

# COMP9517

## Computer Vision

2022 Term 3 Week 1

Professor Erik Meijering



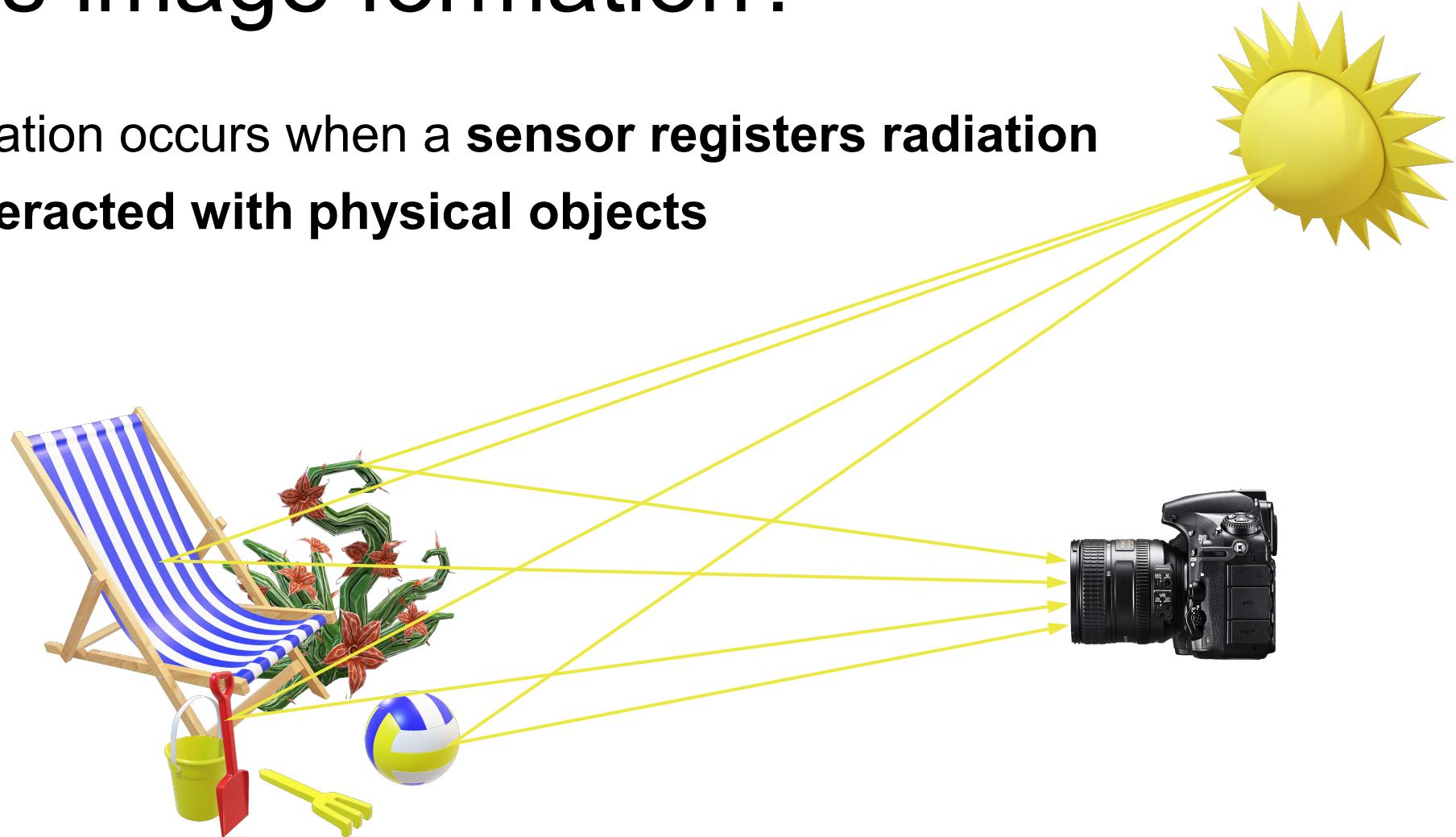
**UNSW**  
SYDNEY



Image Formation

# What is image formation?

Image formation occurs when a **sensor registers radiation** that has **interacted with physical objects**



# Geometry of image formation

Mapping world coordinates (3D) to image coordinates (2D)

- Pinhole camera model
- Projective geometry
- Projection matrix

# Image formation

Idea 1: Put a piece of film in front of an object



Do we get a reasonable image?

# Image formation

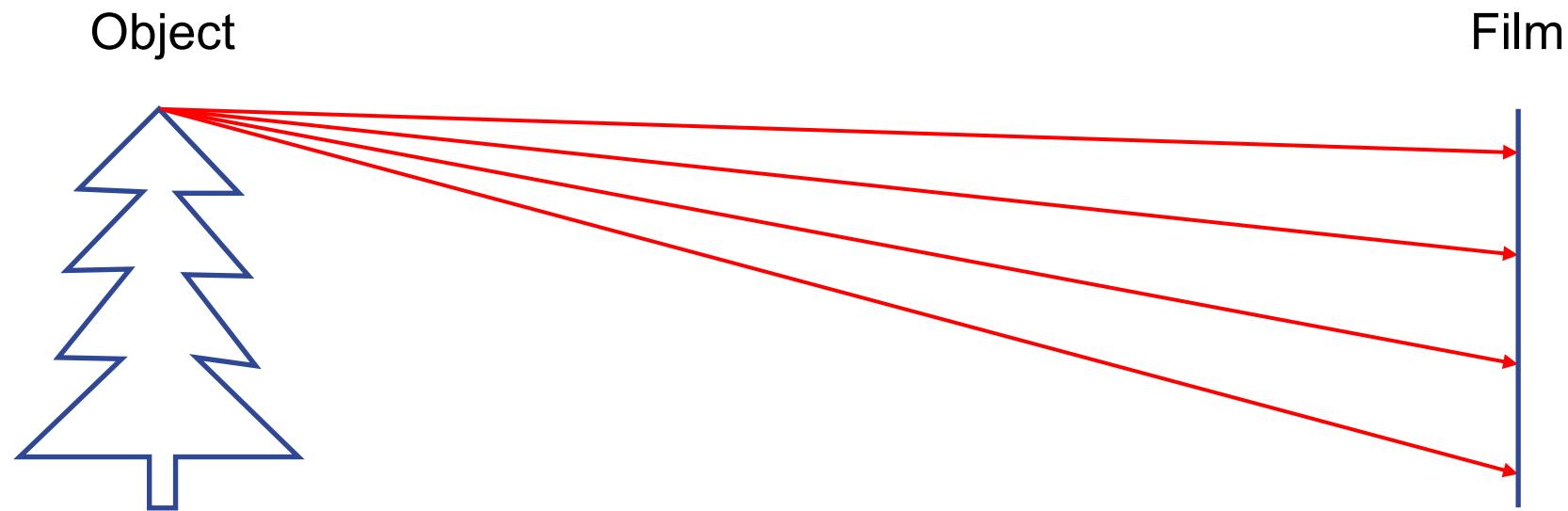
Idea 1: Put a piece of film in front of an object



Do we get a reasonable image?

# Image formation

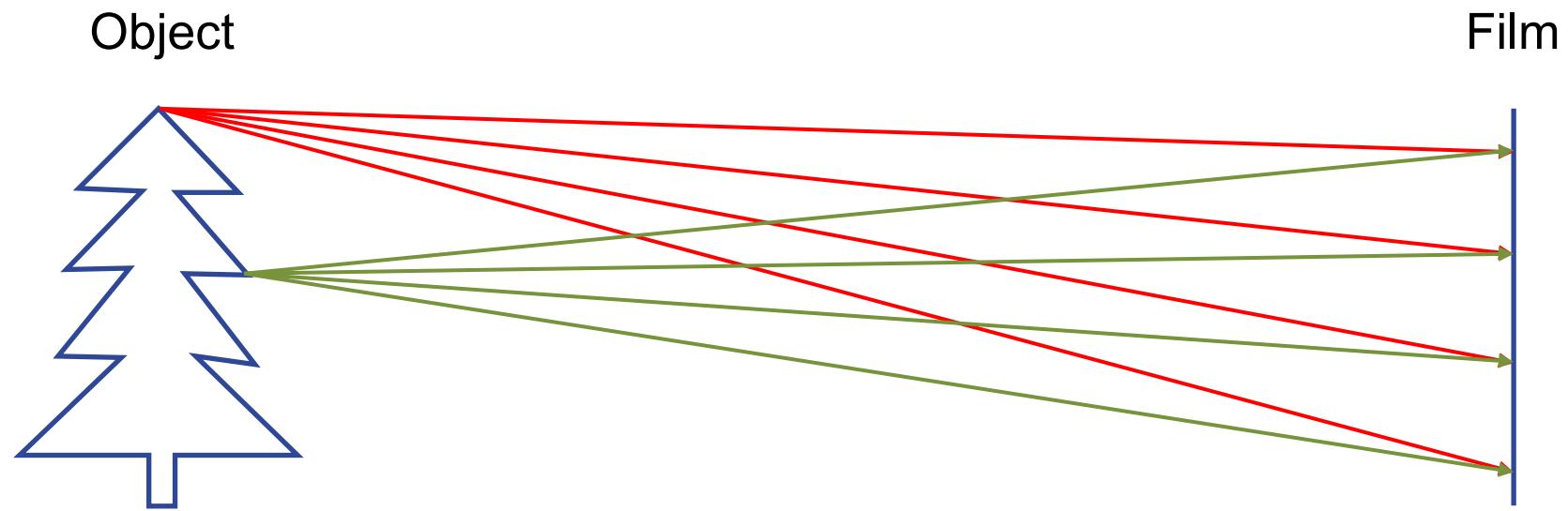
Idea 1: Put a piece of film in front of an object



Do we get a reasonable image?

# Image formation

**Idea 1:** Put a piece of film in front of an object

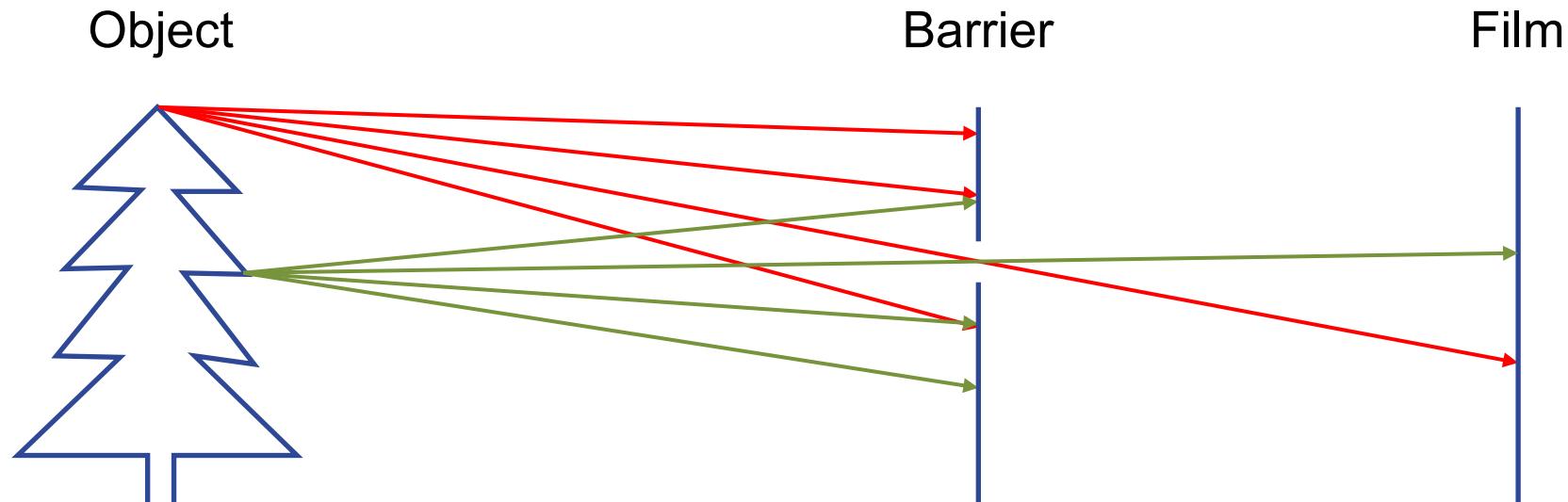


The resulting image is completely blurred

All object points are projected  
to all points on the film

# Image formation

Idea 2: Add a barrier to block off most of the rays

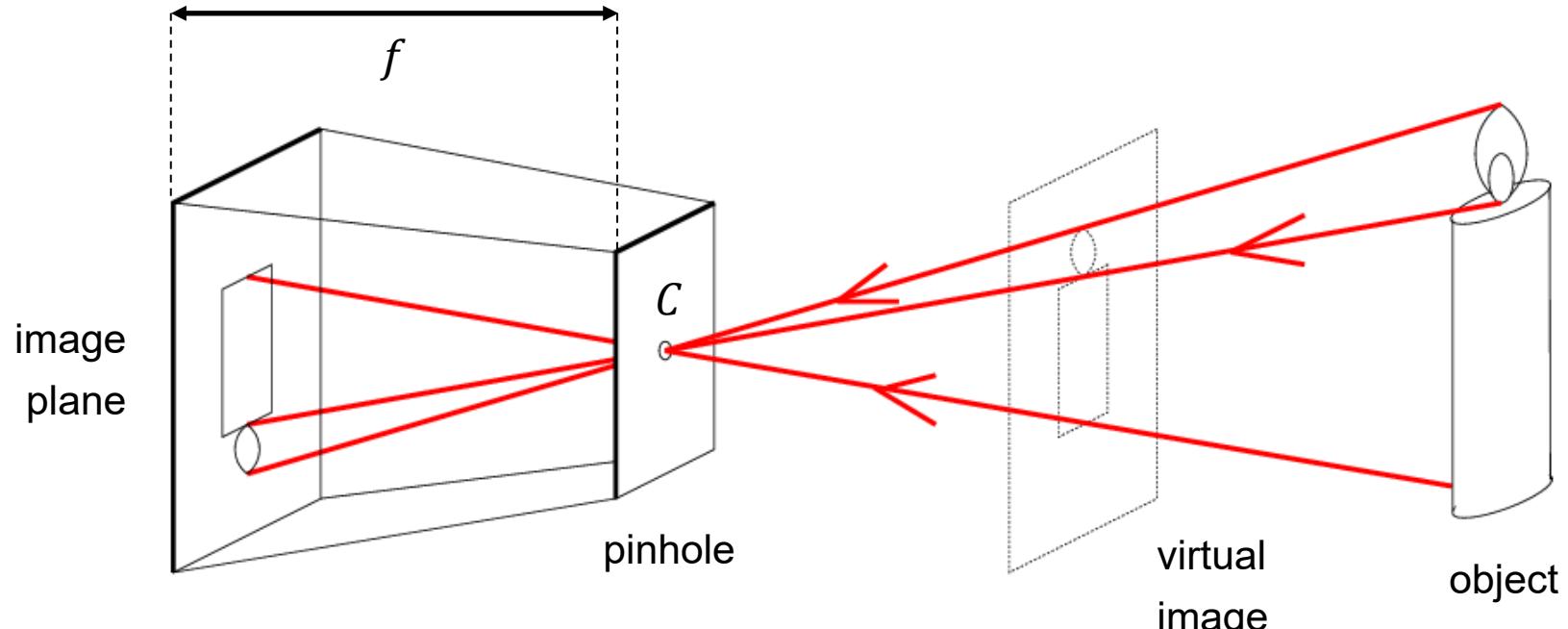


This reduces blurring

Opening known as the  
**pinhole or aperture**

Object points are projected to  
unique points on the film

# Pinhole camera model



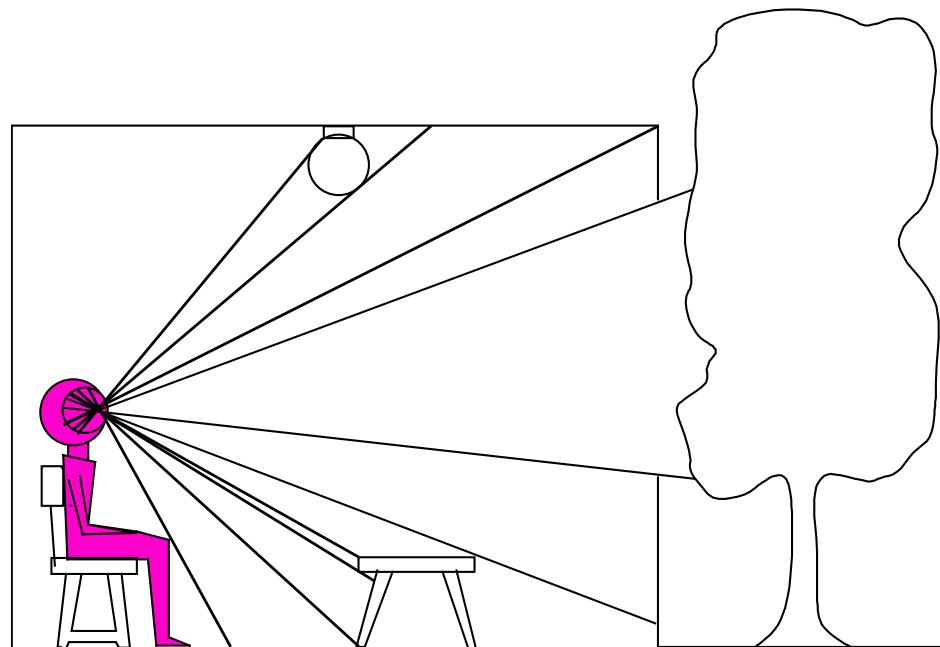
$f$  = focal length

$C$  = camera centre

Figure from Forsyth

# Dimensionality reduction machine

3D world

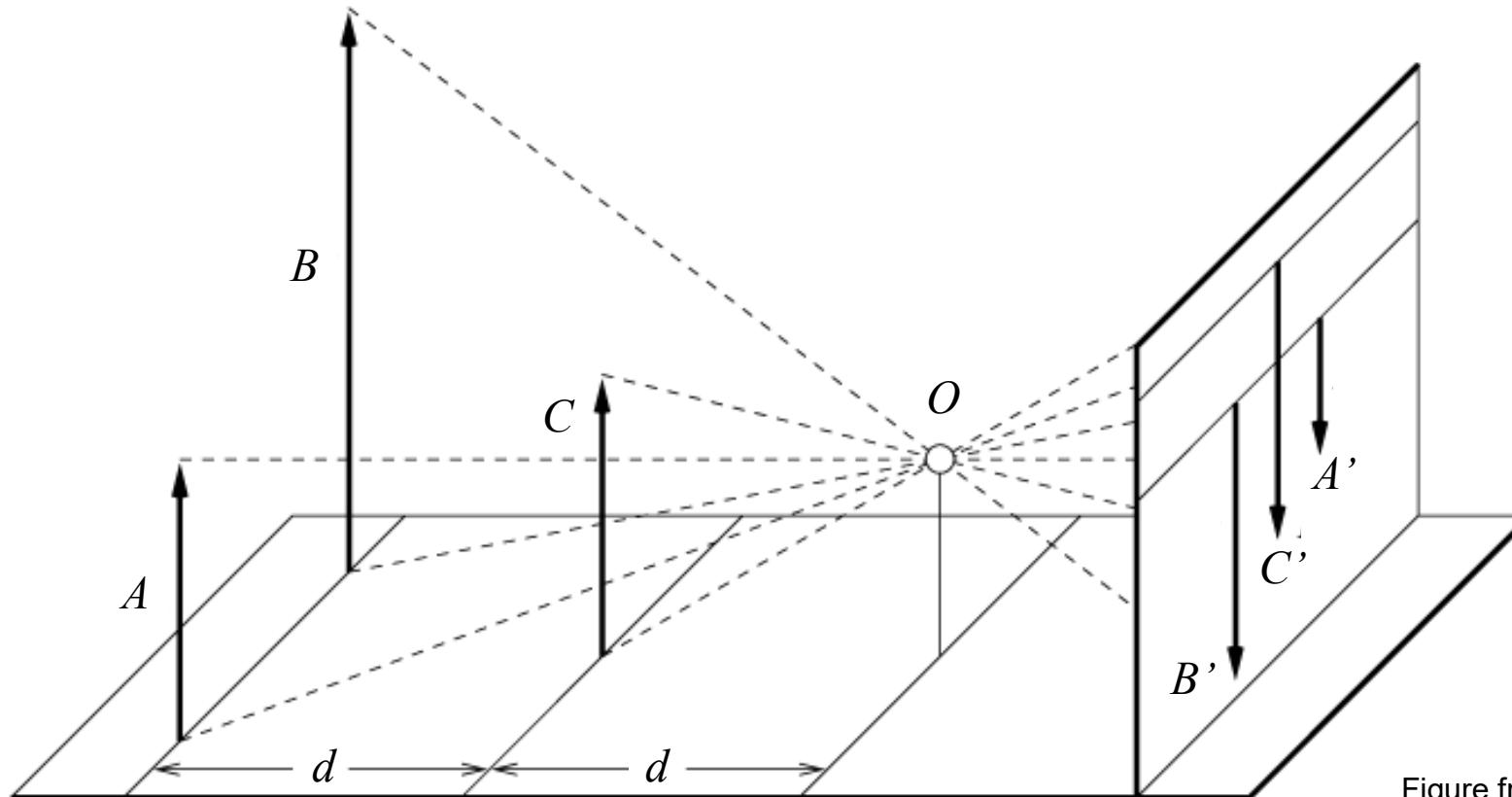


2D image

# Projection can be tricky...



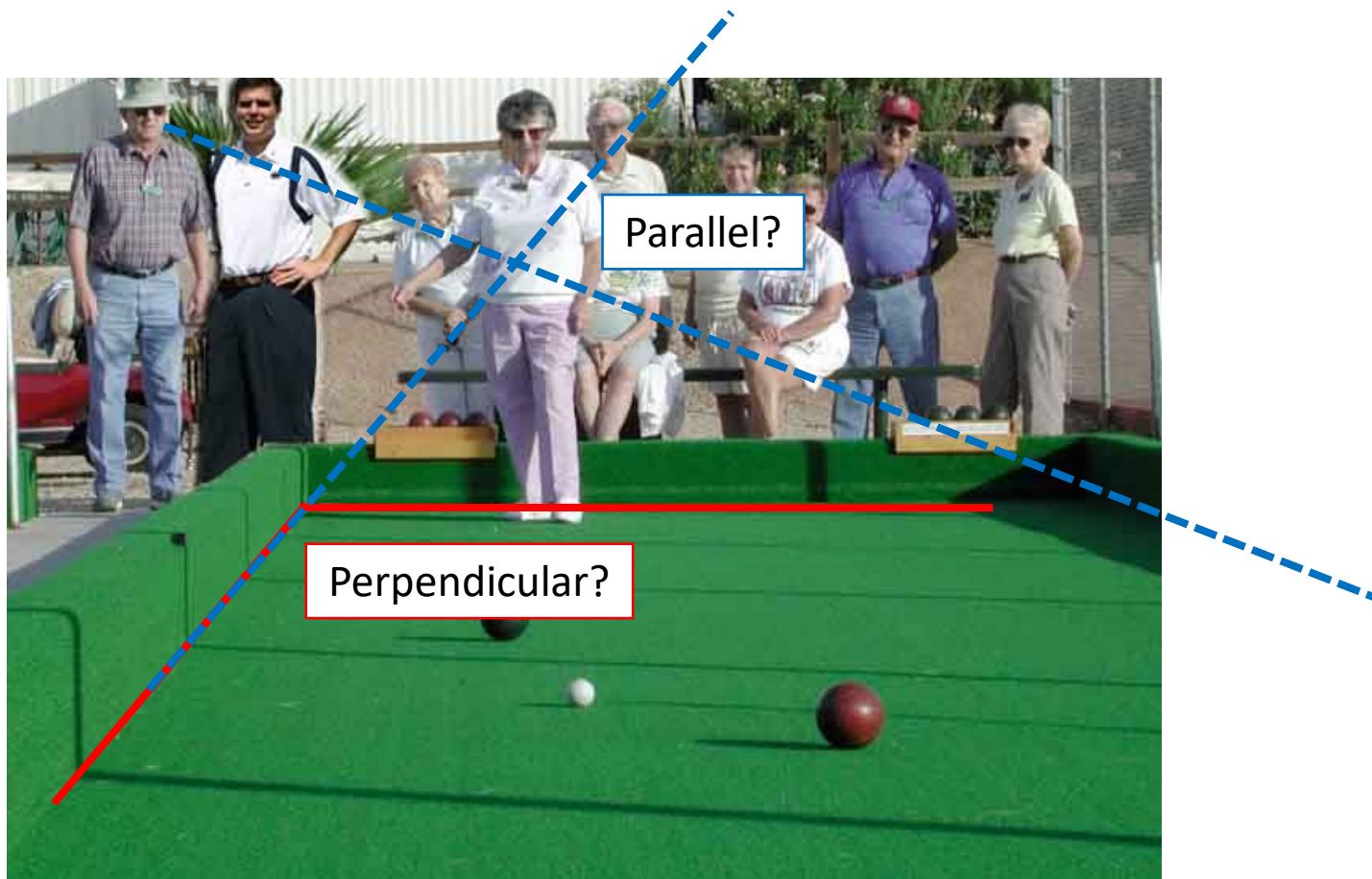
# Projective geometry



Length and area are not preserved

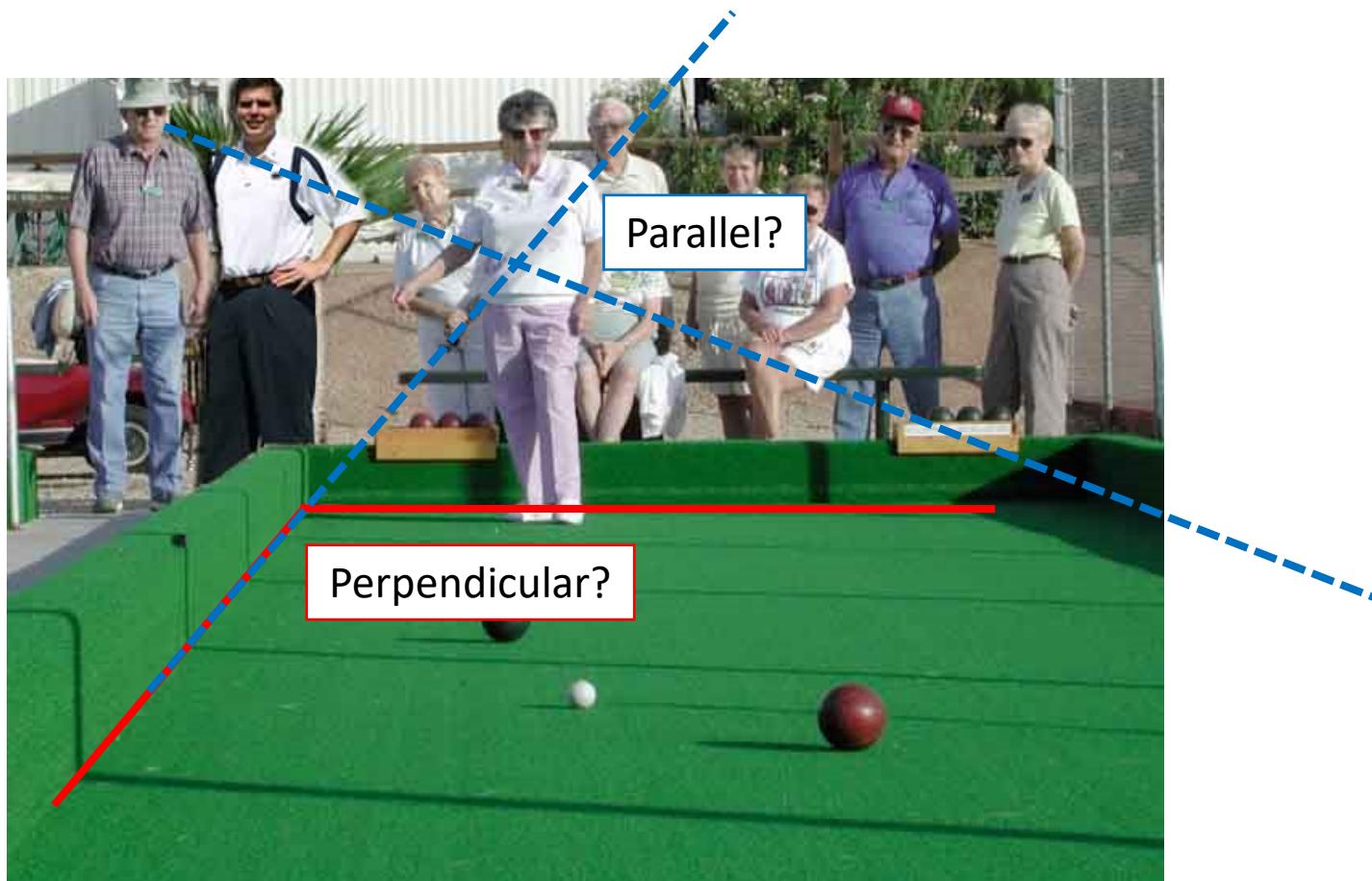
Figure from Forsyth

# Projective geometry



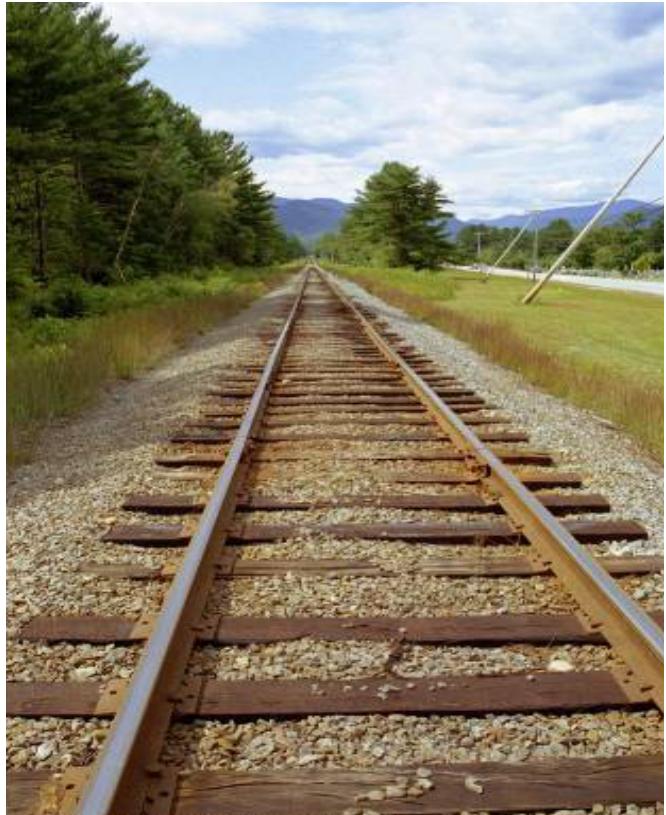
**What is lost?**  
Length and angles  
are not preserved

# Projective geometry



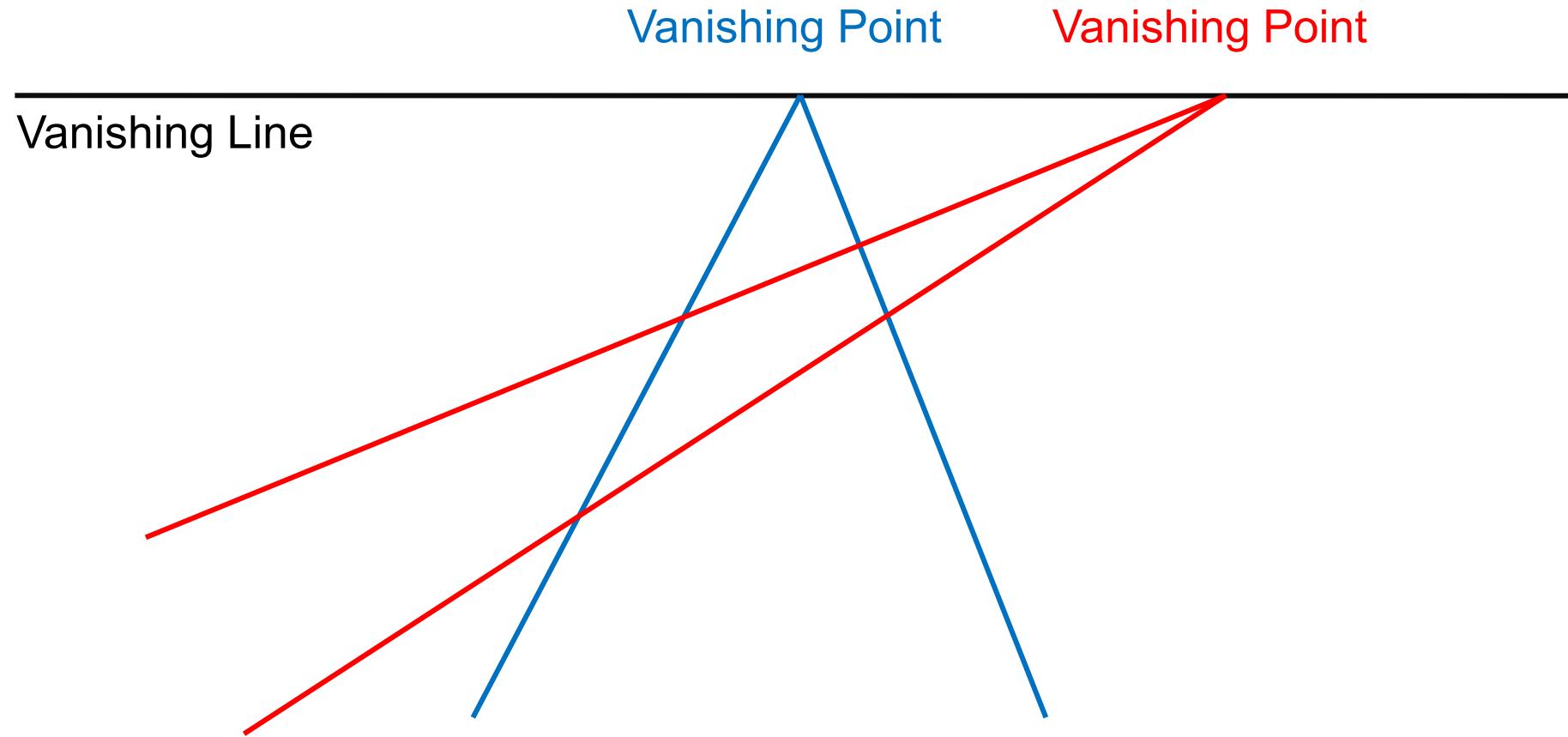
**What is preserved?**  
Straight lines are  
still straight

# Vanishing points and lines



Parallel lines in the 3D world  
intersect in the 2D image  
at a “vanishing point”

# Vanishing points and lines



# Vanishing points and lines



Photo from Criminisi

# Vanishing points and lines

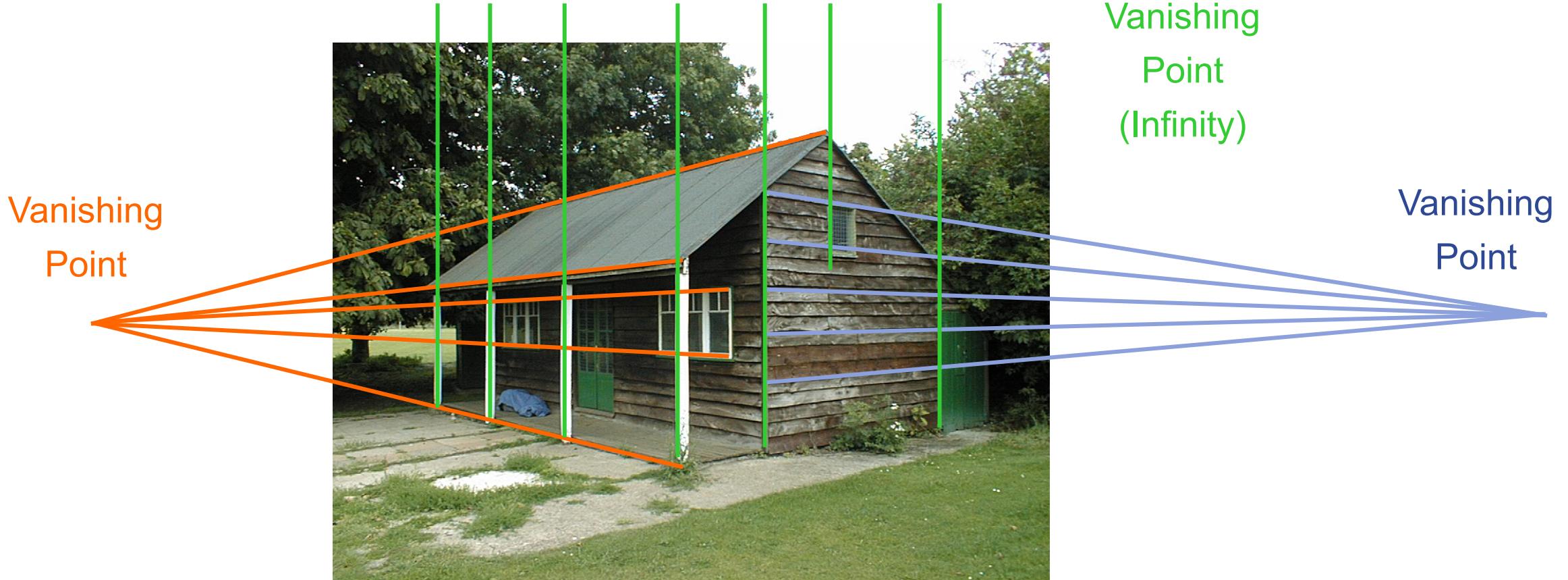
Vanishing  
Point



# Vanishing points and lines

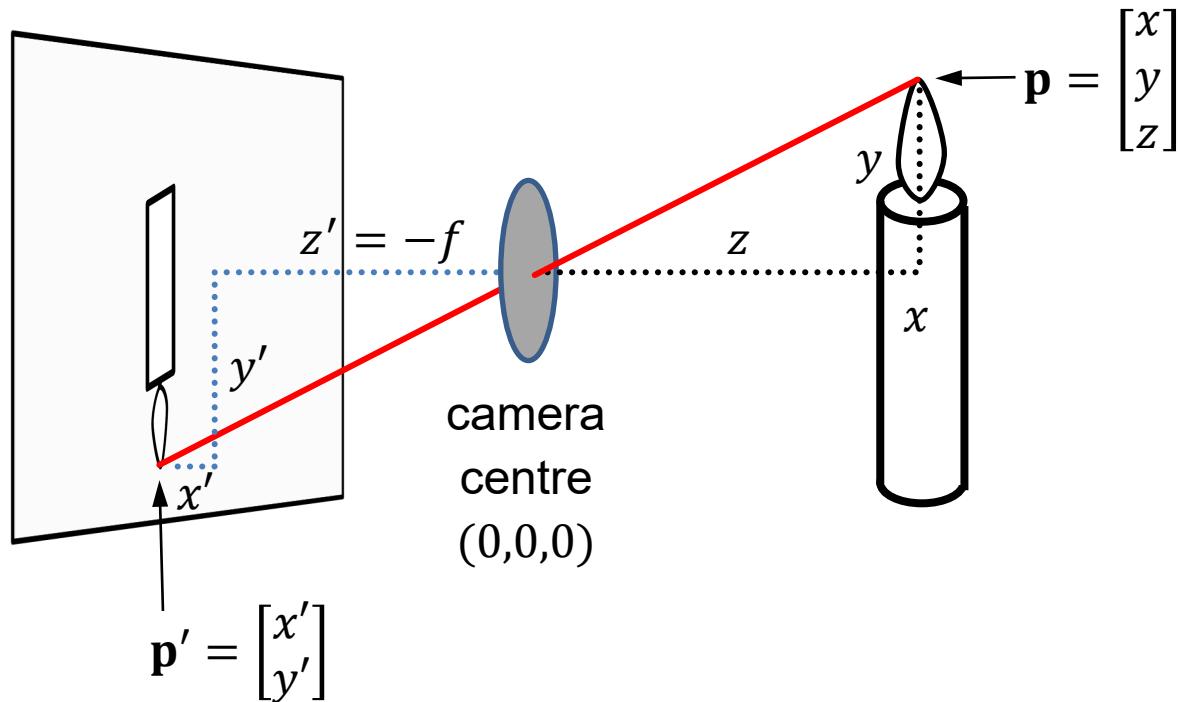


# Vanishing points and lines



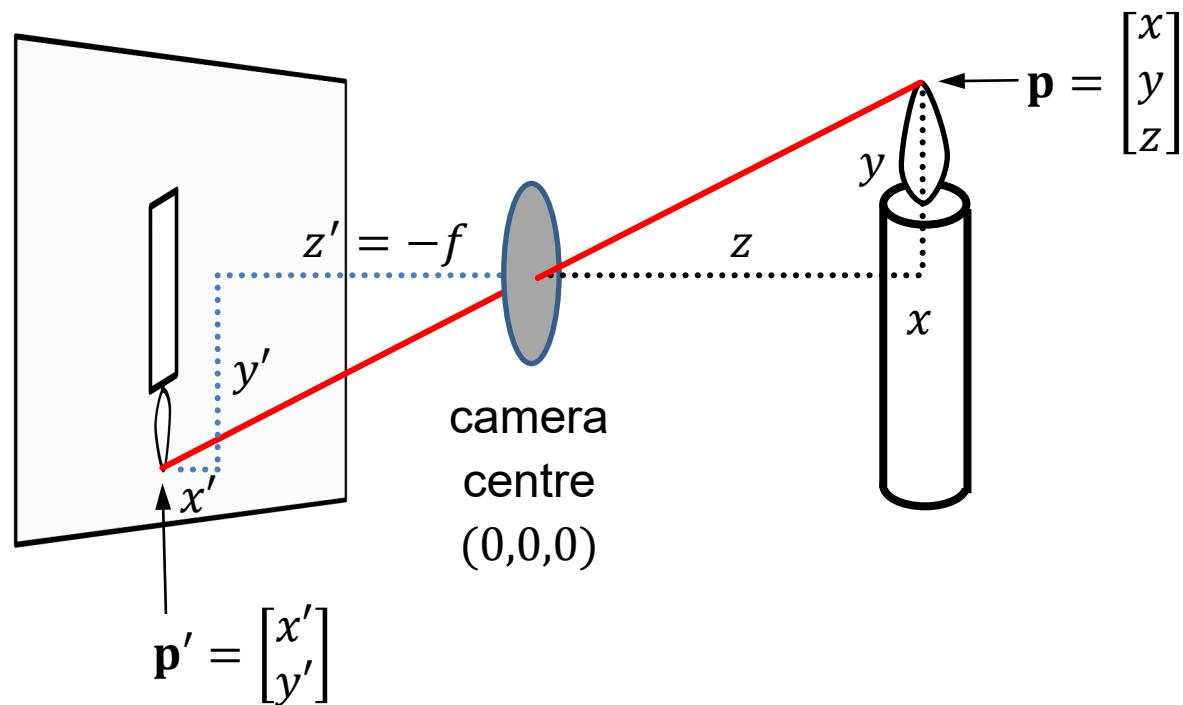
# Projection mathematics

From **world coordinates** to **image coordinates**



# Projection mathematics

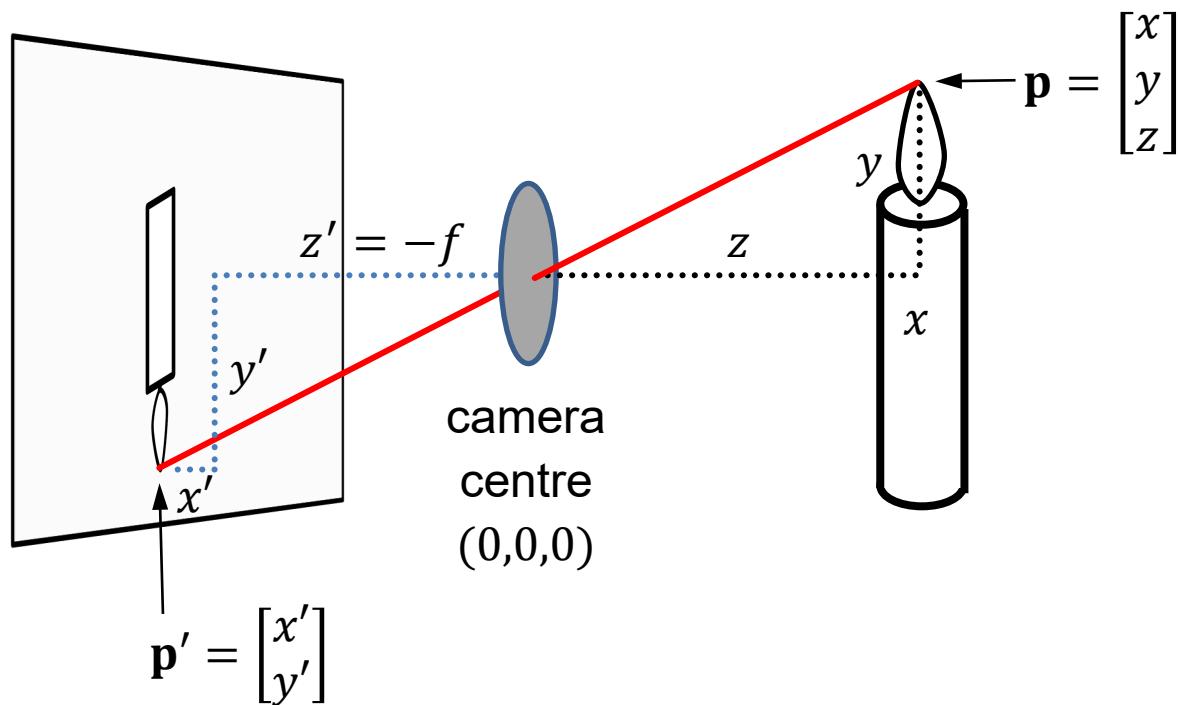
From **world coordinates** to **image coordinates**



If  $x = 2, y = 3, z = 5$ , and  $f = 2$ ,  
what are  $x'$  and  $y'$  ?

# Projection mathematics

From **world coordinates** to **image coordinates**



If  $x = 2, y = 3, z = 5$ , and  $f = 2$ ,  
what are  $x'$  and  $y'$  ?

$$x' = -x \cdot \frac{f}{z}$$

$$y' = -y \cdot \frac{f}{z}$$



$$x' = -2 \cdot \frac{2}{5}$$

$$y' = -3 \cdot \frac{2}{5}$$

# Perspective projection

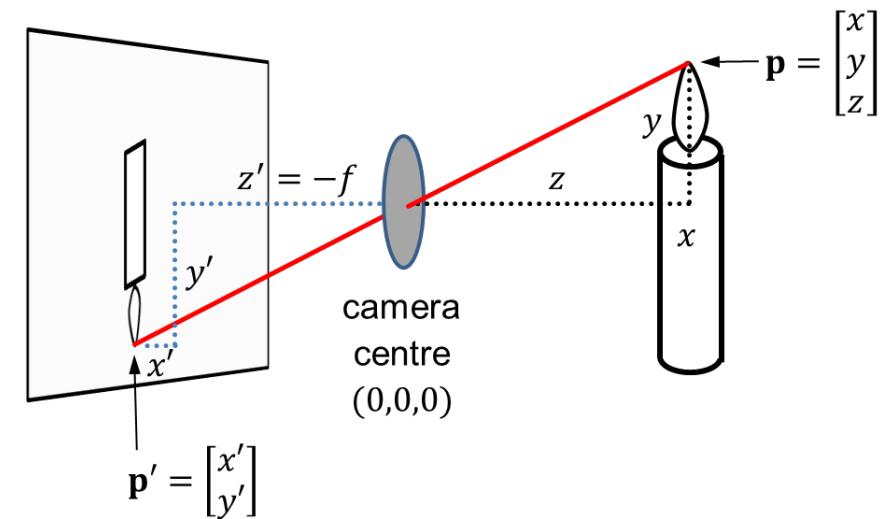
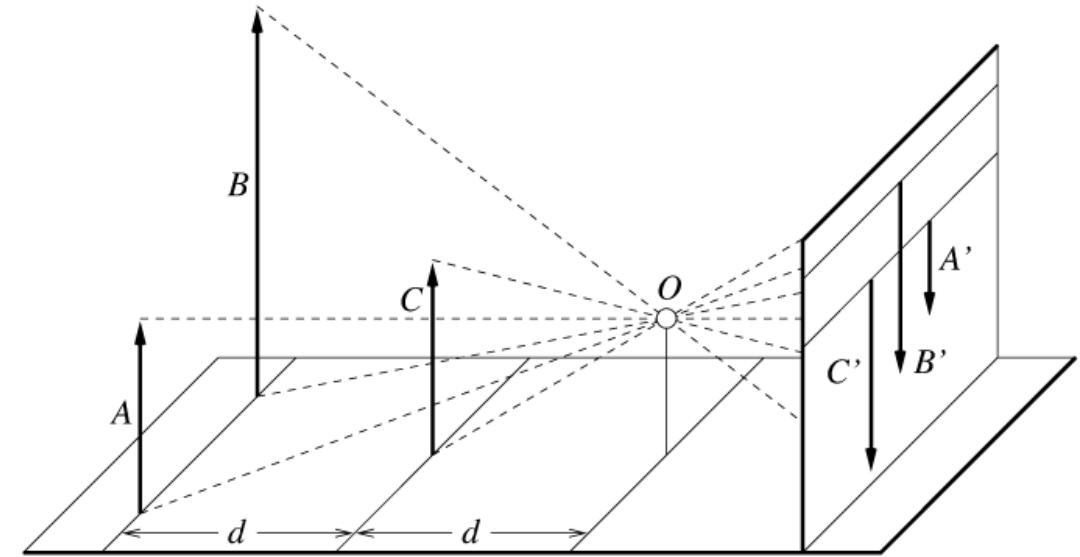
- Apparent size of object depends on its distance:  
far objects appear smaller

- By similar triangles:

$$(x', y', z') = \left( -f \frac{x}{z}, -f \frac{y}{z}, -f \right)$$

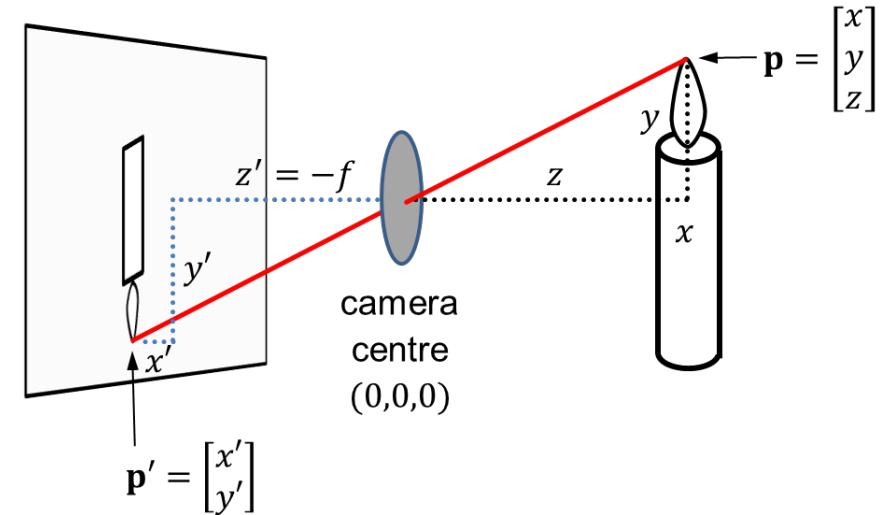
- Ignore third coordinate and mirror:

$$(x', y') = \left( f \frac{x}{z}, f \frac{y}{z} \right)$$

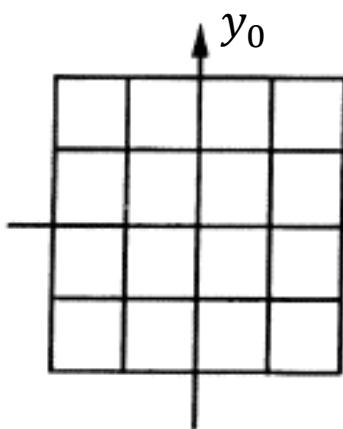


# Affine projection

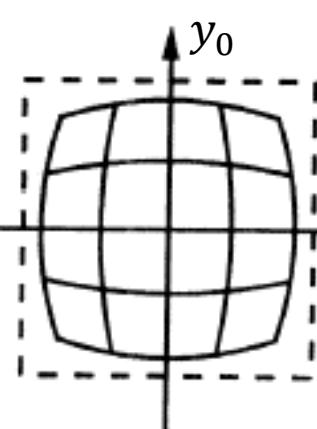
- Suitable when scene depth is small relative to average distance from camera
- Let magnification  $m = f/z_0$  be a positive constant and all points in the scene have approximately constant distance  $z_0$  to the camera
- Leads to weak perspective projection:  
 $(x', y') = (mx, my)$
- Orthographic projection when  $m = 1$ :  
 $(x', y') = (x, y)$



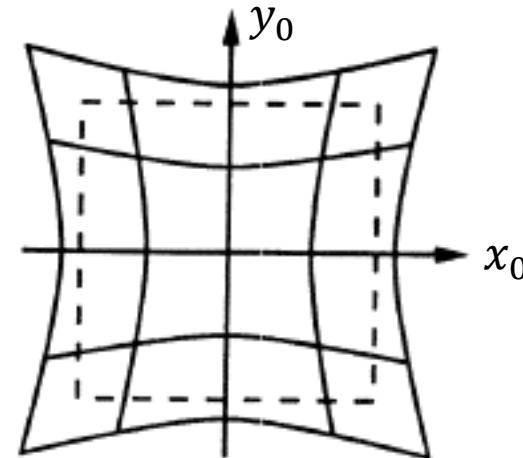
# Beyond pinholes: radial distortions



No distortion



Barrel distortion



Pincushion distortion

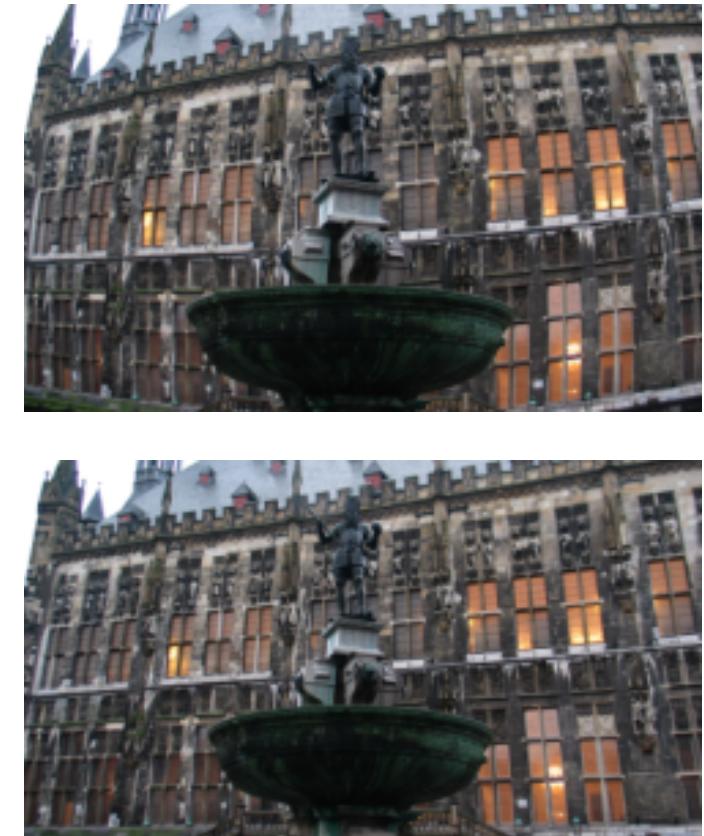
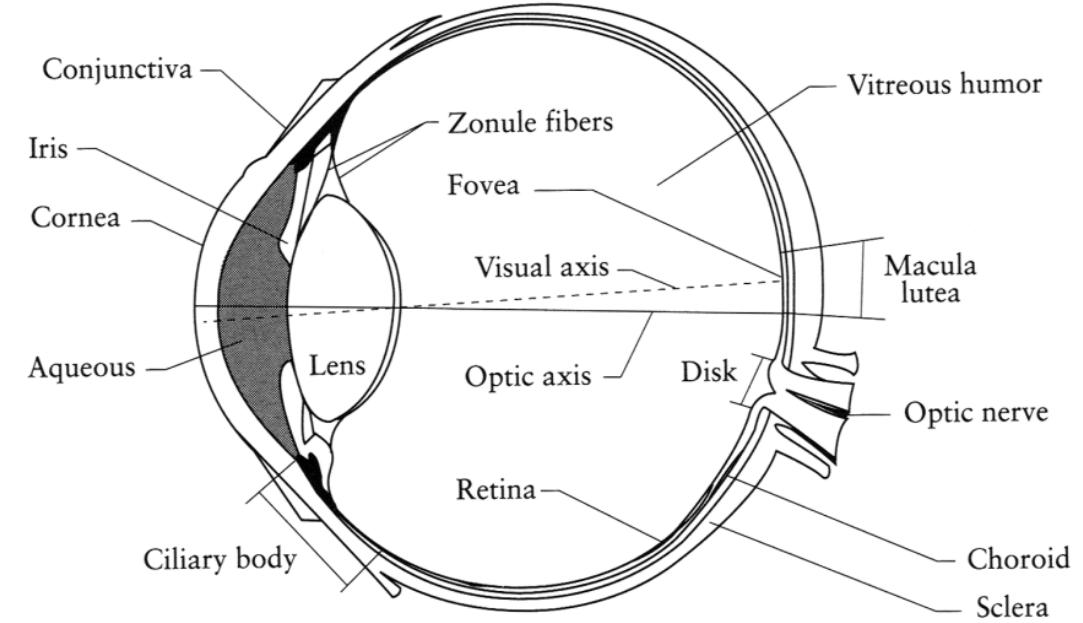


Image from Martin Habbecke

Barrel distortion corrected

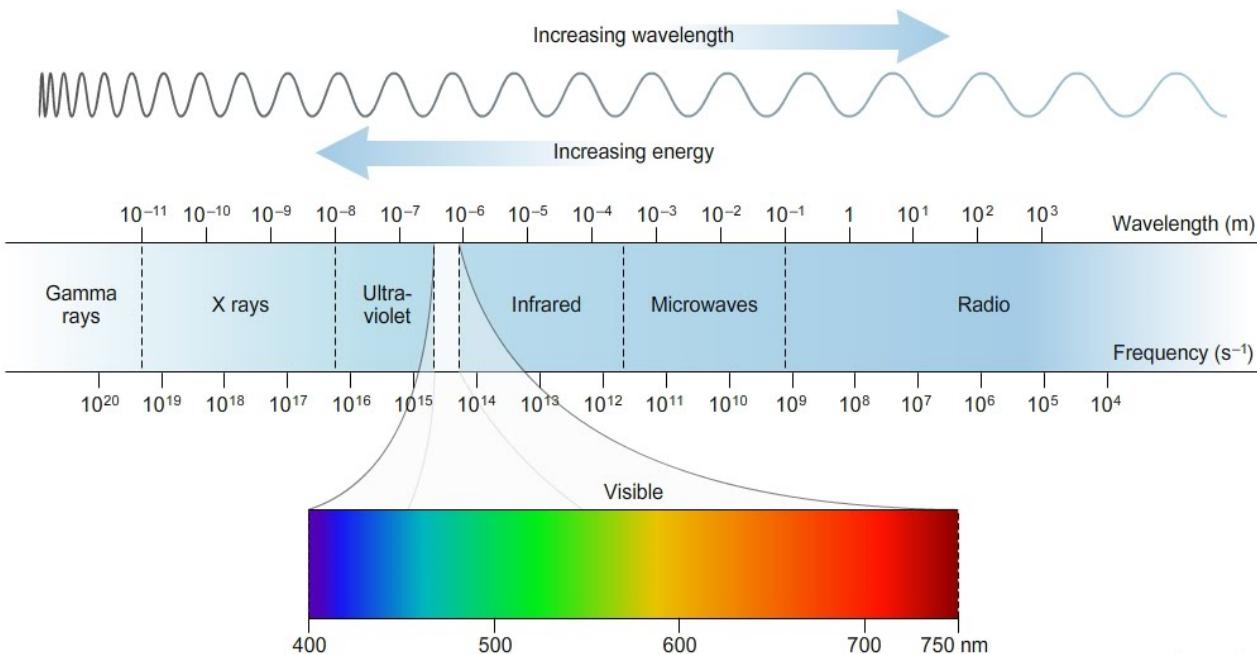
# Comparing with human vision

- Cameras imitate the frequency response of the human eye so it is good to know something about it
- Computer vision probably would not get as much attention if biological vision (especially human vision) had not proven that it is possible to make important judgements from 2D images

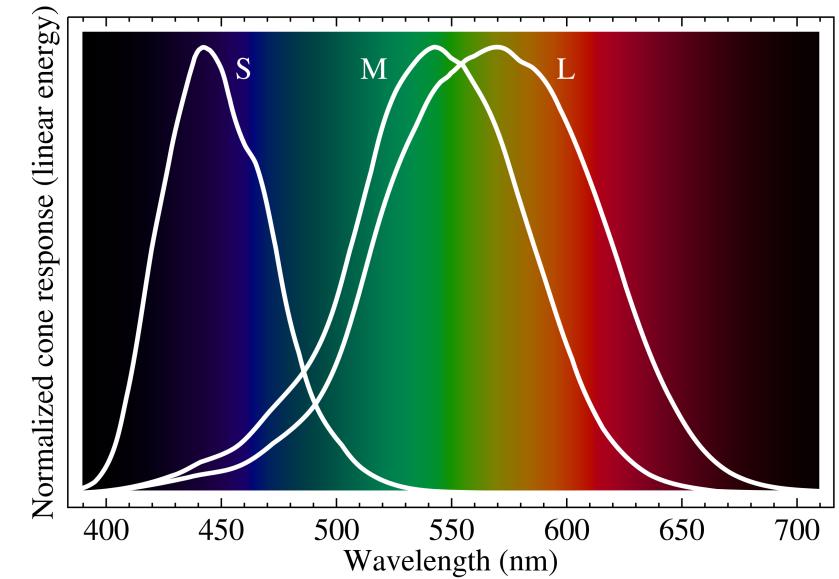


The Eye

# Electromagnetic spectrum

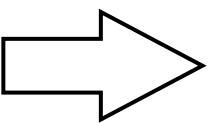


<https://sites.google.com/site/chempendix/em-spectrum>



Normalized responsivity spectra of human cone cells (S, M, L types)

# Colour represented by RGB images



Red



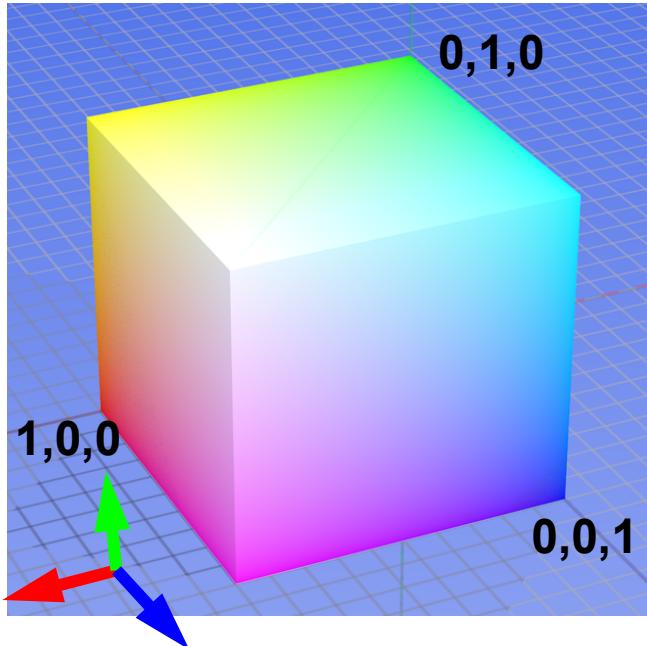
Green



Blue

# Colour spaces: RGB

Default colour space in vision



[Source: Wikipedia](#)



R  
(G=0,B=0)



G  
(R=0,B=0)

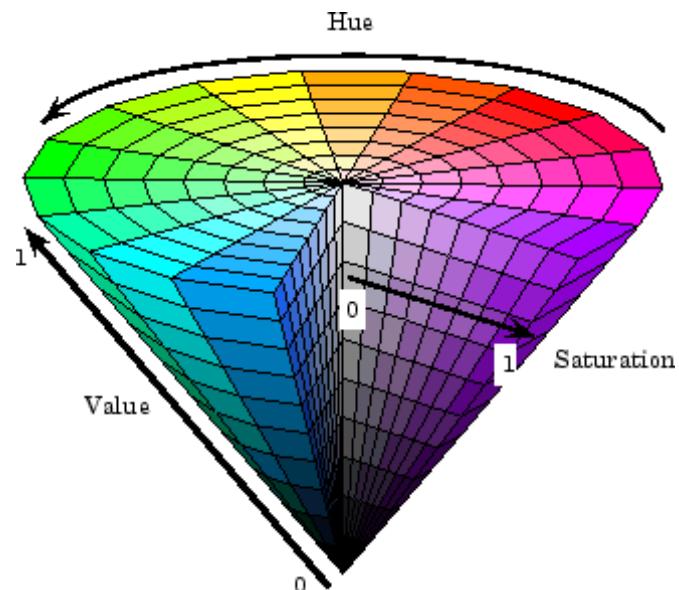


B  
(R=0,G=0)

Drawback: strongly correlated channels

# Colour spaces: HSV

Intuitive colour space



H  
( $S=1, V=1$ )



S  
( $H=1, V=1$ )

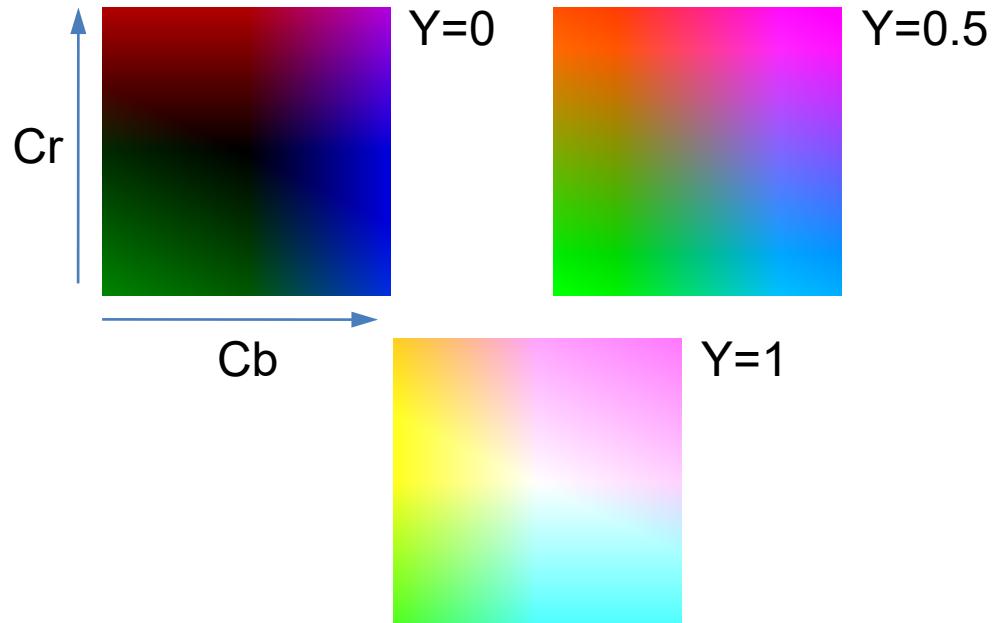


V  
( $H=1, S=0$ )

Drawback: confounded channels

# Colour spaces: YCbCr

Fast to compute, good for compression, used by TV



Y  
(Cb=0.5,Cr=0.5)



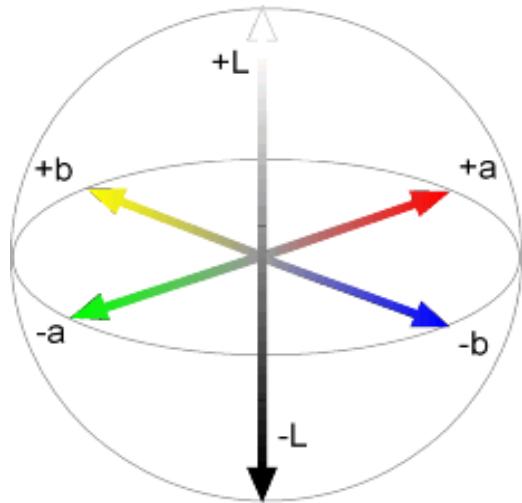
Cb  
(Y=0.5,Cr=0.5)



Cr  
(Y=0.5,Cb=0.5)

# Colour spaces: L\*a\*b\*

“Perceptually uniform” colour space



a.k.a. CIELAB

Any numerical change corresponds to  
similar perceived change in color:  
Euclidean distances make sense



L  
( $a=0, b=0$ )

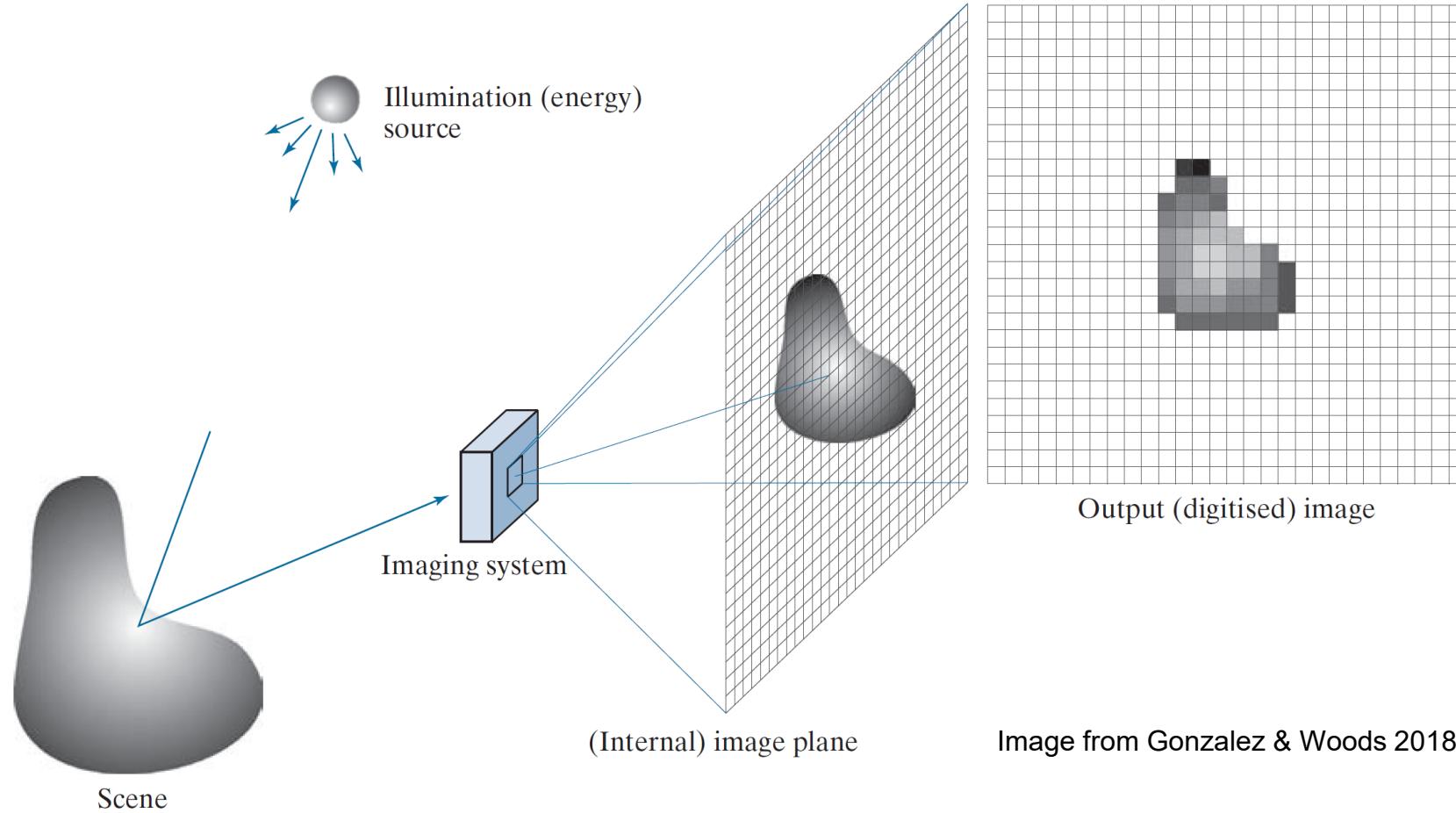


a  
( $L=65, b=0$ )

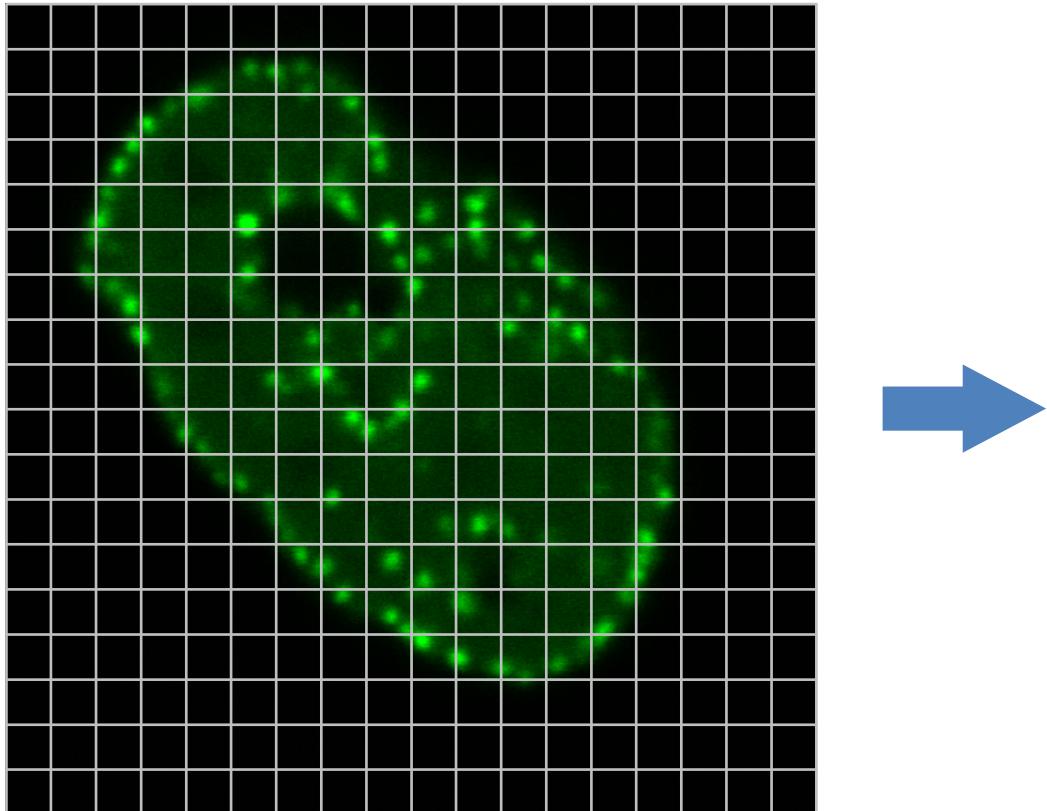


b  
( $L=65, a=0$ )

# Digital image formation

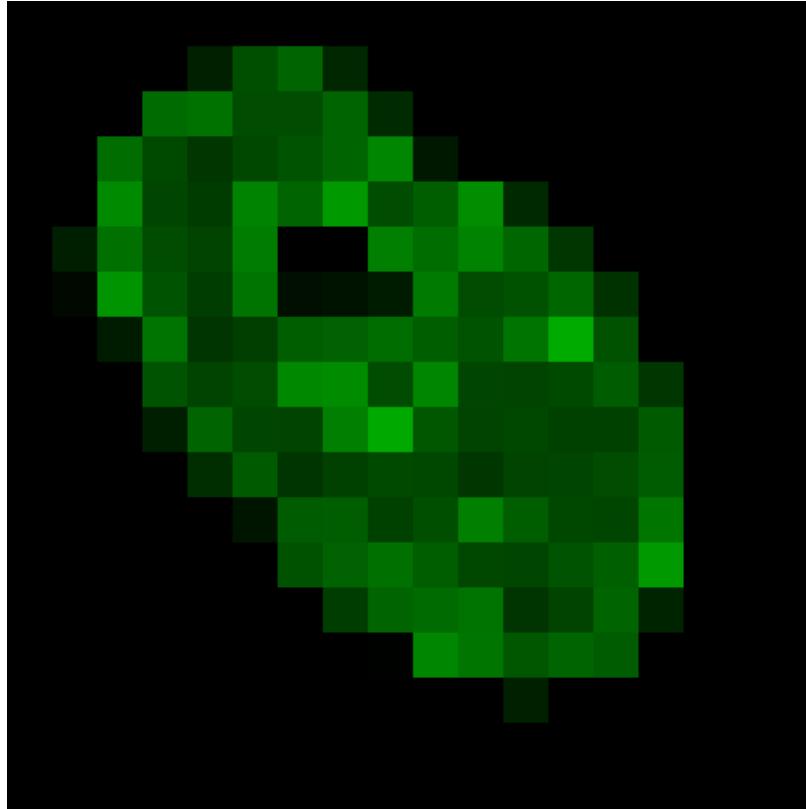
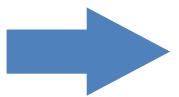


# Digital image formation

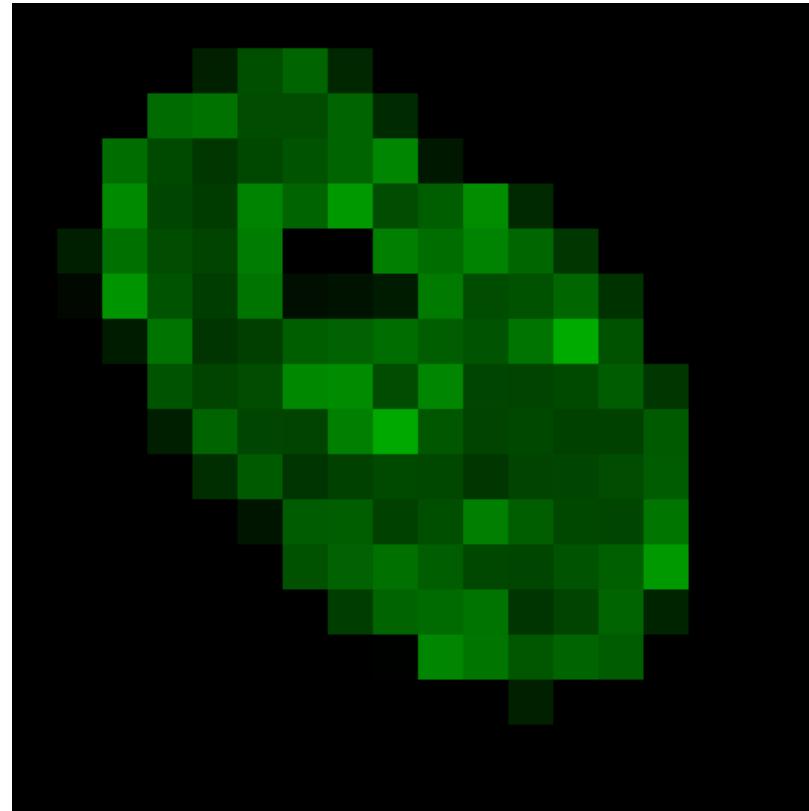
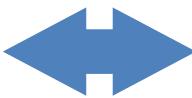
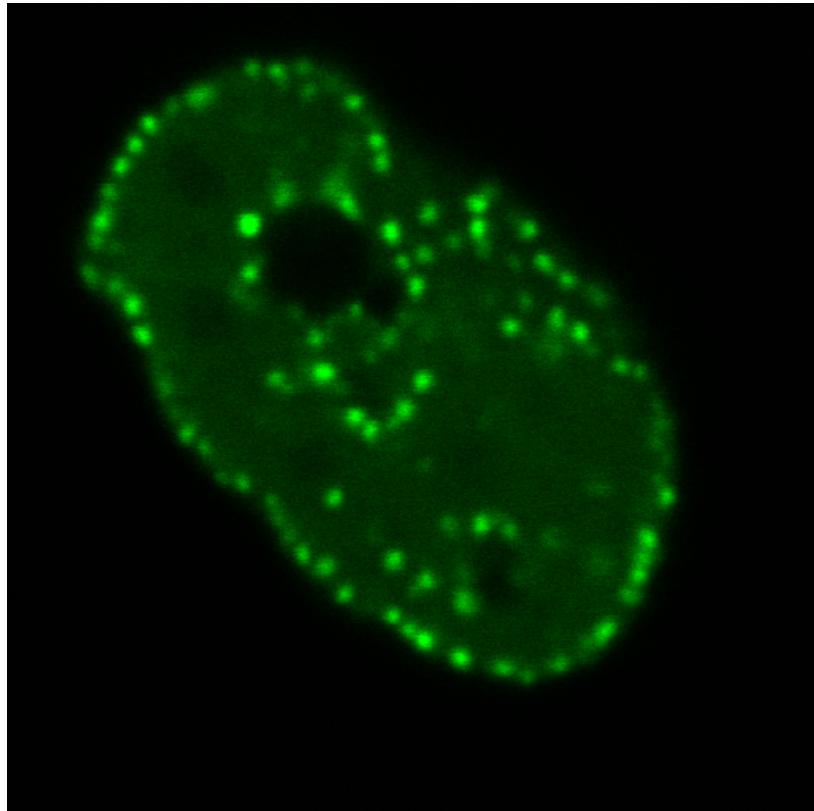


# Displaying a digital image

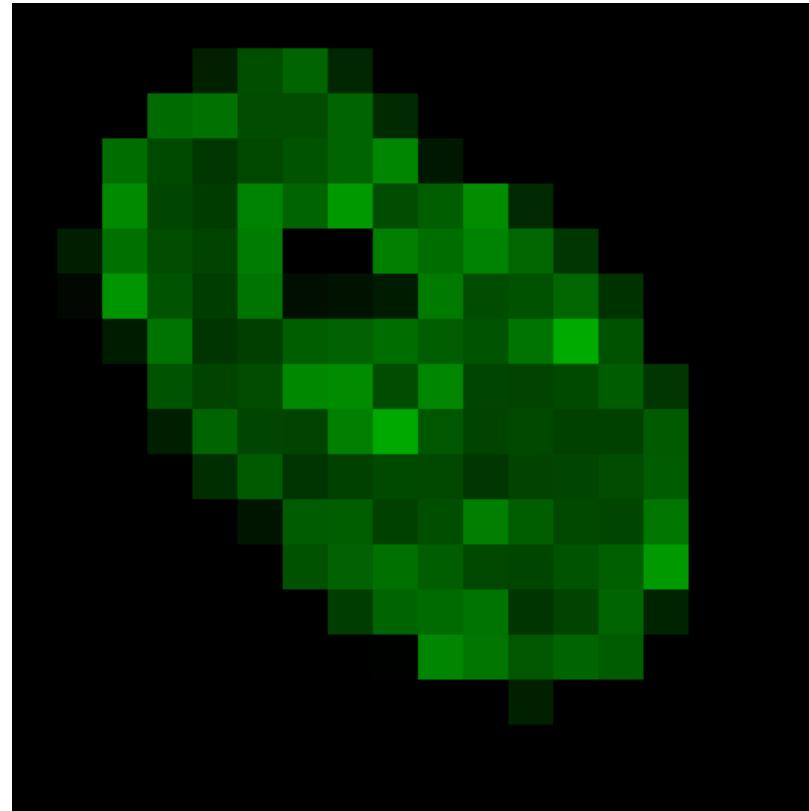
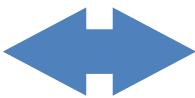
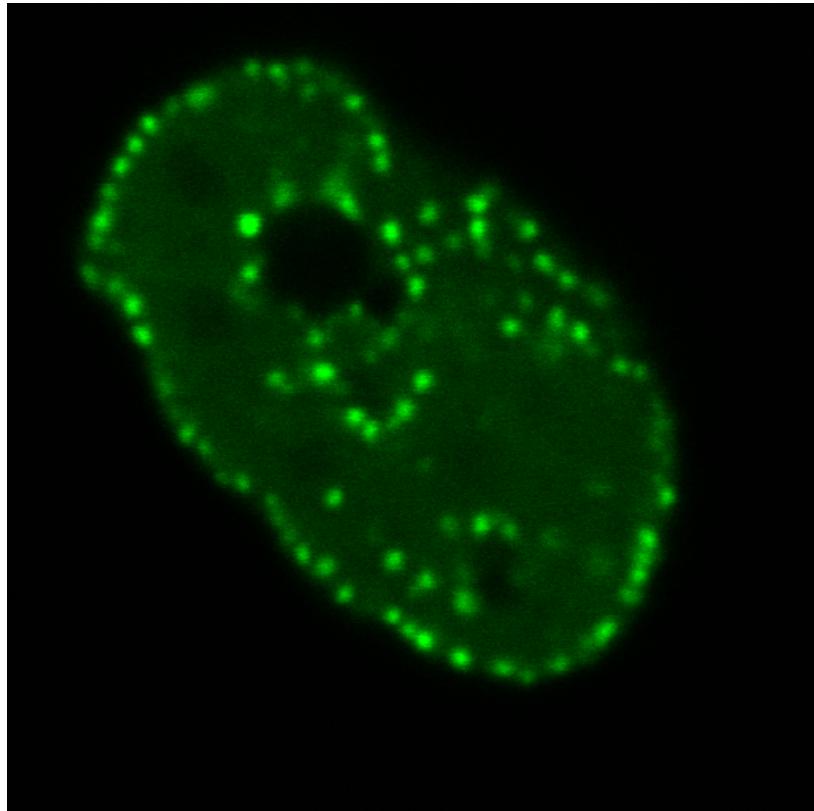
0	2	2	2	5	8	11	8	2	2	0	0	0	0	0	0	0	0	0	
0	0	2	11	76	136	164	85	11	5	2	2	0	0	0	0	0	0	0	
0	2	25	172	181	133	133	164	90	14	5	2	2	0	0	0	0	0	0	
2	5	175	130	104	127	141	164	206	65	31	11	2	2	0	0	0	0	0	
2	28	212	124	110	204	164	232	133	155	218	87	14	2	2	0	0	0	0	
2	73	178	133	121	195	34	31	198	175	204	167	104	14	5	0	0	0	0	
2	45	226	141	113	184	53	59	70	192	133	138	167	99	11	2	0	0	0	
0	2	70	184	102	116	155	161	175	155	141	184	255	138	34	5	2	0	0	
0	0	5	141	121	133	209	215	133	206	124	121	130	153	104	8	2	0	0	
0	0	2	73	164	124	121	198	252	147	121	127	119	119	150	19	2	0	0	
0	0	0	5	93	150	102	119	130	127	104	121	124	133	153	25	2	0	0	
0	0	0	0	5	62	153	155	119	136	198	155	127	124	141	158	232	5	2	2
0	0	0	0	0	5	138	161	178	155	127	124	141	158	232	5	2	2	2	
0	0	0	0	0	0	11	113	164	172	184	102	121	164	79	2	2	2	2	
0	0	0	0	0	0	2	5	36	206	187	147	164	153	5	2	2	0	0	
0	0	0	0	0	0	0	0	2	5	25	76	31	2	2	2	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	



# Comparing the original and digital image

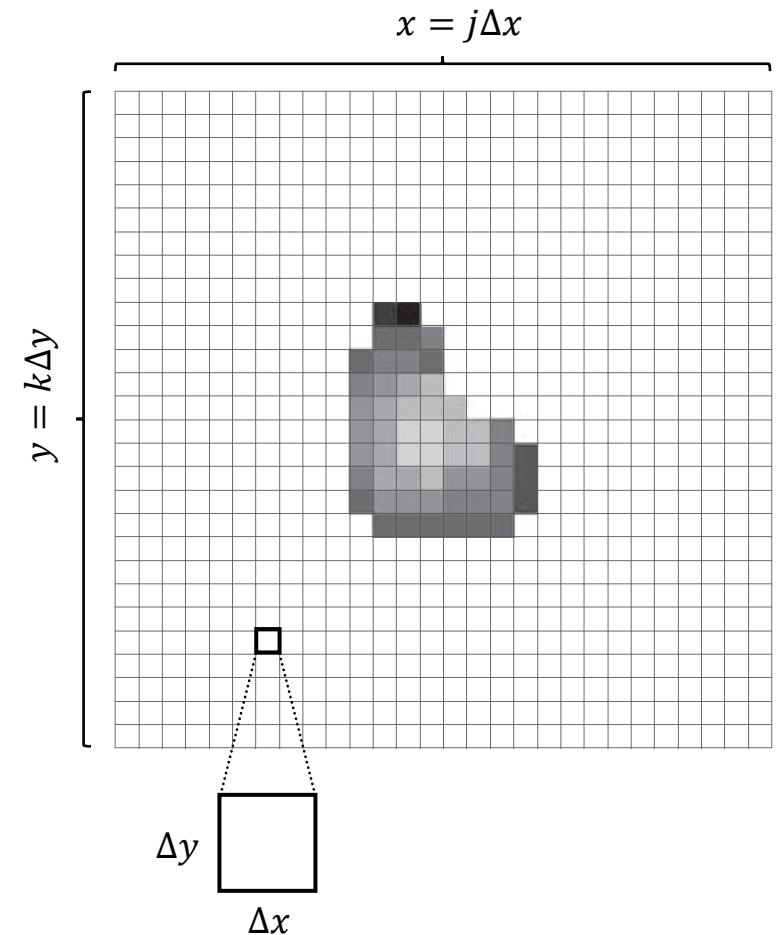


# Comparing the original and digital image



# Digitisation by spatial sampling

- Digitisation converts an analog image to a digital image by sampling the image space
- Sampling discretises the coordinates  $x$  and  $y$ 
  - Spatial discretisation of a picture function  $f(x, y)$
  - Typically a rectangular grid of sampling points is used
  - $x = j\Delta x, y = k\Delta y$  for  $j = 0 \dots M - 1, k = 0 \dots N - 1$
  - The  $\Delta x$  and  $\Delta y$  are called the sampling intervals



# Digital colour images

Each channel is a digital image with the same number of rows and columns

row	column												R	G						B		
0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99												
0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91												
0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92												
0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95												
0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.37	0.85	0.97	0.93	0.92	0.99						
0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.31	0.75	0.92	0.81	0.95	0.91						
0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74	0.42	0.57	0.41	0.49	0.91	0.92						
0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.46	0.91	0.87	0.90	0.97	0.95						
0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.37	0.80	0.88	0.89	0.79	0.85	0.37	0.85	0.99			
0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.60	0.58	0.50	0.61	0.45	0.33	0.31	0.75	0.92	0.81	0.95	0.91
0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.39	0.73	0.92	0.91	0.49	0.74	0.42	0.57	0.41	0.49	0.91	0.92
						0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.46	0.91	0.87	0.90	0.97	0.95
						0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.37	0.80	0.88	0.89	0.79	0.85
						0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.60	0.58	0.50	0.61	0.45	0.33
						0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.39	0.73	0.92	0.91	0.49	0.74
											0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	
											0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	
											0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
											0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

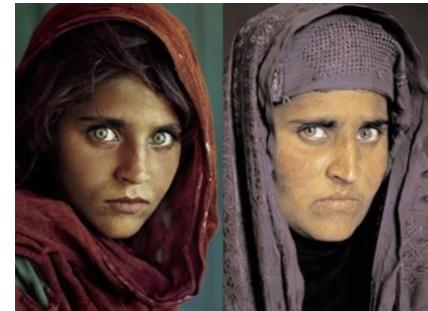
# Spatial resolution

- Spatial resolution: number of pixels per unit of length
- Example: resolution decreases by one half each time (see right)
- Human faces can be recognized at  $64 \times 64$  pixels per face
- Appropriate resolution is essential:
  - Too little resolution yields poor recognition
  - Too much resolution is slow and wastes memory

1/2



1/1



1/8



1/4



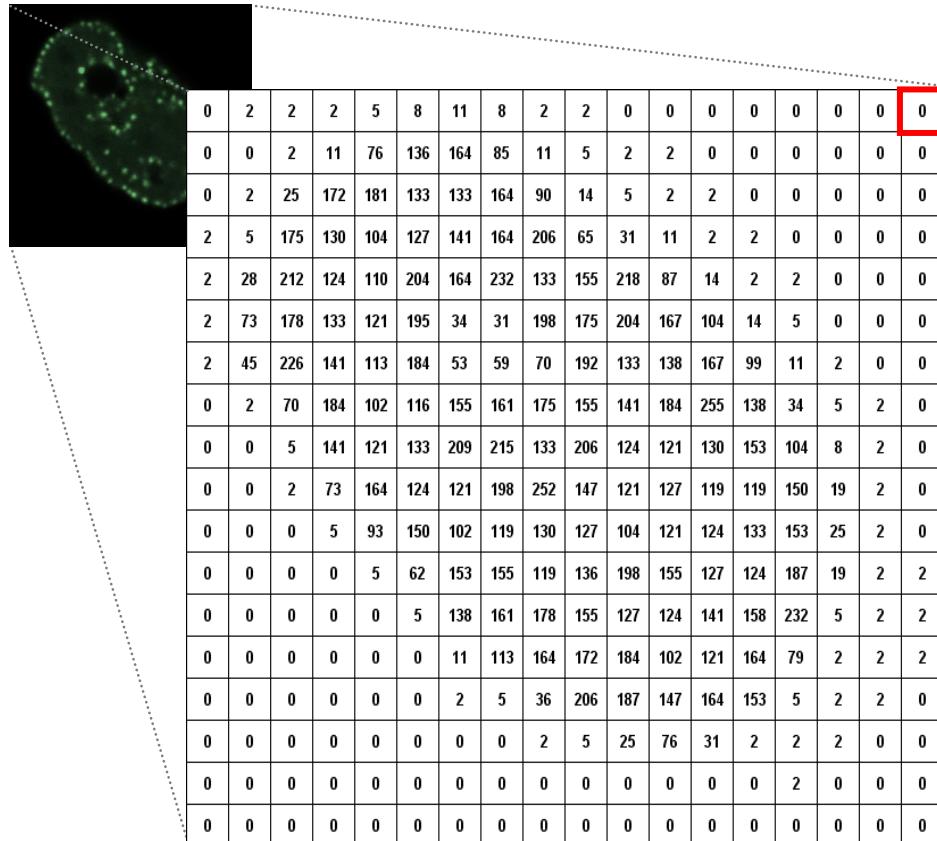
1/16



# Quantisation

- Quantisation digitises the image intensity or amplitude values  $f(x, y)$ 
  - Called intensity or gray-level quantisation
  - Gray-level resolution to be chosen per application
    - ❖ For example, 16, 32, 64, ..., 128, 256 levels
    - ❖ Should be high enough for human perception of shading details
    - ❖ The latter requires about 100 levels for a realistic image
    - ❖ Should not be higher than necessary to avoid wasting storage

# Quantisation and bits per pixel



→ **Pixel (picture element)**

**Levels per pixel:**

$$8 \text{ bits} = 2^8 = 256$$

$$12 \text{ bits} = 2^{12} = 4,096$$

$$16 \text{ bits} = 2^{16} = 65,536$$

$$24 \text{ bits} = 2^{24} = 16,777,216$$

# Further reading on discussed topics

- Chapter 2 of Szeliski
- Chapter 2 of Shapiro and Stockman

# Acknowledgements

- Several slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth
- Some material drawn from referenced and associated online sources
- Image sources credited where possible