# Deep Learning: Deep Learning for Natural Language Processing

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#### Question 1

Let's show that

$$W^* = \underset{W \in O_d(\mathbb{R})}{\operatorname{argmin}} \|WX - Y\|_F = UV^T, \text{ with } U\Sigma V^T = \operatorname{SVD}\left(YX^T\right)$$

Let  $W \in O_d(\mathbb{R})$ . We first notice that :

$$||WX - Y||_F^2 = ||WX||_F^2 + ||Y||_F^2 - 2\langle WX, Y \rangle$$
  
=  $||X||_F^2 + ||Y||_F^2 - 2\langle WX, Y \rangle$   $(W \in O_d(\mathbb{R}))$ 

Where  $\langle WX, Y \rangle = \text{Tr}\left((WX)^TY\right) = \text{Tr}\left(W^TYX^T\right)$ . Hence,

$$\begin{aligned} \underset{W \in O_d(\mathbb{R})}{\operatorname{argmin}} & \|WX - Y\|_F = \underset{W \in O_d(\mathbb{R})}{\operatorname{argmin}} \|WX - Y\|_F^2 \\ &= \underset{W \in O_d(\mathbb{R})}{\operatorname{argmax}} \operatorname{Tr} \left( W^T Y X^T \right) \end{aligned}$$

Let  $U\Sigma V^T$  the SVD decomposition of  $YX^T$ .

$$\begin{aligned} \operatorname{Tr}\left(W^{T}YX^{T}\right) &= \operatorname{Tr}\left(W^{T}U\Sigma V^{T}\right) \\ &= \operatorname{Tr}\left(V^{T}W^{T}U\Sigma\right) \end{aligned}$$

Let  $Z = W^T U \Sigma$ . Z is orthogonal as the product of orthogonal matrices. Tr  $(Z\Sigma) = \sum_{i=1}^n Z_{i,i} \Sigma_{i,i}$ .  $(\Sigma_{i,i})_i$  are non-negative and Z is orthogonal hence the previous quantity is maximized if  $Z_{i,i} = 1$  which means that  $Z = I_n$ . We then conclude that  $W^* = UV^T$ .

# Question 2

We test the sentence classification task using bot the average of word vectors and the weighted-average based on the idf.

We get the following results:

Dataset	Average	IDF
Train	0.4992	0.4993
Dev	0.4405	0.4233

We get slightly better results using the average of word vectors.

A classifier based on SVM was also trained and achieves similar results. Random forest was also tested, but even after tweaking the hyperparameters, it was still overfitting the train dataset.

# Question 3

We use the categorical cross-entropy loss function :

$$-\sum_{o=1}^{N}\sum_{c=1}^{5}y_{o,c}\log(p_{o,c})$$

Where:

• N is the number of observations

- y is the true distribution :  $y_{o,c} = 1$  if observation o is of class c.
- p is the predicted distribution i.e. the output of the model.  $p_{o,c}$  is the probability of observation o to be from class c according to the model.

### Question 4

We train a classifier based on a the LSTM model. Without using pretrained embedding vectors, the model is quite far from beating the logistic regression. Also note that it overfits very quickly: to avoid this the model was just trained on 2 epochs. See Figure 1. After 2 epochs, the dev loss starts to increase.

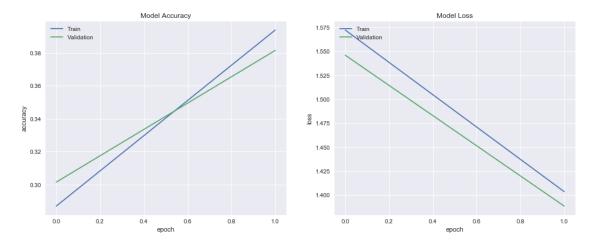


Figure 1: Loss and accuracy for the LSTM model

# Question 5

Given the poor results that we get from simply using a LSTM, we decide to use the pretrained Fasttext vectors as embeddings. We still use LSTM cells, but we put a 1D convolutionnal layer before, which gives a convolutionnal LSTM network. Another nice advantage of this solution is that with the pretrained embeddings and the maxpool layer, training is much faster.

See Figure 2 for the accuracy and loss plots. This models also tends to overfit: we stop the training after 6 epochs. This models gets better results than the vanilla LSTM model, but does not perform better than the logistic regression on the validation dataset.

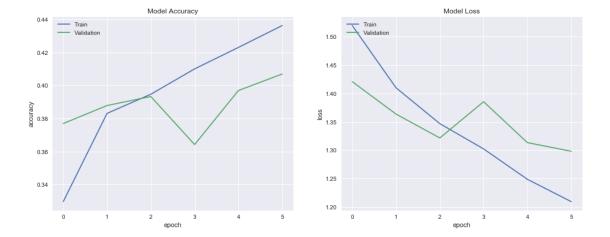


Figure 2: Loss and accuracy for the CNN-LSTM model