



# Lecture 6 | Support Vector Machines

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🏷 Étiquettes	

## Questions

- What are the key ideas?
- What terms or ideas are new to me?
- How would I define them?
- How do the ideas relate to what I already know?
- Should not assume that the professor are always correct. Asking appropriate questions.
- What are the good ideas?
- Do the ideas have other applications?



- Generative models look at each class, one step at a time.
- Discriminative models use Gradient Descent to find the best fit line.

| **Generative** models learn backwards (features to class).

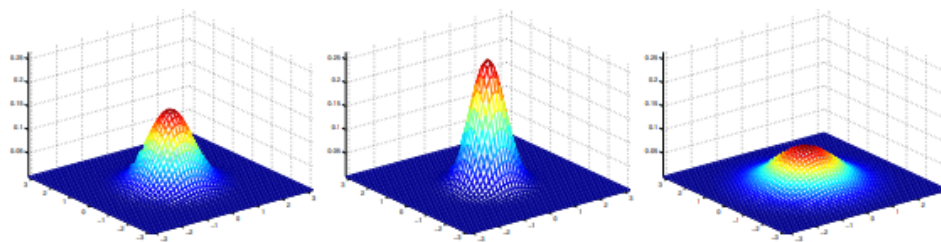


This formula tells us how data behave, and we can use this to make sense of this behavior and make cool stuff, like:

- predict the future.
- analyse data.
- understand patterns.

$$p(x; \mu, \Sigma) = \frac{1}{(2\pi)^{d/2} |\Sigma|^{1/2}} \exp \left( -\frac{1}{2} (x - \mu)^T \Sigma^{-1} (x - \mu) \right).$$

Here are some examples of what the density of a Gaussian distribution looks like:



Even they end up using the same Sigmoid Function GDA makes Strong Assumptions (About the Distribution Of Data) when Logistic Regression Don't.

Using GDA means you know more things (in theory) that makes a good model, since you already knows those things.

## Lecture

### Outline

#### Naive Bayes

- Laplace Smoothing
- Event Models

## Applications ML

### SVM Intro

One simple problem when using Naive Bayes for text classification (spam/not spam) is that it can classify something as no spam, just because the model never saw the word. Laplace smoothing helps address this problem.

Seems like Laplace Smoothing consists in adding 1 to the numerator and one to the denominator. Basically because you want to eliminate the occurrence of zero.

Some models have limitations that we can improve by using some mathematical trick.

Multinomial Event Model is a more efficient adaptation of Naive Bayes focused on text classification, we create a much lower matrix in comparison with Multivariate Bernoulli Event Model. The Multinomial uses a product with length equals to the number of words in the e-mail (for example) and instead of using  $\{0, 1\}$  we use  $\{1, 2, \dots, \text{Num Words}\}$ . To apply Laplace we add 1 to the numerator and the length of email to the denominator.

Even that, for most cases Logistic Regression is superior to Naive Bayes in accuracy, there are some advantages in using it:

- simple to implement
- don't use gradient
- computationally efficient

SVM is great when you want to classify data using a non-linear boundary. We can apply the same logic to Logistic Regression (non-linear boundary) by augmenting data. But, now how to create this situation could be hard, so what SVM does is just create this high dimensional space and then apply a linear classifier.

Two basic ideas in SVM are: Optimal Margin Classifier and Kernels. Kernels consist in converting features to much higher dimensions.

Optimal margin: choose  $w$  and  $b$  that maximizes the Geometric Margin Denoted By  $\gamma$ .

## Vocab

- Laplace smoothing: Laplace smoothing is a smoothing technique that handles the problem of zero probability in Naïve Bayes.
- NIPS: **Conference on Neural Information Processing Systems**
- Functional Margin: The functional margin is a measure of the generalization ability of the classifier.
- Geometric Margin: The distance between the point and the decision boundary is Geometric Margin
- Kernel: It is a mathematical function that helps organize data and make it easier to classify.

## More

- <https://towardsdatascience.com/laplace-smoothing-in-na%C3%AFve-bayes-algorithm-9c237a8bdece>
- <https://neurips.cc/>
- <https://medium.com/@gokcenazakyol/machine-learning-support-vector-machines-svms-7bc389c877d8>
- <https://medium.com/@abhishekjainindore24/svm-kernels-and-its-type-dfc3d5f2dcd8>
- <https://web.mit.edu/6.034/wwwbob/svm-notes-long-08.pdf>