

Read/review Sections 6.1 - 6.4. Then answer the following questions.

1. Find the inner product  $\langle x, y \rangle$  in  $\mathbb{C}^2$  given  $x = (2 - i, 1 + i)$  and  $y = (2 - i, 2 - i)$ .
2. Under what conditions can you guarantee a vector space  $V$  has an orthonormal basis? Given a vector space with these conditions and any basis, what process could you use to find an orthonormal basis?
3. Suppose  $V = \mathbb{R}^3$  and  $S = \{e_1\}$ . Describe  $S^\perp$ .
4. What is the definition of a normal linear operator? What is the definition of a self-adjoint linear operator?
5. Suppose  $T$  is normal linear operator on a finite-dimensional complex inner product space. Is  $T$  diagonalizable?