

All problems are to be written up clearly and thoroughly, using complete sentences. This assignment is due in discussion at 2pm on Thursday, May 23rd.

For all T/F problems on the homework, provide a brief justification for your answer. That may be citing an appropriate theorem or providing a counterexample.

1. Section 5.1 problems 4 a, d, e, h, 6, 8, 9, 10, 11, 14, 15, 17
2. Section 5.2 problems 1, 2, 3
3. Compute the number of invertible matrices  $A$  in  $M_{n \times n}(\mathbb{F}_p)$ .
4. A matrix  $A \in M_{n \times n}(\mathbb{F})$  is called *nilpotent* if there exists a  $k$  such that  $A^k = 0$ . Show that if  $A$  is nilpotent then  $I_n - A$  is invertible. (*Hint:* think about the power series of  $(1 - x)^{-1}$ ).