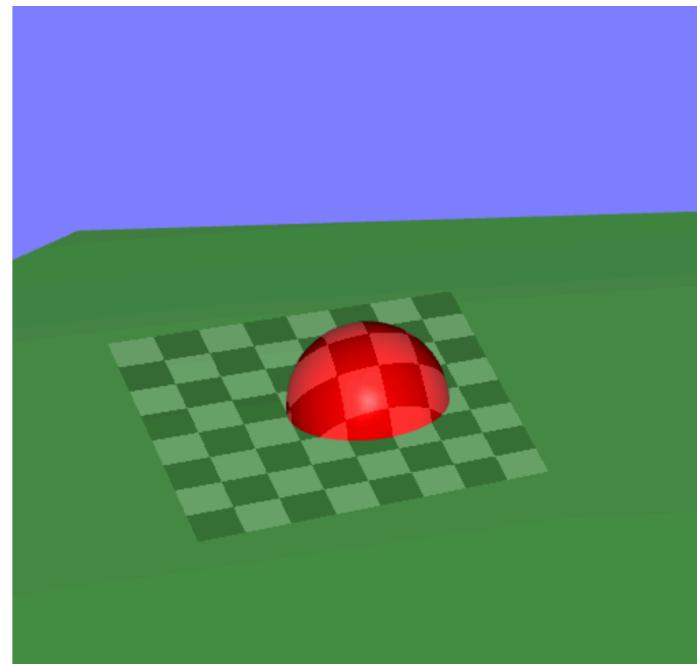
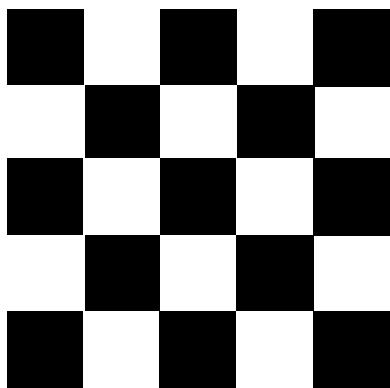


Projective textures

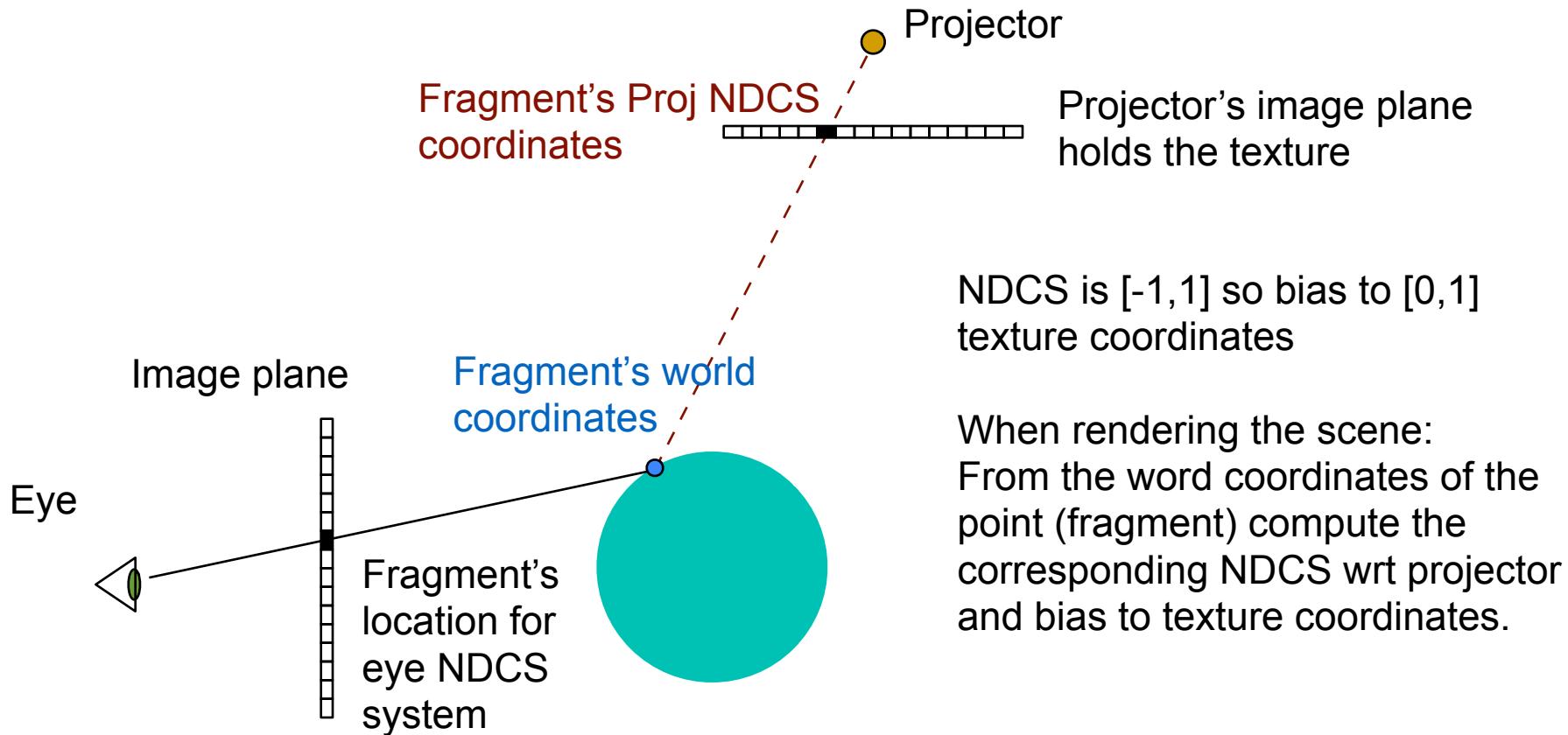
A nice example of a complex light source



Projective Textures

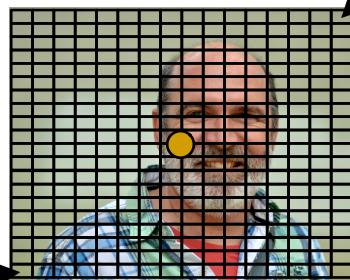
- Define a camera system
- Map a texture to its image plane
- Project the image plane onto the objects
- In some sense we are following the light's trajectory in the opposite direction
- So a pixel on this camera's image plane is now a texel
- Note: we will use the NDCS coordinates of this camera as textures, so they have to be rescaled to $[0,1]$ through a bias matrix

Visually the two pipelines

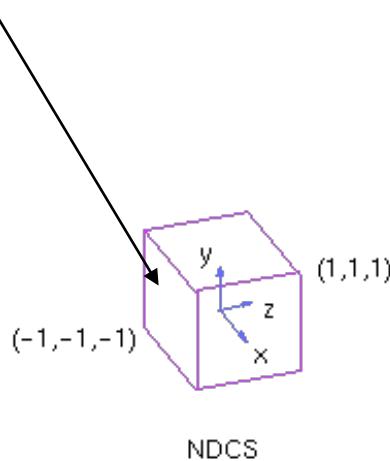
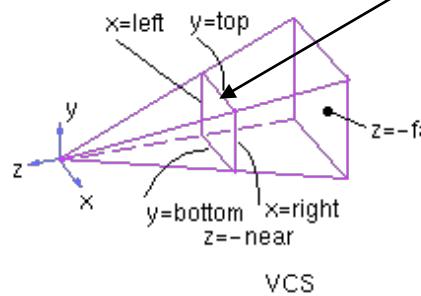


The projector

Bottom left pixel (texel)
View CS: (left,bottom,-near)
NDCS: (-1,-1,-1)
Texture CS: (0,0)



Top, right pixel (texel)
View CS: (right,top,-near)
NDCS: (1,1,1)
Texture CS: (1,1)



Projective textures

Normal texture mapping:

- Texture coordinates assigned by designer

Projective texture

- Texture considered mapped on the near plane covering the visible viewport (in NDCS [-1,1]) of the projector
- Texture coordinates computed for each vertex(fragment) as the NDCS coordinates of the vertex (fragment) of the projector's pipeline, appropriately scaled to be in [0,1]

Projective Textures

- Define a camera system for the projector: View Matrix V, Projection Matrix P (transforms the volume into NDCS)
- Add a bias matrix B, why?

$$\mathbf{B} = \begin{bmatrix} 0.5 & 0 & 0 & 0.5 \\ 0 & 0.5 & 0 & 0.5 \\ 0 & 0 & 0.5 & 0.5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- Combined matrix $\mathbf{M} = \mathbf{BPV}$
- What does this matrix do?

Projective Textures

- Define a camera system: Modelview Matrix V ,
Projection Matrix P (transforms the volume into
NDCS)
- Add a bias matrix B , why?

$$B = \begin{bmatrix} 0.5 & 0 & 0 & 0.5 \\ 0 & 0.5 & 0 & 0.5 \\ 0 & 0 & 0.5 & 0.5 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- Combined projector matrix $M = BPV$
- $P_{proj} = M P_{world}$ Takes world coordinates into
projector's Clipping Coordinates

Example Code

In Javascript host program:

- Load texture to unit 0 and bind it
- Set the filters

Example code

In Javascript host program

- Set the projector matrix and assign it to a uniform

```
var projPos = vec3(2.0,5.0,5.0);
var projAt = vec3(0.0,0.0,1.0);
var projUp = vec3(0.0,1.0,0.0);
var projView = lookAt(projPos, projAt, projUp);
var projProj = perspective(30.0,1.0, 0.2, 1000.0);
var projScaleTrans = mult(translate([0.5,0.5,0.5]),
scale(0.5,0.5,0.5)) ;
var ProjectorMatrix = mult(projScaleTrans, mult(projProj, projView));

var projectorMatrixLoc = gl.getUniformLocation(program,
"ProjectorMatrix") ;

gl.uniformMatrix4fv(projectorMatrixLoc, false,
flatten(ProjectorMatrix) );
// Is the projector fixed in world coordinates or not?? If not what
do you need to do to fix it?
```

Vertex Shader

```
#version 300 es

in vec4 VertexPosition;
in vec3 VertexNormal;

out vec4 ProjTexCoord;
out vec4 fColor;

uniform mat4 modelViewMatrix;
uniform mat4 modelMatrix;
uniform mat4 normalMatrix;
uniform mat4 projectionMatrix;

uniform mat4 ProjectorMatrix;
```

Vertex Shader

...

```
out vec4 ProjTexCoord;  
  
void main()  
{  
    gl_Position = projectionMatrix * modelViewMatrix *  
    vPosition;  
  
    fColor = ads(...);  
    fColor.a = 1.0;  
    ProjTexCoord = ProjectorMatrix * (modelMatrix *  
        vPosition);  
}
```

Fragment Shader

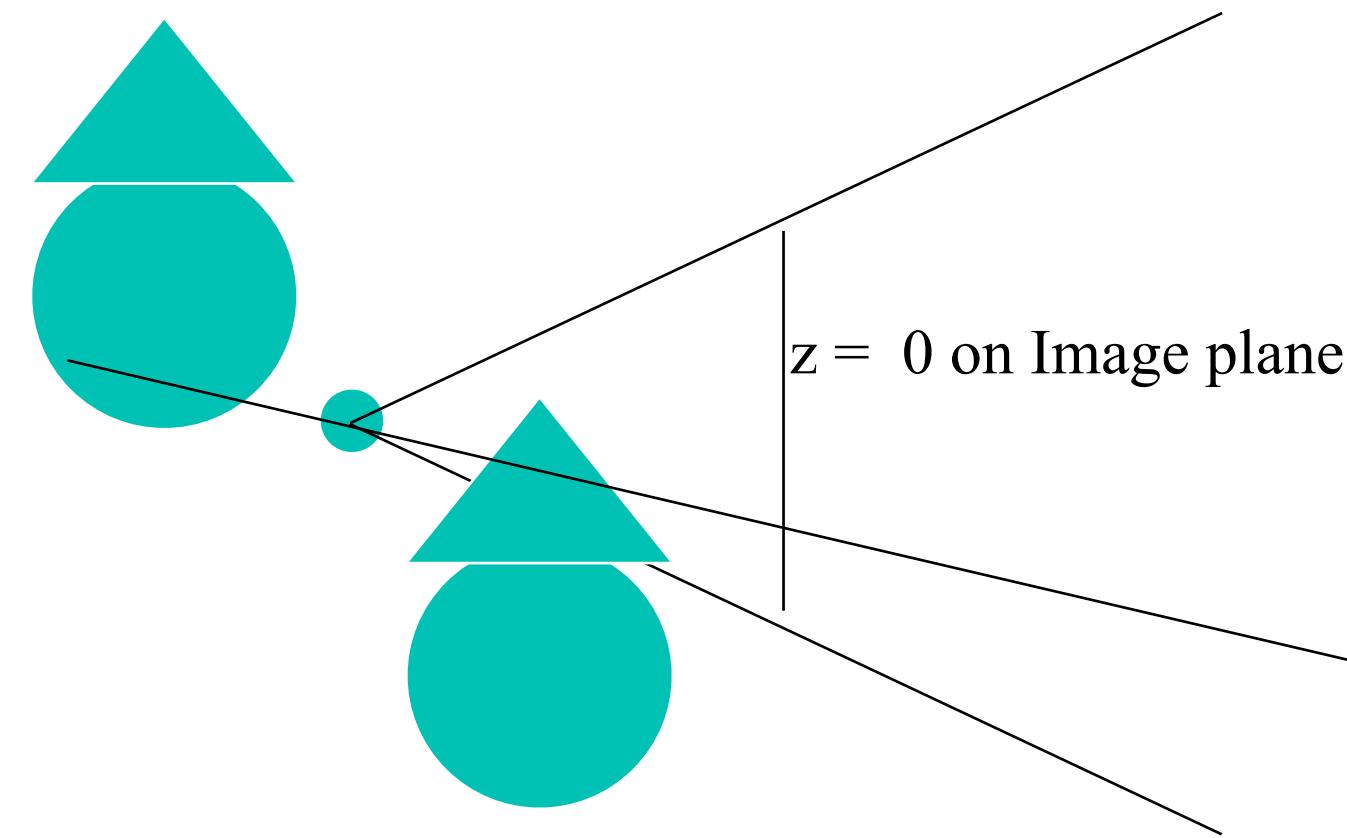
```
...
in vec4 fColor ;
in vec4 ProjTexCoord;

uniform sampler2D texture1;
layout( location = 0 ) out vec4 FragColor;

void main() {
vec4 c1,c2,c3 ;

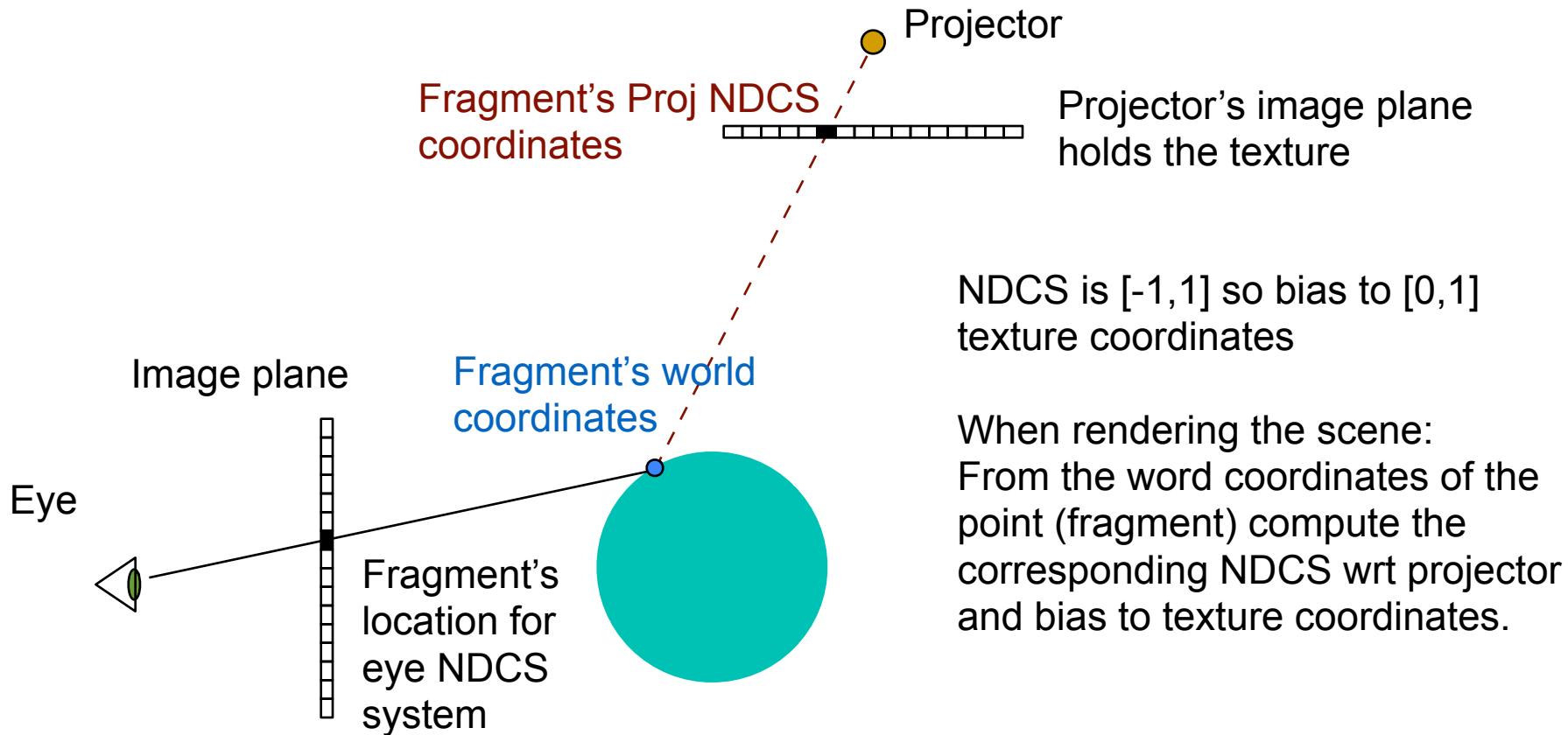
fragColor = fColor;
if( ProjTexCoord.z > 0.0) {
    float x = ProjTexCoord.x / ProjTexCoord.w;
    float y = ProjTexCoord.y / ProjTexCoord.w;
    if( ( x < 0.0) || (x > 1.0) || (y < 0.0) || (y > 1.0) )
        c1 = vec4(0.f,0.f,0.f,1.0f ) ;
    else
        c1 = texture( texture1, vec2(x,y));
}
fragColor = fColor + c1*0.7;
fragColor.a = 1.0 ;
}
```

Cases where $z < 0$

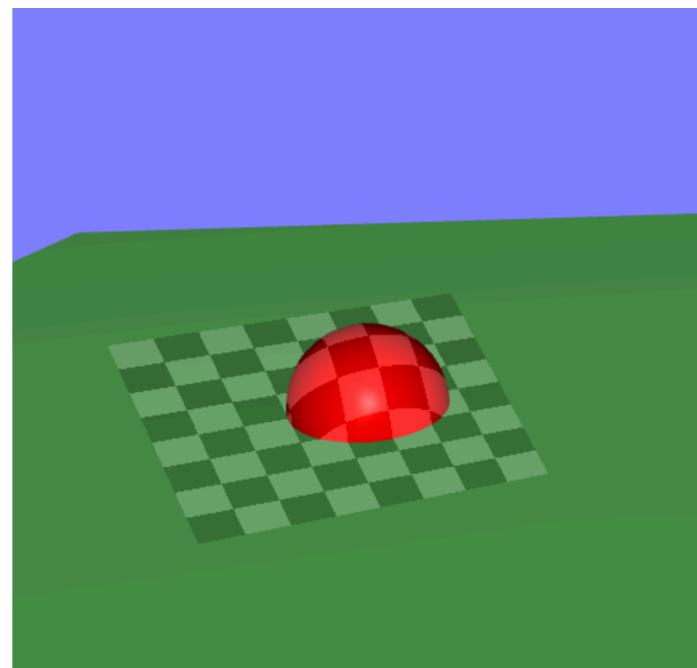
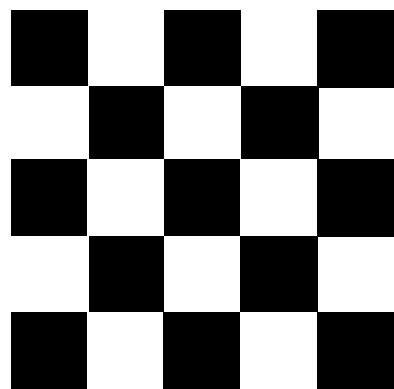


We are essentially doing clipping in terms of z

Visually the two pipelines



Result



Issues

No occlusions

- Texture will project on all objects in its path