# Trax deep learning 6

# Machine learning in Python

#### Imagine some cars to drive 100x slower

To do machine learning, we would ideally want code to:

- Be as fast as possible, especially with matrix multiplications
- Handle the gradient for us, in order to learn weights with back propagation
- Have an ecosystem for machine learning

In terms of speed, Python seems to be a bad choice.



#### Possible solutions

- Use Python libraries that have their backend in C/C++ (e.g. PyTorch or TensorFlow)
- Learn a faster language, that also supports autograd
- Use Python libraries with a backend in JAX









## Jax is fast



```
import numpy as np
   def selu(x, alpha=1.67, lambda_=1.05):
     return lambda_ * np.where(x > 0, x, alpha * np.exp(x) - alpha)
   x = np.arange(1000000)
   %timeit selu(x)
 ✓ 5.7s
7.01 ms \pm 100 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
   import jax
   import jax.numpy as jnp
   def selu(x, alpha=1.67, lambda_=1.05):
     return lambda_ * jnp.where(x > 0, x, alpha * <math>jnp.exp(x) - alpha)
   x = jnp.arange(1000000)
   %timeit selu(x).block_until_ready()
 √ 1.8s
2.24 ms \pm 105 \mus per loop (mean \pm std. dev. of 7 runs, 100 loops each)
   selu_jit = jax.jit(selu)
   # Warm up
   selu_jit(x).block_until_ready()
   %timeit selu_jit(x).block_until_ready()
 √ 5.6s
689 \mus \pm 2.21 \mus per loop (mean \pm std. dev. of 7 runs, 1,000 loops each)
```

# Jax has an ecosystem



https://project-awesome.org/n2cholas/awesome-jax

#### Libraries

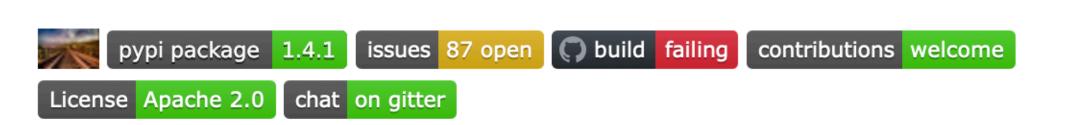
- Neural Network Libraries
  - Flax Centered on flexibility and clarity.
  - Haiku Focused on simplicity, created by the authors of Sonnet at De
  - Objax Has an object oriented design similar to PyTorch.
  - Elegy A High Level API for Deep Learning in JAX. Supports Flax, Hail
  - Trax "Batteries included" deep learning library focused on providing
  - Jraph Lightweight graph neural network library.
  - Neural Tangents High-level API for specifying neural networks of both
  - HuggingFace Ecosystem of pretrained Transformers for a wide range
  - Equinox Callable PyTrees and filtered JIT/grad transformations => ne
- NumPyro Probabilistic programming based on the Pyro library.
- Chex Utilities to write and test reliable JAX code.
- Optax Gradient processing and optimization library.
- RLax Library for implementing reinforcement learning agents.
- JAX, M.D. Accelerated, differential molecular dynamics.
- Coax Turn RL papers into code, the easy way.
- Distrax Reimplementation of TensorFlow Probability, containing probabili
- cvxpylayers Construct differentiable convex optimization layers.
- TensorLy Tensor learning made simple.
- NetKet Machine Learning toolbox for Quantum Physics.

#### Trax

#### TensorFlow 3.0

- In TensorFlow, there is a lot of baggage that it just has to carry because it's backward compatible.
- Trax is a Google project, intended to improve TensorFlow, breaking backward compatibility.
- The focus is clear code and speed; you can literally read Trax sourcecode and understand what's going on.

# Trax — Deep Learning with Clear Code and Speed



Trax is an end-to-end library for deep learning that focuses on clear code and speed. It is actively used and maintained in the Google Brain team. This

https://github.com/google/trax

### Downsides

- Trax is fairly recent. You will not find that much examples as for PyTorch / TensorFlow
- Even though there is an ecosystem, it is smaller than the PyTorch / TensorFlow ecosystems
- You will need to dive into the source code; a lot of documentation is to be found there.

## Trax is clean

#### Implementations of Adam

```
def update(self, step, grads, weights, slots, opt_params):
    m, v = slots
    learning_rate = opt_params['learning_rate']
    weight_decay_rate = opt_params['weight_decay_rate']
    b1 = opt_params['b1']
    b2 = opt_params['b2']
    eps = opt_params['eps']
    m = (1 - b1) * grads + b1 * m # First moment estimate.
    v = (1 - b2) * (grads ** 2) + b2 * v # Second moment estimate.
    mhat = m / (1 - b1 ** (step + 1)) # Bias correction.
    vhat = v / (1 - b2 ** (step + 1))
    new_weights = ((1 - weight_decay_rate) * weights - (
        learning_rate * mhat / (jnp.sqrt(vhat) + eps))).astype(weights.dtype)
    return new_weights, (m, v)
```

#### Trax

```
def _resource_apply_sparse(self, grad, var, indices, apply_state=None):
 var_device, var_dtype = var.device, var.dtype.base_dtype
 coefficients = ((apply_state or {}).get((var_device, var_dtype))
                  or self._fallback_apply_state(var_device, var_dtype))
 \# m_t = beta1 * m + (1 - beta1) * g_t
 m = self.get_slot(var, 'm')
 m_scaled_g_values = grad * coefficients['one_minus_beta_1_t']
  m_t = tf.compat.v1.assign(m, m * coefficients['beta_1_t'],
                         use_locking=self._use_locking)
  with tf.control dependencies([m t]):
   m_t = self._resource_scatter_add(m, indices, m_scaled_g_values)
 # v_t = beta2 * v + (1 - beta2) * (g_t * g_t)
 v = self.get_slot(var, 'v')
 v_scaled_g_values = (grad * grad) * coefficients['one_minus_beta_2_t']
  v_t = tf.compat.v1.assign(v, v * coefficients['beta_2_t'],
                         use_locking=self._use_locking)
  with tf.control_dependencies([v_t]):
   v_t = self._resource_scatter_add(v, indices, v_scaled_g_values)
  if not self.amsgrad:
   v_sqrt = tf.sqrt(v_t)
    var_update = tf.compat.v1.assign_sub(
       var, coefficients['lr'] * m_t / (v_sqrt + coefficients['epsilon']),
       use_locking=self._use_locking)
    return tf.group(*[var_update, m_t, v_t])
   v_hat = self.get_slot(var, 'vhat')
   v_{hat_t} = tf.maximum(v_{hat}, v_t)
    with tf.control_dependencies([v_hat_t]):
     v_hat_t = tf.compat.v1.assign(
          v_hat, v_hat_t, use_locking=self._use_locking)
    v_hat_sqrt = tf.sqrt(v_hat_t)
    var_update = tf.compat.v1.assign_sub(
       coefficients['lr'] * m_t / (v_hat_sqrt + coefficients['epsilon']),
        use_locking=self._use_locking)
    return tf.group(*[var_update, m_t, v_t, v_hat_t])
```

#### **Tensorflow**

```
def _single_tensor_adam(params: List[Tensor],
                        grads: List[Tensor],
                        exp_avgs: List[Tensor],
                        exp_avg_sqs: List[Tensor],
                        max_exp_avg_sqs: List[Tensor],
                        state_steps: List[Tensor],
                        amsgrad: bool,
                        beta1: float,
                        beta2: float,
                        lr: float,
                        weight_decay: float,
                        eps: float,
                        maximize: bool):
    for i, param in enumerate(params):
       grad = grads[i] if not maximize else -grads[i]
       exp_avg = exp_avgs[i]
       exp_avg_sq = exp_avg_sqs[i]
       step_t = state_steps[i]
       # update step
       step_t += 1
       step = step_t.item()
       bias_correction1 = 1 - beta1 ** step
       bias_correction2 = 1 - beta2 ** step
       if weight_decay != 0:
           grad = grad.add(param, alpha=weight_decay)
       # Decay the first and second moment running average coefficient
       exp_avg.mul_(beta1).add_(grad, alpha=1 - beta1)
       exp_avg_sq.mul_(beta2).addcmul_(grad, grad.conj(), value=1 - beta2)
           # Maintains the maximum of all 2nd moment running avg. till now
            torch.maximum(max_exp_avg_sqs[i], exp_avg_sq, out=max_exp_avg_sqs[i])
           # Use the max. for normalizing running avg. of gradient
            denom = (max_exp_avg_sqs[i].sqrt() / math.sqrt(bias_correction2)).add_(eps)
           denom = (exp_avg_sq.sqrt() / math.sqrt(bias_correction2)).add_(eps)
       step_size = lr / bias_correction1
       param.addcdiv_(exp_avg, denom, value=-step_size)
def _multi_tensor_adam(params: List[Tensor],
                       grads: List[Tensor],
                       exp_avgs: List[Tensor],
                      exp_avg_sqs: List[Tensor],
                       max_exp_avg_sqs: List[Tensor],
                       state_steps: List[Tensor],
                       amsgrad: bool,
                       beta1: float,
                       beta2: float,
                       lr: float,
                       weight_decay: float,
                       eps: float,
                       maximize: bool):
   if len(params) == 0:
       return
   # update steps
   torch._foreach_add_(state_steps, 1)
   if maximize:
       grads = torch._foreach_neg(tuple(grads)) # type: ignore[assignment]
   bias_correction1 = [1 - beta1 ** step.item() for step in state_steps]
bias_correction2 = [1 - beta2 ** step.item() for step in state_steps]
   if weight_decay != 0:
       torch._foreach_add_(grads, params, alpha=weight_decay)
   torch._foreach_mul_(exp_avgs, beta1)
   torch._foreach_add_(exp_avgs, grads, alpha=1 - beta1)
   torch._foreach_mul_(exp_avg_sqs, beta2)
   torch._foreach_addcmul_(exp_avg_sqs, grads, grads, 1 - beta2)
       # Maintains the maximum of all 2nd moment running avg. till now
       max_exp_avg_sqs = torch._foreach_maximum(max_exp_avg_sqs, exp_avg_sqs) # type:
       # Use the max. for normalizing running avg. of gradient
       max_exp_avg_sq_sqrt = torch._foreach_sqrt(max_exp_avg_sqs)
       bias_correction_sqrt = [math.sqrt(bc) for bc in bias_correction2]
       torch._foreach_div_(max_exp_avg_sq_sqrt, bias_correction_sqrt)
       denom = torch._foreach_add(max_exp_avg_sq_sqrt, eps)
       exp_avg_sq_sqrt = torch._foreach_sqrt(exp_avg_sqs)
       bias_correction_sqrt = [math.sqrt(bc) for bc in bias_correction2]
       torch._foreach_div_(exp_avg_sq_sqrt, bias_correction_sqrt)
       denom = torch._foreach_add(exp_avg_sq_sqrt, eps)
    step_size = [(lr / bc) * -1 for bc in bias_correction1]
    torch._foreach_addcdiv_(params, exp_avgs, denom, step_size)
```

#### PyTorch

### Trax is readable

#### Linear / Dense layer

Documentation

Warning/ Error

Linear with bias

Linear without bias

```
def forward(self, x):
  """Executes this layer as part of a forward pass through the model.
 Args:
   x: Tensor of same shape and dtype as the input signature used to
       initialize this layer.
 Returns:
   Tensor of same shape and dtype as the input, except the final dimension
   is the layer's `n_units` value.
 if self._use_bias:
   if not isinstance(self.weights, (tuple, list)):
     raise ValueError(f'Weights should be a (w, b) tuple or list; '
                      f'instead got: {self.weights}')
   w, b = self.weights
   return jnp.dot(x, w) + b # Affine map.
 else:
   w = self.weights
   return jnp.dot(x, w) # Linear map.
```

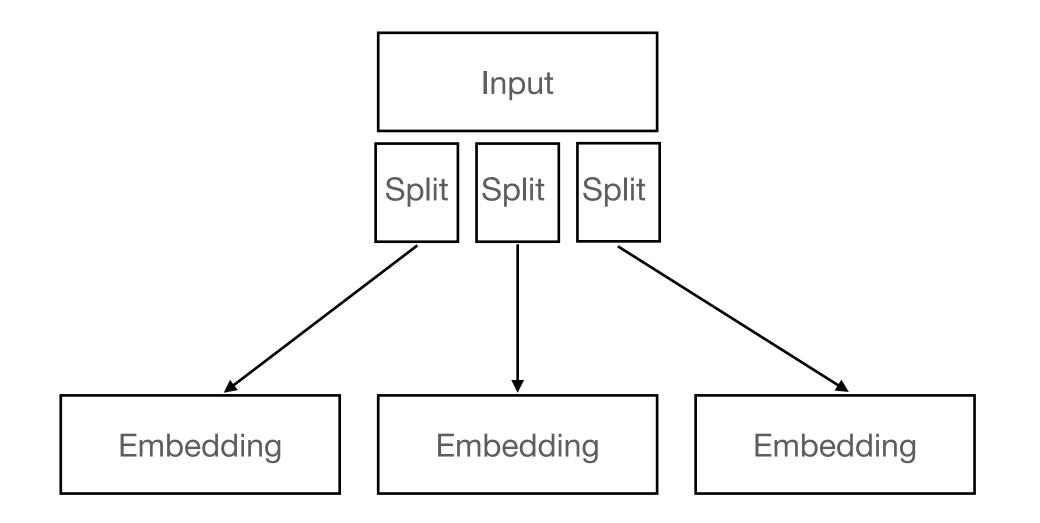
## Trax is readable

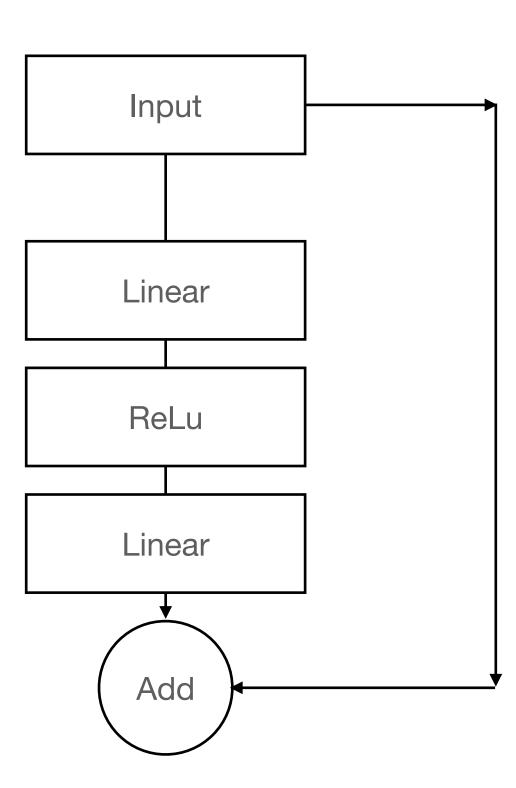
Algorithm 1: Adam, our proposed algorithm for stochastic optimization. See section 2 for details, and for a slightly more efficient (but less clear) order of computation.  $g_t^2$  indicates the elementwise square  $g_t \odot g_t$ . Good default settings for the tested machine learning problems are  $\alpha = 0.001$ ,  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$  and  $\epsilon = 10^{-8}$ . All operations on vectors are element-wise. With  $\beta_1^t$  and  $\beta_2^t$  we denote  $\beta_1$  and  $\beta_2$  to the power t.

```
Require: \alpha: Stepsize
Require: \beta_1, \beta_2 \in [0, 1): Exponential decay rates for the moment estimates
Require: f(\theta): Stochastic objective function with parameters \theta
Require: \theta_0: Initial parameter vector
  m_0 \leftarrow 0 (Initialize 1st moment vector)
  v_0 \leftarrow 0 (Initialize 2<sup>nd</sup> moment vector)
  t \leftarrow 0 (Initialize timestep)
   while \theta_t not converged do
      t \leftarrow t + 1
      g_t \leftarrow \nabla_{\theta} f_t(\theta_{t-1}) (Get gradients w.r.t. stochastic objective at timestep t)
      m_t \leftarrow \beta_1 \cdot m_{t-1} + (1 - \beta_1) \cdot g_t (Update biased first moment estimate)
      v_t \leftarrow \beta_2 \cdot v_{t-1} + (1 - \beta_2) \cdot g_t^2 (Update biased second raw moment estimate)
      \widehat{m}_t \leftarrow m_t/(1-\beta_1^t) (Compute bias-corrected first moment estimate)
      \widehat{v}_t \leftarrow v_t/(1-\beta_2^t) (Compute bias-corrected second raw moment estimate)
      \theta_t \leftarrow \theta_{t-1} - \alpha \cdot \widehat{m}_t / (\sqrt{\widehat{v}_t} + \epsilon) (Update parameters)
   return \theta_t (Resulting parameters)
```

# Parallel flows

- In modern architectures, we will often want to implement models with parallel functions
- This can be done with plain Python, but it adds to the complexity
- Trax has multiple "combinators" designed to handle parallel flows





#### Parallel flows

#### Multi-embedding

```
emblist = [tl.Embedding(car, d_feature) for car in cardinality]
multiembedding = tl.Parallel(*emblist)
```

Trax implementation with a Parallel layer

Part of the 163 line long implementation in the PyTorch-Forecasting library

```
def init_embeddings(self):
    self.embeddings = nn.ModuleDict()
    for name in self.embedding_sizes.keys():
        embedding_size = self.embedding_sizes[name][1]
        if self.max_embedding_size is not None:
            embedding_size = min(embedding_size, self.max_embedding_size)
        # convert to list to become mutable
        self.embedding_sizes[name] = list(self.embedding_sizes]
        self.embedding_sizes[name][1] = embedding_size
```