

CLÉMENT VIGUIER

MOUNTAIN GRASSLANDS
DYNAMICS: INTEGRATING
PHENOTYPIC PLASTICITY
IN A NEW AGENT-BASED
MODEL

ABSTRACT

Mountain grasslands provide numerous ecosystem services that need fine understanding and characterisation to be assessed and predicted. The vulnerability to climate change and the complexity of mechanisms driving alpine community dynamics require the development of new tools to predict the dynamics of these communities facing new conditions. Moreover, individual variation has large effects on community responses to external condition changes, as shown by multiple empirical studies but often overlooked in modelling approaches. In addition to these effects, intra-specific variability has contrasting potential impacts on coexistence mechanisms that need to be disentangled.

To answer both the need for a dynamic model of species rich communities and the integration of individual level , the model *Mount Grass* was developed. It is designed around two main components: (1) a closed strategy space allowing a efficient representation of high species diversity, and (2) a plastic allocation mechanism integrating trade-offs between active and structural tissues, as well as between shoot and root tissues. In a first result part, after a parameter filtering step, the combined effects of allocation rules, species strategy and phenotypic plasticity on individual plants are studied. In a second part, the effect of plasticity is then studied at the scale of the community.

This work demonstrates the importance of phenotypic plasticity both at the individual scale and its role for community dynamics. While further work is needed to fully capture plasticity mechanisms, the model provides sound starting point to further explore the role of intra-specific variability in coexistence mechanisms, the resistance and resilience to drought events, or the detection of regime shift in this type of systems.

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I

INTRODUCTION

1 CONTEXT

1.1 Global change: how to describe the future of alpine ecosystems

1.1.1 The value of ecosystems

1.1.2 Global change

1.1.3 The need for mechanistic models

1.2 Community dynamics: complexity emerging from parts and the role of phenotypic plasticity

1.2.1 The limit of classic patterns

1.2.2 The rise of individual-based approaches

1.2.3 When phenotypic plasticity makes things complicated

2 AIMS, OBJECTIVES AND OVERVIEW

2.1 Aims: understanding and prediction

Functioning Diversity of : drivers, mechanisms, species and strategies
Flexibility:
structure: genericity, experiments, plasticity

2.2 Objectives: a new agent-based model for plant community dynamics

2.2.1 Generic framework for multi-species and plastic plant modelling

2.2.2 Effect of phenotypic plasticity on plant growth and community dynamics

2.3 Thesis overview

Why the how: what makes these objectives valid

The machine

The results

INDIVIDUAL LEVEL
COMMUNITY LEVEL

II

BACKGROUND: COMMUNITY DYNAMICS, TRAITS AND PHENOTYPIC PLASTICITY

1 UNDERSTANDING COMMUNITY DYNAMICS: DRIVERS AND THEORIES OF COEXISTENCE

1.1 The question of coexistence

If ones want to better understand and predict dynamics of complex systems, they first need to understand how such complex is assembled. If it is easy to observe diverse ecosystems (from bacteria, to plants, insects or algea), it is challenging to determine the processes that 1) group the entities together (in time and space), 2) maintain an apparent stability in the group composition (at least at a certain spatial and temporal scale). This set of processes are called the assembly rules. Different type of processes are at stake to maintain a community and the general filters are illustrated in the figure ??.

We can imagine biotic filtering as an physical filter, the same way abiotic filter is often illustrated, but this image does not translate the dynamic and complex nature of underlying processes. Biotic filtering emerge as the result of all the interactions between the entities that make it through the other filters. And how these interactions, direct or indirect, play together to see the stability of the diversity.

Plankton paradox in homogeneous system, where abiotic and dispersion should have little role into maintenance of species diversity.

Focus on interaction: chesson modern coexistence theory.

Other things being equal hypothesis (in models at least) does not allow the full diversity to emerge.

One mechanisms alone seams to not be enough to explain fantastic diversity explain in natural ecosystems. However there are multiple theoretical mechanisms that support species diversity and that should taken into account in community models: diversity of resources, spatial and temporal variability, frequency dependent effects, etc...

1.2 Abiotic and biotic factors: from potential to realised niche

Abiotic drivers main tning at global scale... Then interactions and competition.

The concept of ecological niche serves as a great tool for theoretical research on coexistence. It encompass in a convenient way both abiotic and biotic drivers of one species distribution. The Hutchinsonian niche also captures the multidimensionality of persistence and reproduction.

1.3 The complexity of community dynamics

From the multiple first attends to explain coexistence with one particular mechanism, scientific community realised that indeed multiple mechanisms are at work to make species diversity in ecological community. + multiple drivers that filter down. + temporal effect (metacommunity, invasion, equilibrium vs long transitions) This multiplicity highlight the need for unifying framework able to cover this diversity of mechanisms and dimensions.

2 CONSIDERING STRATEGIES AND FUNCTIONAL TRAITS

2.1 The continuity of functional ecology

The paradigm shift toward functional ecology allowed the shift from discrete to continuous representation of species. This change make easier the representation and study of plant communities, especially along conditions or management gradient. Despite the advantages of functional traits, close comparisons and links with theoretical approaches should be used carefully, and underlying assumptions should be interrogated.

2.2 How trade-offs make strategy space

Diversity of mech: diversisty of strategies. more or less independent.

The multiplicity of mechanisms in these systems lead to similar diversity in plant strategies. These strategies are captured in a strategy space drawn by independent trade-offs. Such trade-offs can be captured and embodied thanks to functional traits.

2.3 Modelling diverse plant community

The use of strategy spaces in models allow the representation of high diversity in a common plant functioning framework requiring limited number of parameters. Such approaches are very useful to follow the dynamics of communities in a mechanistic framework.

3 THE IMPORTANCE OF INTRA-SPECIFIC VARIABILITY

3.1 Intra-specific variability change the rules

More interest in trait distribution, variability and diversity. → Get to look at intra-specific variability.

Jung: not always in the same way [jung_intraspecific_2014]

[kichenin_contrasting_2013] [siefert_global_2015] [albert_importance_2012] [violle_return_2012]

The intra-specific variability has been observed to be both an important part of community functional diversity, but also a way the community respond to changes in conditions. In addition to the empirical evidence of this importance, theoretical approaches support contrasting effects of such variations on coexistence mechanisms, evolutionary processes and community responses to climate event or invasion. It is crucial to disentangle different sources of intra-specific variability in order to understand potential effect on ecosystem dynamics.

3.2 Phenotypic plasticity: a specific case of intra-specific variability

phenotypic plasticity is the capacity of a species to produce individuals with the same genotype but different phenotypes. This difference in phenotype should be an active process, not the results of direct alteration of the phenotype by external factors without changes in internal functioning. This change in internal functioning process has the objective ¹ to match the phenotype with expected future conditions to maximise the individual fitness. The expression "expected future conditions" is key here, as it is this projection that drives the plasticity.

Active plasticity is used for predominantly anticipatory, and often highly integrated, phenotypic changes in response to some environmental cue or signal, and reflect modifications of developmental pathways and regulatory genes. Forsman - 2014

Passive plasticity, on the other hand, may stem from direct environmental influences on chemical, physiological and developmental processes, and is generally not considered anticipatory, but a mere consequence of the environment, such as stunted growth owing to low resource levels.

Phenotypic plasticity requires two main components: (1) a projection of future conditions, (2) a link function between conditions and phenotype. The link function can have an additional parameter in the form of the current state of the individual, parameter that alters the form of the function.

3.3 Beyond the mean and the bell-shape: towards more mechanisms in representing intra-specific variability

The same way the neutral theory is simplifying and brings little understanding to underlying processes and relies on strong hypothesis, considering intra-specificity as a purely random mechanism is insufficient.

Bell shape do not appear in altitude gradient...

Strong theoretical hypothesis

Asymmetric and symmetric competition

¹ in the sense it has been selected because it provides this capacity

As ecology shifted from species to traits syndroms, it seems that it needs to go from syndroms to distributions and drivers. The complexity of living communities requires to go further down and consider the individual scale. This is made possible by the accumulation of more and more numerous and detailed data, the improvement of statistical and simulation tools.

3.4 Toward an integrative framework of plant strategy and phenotypic plasticity

Bradshaw? Dewitt

New simulations tools for understanding community dynamics should try to both include multiple coexistence mechanisms and plant strategies, and focus on individual level mechanisms of competition, growth and survival. This can only be achieved an a constraint high dimensional strategy space based on physical and biological trade-offs. Individual level modelling allows the integration of multiple sources of intra-specific variability: genetic diversity and phenotypic plasticity. Phenotypic plasticity being driven by the perception of environment, it cannot be simply described by normal random distribution and should receive more attention. This focus is particularly important considering both the lack of understanding of this phenomena and the consequences for plant communities.

III

MODELLING ALPINE GRASSLANDS WITH MOUNTGRASS A GENERIC FRAMEWORK INTEGRATING PHENOTYPIC PLASTICITY

The objective of this chapter is to develop the core concepts of the model, introduced in previous chapter, and explain the structure and design choices made during the model development. The first part focuses on the general context of alpine grasslands and some coexistence mechanisms at stake. The following part details the definition of the strategy space and the modelling of phenotypic plasticity, while introducing the key concepts of species memory and individual experience. Finally, the last part is a detailed description of the model following Grimm recommendations [grimm_standard_2006].

1 ALPINE ENVIRONMENT: CONDITIONS, RESOURCES AND PERTURBATIONS

1.1 The scales of alpine grasslands

The scale is a determinant variable in the quantification of mechanisms that structure ecological communities [bello_hierarchical_2013], and therefore in modelling approaches. It is chosen based on structures that the modeller intends to explore, and determine the upper limit of mechanisms the model can reproduce. Large scales will favour geo-climatic and dispersal effects [kleidon_global_2000] while small scales will focus on direct plant interactions processes or resource heterogeneity [soussana_gemini:_2012; maire_plasticity_2013; taubert_modelling_2014].

THE SCALE

This is true for spatial scale, but also temporal scales. Because mechanisms studies at large scales like dispersion, invasion, speciation occur over long time scales whereas mechanisms occurring at smaller spatial scale, like competition, facilitation, disturbances play a role on shorter time scales, spatial and temporal scales are often correlated. The scales are also dependent on the studied environment. There is a high contrast between highly productive environments like tropical forests, and unproductive environments like mountain grasslands. The dimensions of individuals themselves are a constraint on the scales: while tropical trees grow few tens of meter high and above one meter diameter [], alpine grasses do not exceed half a meter [korner_alpine_2011]. Similar difference of an order of magnitude can be observed for life cycles between long live tree and annuals or bi-annuals grasses. The focus of this work being on plant functioning and interaction mechanisms, the scale of the model will be around the meter, while the temporal scale will be in the order of the season.

The same way the scales are constraint by the size or length of the individual, the resolution should be close to the size of the modelled entities. The resolution is also determined by the focus of the model: interactions between individuals must be distinct and not blended to hope see the emergence of spatial patterns. Cell size and time step length should be small enough to take into account heterogeneity that is an important driver of diversity. For these reasons, the spatial resolution is set up to the centimetre and the temporal resolution to the day (can be changed but processes might not scale well).

THE RESOLUTION

Once resolution is fixed there is always the temptation to increase the size, or scale, of the system. This should be avoided for two main reasons. (1) the increase of scale with relatively fine resolution lead to a high increase in computational power required for simulations that are already complex. (2) there is a high chance that the processes modelled at fine resolution loose their sense when scale increases. Indeed, as mentioned, the importance of processes at stake is often dependant on the scale the system is studied. The effect of higher scale processes are often taken into account in inputs or parameters[1]. Calibration these parameters against certain data is a way to better understand these processes [lagarigues].

COMPLEXITY AND PERFORMANCE

1.2 Resources: light and water

As mentioned in the previous chapter, resource fluctuations, heterogeneity and competition are important factors for coexistence. Unlike animals, plant mainly compete for the same resources: light, water and nutrients. Light is the source of energy that allow the transformation of inorganic carbon into organic matter through photosynthesis. Water has multiple function in plants: transport, structural support, and oxygen supply for photosynthesis. Nutrients are used in construction of cells and cell walls, and especially the production of proteins that act as cell machinery.

1.3 Perturbations: frost, grazing and mowing

The most notable specificity of mountain grasslands is the climate. While there is a wide range of mountain grasslands type, the focus of this document is on French Alps. Alpine climate in France is characterise by cold winter with snow precipitations and dry summer. The growing season is relatively short and spread between May and October in low altitude, and June and September in high altitude **need some charts here**. The particularity of this habitat is the presence of snow cover during winter that protects soil, rhizomes and seeds from negative temperatures. Because of this, seasons are decomposed in the model based on the snow melt in spring/summer and the first snowfall in winter. While a rise in temperature is needed to allow snow to melt down, frost event can occur after the beginning of the season. Such events represent strong environmental filter for non adaptive plants that do not invest in specific resistance mechanisms to favour early germination and growth. Therefore there is a strategic trade-off between germination date and early growth with frost resistance.

CLIMATE

Another specificity of alpine grasslands is that they are subject to changing management practices. Mountain grazing by domestic cattle was fairly common in Alps, but changes in agricultural practices and decrease in productivity due to drought lead to less and less grazing or mowing for fodder in alpine grasslands. These two types of management have different impacts on the community. While mowing is non specific and favour small plants, herbivory is known to be specific when the production is greater than the grazing pressure. Leaves with high nutrient content and low structural tissues content are generally favoured because of high input and high digestibility. The grazing pressure plays as ...

MANAGEMENT

mechanisms as it favours conservative species with lower competitive ability.

OTHER FORM OF HERBIVORY

2 MULTI-DIMENSIONAL STRATEGY SPACE, CARBON POOLS AND TRADE-OFFS

2.1 Multi-dimensional strategy space and allocation pools

2.1.1 The strategy space in *Mount Grass*

In an ecological agent-based simulation model a species will be defined by its values for the species specific parameters. They can be estimated from experimental data [taubert_modelling_2014; maire_traits_2009; lohier_explaining_2014] or be picked from a strategy axis [reineking_environmental_2006; kleidon_global_2000] composing a strategy space [westoby_leaf-height-seed_1998]. The diversity of the species pool will depend on the number of values for each of these specific parameters, or traits, and the number of these traits. Each trait increasing the dimension of the strategy space [laughlin_intrinsic_2014]. The ambition of this model being to simulated rich plant communities, the definition of these axis is crucial. Trade-offs between traits are excellent applicants for these specific parameters as they reduce the dimensionality of phenotypes to a small number of dimensions [wright_worldwide_2004; diaz_global_2016; reich_world-wide_2014] while keeping the information of traits needed to describe the plant functioning. Trade-offs emerge from ecological and physical or biological constrains, by considering these constrains Darwinian demons are avoided.

While considering too many axis does not improve community description, a certain number is needed to have strategic diversity [laughlin_intrinsic_2014]. This is intuitively explained by the fact that each trade-off is closely related to a particular aspect of fitness or mechanism for coexistence (e.g. reproduction, competitve ability, resistance to resource shortage, predation, etc.). In this model, multiple aspects of plant life are represented: germination with the germination rate for storage effect [chesson_general_2000; adler_climate_2006], dispersion with seed mass [westoby_leaf-height-seed_1998] or tissue construction cost [reich_leaf_1992; wright_worldwide_2004; reich_world-wide_2014]. Main components of plant growth and life history are covered by such trade-offs and driven by mechanisms shared by all vegetation systems. Because of that, the model has a great potential of genericity and diversity. It can be easily adapted to other plant communities with specific calibration, and extended with couples of biological process and differenciation axis (e.g. root herbivory and associated resistance carbon pool). The the trade-offs used in the model are detailed in the model description below ². These axis should, in such models,

² see serction 4.

be independent, (*i.e.* it is physically and biologically possible for a plant to take any position in the space drawn by two given axis) and result from physical or biological laws (ensuring that impossible strategies are indeed excluded from the model). First, it is a condition for parsimony of the model. Second and more interesting reason is that any trade-off emerging from the model should have an ecological interpretation [**maire_disentangling_2013**].

One way of constraining plant strategies to certain axis is to consider allocation trade-offs [**kleidon_global_2000; reineking_environmental_2006**]. An allocation trade-off is the translation of the mass conservation rule that prevents the allocation of biomass to distinct carbon pools. If biological functions are related to organic matter pools (photosynthesis to leaves, water and nutrient uptake to roots), then the sum of biomass to invest in each carbon pool (therefore in each function) cannot exceed the total available biomass: leaving the plant with a choice on the balance between the different functions. Allocation trade-offs have the advantage to be easily implemented and be intuitive. By design, a partitioning factor value corresponds to a position on the related strategic axis. In *Mount Grass*, five main trade-offs are captured by allocation trade-off: (1) development vs reproduction: partitioning factor between reproduction and maintenance of vegetative tissues (when plant is mature), (2) persistence vs dispersion: partitioning of reproduction biomass between persistence (storage) and production of new propagules (seed/clone production), (3) aboveground vs below-ground competition: investment between shoot and root, [**kleidon_global_2000; reineking_environmental_2006; taubert_modelling_2014**](4) slow vs fast: construction cost trade-offs between active and structural tissues in both shoot and root and (5) growth vs resistance: partitioning between stored biomass and frost resistance carbohydrates [**cai_changes_2004**]. This last trade-off can be extended to other carbon pools of specific resistances, for example to herbivory. Modification of these coefficient during life history is a way to introduce plasticity in the model. The rules driving such changes for some of this partitioning parameters are described in the following section.

One of these trade-offs, (4), is key and related the construction cost of organs (independently leaves and roots). Highlighted at global scale and for leaves, the Leaf Economic Spectrum [**wright_worldwide_2004**] draws an strategic differentiation axis from conservative slow species and exploitative fast species. The construction cost has long been identify as a factor of strategic differentiation in plant communities [**westoby_leaf-height-seed_1998**]. This strategic axis, being related to many functional traits: SLA, LDMC, LNC, leaf longevity, Amass, etc. [**wright_worldwide_2004**] is of crucial importance. First, these traits are closely related to the characterisation of plant communities and the assessment of services [**grime_benefits_1998**]. Second strong links and correlations can be made between these soft traits physiological traits [**craine_functional_2002; reich_variation_2003; wright_worldwide_2004**]. Finally, a species resource use strategy is closely related to its responses and vulnerability to changing conditions [**poorter_causes_2009; dwyer_specific_2014; deleglise_drought-induced_2015**]. The traits related to this trade-off play a major role both in individual growth and physiology, and in community services and response to gradient. Therefore it is essential to the model. Questioning the underlying mechanisms for

such strong trade-off is necessary to implement satisfying representation in the model.

Change this: may be start with shipley results, then composite stuff. Question: should it be here, or in the following part ?

These trade-offs between highly productive tissues with low construction cost and short lifespan called exploitative, and more conservative strategy with longer lifespan but lower productivity are mainly observed thanks to soft traits such as SLA for LNC [wright_worldwide_2004]. Mechanistic model require traits related to physiology and organ performance [soussana_gemini:_2012; lohier_explaining_2014], but link can generally be done between these traits and soft traits. However traits such as SRL or SLA are composite traits emerging from different organ properties [ryser_importance_1996; john_anatomical_2017], where tissue density and organ thickness are the main determinants. "A necessary trade-off between allocation to structural tissues versus liquid phase processes" has been identified by Shipley et al. [shipley_fundamental_2006] as one of the two main factors for the leaf economic spectrum to emerge. Such allocation trade-off can indeed explain differences in construction cost as the liquid phase corresponding to the "active" part of plant tissue, the cell content, have much lower dry volumetric mass than its "structural" counterpart, the cell-wall. Also active tissues containing the protein machinery for photosynthesis and water absorption, a higher proportion of high protein concentration tissue would be correlated to higher nitrogen concentration in the organ on the "fast-slow" spectrum, along with a higher mass-based photosynthetic rate [reich_world-wide_2014]. On the other end, the structural tissues give the organ a higher lifespan [mediavilla_internal_2001; ryser_importance_1996] that compensate for lower productivity [westoby_time_2000]. Such trade-off can be apply to both shoot and roots [craine_functional_2002; tjoelker_linking_2005; reich_world-wide_2014]. From that, the decomposition of organs between active and structural tissues constitutes a strong basis to model construction cost trade-offs as the main parts of the global strategy space.

The Similar axis of differentitaion has been demonstrated for roots [reich_world-wide_2014; tjoelker_linking_2015]. The necessity for independent similar axis for leaves and root can be discussed with respect to coordination between shoot and root activities. Because perfect equilibrium cannot be guaranteed in all conditions, strict coordination cannot taken as a principle for the reduction of strategy space. Moreover, empirical results suggest small deviations from coordination are common [freschet_explaining_2015]. The leaf economic spectrum being conserved at the intra-specific level [hu_novel_2015] is another reason to include such trade-of as it would be a good basis for phenotypic plasticity [freschet_plasticity_2013].

The use of allocation trade-offs allows the construction of a generic multi-dimensional strategy space where a high diversity of species can potentially coexist. Because this space is based on physic laws, it ensures the non existence of Darwinian demons and does not limit the species or individual plants to tested parameters and strategies. To be complete the link between carbon pool allocation and physiology must be determined within the respect of similar biological or physical laws.

2.2 Craft a trade-off: active and structural tissues

Allocation trade-offs offer great flexibility and are easily understood and implemented. However, when they control the value of traits (SLA or SRL) involved in multiple processes, a balance must be found to avoid that: (1) one process is ignored because has a low relative importance on fitness (becoming useless to the model), (2) the effects of processes involved show strong response curves to the allocation and there is only one global¹ optimum. The idea behind a trade-off is that multiple positions are viable in different conditions or in association with other strategies. The leaf-economic spectrum, in addition to rely on the active-structural tissue trade-off, also requires "*an evolutionary trade-off between leaf photosynthetic rates, construction costs, and leaf longevity*". This trade-off is explore in this section of the document.

¹ I use the term global here to designate the multidimensional space draw by the axis of interest and other variables play a role in involved process (e.g. resource availability, temperature etc...).

In the framework of the model, plants share the same global parameters, and the maximum photosynthetic rate should be the same. Because photosynthesis relies on the exchange of gases (CO_2 , O_2 and H_2O) and the interception of light, it is related to exchange area. Considering one shared parameter for maximum area-based potential exchange rate satisfy both the need for a shared parameter and a way for plant to vary their mass based exchange rate by changing its proportion of active tissues. This is in agreement with the LES that describe strong relationship between mass based traits and limited ones for area-based variables [**wright_worldwide_2004**], and explain the first part of the trade-off between photosynthetic rate and construction cost. The second part is the relationship with the longevity. The longevity is often correlated to SLA in empirical studies, however this is mainly explained by differences in tissue density and toughness than in thickness (other component of SLA) [1]. For this reason we can directly link the leaf longevity to active tissue proportion. Respiration is also increased by the increase of proportion of photosynthetic tissues [**kleidon**; **reich**]. We have now a trade-off between a gain function (exchange area gain by changes in densities) and a cost function (tissue turn over and respiration). This should be enough to explain different strategies [**westoby**]. However the model need internal limits to avoid the gain function to lead to only active tissue organ (or only structural). These limits are required to allow individuals or species to change position along these axis (plasticity or strategic shift). The convex shape of gain function in association with a minimal cost (minimum turn-over cost above maximum potential gain) is enough to limit the allocation to structural tissues only. To avoid allocation to only active tissue, that would correspond to an organ made of protoplasts, the cost function need higher than the potential gain. To achieve that an ... function is chosen. This choice ensure that the potential gain function has an optimum different from the borders. (**see figure**).

Active got closer to optimum, but less active and positive gain in more conditions. Can I demonstrate this with formulas ? (gain = function(condition))

GAIN AS FUNCTION OF CONDITIONS

The potential gain is not only function of active tissue proportion, but also depends on resource availability. Changes in resource level imply changes in slope of gain function and a shift of the organ optimum for tissue allocation. This shift make more conservative strategies more interesting when resources are scarce,

while more exploitative allocation strategies are better for high resource availability. This link between optimum allocation and resource level could be used to define the best phenotype according to experience conditions, but the organ strategy cannot be disconnected from the whole plant strategy and allocation.

The phenotype (within the subspace of vegetative allocation) depends both on the individual efficiency of organs and the balance between shoot and root activity. This balance, often used to model plant plastic allocation and considered between light and nitrogen [lohier; soussana]. In the context of mountain grasslands and global change, the water... The integration of nitrogen as a limiting solution is discussed in latter chapter. The balance between shoot and root activity being key in overall performance, the root shoot ratio (RSR) will be determined as a function of estimated availability.

2.2.1 Species memory and phenotype determination

phenotype = ensemble of response trait values. Emerge from default trait + environment.

Composite traits are defined by the interaction of different, independent, driving traits. What is a driving traits ? Biology: genetic information. This genetic information is selected by climatic conditions. If we can make a link between optimum value for a trait and environmental conditions, then store external conditions and use link between.

MEMORY OF SPECIES: A DRIVING TRAIT

The decomposition of organs organic matter in active and structural carbon pools makes a link between allocation and physiology and draws a subspace within the strategy space where individuals can move and change their phenotype. Limiting mechanisms restrain the viable options to realistic values along these axis. Within this space, the resource availability and external conditions play a major role in the expression of the strategy.

VEGETATIVE PHENOTYPE AXIS

Flexible, allocation based, diversity and movement

3 MODELLING PHENOTYPIC PLASTICITY

3.1 Plasticity as a strategy: between species memory and individual experience

3.1.1 Concept of active plasticity as a strategy

Active plastic response is highly integrated and involve a lot of regulatory processes. It is impossible to represent all regulatory processes involved in an APR (because of our lack of knowledge and their complexity). Alternatively, the

DECOMPOSITION OF PLASTIC RESPONSE

concept of *integrated response* can be conceptualised. It supposes link, or coordination, between the experienced conditions and the phenotypic response. This can be translated, in the model framework, by the existence of explicit link between a representation of external conditions and a phenotype matching this conditions: the ¹. Another key work is *anticipatory*. It supposes that the plant knows, or at least have an idea of the future conditions. This is really the point of an active plastic response: change the phenotype to better match future conditions. A representation of future is also called a . The projection and the allocation rule together form the active plastic response.

If allocation rule is not obvious and is discussed latter², the idea of projection is fairly intuitive. The projection will correspond to a value for a given metric that represent the external conditions. It can be resource availability level, temperature, herbivory risk, etc... If such metrics can be given at the community scale, it make sense to use plant centred measure of these variables for two reasons: (1) take into account the spatial heterogeneity, (2) plant experience of conditions is necessarily egocentric. The details on how experienced conditions are interpreted by plants in *Mount Grass* is described in section 4.

Active plasticity is now represented by a projection and allocation rule. However, how a species can control the whole process is unclear. In theory both projection and allocation rule can species specific. In nature plants generally have structurally similar regulatory processes³ and response to external stimuli is translated (and stored temporarily) thanks to the accumulation of chemical compounds[need-references]. These mechanisms suggest that, while the allocation rules are mainly shared, individuals vary on the information level (i.e. concentration of phyto-hormones), or in the context of the model: plant vary in projection. This control of active plasticity is supported by the model design. The number of rules that can drive the allocation is reduced and discrete, while the projection is multi-dimensional (one dimension per external variable considered), continuous and high flexible with a reduce number of parameters⁴. For this reason is chosen to be the of active plasticity, while the allocation rule is and between all species. Therefore an individual with fixed projection wont be actively plastic, despite the fact that it could express apparent plasticity because of external factors: reduced resource availability, grazing, frost damage, etc... The model has now a concept for active plastic response⁵ controlled by the projection of external condition. The next question that need to be answered is: how do species differ in their plastic response ?

In *Mount Grass* , the projection of external conditions is the mean for plants to alter their phenotype in response to changes in experienced conditions. Since the allocation (or driving) rule is shared by all plants, if the projection of external conditions is also shared by all plants, then is the response still active plasticity ? The first intuitive answer is yes, since the conceptual framework is respected and plants would react to changes in conditions that would affect the projection. But, such response would be equivalent to a direct external control of the climate on the phenotype. In such case, species would not have control on how the phenotype varies, that would be fully controlled by shared projection and shared allocation rule. This is passive plasticity. To have proper active plasticity, the species need to be able to the plastic response. If species can regulate plastic response

¹ the use of the word *allocation* is justified here since the phenotypic plasticity in *Mount Grass* is reduced to changes in allocation.

² see paragraph 3.2

CONTROL OF PLASTICITY

³ see box ??.

⁴ details in paragraph *estimation of conditions* in section 4.

⁵ In the rest of the document terms *plasticity* or *phenotypic plasticity* will refer to *active plastic response*.

SPECIES SPECIFIC PLASTICITY

thanks to species specific parameters, plasticity becomes a . This is in agreement with Bradshaw vision of phenotypic plasticity as a trait, or a character, subject to selection and evolutionary processes[[bradshaw_evolutionary_1965](#); [bradshaw_unravelling_2006](#)]. How do species regulate plastic response to make it a strategy?

Plasticity: expected environment -> phenotype, here phneotype is equivalent to biomass partitioning, that means expected environement -> allocation coefficients. Then memory -> expectations -> allocation. Because low dimensions, and we want diversity, and the link between memory and allocation might not be a function (one memroy give exactly one optimum allocation), in the model this relationship is not verified. Species specific traits are used to allow for different strategies to be associated to a same memory (different plants won't have the same strat, despite sharing the projection)

3.1.2 Projection of external conditions: between species memory and individual experience

The projection is the way plant controls phenotypic plasticity. A projection is an idea of the future based on available information and understanding of phenomenon. Ones could discuss what is the understanding of the climate by plants, while others can focus on how to represent such understanding and state that fine molecular regulatory processes can reproduce and store such information. The focus is on the construction of the projection with respect to the different sources of information a plant has: (1) its experience of climate and external factors, and (2) its ancestors memory¹.

BUILD A PROJECTION

While, for any given individual plant, the experience of external conditions varies in time, the memory stays fixed. There is a clear contrast between variable experience of conditions and the fixed species memory. A way to represent different strategies and the level of control the plant apply on projection is to vary, between species, the relative weight of species memory against individual perception. This species specific parameter, the , sets the of the projection with respect to individual experience. The capacity to adapt the phenotype to changing conditions is directly linked to the projection changes. High confidence in species memory translates in low amplitude of projection variations, and though in low active plasticity.

¹ see paragraph 2.2.1.

The calculation of projected resource availability levels, or temperatures, are detailed in dedicated paragraph of the model description. The key message is that the species has control on plasticity with both its confidence in species memory, and the said memory that alters the projection. The relative impact of memory and confidence is described in figure ??.

While the representation of plasticity as a strategy increases both model species diversity and potential diversity of response [[ryser_consequences_2000](#); [kichenin_contrasting_2013](#)], plasticity itself may reduce plasticity. Indeed, plasticity lead to a change in phenotype in response to condition changes, while this phenotypic change is unlikely to be identical, its direction will probably be similar. Few mechanisms can prevent convergence of phenotype besides the diversity in memory and plasitcity: (1) changes in competitive hierarchy may lead to differences in individual expe-

THE PARADOX OF PLASTICITY

rience of conditions, (2) specificity of the external driver, e.g. selective herbivory of more digest species, (3) relative position of the optimum phenotype.

Or can a plant be plastic and unique ? The paradox of plasticity and diversity. Plastic will neceseraly reduce the space (as there is convergence, unless different strategies of adaptation).

Because the plasticity is a strategy and not a default behaviour, its effects on individual performance have to be tested. But it also opens a lot of interesting questions around the costs and benefits of plasticity, and the co-selection with the resource use strategy.

Moreover this particular implementation of plasticity limits risks of convergence while allowing plants to evolve in the strategy space defined earlier.

3.1.3 On the difficulty to match strategy and conditions.

The projection of external conditions, driving the plastic allocation of organic matter, lies on a balance between species memory and individual experience. Its design make of plasticity an axis of strategic differentiation alongside the other strategy axis. Thanks to this innovative design, the model can be used to examine the ecological relevance of plasticity in different conditions and in association with different strategies. The effect of allocation rules and projection stability can be explore independently or conjointly for a better understanding of relative importance of allocation and plasticity.

3.2 Driving rules of allocation

Allocation rules is determinant in the model behaviour as it is shared by all species, and link the projection of conditions with the phenotype. Multiple options are possible to drive plasticity, but they can be divided in two main categories: (1) determining, (2) directive. Function from the first category fully determine the phenotype (within the plastic strategy space), while functions from the latter group direct the phenotype toward a sub-space and other parameters are needed to determine the exact new phenotype.

The two type of rules have different strengths and weaknesses that are detailed in table ??

Strength or weakness	Determining	Directive
Phenotype fully determined	●	○
Risk of convergence	●	○
Reduction of functional diversity	●	○
Discrepancy between parameters	○	●
Strong plasticity effect	●	○

Table 3.1: Two types of allocation rules: strengths and weaknesses

The driving rule of plasticity defines whether or not the choice of the phenotype is fully determined by the projection of external conditions or also constrained by some species specific parameters. The effect of this balance between projection and parameters has a large influence on the model be-

haviour. In any case the projection is the main control on individual plastic response to change in conditions, offering possibilities to modulate individual plasticity despite a allocation rule shared by all species. The role of both projection and allocation rule will of particular interest during the analysis of the impact of phenotypic plasticity of plant growth and community dynamics.

4 ODD DESCRIPTION OF THE MODEL *MountGrass*

This document is a detailed description of the *MountGrass* model. This description is based on the ODD protocol of Grimm et al.. The model is inspired by multiple other forest and grassland models (for grassland models see particularly Taubert [[taubert_modelling_2014](#)] and Lohier [[lohier_explaining_2014](#)]). It differentiates itself from these models by the incorporation of phenotypic plasticity in a generalizing framework for plant functioning. This allows it to be used to both to explore the fundamental effects of phenotypic plasticity the dynamics of rich grass communities and the impact of the phenotypic plasticity on plant interactions. The general approach and the practical details are further detailed in this document.

4.1 Model overview

4.1.1 Model purpose

The development of *MountGrass* is motivated by the need for a flexible tool to explore the complex dynamics of mountain grassland communities, in the context of global change. This tool should, by a better understanding of community dynamics and representation of plant strategies and interaction, also help in the assessment of ecosystem services in new conditions. We believe that to capture the dynamic of such communities, we need to understand and represent first the individual response of plants to fluctuating levels of resources, and the impact of plants on the resources. Individual responses and relative impact should follow general rules of plant physiology but also integrates specific behaviour based on the species resource use strategy and individual characteristics. Therefore the model should allow to follow distinct individuals from different groups (e.g. species) in a spatially explicit environment where they compete for resources.

Moreover, since we focus on the community levels, coexistence mechanisms are important and we should include a certain number of these if we want to maintain diversity to observed levels. These mechanisms include: multiple resources competition (water and light), spatial and temporal heterogeneity of resource levels, strategic trade-off between species, perturbation mechanisms (frost, management), link to meta-population, etc...

The model is built to try to satisfy conditions to reproduce and explore mountain grassland community dynamics. In the current version of the model (*MountGrass2.0*), a generalist approach has been privileged, and focus on some coexistence maintenance mechanisms and integration of phenotypic plasticity framework. In this state the model has to be seen as a toy model with good generalisation poten-

tial. The link between ecosystem services are not included, but we can easily imagine to compute them from the community trait distribution. All processes and mechanism are detailed below.

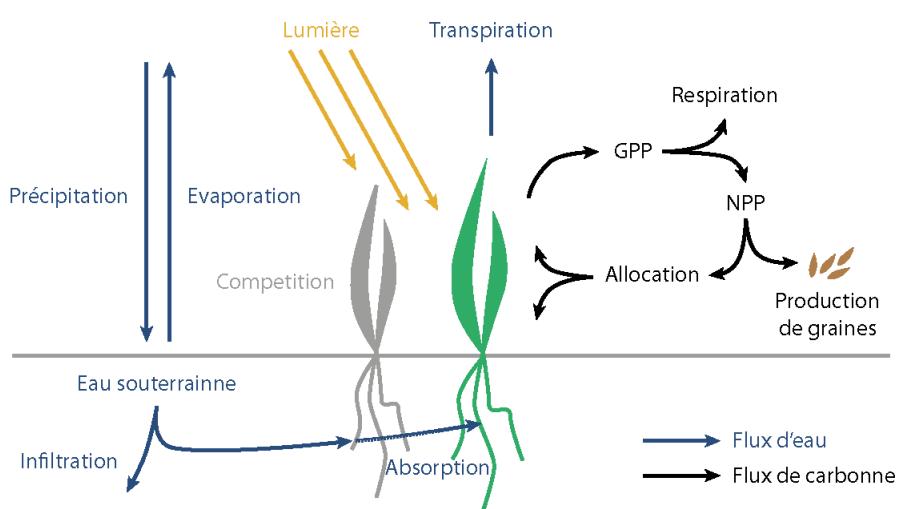


Figure 4.1: Model overview

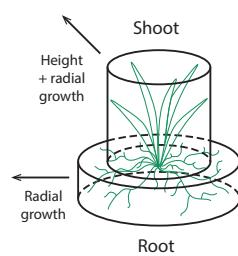
4.1.2 State variables

In mountain grasslands individuals (tillers) generally do not grow big and interact only with close neighbours and form little patches. And thus it is possible to represent rich community at a fairly small scale (\approx dm or m), but the spatial resolution should be relatively fine (\approx cm) to capture inter-individual interactions. Because the model is intended to explore climate change impact on mountain grasslands, it can run on multiple growth seasons separated by snow covered periods, but must also integrate the intra-seasonal variations at daily scale. Mountain weather (mostly temperature) is known for its large hourly variations, it would however require too much computational power to consider such variations. In addition to this argument, we believe that even-though they imply physiological flexibility and specific strategies for plants experiencing these conditions, they will not have a huge impact on overall community dynamics changes caused by the climate change. That's why hourly variations will not be considered, and physiological processes are estimated at the daily time scale.

SCALES

The plants are described in the model by state variables described in table 4.1. The best way to understand how plants are represented is to imagine two homogeneous cylinders on top of each other, the shoot cylinder varying in radius and height representing the light acquisition (and shading) zone, and the root cylinder varying only in diameter (because of shallow soil in mountain ecosystems) representing the water acquisition zone. These cylinders are centred on cells of the torus simulation plan.

PLANTS



In addition to classic variables (age, position, height, diameter, shoot and root biomasses) the plants are described by traits, that can be species specific or non-specific, others are variable (SLA, SRL) and depend on particular traits

Figure 4.2: Plant geometry and growth axis.

that are unique to this model: the **ratio between active tissue and structural tissue** (in shoot and root) (variables $\frac{act}{str\ ag}$ and $\frac{act}{str\ bg}$ in table 4.1). This couple of traits come from the evidences that numerous trade-off observed in leaves can be explained (at least partially) by this allocation trade-off between active tissue producing organic matter, but increasing respiration, and structural tissue that increase tissue lifespan.

Variable	Description	Unit
x	x position on the grid	cells
y	y position on the grid	cells
age	age	days
sp	species	-
BM_{ag}	above-ground biomass	g
BM_{agsen}	senescent above-ground biomass	g
SLA_{sen}	senescent above-ground biomass	$cm^2.g^{-1}$
BM_{bg}	below-ground biomass	g
stem	stem biomass	g
$\frac{act}{str\ ag}$	above-ground active on structural biomass ratio	g/g
$\frac{act}{str\ bg}$	below-ground active on structural biomass ratio	g/g
h	height	cm
r	shoot radius	cm
r_r	root radius	cm
$light_{exp}$	above-ground potential resource availability	$gH_2O.\text{leaf area}$
$water_{exp}$	below-ground potential resource availability	$gH_2O.\text{root area}$

Table 4.1: State variables of individual plants
SPECIES

Plants are characterised by state variables that describe them individually, but they also share common characteristics with individuals of the same group, (we will refer as *species* to talk about this group in the rest of the document even though it could be a group at an other scale (i.e. population, clones). These species are the groups present in the meta-population and that can invade the simulated ecosystem. There are described by multiple traits characterising the strategy of the species (table 4.2).

The seed-bank is the transition state between the different seasons. Individuals may persist thanks to stored resources, but they can also reproduce by the production of new individuals. Lot of grasses use clonal reproduction, in addition or replacement of sexual reproduction. This type of reproduction is characterised by a persistent link between the newly produced individuals and the parent one that allow the two to communicate and exchange resources. Such dynamics are complex and costly to represent as the link between ramets must be stored and strategies defined for the resource distribution (see Oborny 2012) for more details on clonal growth modelling). To avoid too much complexity, it is possible to approximate the representation of clones to big seeds with little dispersion around the parent plant¹. For this reason, reproduction mechanism is reduce to sexual reproduction mechanism with production of "seeds". Seeds are stored in the seed-bank and only defined by their species and positions.

SEED-BANK

¹ This would take advantage of dispersion kernels. Not implemented in current version. Dispersion is uniformly random within the simulation plan

SOIL

Trait	Range (close range)	unit	trade-off or strategy
seed mass	(0.00001 - 0.001)	g	seed output vs seedling productivity
maturity	-	green biomass	flowering time vs reproduction potential
fract_dev	0-1 (0.05-0.6)	-	blooming vs persistence
fract_rep	0-1 (0-1)	-	reproduction vs persistence
geometric constant (k_g)	(0.1 - 20)	-	competition sensitivity vs self-shading
plasticity stability	0-1 (0.8-1)	-	genetic information vs experience
initial water resource	(0.001 - 0.05)	$gH_2O.cm^{-2}$	water resource niche
initial light resource	(0.001 - 0.05)	$gH_2O.cm^{-2}$	light (in H_2 equivalent) resource niche
$\frac{act}{str ag,d}$	(0.03 - 0.3)	$g.g^{-1}$	active vs structural tissue
$\frac{act}{str gg,d}$	(0.03 - 0.3)	$g.g^{-1}$	active vs structural tissue
mean temp.	(0 - 5)	°C	early vs late germination
germination rate	0-1 (0.5 - 1)	-	good season bet-hedging
thickness	(0.012 - 0.05)	cm	WUE vs light efficiency (not in this version)

Table 4.2: Species traits

Soil is an important aspect of the model as it drives (with the precipitations) the water competition between individuals. It is however limited, as in numerous vegetation models, to a grid characterised by: its capacity to retain water, and its depth. Only the first component (water retention capacity) is spatially variable and is described by the critical water content (minimum soil water content), the saturation water content (maximum water content, the water non absorbed leaves the system we assume the same root depth for all species), and the current water content (temporally variable, depending on competition, precipitation and evaporation, between the critical and the saturation water content) only dynamic variable among the three.

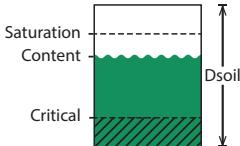


Figure 4.3: Soil section.

4.1.3 Process overview and scheduling

As mentioned the model runs at daily step to capture individual responses to conditions and over multiple seasons to capture long temporal dynamics. Some processes occur (or are evaluated) at the daily time-step, some at the season time-step. The following ordered list presents the different processes and the scheduling over days and season of one simulation.

One season can be divided in the following parts:

- *germination*: marks the beginning of the season when the ground is no more snow-covered;
- *growing season*: consists in daily processes like competition, production of organic matter (OM), allocation, and death lottery;
- *reproduction-invasion-persistence*: marks the end of the season when the first persistent snow-fall occurs. OM invested in reproductive tissues turns into seeds that are sampled to create the seed-bank. Seeds from the meta-population may integrate the seed-bank. Persistent perennials loose most of their biomass but storage (and eventually stem) and regrow from stored organic mass at the begining of the following season.

Figure 4.4: Seasons cycle in *MountGrass*.

The *growing season* part consists in all processes evaluated every day of the growing season. These processes are:

- *light competition*: the individual potential photosynthetic activity is computed based on average daily light and shoot properties;
- *water competition*: evaporation and the individual water update (and potential water uptake) are computed based on potential transpiration, water availability and potential evaporation;
- *production*: respiration and production are computed to give the net productivity in OM;
- *senescence*: based on lifespan a part of tissue is no longer active.
- *death*: death of individuals based on their age and their desiccation stage (number of consecutive days with negative growth).
- *allocation*: allocation of produced OM to the different carbon pools of the plant.
- *grazing/cutting*: (optional) grazing or cutting of plants to a certain height. The grazing can be selective.¹

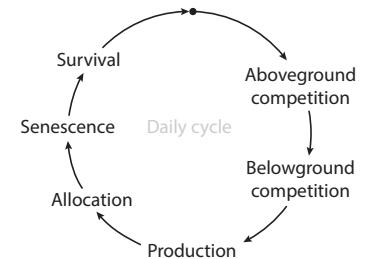


Figure 4.5: Processes in order during the daily cycle.

¹ remarks in grey are features or components implemented in the model but not used and-or calibrated.

4.2 Design concepts

4.2.1 Design concepts

This part clarifies the rules that drives the dynamics of the model.

The purpose of the model being to understand the rules that drive the community responses, we tried make the community dynamics emerge from the underlying processes of plant growth, resource use and reproduction. That means that population dynamics is at least partially emergent from the surviving and reproducing individuals. *Partially* emergent because it depends on the invasion rules applied to the system. The traits and biomass distribution that describe the community are completely emergent from the individual traits exposed by the individuals and their relative biomass and abundance.

Plants have in theory many options to adjust their phenotype and increase their fitness in response to changes in environmental conditions (resource availability, temperature, ...). High diversity of mountain grasslands suggests that multiple strategies coexist and that individuals do not change to converge toward a unique strategy. These strategies are set up at the species level by the species specific traits (see table 4.2). Therefore, individuals may only adapt morphological traits but not strategic traits (unless there is an epigenetic mechanism added). These morphological traits are: the relative biomass of shoot and root, relative proportion of active and structural tissues in each leaves, and roots (controlling respectively the SLA and SRL and the overall resource acquisition cost)². Geometry traits (distribution of leaves and roots within space) are not considered plastic as grasses have far less control on their geometry than forbs or trees. Root distribution plasticity has been shown to greatly improve the individual and community productivity (Gemini article), but to keep the model (and implementation) simple we will ignore root distribution plasticity and foraging

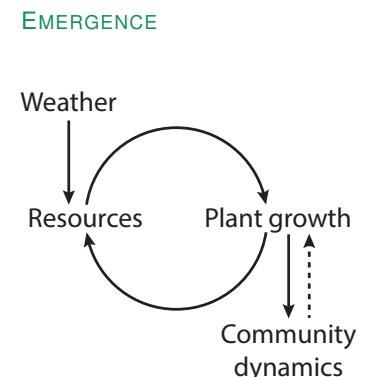


Figure 4.6: Population dynamics emerging from plant growth and weather.

ADAPTATION

² and optionally the proportion of stored OM dedicated to frost resistance and not to growth

strategies to focus on allocation problems instead of spatial distribution questions. Shallow soils and relative small rooting zone are also arguments to ignore spatial distribution plasticity for roots.

In the model the realised fitness can be estimated as the capacity of plants to maintain themselves or their descendants through time. It emerges from the productivity, allocation to storage or reproductive carbon pools, and survival. Assessing fitness as the average number of persistent individuals is however a bit hazardous in simulations limited in time and to a relatively small spatial scale. Plus, plants cannot easily make prediction of such variable to adjust their phenotype. They need a proxy function for fitness that integrate measures of external conditions to evaluate the best strategy to develop. As said above, this strategy should be a composite between the species strategy and individual adjustment specific to the individual experience of the environment. Plant fitness is estimated by individual plant thanks to a gain function integrating current phenotype, species strategy and projection of future conditions. This gain function can take multiple forms and be more or less constraint. In the context of the model, the function should include a measure of productivity that relies on the principle of functional equilibrium - that is the allocation of organic matter to maintain the balance between the shoot activity (transpiration) and root activity (water uptake). This equilibrium can be achieved by changes in shoot:root ratio only, or also changes in active over structural tissues ratio. Further details about the gain function are discussed in the dedicated paragraphs (4.3.3). More complex form of functional equilibrium incorporating nutrients (like nitrogen) could be added to the framework of this model.

Adaptation or plasticity mechanisms imply that agents have an insight of what will be the future. In *Mount Grass* we consider that plants have two main sources of information. The first source of information is the genetic information. Indeed, the evolutionary process of genotype selection has led to the selection of genotypes adapted to the local conditions. This selection relationship can be seen as a link between environmental conditions and genetic information. Because plants cannot fully predict future environmental conditions, they grow following (at least partially) the plan contained in genetic information that match conditions where previous generations grew in. This is an internal *a priori* information about the external conditions. If the conditions where the seed grow change from the conditions its genotype has been selected for, the genetic information does not fit the environmental conditions is not sufficient enough to build a working phenotype. In this case, if the plant has a plasticity capacity, it can integrate the second source of information, in the form of the experienced conditions, to its "a priori" and forge a new estimation of what conditions will be. One question emerges to this idea is: how to create an image of future conditions and how to balance the genetic *a priori* information with the experienced information ? This balance can be described by a term of "reactivity" that describe the relative weight of genetic and experienced information. A reactive species will give a higher weight to experienced condition information, whereas an stable species will give a higher weight to genetic information.

The way the two source of information are brought together and used to define the plant phenotype is at the core of plant strategy and is the main feature of the model *Mount Grass*.

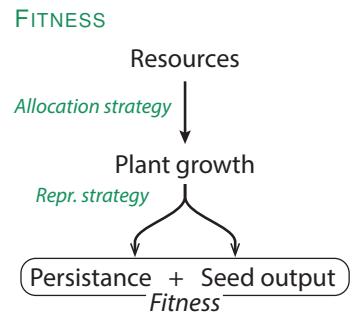


Figure 4.7: Fitness emerges from the plant growth and the plant reproductive strategy.

The plant growth is the result of the interaction of the resource levels, the plant strategy and the competitors.

PREDICTION

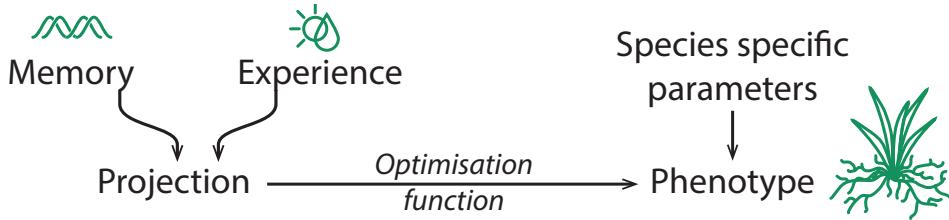


Figure 4.8: Genetic and perceived information are both considered to determine the phenotype.

4.3 Details

Further details on daily mechanisms are described in the following paragraphs.

4.3.1 Initialisation

The model doesn't need particular initialisation if the state of the community species pool, the seedbank and the soil are given as inputs. Otherwise, a set of $E(n/s)$ individuals are created from a set of s species (randomly generated if not given) and randomly positioned on the soil grid, where s and n are respectively the number of species and the approximate number of individuals within the grid. Soil grid is also randomly generated within default ranges for critical and saturation water contents then slightly smooth, and homogeneously filled ($filling = \frac{w_{cont} - w_{crit}}{w_{sat} - w_{crit}}$).

4.3.2 Inputs

Mount Grass needs system state information (individuals, species, seed-bank and soil) and climate data. If the state of the system is not completely given, then the complete state is generated in the initialisation. The daily climate data at must contain the following fields:

- *date*;
- *radiance*, in Watt.m^2 ;
- *precipitation*, in mm;
- *mean temperature*, in K;
- *mean day temperature*, in K;
- *min temperature*, in K;
- *max temperature*, in K;
- *relative humidity* in %;

Vapour pressure deficit is then computed from temperature and relative humidity.

The climate data must explicitly differentiate the seasons (delimited by the first day of the year without snow and by the first day of the second semester with snow).

4.3.3 Submodels

Individuals from the seed-bank randomly germinate according to their species specific germination rate. Germination consist of investing a percentage (*mob*

Figure 4.9: Overview of the model inputs and outputs.

parameter) of the seed mass into shoot and root biomass according to default traits. This is coupled with a round of random seed death following uniform law of parameter $seed_{surv}$. Living non germinating seeds stay in the seed-bank until the next season.

Daily processes

Light competition is central in all vegetation model as it constraints the photosynthetic activity and so plant growth. To avoid costly calculation of ray propagation we assume vertical homogeneous top radiation. Relief and orientation effects is taken into account in the computation of irradiance data.

Light competition sub-model allows calculation of individual potential photosynthesis activity and light at soil surface for evaporation calculation.

Competition for light is calculated independently for each pixel, potential photosynthetic activity is then aggregated at the individual level. Each pixel can be seen as a column of homogeneous layers containing at least one individual (top layer). For each layer the light transmission is computed based on leaf density.

$$I(h) = I_0 e^{-LAI(h)} \quad (4.1)$$

where $LAI(h)$ is the cumulative LAI at the bottom of layer l (between h and $h + \Delta_h$) defined as the homogeneous layer delimited by the top of consecutive individuals in the same pixel. The LAI is calculated like this:

$$LAI(h) = LAI(h + \Delta_h) + \Delta_h \cdot pix_width^2 \sum_{i \text{ in } l} d_i.coverage_{i,p} \quad (4.2)$$

where d_i is the individual leaf area density corrected by the coverage ($0 < coverage < 1$) of the pixel p by the plant i , $\Delta_h = (h_l - h_{l-1})$ is the height of the layer l .

Following Thornley and Johnson, the potential photosynthetic leaf activity is calculated as:

$$P_{leaf}(h) = \frac{\alpha \cdot I_{leaf}(h) \cdot P_{max}}{\alpha I_{leaf}(h) + P_{max}} \quad (4.3)$$

where $I_{leaf}(h)$ is the light absorbed by the leaf at height h , α the initial slope of the light response curve and P_{max} the maximum photosynthetic rate per unit of area and unit of time. I_{leaf} is the radiance at the leaf surface, derived by correcting the radiance at the top of the layer following the equation used in Taubert with the extinction and transmission coefficients k and m :

$$I_{leaf}(h) = \frac{k}{1-m} I(h) \quad (4.4)$$

The equation (4.3) can be integrated over the leaf surface by mixing it with equations (4.1) and (4.2) to give the total potential photosynthesis for layer l in pixel p :

$$P_{leaf}(p, l) = d_i.coverage_{i,p} \cdot \Delta_h(l) \int_{h_{bottom}}^{h_{top}} P_{leaf}(h) \quad (4.5)$$

the total leaf potential photosynthesis is then calculated as follow:

$$PS_{pot} = \sum_{p \text{ in shoot } l \text{ in pixel}} \sum_{p \text{ in shoot } l \text{ in pixel}} P_{leaf}(p, l) \quad (4.6)$$

LIGHT COMPETITION

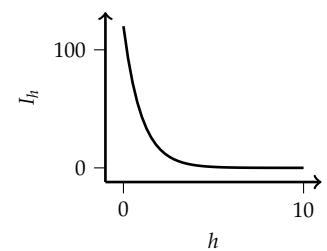


Figure 4.10: Net gain function and its first derivative.

Looks like there is some kind of mismatch here.

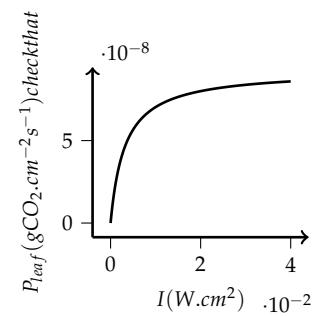


Figure 4.11: Photosynthetic saturation function

Potential photosynthesis must then be converted to potential transpiration to define the water demand. The conversion from photosynthesis to transpiration is done by dividing the potential photosynthesis by the water use efficiency (WUE). The potential activity of leaves are also dependent on the regulation of stomata so the transpiration can be written:

$$transp = \frac{PS_{pot} \cdot g_{red}}{WUE} \quad (4.7)$$

Photosynthesis depends on gases exchanges at the leaf surface. These fluxes result from relative concentration in carbon dioxide and water, and from the stomatal conductance. Stomatal conductance is reduced and limits productivity when vapour pressure deficit is too high ¹. A linear relationship describe this relationship:

$$g_{red} = 1 + VPD_{g_red} \quad (4.8)$$

STOMATAL REGULATION

¹ g_{red} is set to 1 for current version to avoid potential problems between allocation and regulation

Potential evaporation is calculated for each pixel depending on the light at soil surface:

$$\beta = 0.25 * (1 - \cos(\frac{\theta}{\theta_{sat}} * \pi))^2 \quad \text{if } water_{cont} \leq water_{sat} \quad (4.9)$$

$$\beta = 1 \quad \text{otherwise} \quad (4.10)$$

$$PET = 0.0023 \cdot \sqrt{(T_{max} - T_{min})} * (T_{mean} + 17.8) \quad (4.11)$$

$$evap = PET \cdot \beta \cdot I_{surface} \cdot daylength \quad (4.12)$$

Water competition is also computed at the pixel level. To determine the water uptake, first the individual water demand is computed as the minimum between the transpiration and the potential water uptake. Transpiration demand per pixel is easily calculated by dividing the total potential transpiration by the volume in the pixel $V_{i,p}$ over the overall root volume V_i . Water potential uptake is the product of root area in the pixel and root water uptake rate reduced by the water availability reduction factor U_{lim} , leading to the water demand for individual i in pixel p :

$$transp_i(p) = transp \cdot \frac{V_{i,p}}{V_i} \quad (4.13)$$

$$Wpot_i(p) = Root_{area}(p) \cdot U_{max} \cdot U_{lim} \quad (4.14)$$

$$Wdem_i(p) = \min(transp_i(p), Wpot_i(p)) \quad (4.15)$$

$$(4.16)$$

where, the limitation function U_{lim} is defined as in [reineking_environmental_2006]:

$$U_{lim} = \exp \left(\beta_\theta \left(\frac{1}{\theta_s - \theta_{crit}} - \frac{1}{\theta - \theta_{crit}} \right) \right) \quad \text{if } \theta < \theta_{crit} \quad (4.17)$$

$$= 0 \quad \text{otherwise} \quad (4.18)$$

The total water demand per pixel is then the sum of all individual water demand of the pixel and potential evaporation. If the total water demand exceeds

EVAPORATION

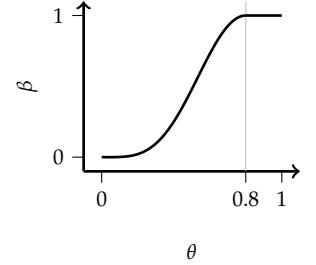


Figure 4.12: Evaporation limitation function.

WATER COMPETITION

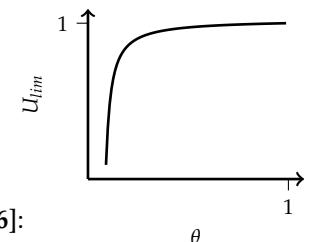


Figure 4.13: Water uptake limitation response function to soil saturation

the total water availability (W_{av} product of water content and soil volume in the pixel) then the available water is distributed proportionally to the individual demand.

$$W_{up_i} = W_{dem_i} \cdot \frac{W_{dem_{total}}}{\min(W_{dem_{total}}, W_{av})} \quad (4.19)$$

The potential water uptake (W_{up}), non limited by the transpiration is calculated the same way but considering $W_{dem_i} = W_{pot_i}$ in equation (4.19).

Because the water competition is computed at the pixel level, there is no compensation between two pixels containing respectively not enough and too much water.

No radial flow of water between pixel is implemented in the model. This simplification leads inevitably to edge effects, but allows simpler implementation and is partially covered by the effect of the pixel size. Indeed, increasing pixel size would have similar effect in the pixels at the border of the rooting zone than radial flow because it would increase the potential water pool plant has access to.

Once potential and realised transpiration and water uptake are computed, plant productivity can be calculated.

Following previous vegetation models, the respiration is decomposed in growth respiration and maintenance respiration. The first is function of trait values, biomass and temperature:

$$R_m = \left(R_{act} \cdot \left(Act_{ag} + Act_{bg} \right) \right) . daylength.T_{effect} \quad (4.20)$$

where R_{act} is the respiration rate of active tissues, and Act_{ag} and Act_{bg} are the active biomass pools in shoot and root.

Net Primary production (in CO_2 equivalent) can then be calculated the difference of GPP and respiration, then converted in OM production thanks to tissue carbon content (under the assumption of fixed carbon content for leaf and roots between species):

$$NPP_{carbon} = (1 - R_g) \cdot (WUE \cdot \min(w_{up}, trans_p) - R_m) - BM_{total} * Pl_{cost} \quad (4.21)$$

$$NPP_{OM} = NPP_{carbon} \cdot (12/44) / TCC \quad (4.22)$$

Here R_g is a fixed parameter but is set to 0 if the difference between gross productivity ($GPP = WUE \cdot \min(w_{up}, trans_p) - R_m$) and maintenance respiration is negative. Pl_{cost} is the plasticity cost as calculated in the dedicated paragraph below.

Temperature has a effect of plant activity, this effect can be modelled by a bell shape function around an optimum value of 20 °C. See Lohier for details.

The projection of environmental conditions is central in any implementation of phenotype plasticity. Differences between the current perception of environment and the projections lead to adjustment of phenotype to increase fitness. In the model *Mount Grass* this projection results from the averaging of two key concept: memory and perception. The latter is relatively simple to understand and corresponds to the perceived resource availability computed as the mean potential exchange rate per unit of area (total leaf or root area) and per hour (the hourly measure is used instead of daily measure to simulate the ability of plant

PRODUCTION, AND RESPIRATION

TEMPERATURE EFFECT

CONDITION ESTIMATION

to perceive the photoperiod. This is an easy way of taking into account one aspect of seasonality without complicating the model. However, it also reduce the range of memory and its impact to determine the phenotype, as an additional information would be needed to define the optimum phenotype: the day length).:

$$light_{exp} = \frac{transp}{exchangearea_{ag}} \quad (4.23)$$

$$water_{exp} = \frac{Wpup}{exchangearea_{bg}} \quad (4.24)$$

(4.25)

The former is related to the species (or group) history and result from processes of selection and acclimation. It is the default projection of resource availability when the plant is not plastic.

$$light_{est}(t+1) = (1 - \tau).light_{exp}(t) + \tau.light_{memory}.daylength(t+1) \quad (4.26)$$

$$water_{est}(t+1) = (1 - \tau).water_{exp}(t) + \tau.water_{memory}.daylength(t+1) \quad (4.27)$$

Because these are supposed to be expected conditions for the future, other formulation can be used instead of an average that is likely to introduce a lag in estimations. For example the following equation allow for a more stable projection that better fits the slower process of plant physiology adjustments:

$$light_{est}(t+1) = ((1 - \tau_{react}).light_{exp}(t) + \tau_{react}.light_{est}(t))((1 - \tau_{amp}) + \tau_{amp}.light_{memory}).daylength(t+1) \quad (4.28)$$

with τ_{amp} and τ_{react} being respectively amplitude and reactivity where only τ_{amp} is used in the first equation. Such solution could limit sensitivity and phenotypic instability.

The estimation of external conditions as expressed here is then used to select the best allocation scheme during the allocation process. Limited here to levels of two resources (light and water), this estimation equation could be extended to other mechanisms such as herbivory risk, frost risk, humidity impact on water pressure deficit.

Allocation is primordial in plant development and ontogeny. The following paragraph detail the implementation of the plastic allocation in *Mount Grass*.

ALLOCATION

Maturity: For most of plants the development cycle is divided in two phases of different durations: the vegetative phase when plant growths organs to gather resources and product OM, and the reproductive phase when plant take advantage of these organs to accumulate carbon and invest them in reproduction mechanisms. Plants are considered mature (they switch from vegetative to reproductive phase) in *Mount Grass* when the phenologic variable has reach a species specific threshold. The phenologic variable can be either the age, the height, the biomass, degree.days, in the current version total living biomass is used as trigger for reproductive phase.

Allocation to supporting tissues: Even-though grasses do not grow tall vegetative parts like trees, some grow vertically and they are exposed to stronger

winds than most of forest. Therefore they need structural supports¹. Not all grasses grow stem, but they'll have stronger central vein in their leaves to structurally support the weight of leaves. In addition shoots and roots also need supporting tissues for water transport, for this reason the minimal mechanical support needed is calculated as a function of total living biomass:

$$\text{support} = \alpha \cdot (BM_{ag} + BM_{bg})^\gamma \quad (4.29)$$

where α and γ are allometry coefficients.

At each time step we must determine what fraction of new OM will be allocated to tissues growth while the remaining will support these need tissues. This leads to an optimisation problem numerically solved by the function `uniroot`.

¹This supporting tissue mechanic is also needed to avoid exponential growth rate.

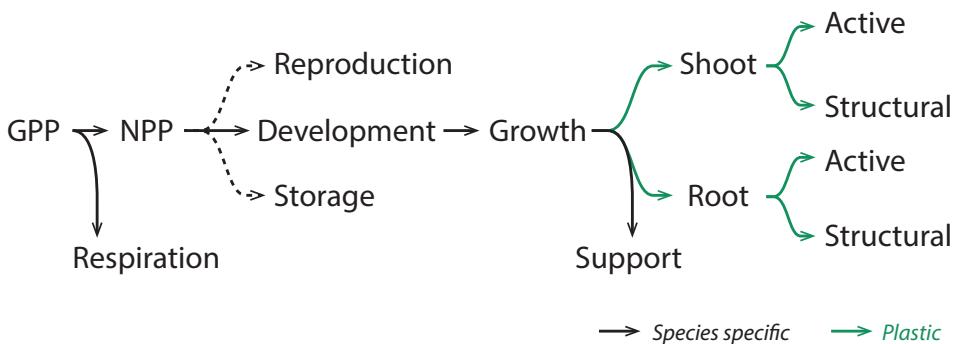


Figure 4.14: Allocation of produced organic matter to different processes and pools.

Allocation to organs: Allocation of produced organic matter is central in vegetation as it shapes the plant and define the strength of the different organs. There are multiple ways to model the distribution of produced organic matter between the plant organs. We believe that such mechanism has great impact on individual development and response to external conditions, and so on community dynamics. To explore the role of this mechanism, multiple options are implemented. The different allocation algorithms are summarised in table 4.3.

There are two major components in the allocation algorithm:

- the objective function;
- the plastic dimensions.

The *objective function*: it is the function that give an fitness estimation or gain metrics for any given phenotype. This function is used to compute the optimum phenotype (phenotype at which the function is evaluated at the maximum value), or rank alternative phenotypes².

The *plastic dimensions*: they are the dimensions along which the individual can move. The space defined by these dimensions is the phenotypic space within which each individual plant can look for an alternative phenotype. They do not necessarily fully define a phenotype since some dimensions of the individual's phenotype can be fixed³.

The objective of this step of the model is to solve the objective function with the unknown variables being the plastic dimensions (RSR, SLA and SRL). In case of simple equations an analytical solution could be used to find an optimum⁴.

²in this case, if not all possible phenotypes are tested, the solution might be only a local optimum. This is the case in *MountGrass*.

³either by shared parameters of species specific ones.

⁴under the condition that such optimum exists. The design of the model should ensure that.

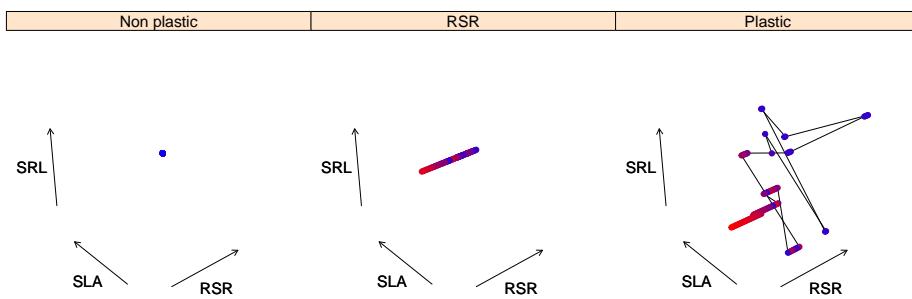


Figure 4.15: Trajectories of a plant in the trait space depending on the plastic dimensions explored.

However, because the analytical solutions are already non trivial and the model is likely to evolve, a numeric solving method is adopted. **Need to detail the random algorithm.**

Also make a note on multiple optimum and the choice for a 'gradient descent' type of algorithm. Also sensitivity at eraly stages

Algorithm	Objective	variable RSR	variable SLA-SRL	stochastic
No plasticity	—	○	○	○
Equilibrium	functional eq.	●	●	●
Eq-Fixed	functional eq.	●	○	●
Optimisation	instantaneous gain	●	●	●
Optim-Fixed	instantaneous gain	●	○	●

Table 4.3: Allocation algorithms implemented in *Mount Grass*

No plasticity allocation: this allocation is very similar to classic vegetation model where the biomass is allocated to the different carbon pools according to species specific parameters. But *Mount Grass* differs from other models by the order of the different steps of growth. In this model, the senescence comes between the allocation step and the resource competition-production steps¹. The partitioning coefficient are directly computed from species default trait to maintain the phenotype after senescence.

Fixed trait allocation: The fixed allocation supposes the allocation on OM to maintain trait values to fixed species specific values. The shoot:root ratio may however change to maintain functional equilibrium. The shoot root ratio is derived from the following equation of the functional equilibrium:

$$SLA \cdot BM_{ag} \cdot light_{est} = SRL \cdot BM_{bg} \cdot water_{est} \quad (4.30)$$

$$\frac{BM_{ab}}{BM_{bg}} = \frac{SRL \cdot water_{est}}{SLA \cdot light_{est}} \quad (4.31)$$

where $light_{est}$ and $water_{est}$ are the estimated resource availabilities.

Plastic trait allocation: Another approach to allocation is to try to optimize phenotype based on a fitness proxy. This proxy can be the sum of NPP, tissue turn-over loss and plasticity cost. But in a complex model like *Mount Grass*, plant performance is function of multiple aspects:

- individual organ efficiency;
- relative mass of each organ;

¹ see plastic allocation algorithm for explanation

- balance between organ water exchange activities.

And this could be extended to herbivory or frost risks. To take into account all these components, and take advantage of having all processes already made explicit by the implementation in the model, the daily processes of senescence and production are recalculated according to the **estimation of conditions** and the plant phenotype. This function is used to rank different alternative phenotypes (algorithm detailed below).

Plastic trait equilibrium: An alternative approach can be easily derived from the previous one and extend the principle of the first: the functional equilibrium with plastic traits. This approach consists in using the same algorithm as before but rank phenotypes with a function negatively correlated to the difference between estimated shoot and root activity. Such mechanism would nonetheless require the algorithm to look for close solutions within the allocation space to avoid convergence or drift from species strategy. Having non zero cost of plasticity in this approach should limit the drifting of the plant phenotype.

Fixed trait optimisation: This algorithm takes the idea of the optimisation algorithm but limits the plastic traits to the RSR ratio. If we can expect similar response than the fixed trait equilibrium if we suppose that the equilibrium is the main aspect of plant performance, global efficiency being considered in this case the result may vary.

Alternative phenotypes are computed from the actual phenotype and random uniform distribution of available organic matter to the main active and structural carbon pools of the plant.¹ ... This algorithm has the advantage of being relatively cheap compare to other optimization functions, however its performances are variables and it is very sensitive to the number of samples used. As a consequence there is a trade-off between model stability and performance as a function of number of samples (*i.e.* alternative phenotypes) considered.

PLASTIC ALGORITHM

¹ talk about the order senescence production, and the way exchange rates are computed.

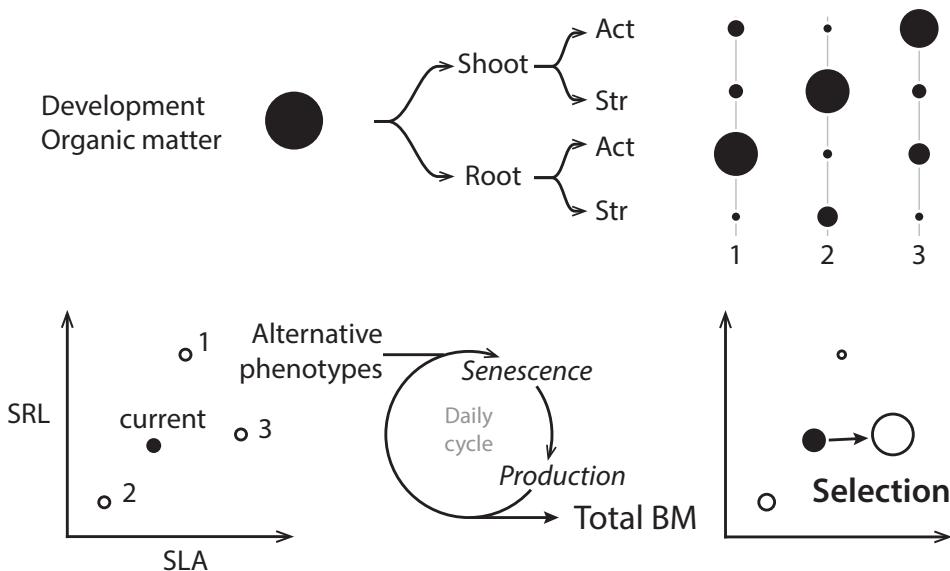


Figure 4.16: Algorithm for the evaluation and selection of randomly generated alternative phenotypes.

The limits and costs of plasticity has long been discussed in related litterature. If *MountGrass* is intended to be used to examine ecological costs and limits, it has to include physiological aspects of plasticity limits. There are two physiological

PLASTICITY COST

processes involved in the mechanism of altering a phenotype based on changes in external conditions: sensing and signalling. 'Sensing' relates to the capacity of the individual to perceive environmental conditions. This is related to capacity of the individual to perceive the environment and should therefore be considered constant over time. To take into account the cost of precise sensing, the first component of the plasticity cost is proportional to τ .

The other component is related to the capacity of the plant to transmit this knowledge of conditions to change the development plan toward a new phenotype. This cost is proportional to the carbon based distance (calculated as the difference between proportion of active tissues) between the default phenotype and the alternative (during allocation algorithm) or current phenotype.¹

Plasticity cost is the sum of both component and is proportional to the total biomass since most of tissues should have the appropriated cell machinery and are affected by plasticity.

¹ We could imagine cost based not on the default, but previous phenotype, but it would have lead to large phenotypic shifting and convergence.

$$pc_{maintenance} = (1 - tau) * pc_m \quad (4.32)$$

$$pc_{plasticity} = d_{traits} * pc_p \quad (4.33)$$

where d_{traits} is the euclidean distance between default phenotype and the alternative phenotype in the space defined by the proportion in active tissue for shoot and for roots.

Plasticity in trait suggests that trait values are modified in time. Because plants are described by single values (e.g. one SLA value for all leaves), this values must be updated after the plastic allocation. This values could be updated as average of old tissue value weighted by old biomass and new tissue value weighted by the freshly produced biomass. This however would work only if active on structural tissues ratio were linearly linked to others traits. This is not the case, it is then simpler to consider that organs have uniform active and structural distribution. This hypothesis suggests that whenever the allocation scheme changes, old tissue reallocate their own biomass to follow the new scheme. Nevertheless, to avoid full plasticity allowed by this hypothesis, the changes in trait carbon pool sizes is limited by the produced biomass available for plant development.

following the following survival probabilities:

From this, supposing homogeneous distribution of active and structural tissues within an organ allow to directly link the size of the carbon pools to average traits by the following relationships:

TRAIT UPDATE

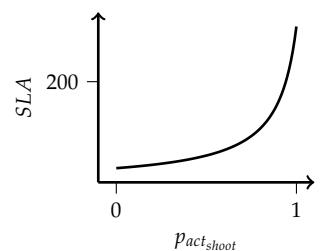


Figure 4.17: Specific Leaf Area as a function of the proportion in active tissues in shoot

$$SLA = \frac{1}{(th.p_{act_{shoot}}.\rho_{as} + th.(1 - p_{act_{shoot}}).\rho_{ss}).V_t} \quad (4.34)$$

$$SRL = \frac{1}{(sr.p_{act_{shoot}}.\rho_{ar} + sr.(1 - p_{act_{shoot}}).\rho_{sr})} \quad (4.35)$$

Senescence is the process of ageing of tissues. This process usually occurs at the scale of an individual organ (e.g. a leaf), however *Mount Grass* does not consider organs independently because it would be complex and computationally expensive to follow multiple leaves and roots for all individuals. So the process is considered homogeneous over all tissues. To emulate the senescence process senescence is calculated from the tissues lifespan, giving :

SENECENCE

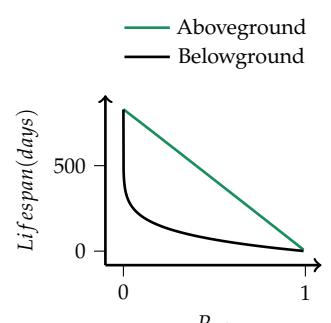


Figure 4.18: Lifespan of organs as a function of proportion of active tis-

$$sen_{leaf} = \frac{1}{LLS} \quad (4.36)$$

$$sen_{root} = \frac{1}{RLS} \quad (4.37)$$

Because *Mount Grass* does not contain any mechanism preventing plant from growing only active tissues¹, it is necessary for this cost function to make this strategy unreliable. This is then expressed as follow:

$$LLS = LSS_{s0} * (1 - p_{act_{shoot}}^{LSS_1}) \quad (4.38)$$

$$RLS = LSr_{s0} * (1 - p_{act_{root}}^{LSR_1}) \quad (4.39)$$

where *LLS* and *RLS* are respectively the leaf and the root lifespans calculated as negative log-linear relationships with proportion of active tissue.

Root senescent tissues disappear from the system. Information about senescent aboveground biomass is stored, but senescent biomass effect of light competition is ignored in this version because as it is implemented senescent tissues appear early in plant development and have large negative effect on light absorption.

To the natural senescence and artificial cost of having only active tissue, an additional component can be added to the turn-over rate: the negative NPP. In case of negative NPP the biomass will be taken from the already allocated following the shoot root ratio. This can lead to a lower overall productivity (negative growth during unproductive periods) but also changes in the equilibrium if tissue have different efficiencies.

Death is modelled as in Reineking [reineking_environmental_2006]. Age and desiccation (negative NPP) are the two reasons why a plant can die. The two death mechanism are simulated by independent random lotteries following the following survival probabilities:

$$P_d = \exp \left(- \left[\left(\frac{des}{\alpha_d} \right)^{\gamma_d} - \left(\frac{\max(des - 1, 0)}{\alpha_d} \right)^{\gamma_d} \right] \right) \quad \text{if } NPP \leq 0 \quad (4.40)$$

$$= 1 \quad \text{otherwise} \quad (4.41)$$

$$P_a = \exp \left(- \left[\left(\frac{age + 1}{\alpha_a} \right)^{\gamma_a} - \left(\frac{age}{\alpha_a} \right)^{\gamma_a} \right] \right) \quad (4.42)$$

State of dead individuals is stored until the end of the season when seeds are stored in the seed bank. Seeds of dead individual then join other seeds.

Sexual & clonal reproduction: reproduction is handled at the end of the season. To limit the number of parameters reproduction is limited to the division of the invested biomass in reproduction by the species specific seed biomass into a round number of seeds (the number of seed per plant could also be a differentiation axis). Clonal reproduction is not explicitly represented but can be mimic with bigger seeds and by adding a dispersion process around the parents. The seeds then are added to a potential seed-bank. This potential seed-bank is sampled, after eventual invasion, and merged with the existing seed-bank.

¹ it was intended to make the WUE negatively correlated to the amount of structural tissue per area.

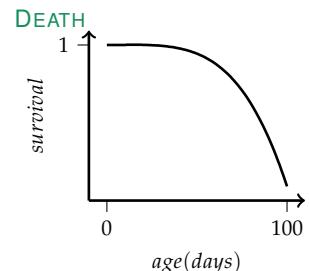


Figure 4.19: Age related survival probability function

REPRODUCTION & PERSISTENCE

Persistence Some grasses are perennial and persist over the cold season. This is allowed in the model by investment in storage tissues instead of reproductive tissues. At the end of the season, marked by the first snowfall, these plants (with non-null storage biomass) loose their living and supporting biomass, but will regrow from a large pool of store organic matter.

Explore management effect on the community is one of the aim of the *Mount Grass* model. The management of mountain grassland will be explore only of the aspect of biomass removal, as productivity changes can be explore by changing the parameters value as the nutrients are not explicitly modelled. The management sub-model is not detailed here but it is based on the mapping of biomass and target trait (e.g. fraction of structural biomass as proxy for digestibility). Both cutting and grazing can be modelled but require management plan in the form of calendar of management operation and a cutting height or harvest objective.

GRAZING/CUTTING

4.4 Limitations and problems

4.4.1 Link to the real world and data

The generalized framework introduced in *Mount Grass* allows to create a rich community in a high number of dimension strategy space, it however comes with downsides.

One of the first problem is that some parameters (not explicitly detailed here) are hard to access (e.g. tissue density of active, or structural, tissue). It makes the calibration long as the incertitude for some parameters is very high. This is problematic when calibration is made difficult by a large execution time (see subsection below).

Another issue with such model is that the high dimensionality of the species strategy space allows a lot of different strategies that are not viable. This could be overcome by selection mechanism over multiple plots, but again require a lot of simulation. Moreover, there are dependencies between viable strategies and parameter values that makes it hard to restrict meta-community to viable species to set-up calibration runs.

It is possible to extract summary statistics from the model output and compare them to information from collected data making calibration and community analysis easy. However going from the data to feed the model is harder, indeed without a great knowledge of a species it is hard to define its representation within the model framework. To do so would require the knowledge of the plasticity capacity to set the reactivity, anatomical traits to define default ratios of active over structural tissues, and climatic niche to define the *a priori* estimation of external conditions. Without making direct association with real species, it is possible and interesting to try to reproduce some strategies and explore their response to various conditions.

4.4.2 Technical problems

The model is implemented in R with some limiting function using RCPP to speed up the process. Simulations are fairly slow compare to theoretical C++ equivalent

code. The main problem is in the choice of the data structure. Indeed agents are stored in data.frames that are often modified with the `mutate` function, that makes the implementation much easier and the code readable, but slow down the execution due to constant condition checking on operations. This makes calibration routine methods almost impossible to use as they demand a very number of runs to be efficient.

The slowness of the model also limit to simple algorithms for the research of favourable positions in the allocation space.

IV

INDIVIDUAL PERFORMANCE: STRATEGY AND PLASTICITY

1 MODEL PROPERTIES AND INDIVIDUAL RESPONSES

Question I try to answer: (use of schematics ?)

1.1 Parametrisation and sensitivity analysis

Obj: give confidence in the model, demonstrate it is able to reproduce simple growth pattern.

Obj2: have a better idea of plasticity effect on growth. growth plastic and non plastic parameter filtering: can we distinguish species thanks to species specific parameters instead of shared parameters.

does plasticity make it easier ?

Impact of plasticity related parameters.

1.1.1 Method

Pot data consists in total biomass and root shoot ration (RSR) data of ... species grown in pots by Peterson and al. (peterson). This old dataset has the advantages of being grass species grown in a described steady environment with two conditions of watering with measures of essential components of growth: biomass and RSR. The inputs used to simulate these experiments are detailed in appendix.

POT DATA

Bayesian calibration could not be used for the model considering the number of parameters and the simulation time. A filtering process has been implemented in R. Parameters are sampled following the LHS method (from lhs package) within parameter ranges (described in table ...) defined from the literature, and constraints dictated by desired behaviours from the model. When necessary the sample is log transformed. Because of strong relationship between exchange rate parameters and cost of exchange area, exchange rates parameters are expressed on a mass basis for sampling then transform to an area basis for the model. Photosynthetic activity is defined relatively to the water uptake activity and water use efficiency (WUE) to avoid extreme root shoot ratios.

INDIVIDUAL CALIBRATION PROCESS

Once generated a first filtering is applied to save simulation time and avoid unrealistic trait values (see table for ranges extracted from LES data in alpine biome) that are not tested against calibration data.

Once the parameters transformed and filtered, simulations matching growth conditions in Peterson experiments.

Generated data from finished simulations (i.e. plant lives until the end and do not exceed model's internal size limits) are then compared to experiment data

species by species. Parameters of logistic distribution are computed from species means and standard deviations for RSR and total biomass. The use of this distribution form is justified by the intrinsic form of RSR measure and the need to reject negative values for total biomass. A parameter set is accepted for one species if it is within a 95% range of the calculated distribution for both RSR and total biomass in wet and dry conditions.

Include chart to show how calibration was made.

1.1.2 Results

. Calibration filtering results in the selection of n parameter sets over m pre-selected parameter sets. Accepted sets are distributed among the 11 species of the dataset like presented in the table. Species A, B and C are the most numerous. sensitivity analysis. The models about seems to be sensitive to the following parameters: r_1 , β_0 , P_{max} , u_{max} , k_{or} , ρ_{ar} . The four first parameters are related to global resource availability and directly related to growth rate, while the second and the last three are related to the below-ground resource foraging and exchange rate. Total biomass is particularly sensitive to exchange rate parameters, but also tissue construction cost. (not shown)

INDIVIDUAL CALIBRATION

Plasticity does not change the acceptance rate in any form (only slight increased from 0.26% to 0.38%). Despite non overlapping (around respectively and third and a quarter of accepted parameter sets are shared between non plastic and plastic calibration) the distribution of not shared parameter sets are very similar and does not show any clear pattern.

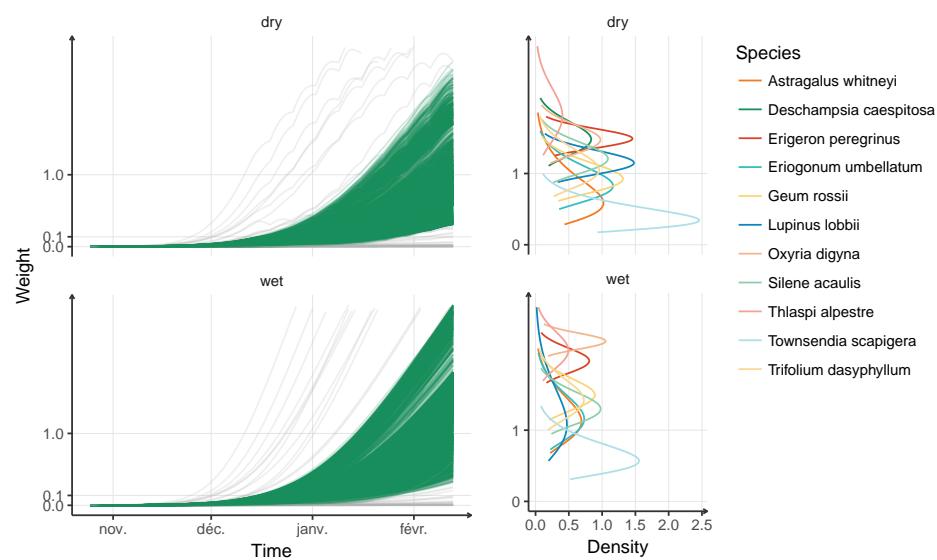


Figure 1.1: Comparison of simulated weights with distribution of weights of real alpine species for contrasting conditions.

Acceptance rate without plasticity: Acceptance rate with RSR plasticity for equilibrium:

Change of relationship between parameters and acceptance rate -> none

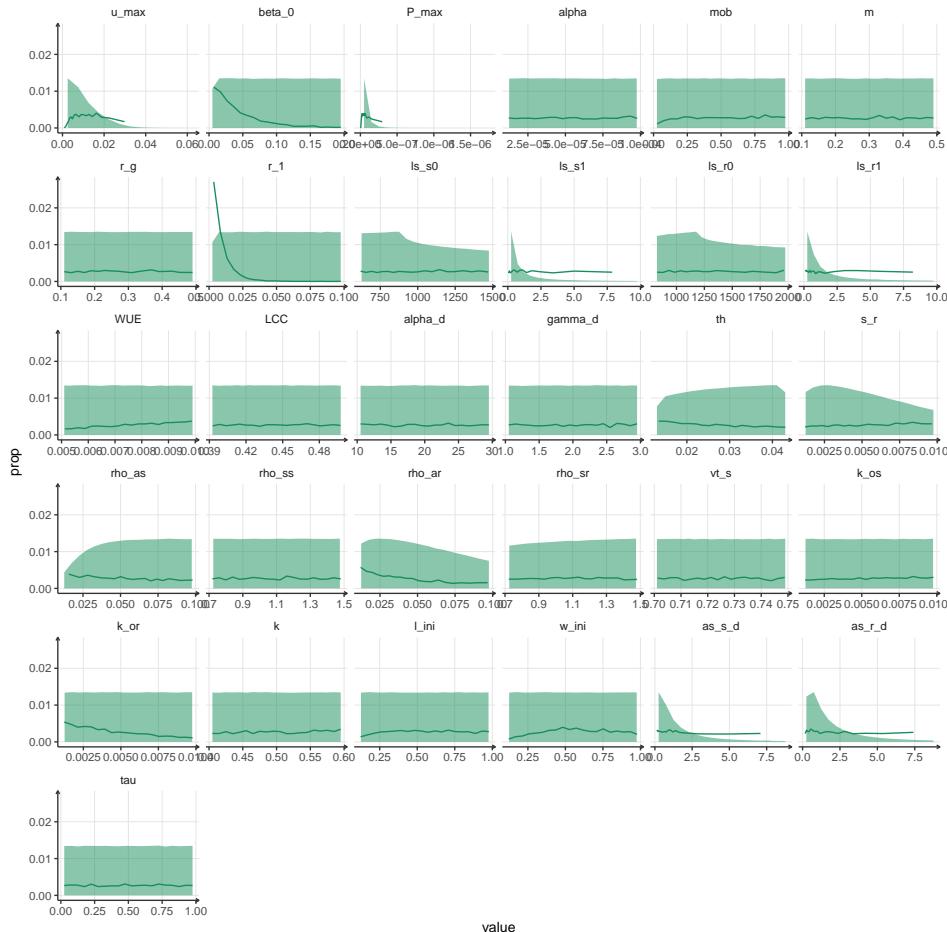


Figure 1.2: Acceptance rate per parameter for individual growth. No plasticity

Figure 1.3: Acceptance rate per parameter for individual growth. RSR plasticity

	species	nb accepted	rate
1	Silene acaulis	227	0.02
2	Trifolium dasypodium	271	0.03
3	Geum rossii	51	0.01
4	Thlaspi alpestre	342	0.03
5	Deschampsia caespitosa	0	0.00
6	Eriogonum umbellatum	500	0.05
7	Townsendia scapigera	593	0.06
8	Astragalus whitneyi	1570	0.16
9	Lupinus lobbii	678	0.07
10	Erigeron peregrinus	1	0.00
11	Oxyria digyna	0	0.00

	species	nb accepted	rate
1	Silene acaulis	396	0.04
2	Trifolium dasypodium	317	0.03
3	Geum rossii	72	0.01
4	Thlaspi alpestre	360	0.04
5	Deschampsia caespitosa	0	0.00
6	Eriogonum umbellatum	805	0.08
7	Townsendia scapigera	930	0.09
8	Astragalus whitneyi	2424	0.24
9	Lupinus lobbii	868	0.09
10	Erigeron peregrinus	0	0.00
11	Oxyria digyna	0	0.00

accept = f(tau)

PCA reveal that sensitive parameters are also the dominant variables in the main components of the component analysis of the accepted parameter sets. Species cannot be distinguished on the two main component space, neither on 1 or 2D species specific parameters space (l_{ini} , w_{ini} , w_{ini} vs l_{ini} , as_s_d , as_r_d , as_r_d vs as_s_d) despite small variations in distribution shapes between species.

Figure 1.4: Importance of the random forest to explain filtering outcome (accepted or rejected) of a balanced sample of parameter set between all tested (all accepted parameters and an equivalent sample in rejected parameters). RSR plasticity is reproduced, but only for one species, not full strategy space.

1.1.3 Discussion
Sensitivity of different variable to the parameters make sense and align with the two criterion of selection (that work with the independence of trade-off).

Root shoot ratio changes were not captured by the model. The structure of the plasticity mechanisms does not work with the given watering cycle. Needs to add one parameter for reactivity.

ACCEPTANCE RATE

SENSITIVITY ROOT SHOOT RATIO AND PLASTICITY GROWTH AND STRATEGY SPACE

Figure 1.5: Accepted parameters set for plastic individual growth calibration filtering on the two main components of PCA.

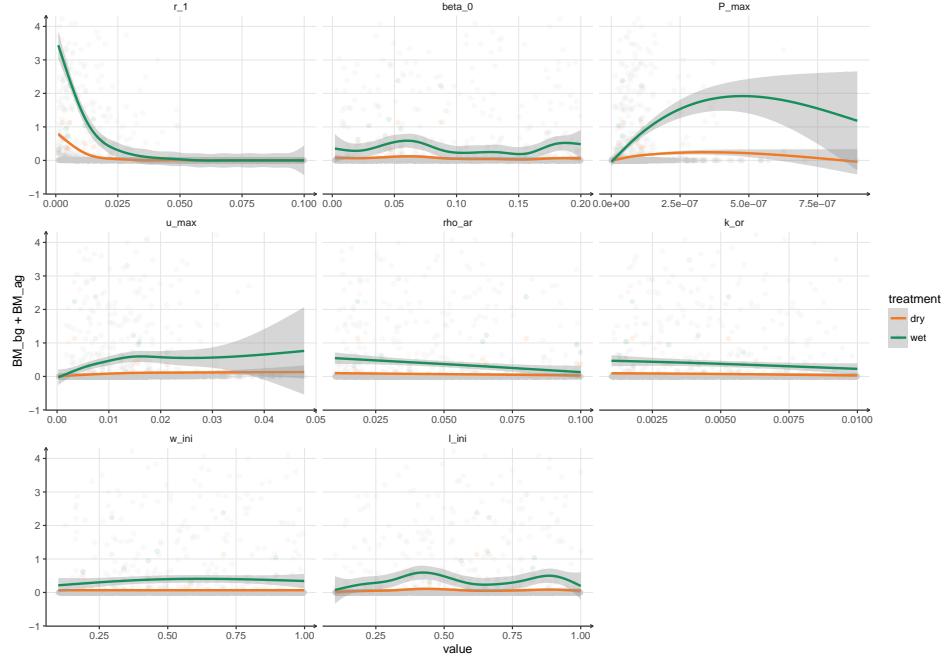


Figure 1.6: Main parameters effect on the total plant biomass. No plasticity.

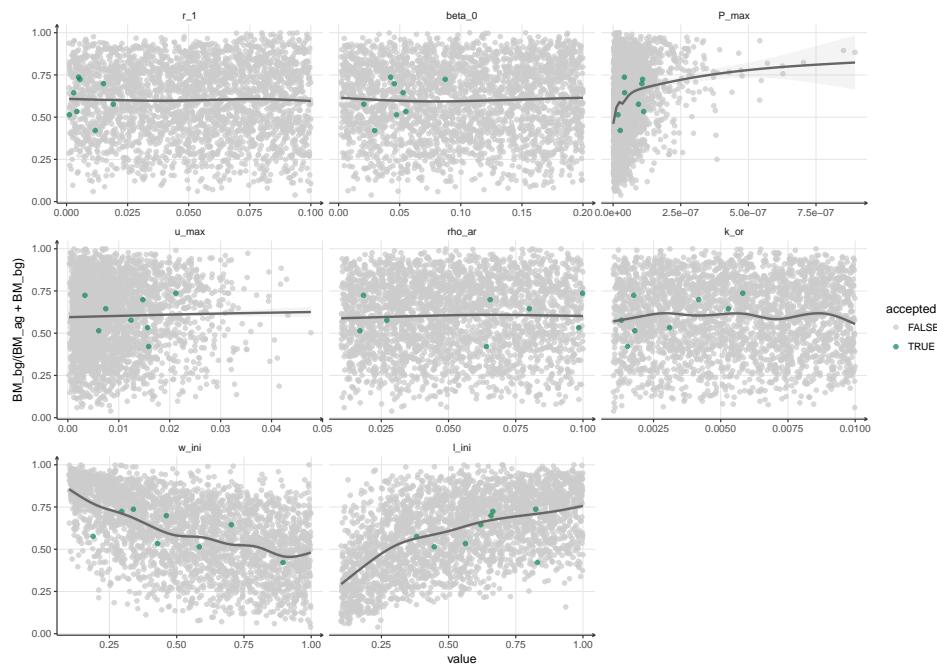


Figure 1.7: Main parameters effect on the total plant Root Mass Fraction (RMF). No plasticity

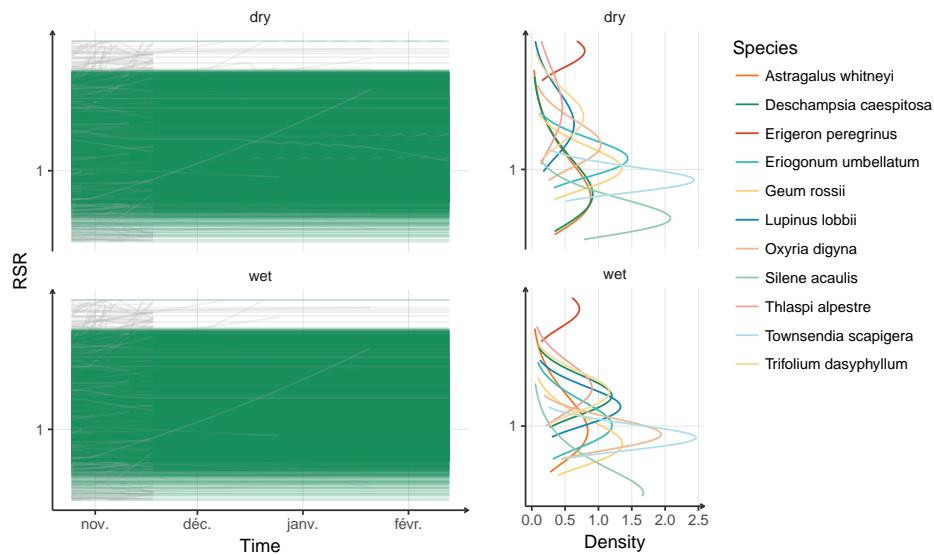


Figure 1.8: Comparison of simulated values (over time) of RSR with real species RSR in two contrasting conditons. Because there is no plasticity or ontogeny, the simulated plant do not express any chagnes in RSR

1.2 Individual level behaviour and properties

Question I try to answer: (use of schematics ?)

1.2.1 Method

To further reduce the number of parameter sets considered, we proceeded in an additional filtering step. Because the first filtering was conduced for only one strategy over the whole 4D strategy space (l_{ini} , w_{ini} , as_s_d , as_r_d) it is necessary to verify that other strategies do not lead to potential Darwinian demon. This should be limited by the choice of priors, while at the same time promoted by the selection of parameters increasing growth to counter balance potential unfitted strategies¹.

All common parameters for pot simulations. i.e. weather, soil, default species parameters.

1.2.2 Results

1.2.3 Discussion

include figure from "showtime" data to illustrate the differences between allocation algorithms.

Allocation rules are extremely important as they reduce the phenotypic space explore. Without even considering plasticity. Need a good understanding of the performance within the phneotypic landscape. Plus there is a need for alignment between starting phenotype and endpoint. Will also affect how plasticity is driven.

... nothing here, the idea was to show that the "strategy" of the species conduce to slow and fast archetypes.

Allocation trade-off allow for strategies from the fast-slow spectrum to arise, independently for shoot and root, in coherent framework. Potential effect of other strategy axis can be analysed alongside this trade-off, even if

STRATEGY DIVERSITY FILTER-
ING

¹ Better do that beforehand than af-
ter... But I guess it's too late now.

SIMULATION SET-UP

COMPARISON OF DIFFERENT
ALLOCATION ALGORITHM
MEMORY EFFECT ON PHENO-
TYPE
ALLOCATION RULES, PLASTIC-
ITY AND PERFORMANCE

FAST SLOW STRATEGY AND AL-
LOCATION TRADE-OFF

they affect composite traits like SLA or SRL.

MEMORY AND PHENOTYPES

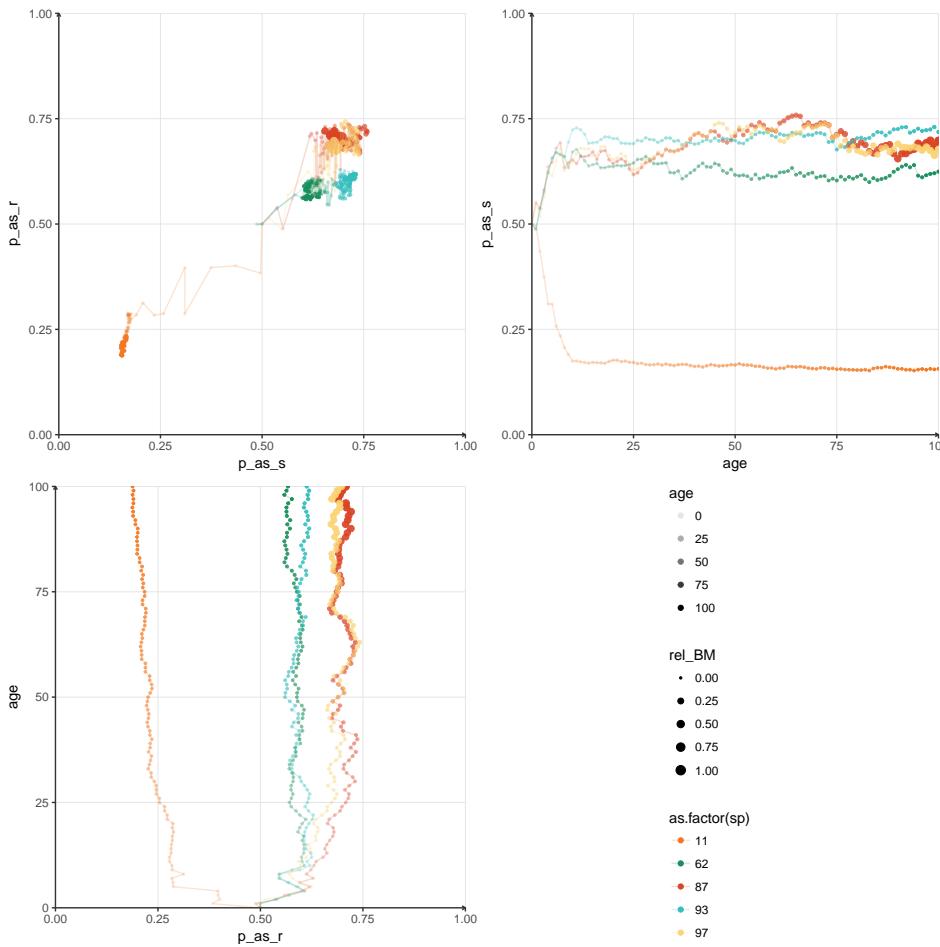


Figure 1.9: Trajectories along time in the strategy space of 5 plants with different memories. After 10 days, all plants have converged toward the estimated optimum.

Strong effect with saturation: optimum.

There is also a positive effect, that is smoother and have lower values. Same pattern for light memory respectively with proportion of active tissues in shoot, and proportion of active tissues in roots. This symmetry and the curves shapes suggest that resource related organ is more sensitive and that "apparent" increase in resource availability promote more exploitative strategy.

For each parameter set the alpha shape of the volume could be drawn to have an idea on how parameters impact potential functional diversity.

Memory is a strong enough driver to control plant organ strategy. The effect of overall activity should be studied too and considered if memory is used to determine the default phenotype.)

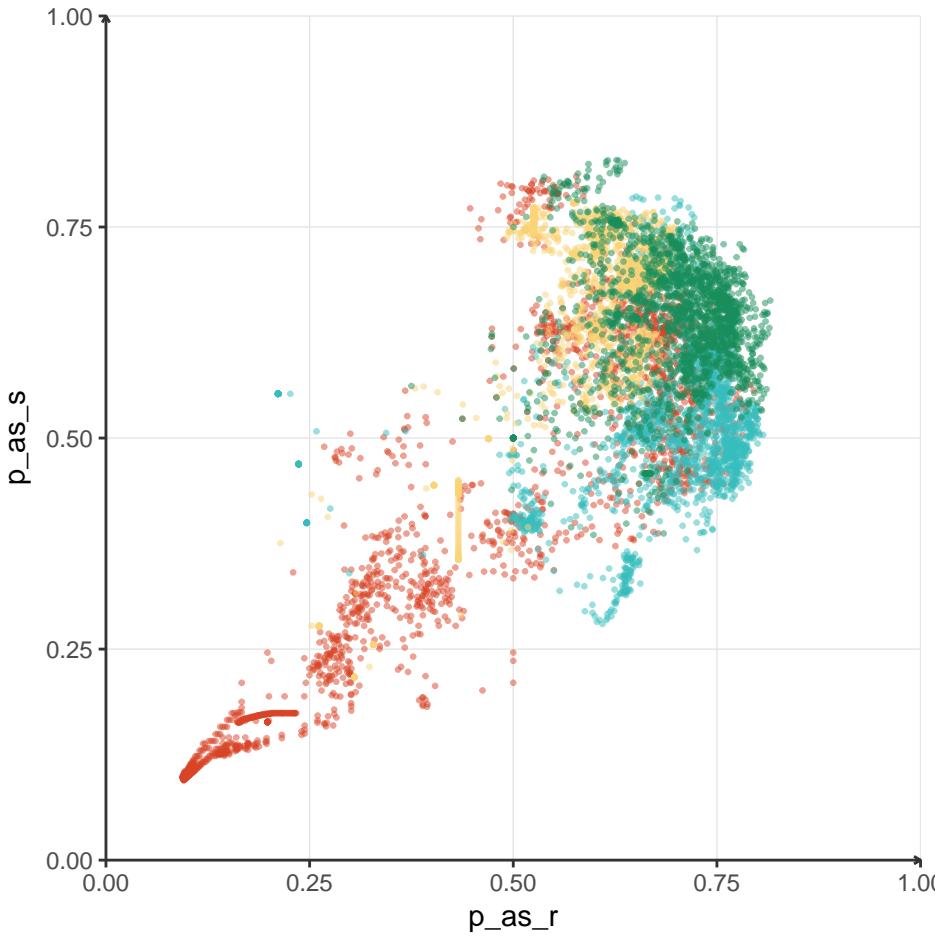


Figure 1.10: Impact of species memory on final phenotype in case of fully plastic allocation. Each point corresponds to a plant phenotype for a memory syndrome for a given parameter set. Colours denote the memory syndromes.

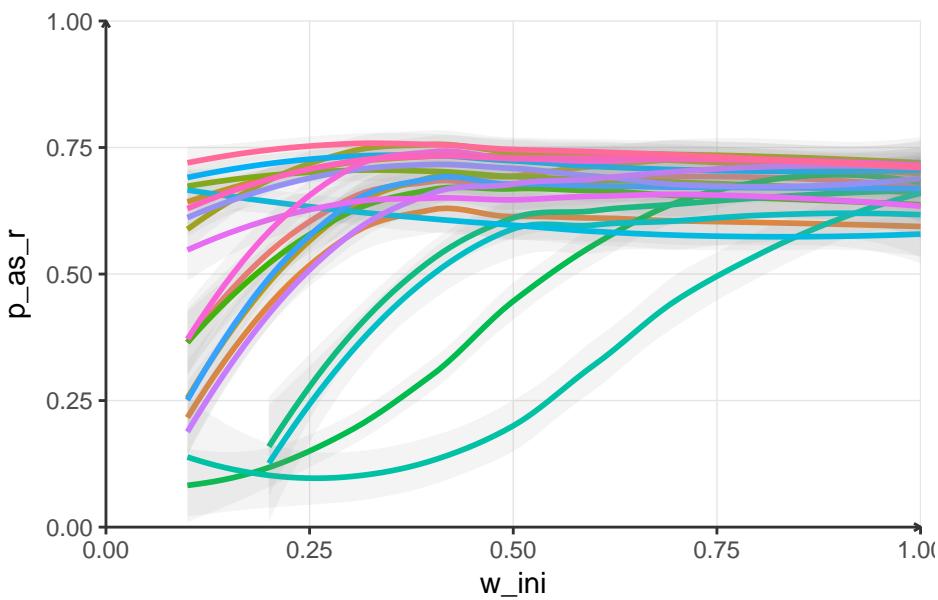


Figure 1.11: Effect of memory of water availability on proportion of active tissues in root.

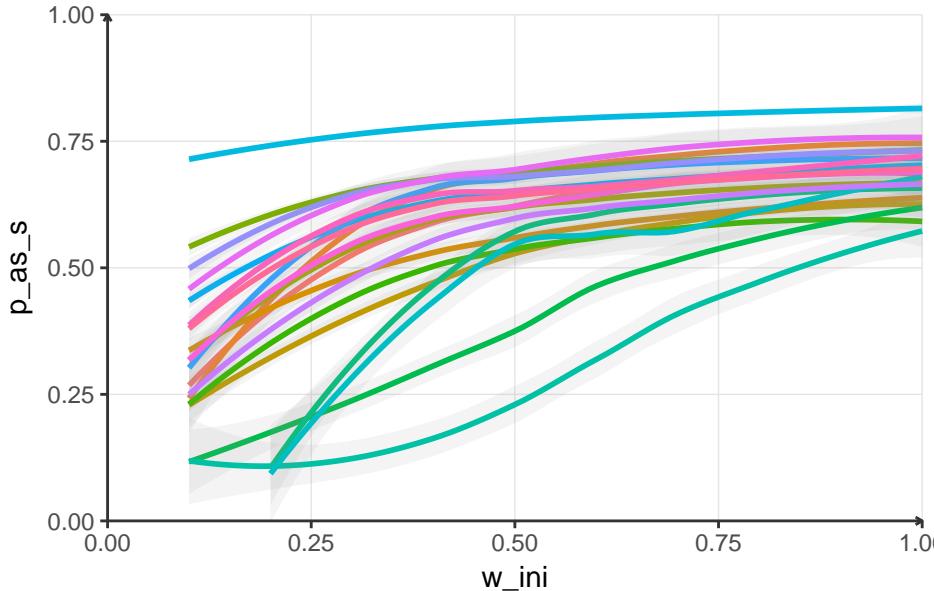


Figure 1.12: Effect of memory of water availability on proportion of active tissues in shoot.

2 INDIVIDUAL PERFORMANCE, PLASTICITY AND VARIABLE CONDITIONS

2.1 Individual performance: between strategy, memory and plasticity

Question I try to answer: (use of schematics ?)

2.1.1 Method

Idea, having an idea on how the

STRATEGY SPACE SAMPLING

Two climatic conditions. ... Watts per square metters and .. mm, days of 15h. Low resource availability conditions correspond to a reduction by a factor 4 of resource influx, but the day length was conserved.

SIMULATION SET-UP

2.1.2 Results

Increase in average biomass. The biomass profile is not visualised, but following figures suppose fitness equivalence as less than 10% under the maximum local biomass.

2.1.3 Discussion

Somehow I need to talk about the cost of being wrong. Can be observe in the delta heatmap on delta strat and delta w-ini: in this case there is less impact of being wrong of memory if you're good with strategy, because your not in differ-

CONVERGENCE TO SUBSPACE

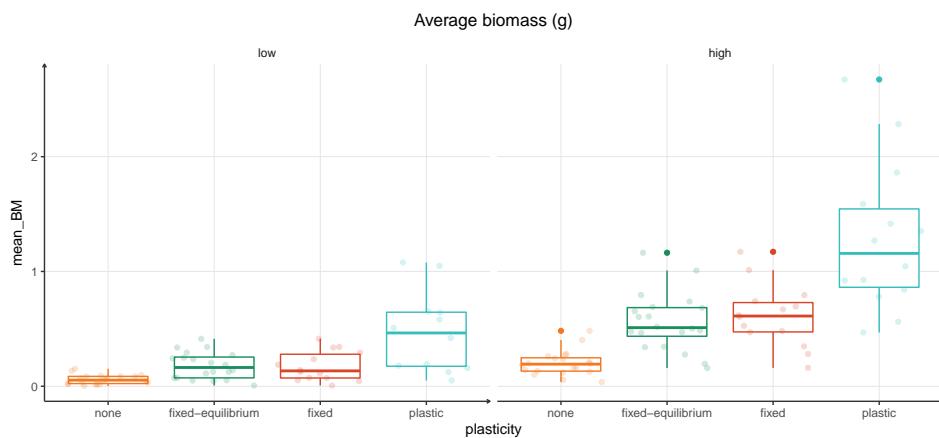


Figure 2.1: Effect of plasticity and resource availability on average biomass of living species.

ent conditions...

The phenotypic plasticity implemented in *MountGrass* improve the relative performance of multiple strategies by concentrating the plant toward a subspace of higher performance for most of plants. Convergence to a smaller subspace can be assimilated to reduction in phenotypic diversity, but it reduce performance heterogeneity and should favour local plant diversity. Meta-community diversity is however reduces by the reduction of potential axis for niche differentiation. Plasticity costs and limits should play major role in the balance between these mechanisms. Community level simulations are needed to further understand the cumulative role of competition, spatial and temporal variability and plasticity costs on phenotypic plasticity influence on plant community dynamics.

2.2 Plasticity and variability of conditions

Question I try to answer: (use of schematics ?)

Phenotypic plasticity

Kichenin (different response to gradient) Doesn't work in this framework: Not so sure about that: depending on your initial memory plants show directional changes toward one phenotype. Yeah, but they should have converged for other conditions too... So, it doesn't work. Might be explained by:

IMPROVEMENT IN VARIABLE
CONDITIONS
HETEROGENEITY OF RE-
SPONSE

- different conditions: because heterogeneity and habitat selection, or changes in competition hierarchy;
- different ways to tackle changes on one dimensions;
- different weights between mechanisms impacting composite traits, because of the different traits.

V

COMMUNITY DYNAMICS

1 COMMUNITY LEVEL PARAMETRISATION

1.1 Method

New random parameters sets (with no species specific parameters) for population dynamics and competition specific parameters (see table ...). Shared parameters previously selected were used. Sequence of around 300 year for each site. Parameters were selected by...

FIELD CALIBRATION

Field data has been collected between years 201 .. and 201 by Claire Deleglise and al. () .

FIELD DATA

Weather data has been computed by the MeteoFrance model SAFRAN by ... using GPS coordinates and slope, azimuth and horizon computed from a "MNT". These parameters were also used by the model CROCUS to compute snow accumulation and melting. These high frequency data (resolution under 1h) have been average daily and used to compute input variables for *Mount Grass* .

WEATHER DATA

1.2 Results

Simulations done. Need to illustrate the results.

On stability and on diversity (functional and species)

EFFECT OF PARAMETERS

Random forest approaches like sensitivity analysis at individual scale.

Is there a selection of some parameters ? Are there ecological trade-off (resource use strategy and reproduction) emerging from the model ?

ECOLOGICAL TRADE-OFF ?

2 PLASTICITY: IMPACT ON SPECIES FITNESS AND DIVERSITY

2.1 Method

2.2 Results

Need to run the simulations. Script is almost ready, parameters are filtered from previous step.

2.2.1 Plasticity: a winning strategy ?

GENERAL BEHAVIOR

Are plastic species more selected than the other ? Probably a bell-shape curves

2.2.2 Effect on coexistence

VI

SYNTHESIS & OUTLOOK

1 SYNTHESIS

Point out the novelty, achieved work

In this work, but also because of the improvement of molecular biology, and the deeper and deeper dive ecology is doing within individual, the limits of species are fuzzy (started with trait and the introduction of continuity). At some point, there will be a need for a way to go back from the a space of numerous continuous dimensions to the species. Also, understanding species as evolving 3D objects, where the different aspects of intra-specific variations play different shaping roles.

2 OUTLOOK

Further reading, thinking and rambling about what's developped in the papers.

3 EXTENSIONS

THIS SECTION IS MEANT TO INCLUDE THOUGHTS AND IDEAS ON HOW TO EXTEND *Mount Grass* BUT THAT COULD NOT BE INCLUDED IN THE FIRST VERSIONS OF THE MODEL FOR VARIOUS REASONS. DESPITE NOT BEING INCLUDED, THESE EXTENSIONS ARE INTERESTING FROM A SCIENTIFIC OR TECHNICAL POINT OF VIEW, AND I HOPE THESE NOTES CAN BE USEFUL TO ANYONE INTERESTED IN *Mount Grass* OR INDIVIDUAL BASED VEGETATION MODELLING.

As seen previously in chapter , the emergence of trade-off in growth strategy in the actual framework actually rely on a strong genetic constraint over plant plasticity. Indeed, without plasticity cost and low reactivity there would be a high rate of phenotypic convergence of individuals from different species. This is explained by the existence of optimum carbon partitioning (for a given size) in a stable environment. The coexistence of different resource use strategies (exploitative vs conservative) is allowed only through temporal variations and non equilibrium state. This is quite common since a lot of models will predict rapid dominance of one entity in case of equilibrium (need references here).

Multiple questions arise from this observation: are the conclusions of this work still interesting in the understanding of the coexistence mechanisms? (I hope I did convince you in the dedicated part of this document, see .. for more details), is it possible to see coexistence of multiple strategies in a temporally stable environment? how can we produce trade-off by including only one more resource?

In the following paragraphs I try to answer these questions with theoretical arguments and suggestions on how to integrate them in *Mount Grass* .

Coexistence mechanisms are listed and detailed in the introduction of this thesis (see chapter ??). Here I focus on the efficiency of tissues... Nitrogen based, why coexistence ? different phenotype correspond to different limiting resources and for different resource availabilities, different phenotype will optimize the return cost of tissues.Nitrogen also allow the model to have an extra dimension into strategy: WUE (local scale) versus NUE (global scale) (element of reflexion in Maire's thesis).

Its also can be related to

Original idea was to have specific carbon pools for different function, and weight the relative allocation based on gain projections.

3.0.1 Resistance carbon pools

