_abline(a = a, b = b, h = h, v = v, untf = untf, ...):  
## "color" is  
## not a graphical parameter
```



```
library(lmtest)
bptest(modelo1)

##
##  studentized Breusch-Pagan test
##
## data:  modelo1
## BP = 3.2149, df = 1, p-value = 0.07297

gqtest(modelo1)

##
##  Goldfeld-Quandt test
##
## data:  modelo1
## GQ = 1.5512, df1 = 23, df2 = 23, p-value = 0.1498
## alternative hypothesis: variance increases from segment 1 to 2

library(lmtest)
resettest(modelo1)

##
##  RESET test
##
```

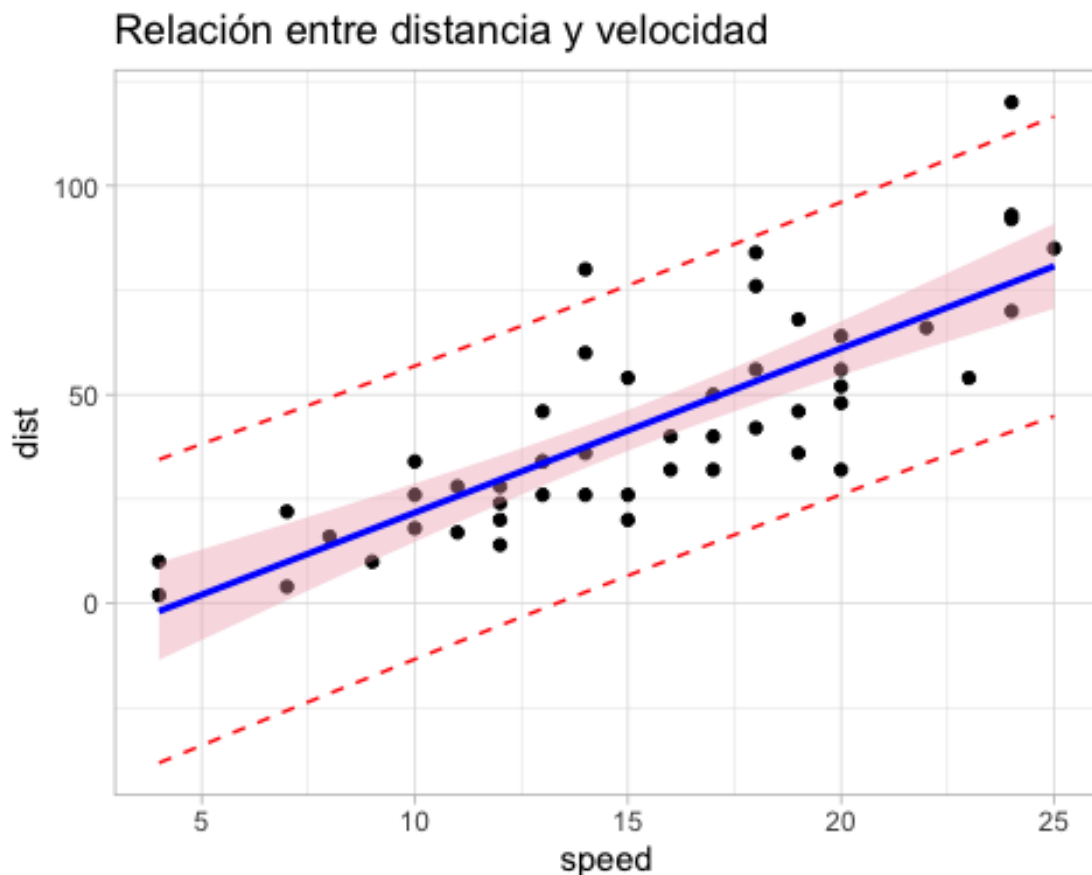


```
## data:  modelo1
## RESET = 1.5554, df1 = 2, df2 = 46, p-value = 0.222

modelo1 = lm(dist ~ speed, data = cars)
Ip = predict(object = modelo1, interval = "prediction", level = 0.97)

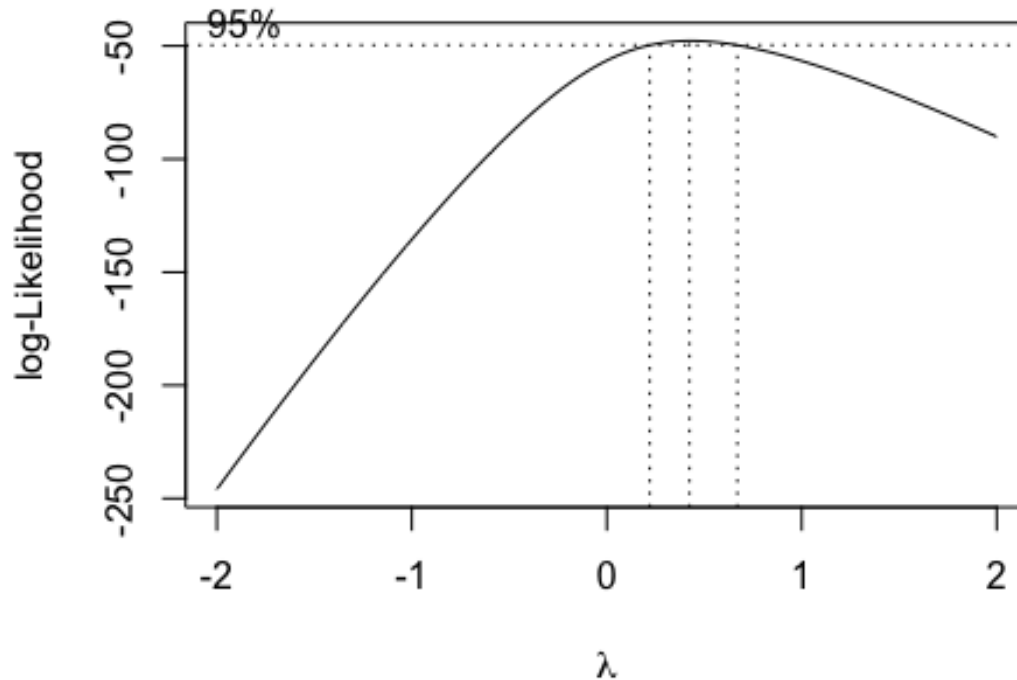
## Warning in predict.lm(object = modelo1, interval = "prediction", level =
0.97): predictions on current data refer to _future_ responses

datos1 = cbind(cars, Ip)
library(ggplot2)
ggplot(datos1, aes(x = speed, y = dist)) +
  geom_point() +
  geom_line(aes(y = fit), color = "blue") + # Línea de ajuste del modelo
  geom_line(aes(y = lwr), color = "red", linetype = "dashed") + # Línea
inferior del intervalo de predicción
  geom_line(aes(y = upr), color = "red", linetype = "dashed") + # Línea
superior del intervalo de predicción
  geom_smooth(method = "lm", formula = y ~ x, se = TRUE, level = 0.97, col =
"blue", fill = "pink2") +
  ggtitle("Relación entre distancia y velocidad") +
  theme_light()
```



Parte 3: Regresión no lineal

```
library(MASS)
modelo2 = lm(dist ~ speed, data = cars)
bc = boxcox(modelo2)
```



```
lambda_opt = bc$x[which.max(bc$y)]
lambda_opt

## [1] 0.4242424

if (lambda_opt == 0) {
  cars$dist_transformed <- log(cars$dist)
} else {
  cars$dist_transformed <- (cars$dist^lambda_opt - 1) / lambda_opt
}

dist2skew <- skewness(cars$dist_transformed)
dist2kurt <- kurtosis(cars$dist_transformed)
cat("Sesgo de la transformación:", dist2skew, "\n")

## Sesgo de la transformación: -0.1701619

cat("Curtosis de la transformación:", dist2kurt, "\n")
```

```
## Curtosis de la transformación: -0.186884

modelo_transformed <- lm(dist_transformed ~ speed, data = cars)
summary(modelo_transformed)

##
## Call:
## lm(formula = dist_transformed ~ speed, data = cars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.0926 -1.0444 -0.3055  0.7999  4.7520
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  1.08227    0.73856   1.465    0.149
## speed        0.49541    0.04541  10.910 1.35e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.681 on 48 degrees of freedom
## Multiple R-squared:  0.7126, Adjusted R-squared:  0.7066
## F-statistic: 119 on 1 and 48 DF, p-value: 1.354e-14

plot(cars$speed, cars$dist_transformed, main="Distancia Transformada vs
Velocidad", xlab="Velocidad (speed)", ylab="Distancia Transformada")
abline(modelo_transformed, col="blue", lwd=2)
```

Distancia Transformada vs Velocidad

