

Read Section 6.11 and answer the following questions.

1. How do we define a rotation on a 1-dimensional inner product space?
2. Let  $V$  be a nonzero finite-dimensional real inner product space. Then there exists a collection of pairwise orthogonal  $T$ -invariant subspaces  $\{W_1, \dots, W_m\}$  such that
$$V = W_1 \oplus \cdots \oplus W_m.$$
  - (a) What can you say about the dimension of each  $W_i$ ?
  - (b) If you know  $T_{W_i}$  is a reflection, what can you say about the dimension of  $W_i$ ?
3. Prove that if  $T$  is a reflection on a 2-dimensional inner product space then  $T^2 = I$ .