

$$1a. f(x) = x - 5$$

$$f^{-1}(x) = \frac{x+5}{1}$$

$$b. g(t) = 2t - 7$$

$$g^{-1}(t) = \frac{t+7}{2}$$

$$c. y(x) = (2x)^3$$

$$y^{-1}(x) = \sqrt[3]{\frac{x}{2}} \Rightarrow \left(\frac{x}{2}\right)^{\frac{1}{3}}$$

$$d. h(t) = \frac{t^2}{3}$$

$$h^{-1}(t) = 3(t+2)$$

$$2. f(t) = 3t, g(t) = t+2, h(t) = t^3$$

$$a. f(g(t)) = f(t+2) = 3(t+2)$$

$$b. f(g(x)) = f(y+2) = 3(y+2)$$

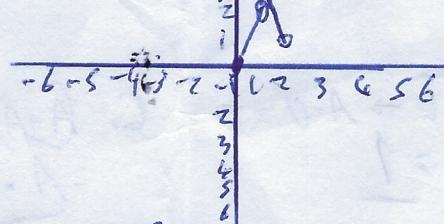
$$c. f(h(t)) = f(t^3) = 3(t^3)$$

$$d. f(f(g(h(t)))) = f(g(t^3)) = f(t^3 + 2) = 3(t^3 + 2)$$

$$e. (f(f(y))) = (f(3(y))) = 3(3(y)) = 9(y) = 9x$$

$$3. f(t) = \begin{cases} 2t, & 0 \leq t < 1 \\ 6-t, & 1 \leq t < 2 \end{cases}$$

a. It is neither a PWCF
or a CTF

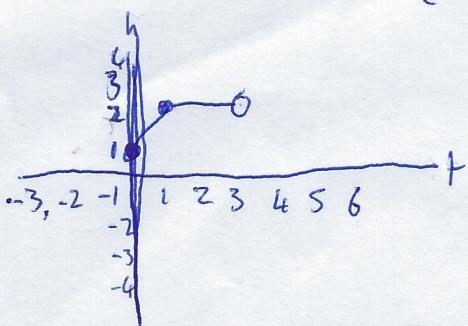


b. There are discontinuities at ~~t=0, 1, 2~~ ~~at t=0, 1, 2~~ $t=1$

c. ~~f(t)~~ Range $[0, 2]$

$$4. h(t) = \begin{cases} t+1, & 0 \leq t \leq 1 \\ 2, & 1 \leq t < 3 \end{cases}$$

h on $[3, 6]$



No discontinuities between $[3, 6]$

5. a. $-2x > 7$ is true if ~~$x < -4$~~ $x \leq -4$

b. $3v - 7 \leq 2$

$$\begin{array}{rcl} -2 & -2 \\ 3v - 9 & \leq 0 \\ +9 & +9 \\ \hline 3v & \leq 9 \\ \hline 3 & 3 \end{array}$$

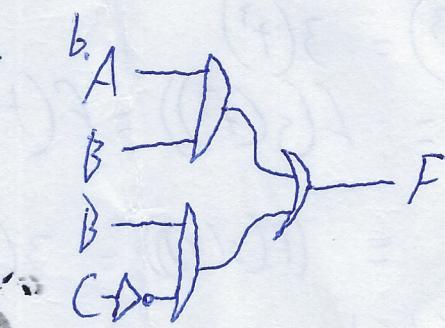
c. ~~$v \leq 9$~~

c. $\frac{4-2w}{3} < 2 = \frac{4-2w < 6}{-4} = \frac{-2w < 2}{x-2} = w < -4$

d. $(x-2)^2 < 1 = x-2 < \sqrt{1} = x < 3$ if $x < 3$ then

e. $(A \cdot B) + (B \cdot \bar{C})$

| A | B | C | \bar{C} | $A \cdot B$ | $B \cdot \bar{C}$ | F |
|---|---|---|-----------|-------------|-------------------|---|
| 1 | 1 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 |



7. a. $(A \cdot A) + \bar{A} = 1$
 $= A + \bar{A} = 1$

b. $\overline{A \cdot 0} = A \cdot 0 = 0$
 $\therefore \overline{0} = 1$

c. $(A+A) \cdot (B+B)$
 $= A \cdot B$

d. $(A \cdot B + A \cdot \bar{B}) \cdot B \cdot C + A \cdot B \cdot C$
 $= A(B + \bar{B}) \cdot B \cdot C + A \cdot B \cdot C$
 $= A(1) \cdot B \cdot C + A \cdot B \cdot C$
 $= A \cdot B \cdot C + A \cdot B \cdot C$
 $= A \cdot A \cdot B \cdot C$
 $= A \cdot B \cdot C$
 $= A + A \cdot (B \cdot C)$
 $= A + (B \cdot C)$

8. $(A \cdot B) + (\bar{A} \cdot \bar{B})$
 $= \overline{A \cdot B} + \overline{\bar{A} \cdot \bar{B}}$
 $\cancel{A \cdot B} + \cancel{\bar{A} \cdot \bar{B}}$

$\overline{A \cdot B} \cdot \overline{\bar{A} \cdot \bar{B}}$

Ex 9.

| A | B | C | X | |
|---|---|---|---|--------|
| 1 | 1 | 1 | 1 | ABC |
| 1 | 1 | 0 | 1 | $+ABC$ |
| 1 | 0 | 1 | 1 | $+ABC$ |
| 1 | 0 | 0 | 1 | $+ABC$ |
| 0 | 1 | 1 | 1 | $+ABC$ |
| 0 | 1 | 0 | 0 | |
| 0 | 0 | 1 | 0 | |
| 0 | 0 | 0 | 0 | |

$$DNF = \boxed{ABC + AB\bar{C}} + A\bar{B}C + \cancel{\bar{A}BC} + \cancel{\bar{A}\bar{B}C}$$

$$= A \cdot B \cdot (C + \bar{C})$$

$$= AB1$$

$$= AB$$

$$AB \cancel{ABC} + \boxed{\bar{A}\bar{B}C + A\bar{B}\bar{C} + \bar{A}BC}$$

$$= AB(\bar{C} + \bar{C})$$

= as before

$$\boxed{AB + \bar{A}\bar{B} + \bar{A}BC}$$

$$= A(B + \bar{B}) + \bar{A}BC$$

= as before $\bar{A} + \bar{A}BC$

$$= A + \bar{A}BC$$

As DNF

$$A + A \geq A$$

so $\bar{A}BC$

$$\begin{array}{c} A \\ \swarrow \\ B \\ \searrow \\ C \end{array} \rightarrow A + B \cdot C$$