

Sam Hopkins

Cs355

Hw 8

$$1. C_{diff} = (S \otimes M_{diff}) (n \cdot 1) \quad n = [.58, .58, -.058]^T \quad L = [.53, .80, -.27]$$

$$(n \cdot 1) = \begin{bmatrix} .58 \\ .58 \\ -.58 \end{bmatrix} \begin{bmatrix} .53, .8, -.27 \end{bmatrix} = .3074 + .464 + .1566 = .928$$

$$S = .9 \begin{bmatrix} 1 \\ 1 \\ .8 \end{bmatrix} \quad M_{diff} = \begin{bmatrix} .1 \\ .2 \\ .5 \end{bmatrix} \quad = (S \otimes M_{diff}) = \begin{bmatrix} .1 \\ .2 \\ .4 \end{bmatrix} \cdot .928 = .835$$

$$\begin{bmatrix} .0835 \\ .167 \\ .334 \end{bmatrix}$$

$$2. C_{spec} = (S \otimes M_{spec}) (v \cdot r)^{m_{spec}}$$

$$m_{spec} = 4 \quad v = [0, 0, -1] \quad r = \frac{2(1 \cdot n)}{2 \cdot (.928) n - 1}$$

$$1.856 \begin{bmatrix} .58 & 1.076 & .53 & .546 \\ .58 & 1.076 & .8 & .276 \\ -.58 & -1.076 & -.27 & -.806 \end{bmatrix} = 1.076 - .8 = .276 = r$$

$$v \cdot r = \begin{bmatrix} 0 & .546 \\ 0 & .276 \\ -1 & -.806 \end{bmatrix}^4 = (.806)^4 = .422$$

$$(S \otimes M_{spec}) \cdot .422 = \begin{bmatrix} .1 & .5 & .9 & .5 \\ .9 & 1 & .5 & .5 \\ .8 & .5 & .4 \end{bmatrix} \cdot .422 = \begin{bmatrix} .45 \\ .45 \\ .36 \end{bmatrix} \cdot .422 = \begin{bmatrix} .1899 \\ .1899 \\ .1519 \end{bmatrix}$$

$$3. C_{amb} = S_{amb} \otimes M_{amb} \rightarrow$$

$$\begin{bmatrix} 1 & .1 \\ .1 & 1 \end{bmatrix} \otimes \begin{bmatrix} .1 & .2 \\ .5 & .5 \end{bmatrix} = \begin{bmatrix} .1 & .2 \\ .1 & .2 \\ .4 & .4 \end{bmatrix} = \begin{bmatrix} .01 \\ .02 \\ .04 \end{bmatrix}$$

$$4. C_{spec} + C_{diff} + C_{amb} = L_{it}$$

$$\begin{bmatrix} .1899 \\ .1899 \\ .1519 \end{bmatrix} + \begin{bmatrix} .0835 \\ .167 \\ .334 \end{bmatrix} + \begin{bmatrix} .01 \\ .02 \\ .04 \end{bmatrix} = \begin{bmatrix} .2834 \\ .3769 \\ .5259 \end{bmatrix}$$