

```

> 12 + 4 - 5
11
(1)

> 12 + 4 - 5
11
(2)

> 2^10
1024
(3)

> sin(0.1)
0.09983341665
(4)

> (a+b)*(a-b)
(a + b) (a - b)
(5)

> expand((a+b)*(a-b))
a2 - b2
(6)

> y:=x->3*(x^3)+2*(x^2)-5
y := x → 3·x3 + 2·x2 - 5
(7)

> diff(y(x),x)
9 x2 + 4 x
(8)

> y:=x->sqrt(1+x^4)
y := x → √(1 + x4)
(9)

> diff(y(x),x)

$$\frac{2 x^3}{\sqrt{x^4 + 1}}$$

(10)

> y:=x->(exp(x))*(sin(x))*(cos(x))
y := x → ex·sin(x)·cos(x)
(11)

> diff(y(x),x)
ex sin(x) cos(x) + ex cos(x)2 - ex sin(x)2
(12)

> int(3*x^3+2*x^2-5,x=0..1)
-  $\frac{43}{12}$ 
(13)

> int(1/x^2,x=0..infinity)
∞
(14)

> int(exp((-1)*x^2),x =-infinity..infinity)

$$\sqrt{\pi}$$

(15)

> evalf(%)
1.772453851
(16)

> limit(sin(x)/x,x=0)
1
(17)

> limit((x^3+3*x^2-5)/(2*x^3-7*x),x=infinity)

$$\frac{1}{2}$$

(18)

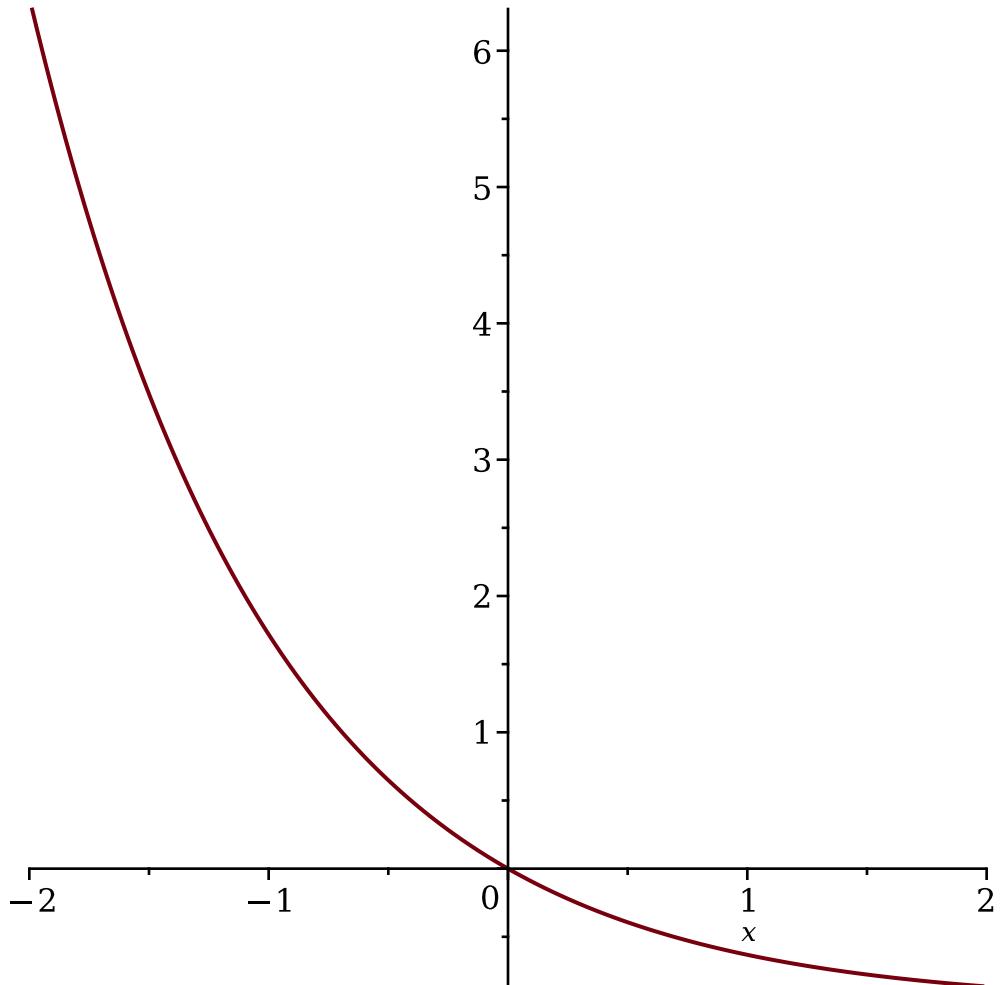
```

```
> limit((cos(x)+1)/(x-Pi),x=Pi) 0 (19)
```

```
> with(plots)  
[animate, animate3d, animatecurve, arrow, changecoords, complexplot,  
complexplot3d, conformal, conformal3d, contourplot, contourplot3d,  
coordplot, coordplot3d, densityplot, display, dualaxisplot, fieldplot,  
fieldplot3d, gradplot, gradplot3d, implicitplot, implicitplot3d, inequal,  
interactive, interactiveparams, intersectplot, listcontplot, listcontplot3d,  
listdensityplot, listplot, listplot3d, loglogplot, logplot, matrixplot,  
multiple, odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot,  
polygonplot, polygonplot3d, polyhedra_supported, polyhedraplot,  
rootlocus, semilogplot, setcolors, setoptions, setoptions3d,  
shadetbetween, spacecurve, sparsematrixplot, surfdata, textplot,  
textplot3d, tubeplot]
```

```
> f:=x->exp(-x)-1  
f := x → e-x - 1 (21)
```

```
> with(plots)  
[animate, animate3d, animatecurve, arrow, changecoords, complexplot,  
complexplot3d, conformal, conformal3d, contourplot, contourplot3d,  
coordplot, coordplot3d, densityplot, display, dualaxisplot, fieldplot,  
fieldplot3d, gradplot, gradplot3d, implicitplot, implicitplot3d, inequal,  
interactive, interactiveparams, intersectplot, listcontplot, listcontplot3d,  
listdensityplot, listplot, listplot3d, loglogplot, logplot, matrixplot,  
multiple, odeplot, pareto, plotcompare, pointplot, pointplot3d, polarplot,  
polygonplot, polygonplot3d, polyhedra_supported, polyhedraplot,  
rootlocus, semilogplot, setcolors, setoptions, setoptions3d,  
shadetbetween, spacecurve, sparsematrixplot, surfdata, textplot,  
textplot3d, tubeplot]  
> plot(f(x),x=-2..2)
```

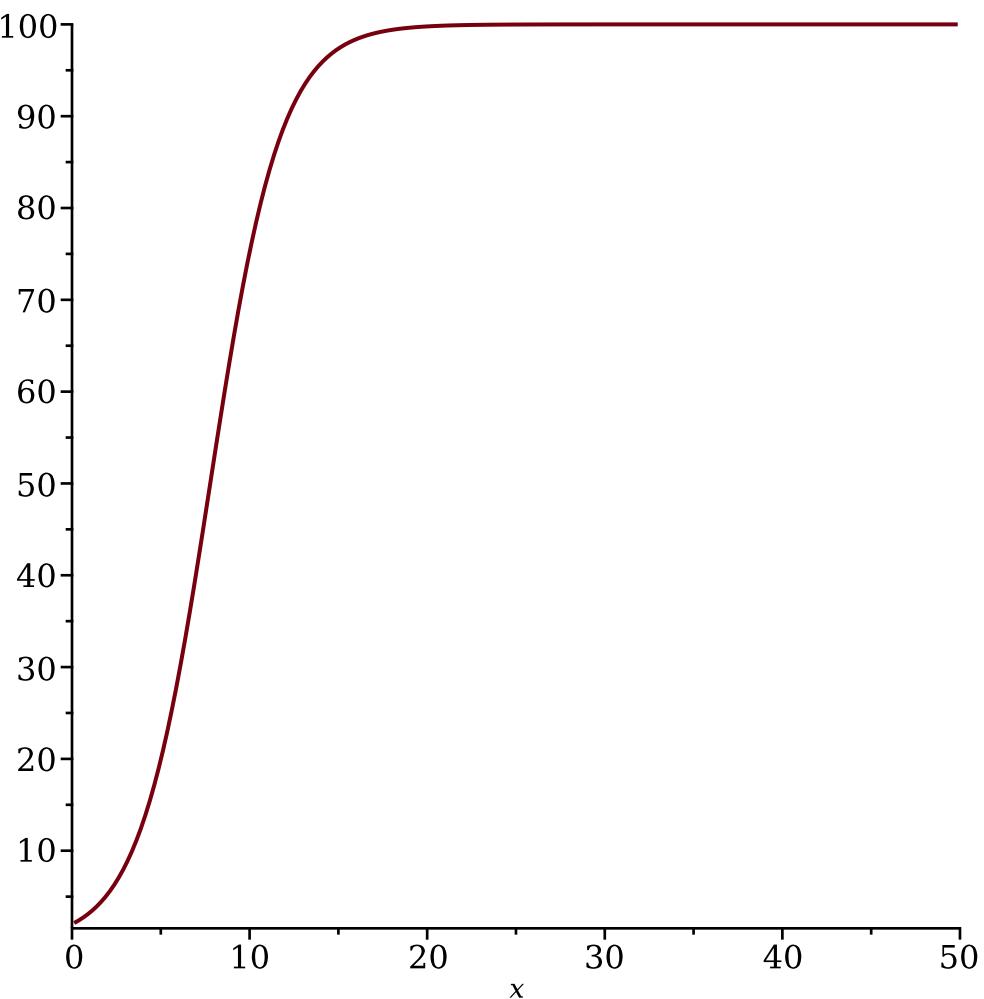


```
> f:=(x,r)->(200*exp(r*x))/(2*(exp(r*x)-1)+100)
```

$$f := (x, r) \mapsto \frac{200 \cdot e^{rx}}{2 \cdot e^{rx} + 98}$$

(23)

```
> plot(f(x,0.5),x=0..50)
```

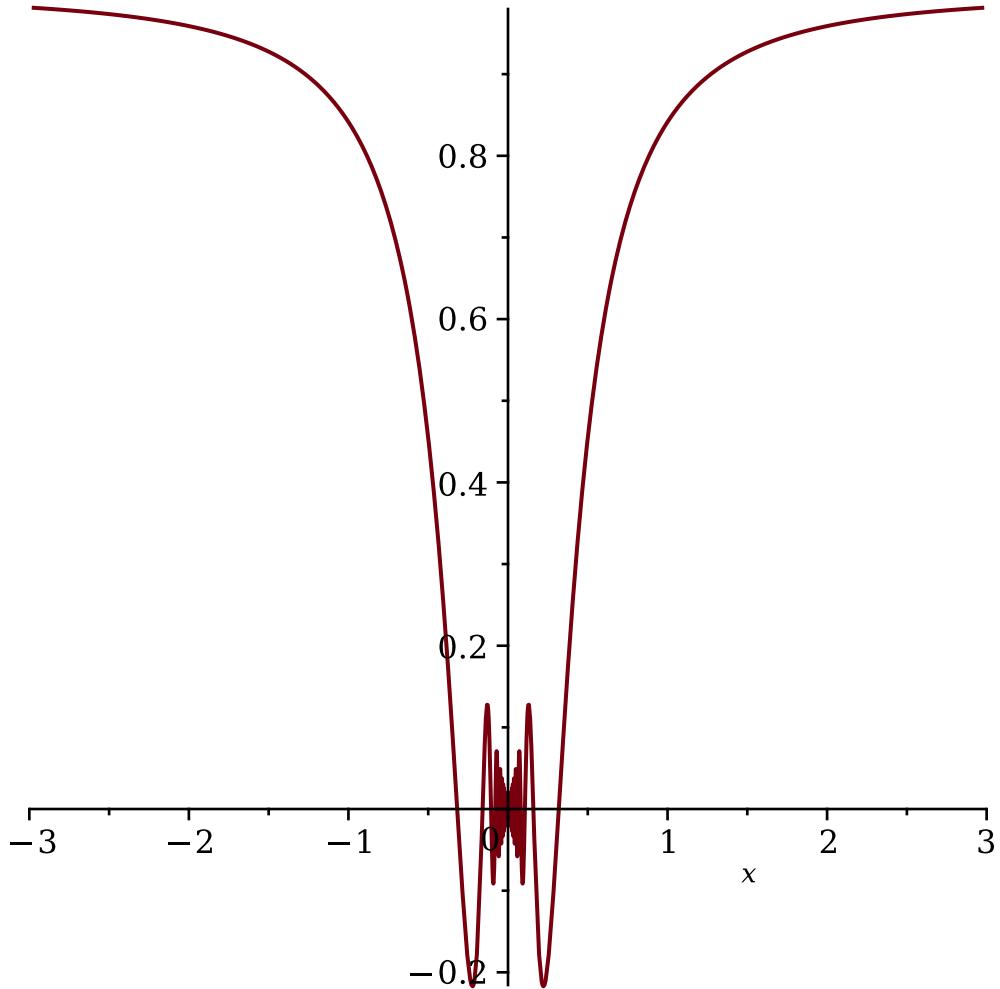


```
> f:=x->x*sin(1/x)
```

$$f := x \mapsto x \cdot \sin\left(\frac{1}{x}\right)$$

(24)

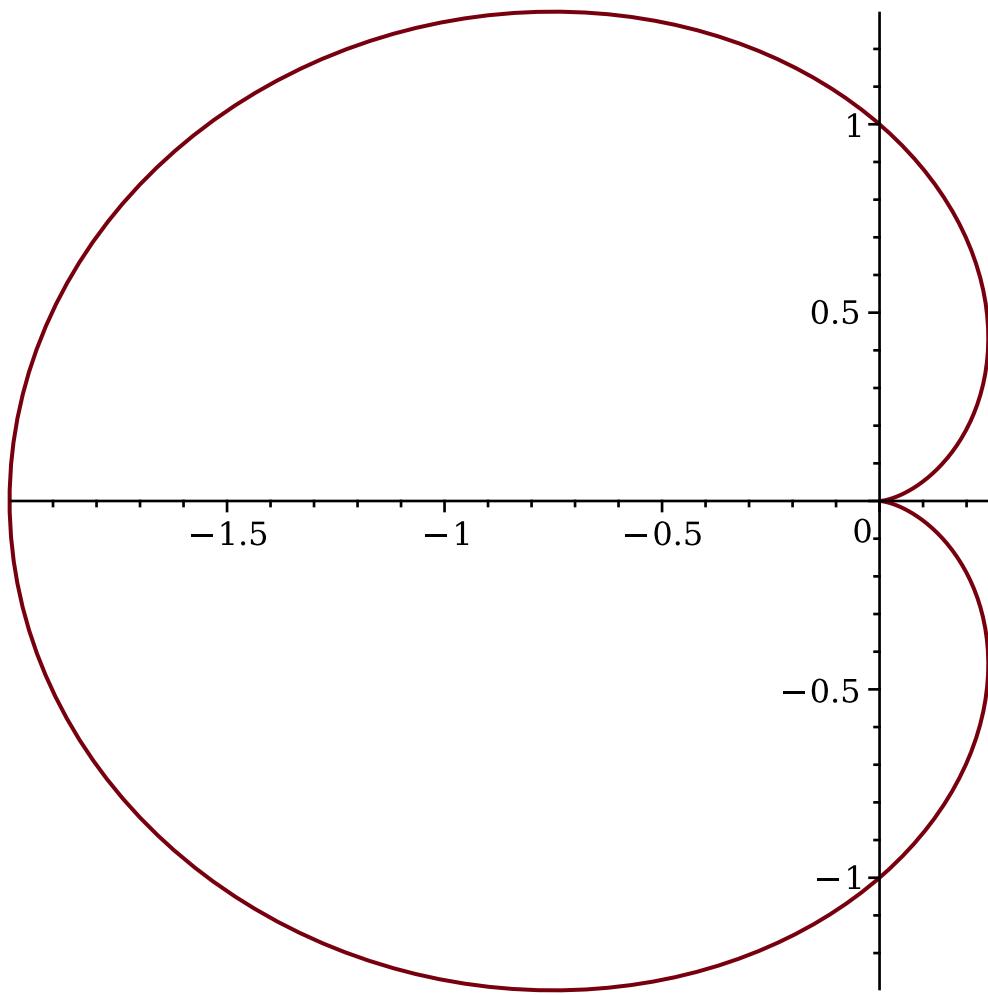
```
> plot(f(x),x=-3..3)
```



```
> x:=t->(1-cos(t))*cos(t)
       $x := t \mapsto (1 - \cos(t)) \cdot \cos(t)$  (25)
```

```
> y:=t->(1-cos(t))*sin(t)
       $y := t \mapsto (1 - \cos(t)) \cdot \sin(t)$  (26)
```

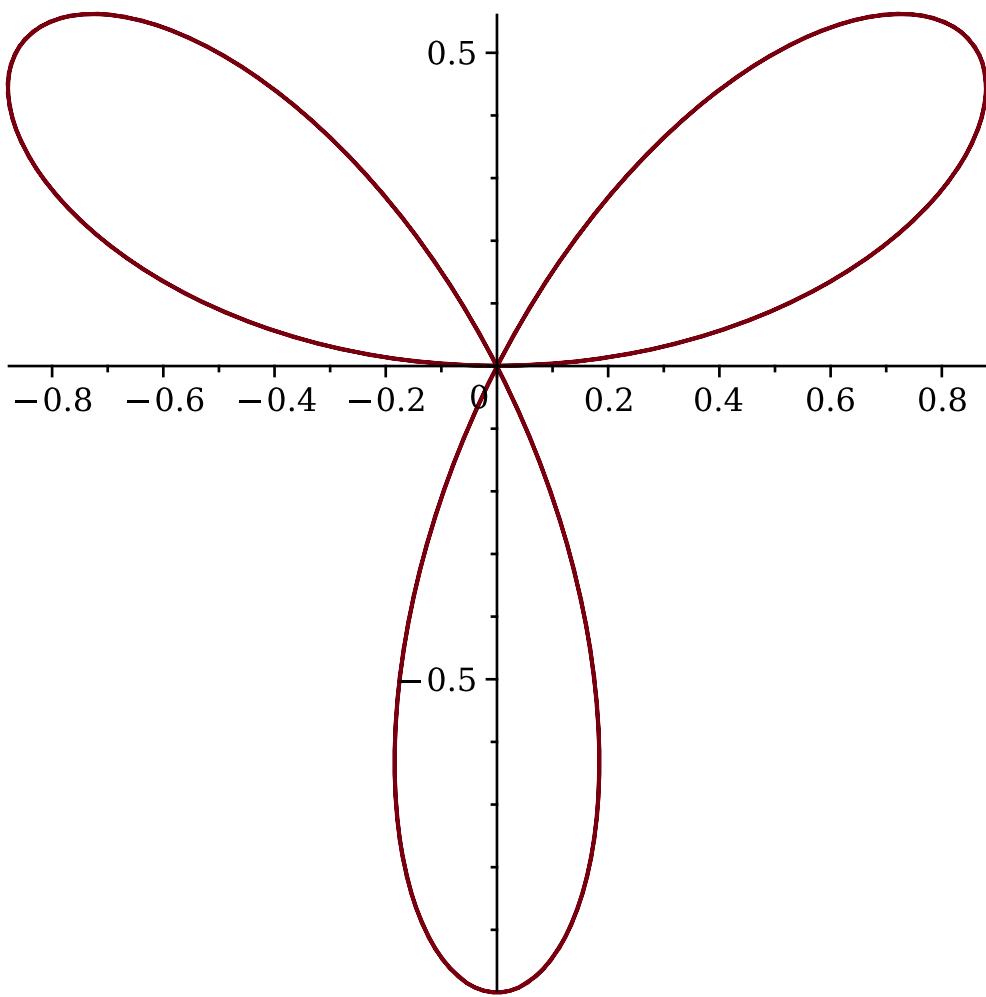
```
> plot([x(t),y(t),t=0..2*Pi])
```



```
> x:=t->sin(3*t)*cos(t) x := t → sin(3·t)·cos(t) (27)
```

```
> y:=t->sin(3*t)*sin(t) y := t → sin(3·t)·sin(t) (28)
```

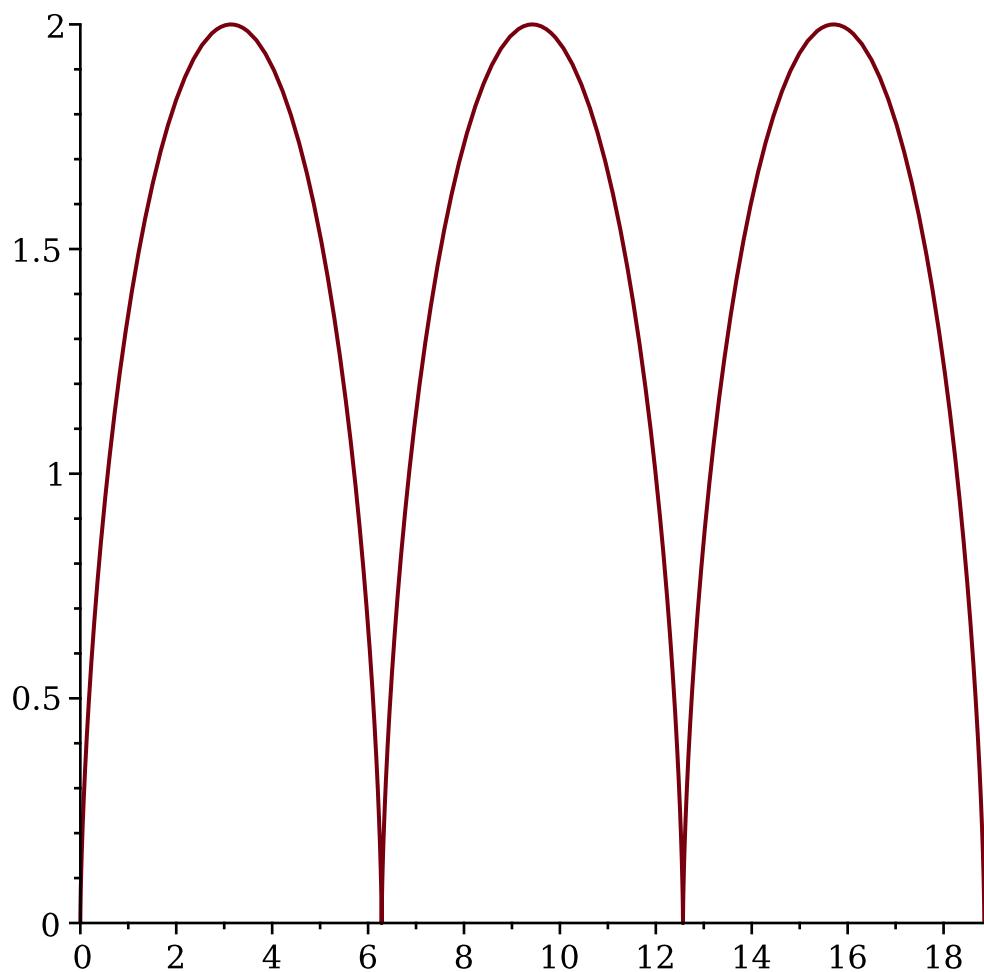
```
> plot([x(t),y(t),t=0..2*Pi])
```



```
> x:=t->t-sin(t)           x := t → t - sin(t)      (29)
```

```
> y:=t->1-cos(t)          y := t → 1 - cos(t)     (30)
```

```
> plot([x(t),y(t),t=0..6*Pi])
```



```

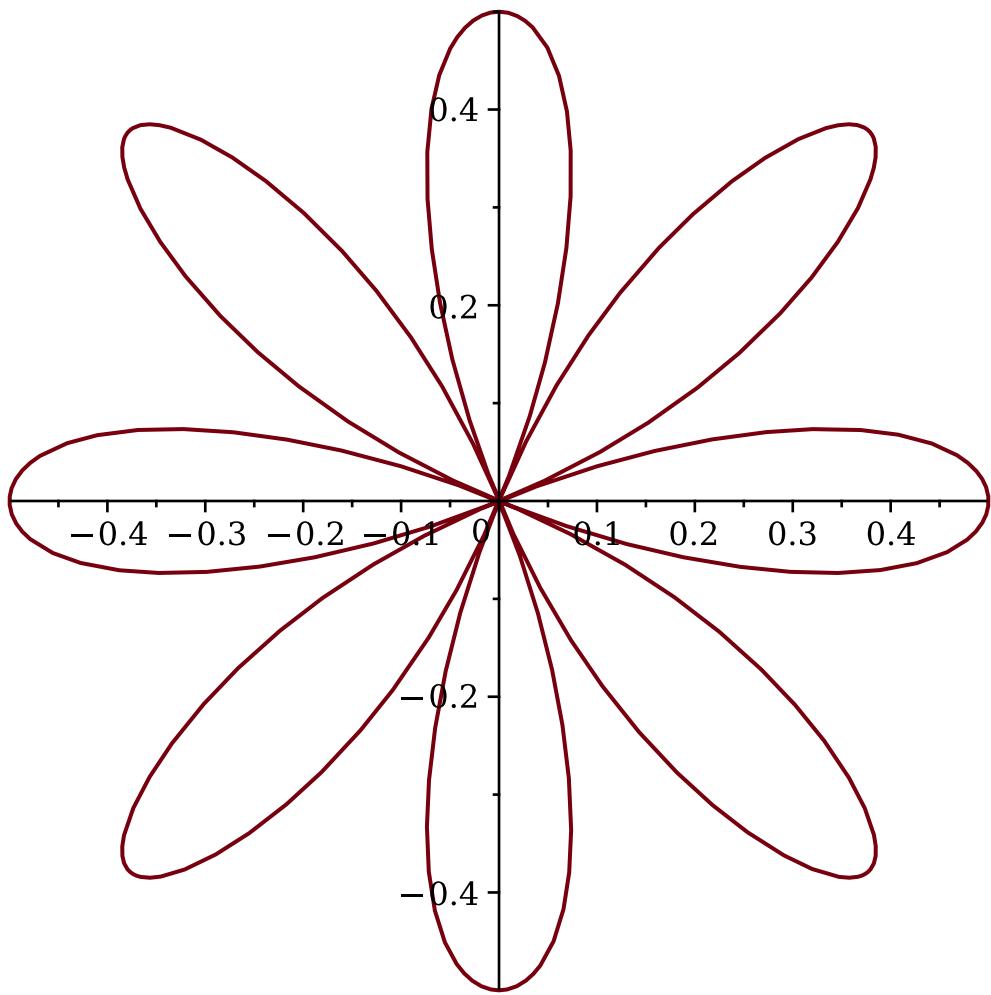
> f:=(t,s)->(s*cos(4*t)*cos(t))/sqrt(1-s^2*cos(4*t)^2*sin(t)^2)
      
$$f := (t, s) \mapsto \frac{s \cdot \cos(4 \cdot t) \cdot \cos(t)}{\sqrt{1 - s^2 \cdot \cos(4 \cdot t)^2 \cdot \sin(t)^2}}$$
 (31)

> x:=t->f(t-Pi/2,0.5)
      
$$x := t \mapsto f\left(t - \frac{\pi}{2}, 0.5\right)$$
 (32)

> y:=t->f(t,0.5)
      
$$y := t \mapsto f(t, 0.5)$$
 (33)

> plot([x(t),y(t),t=0..2*Pi])

```



> **list_f:=[f(t-Pi/2,s/10),f(t,s/10),t=0..2*Pi]\$s=1..10;**

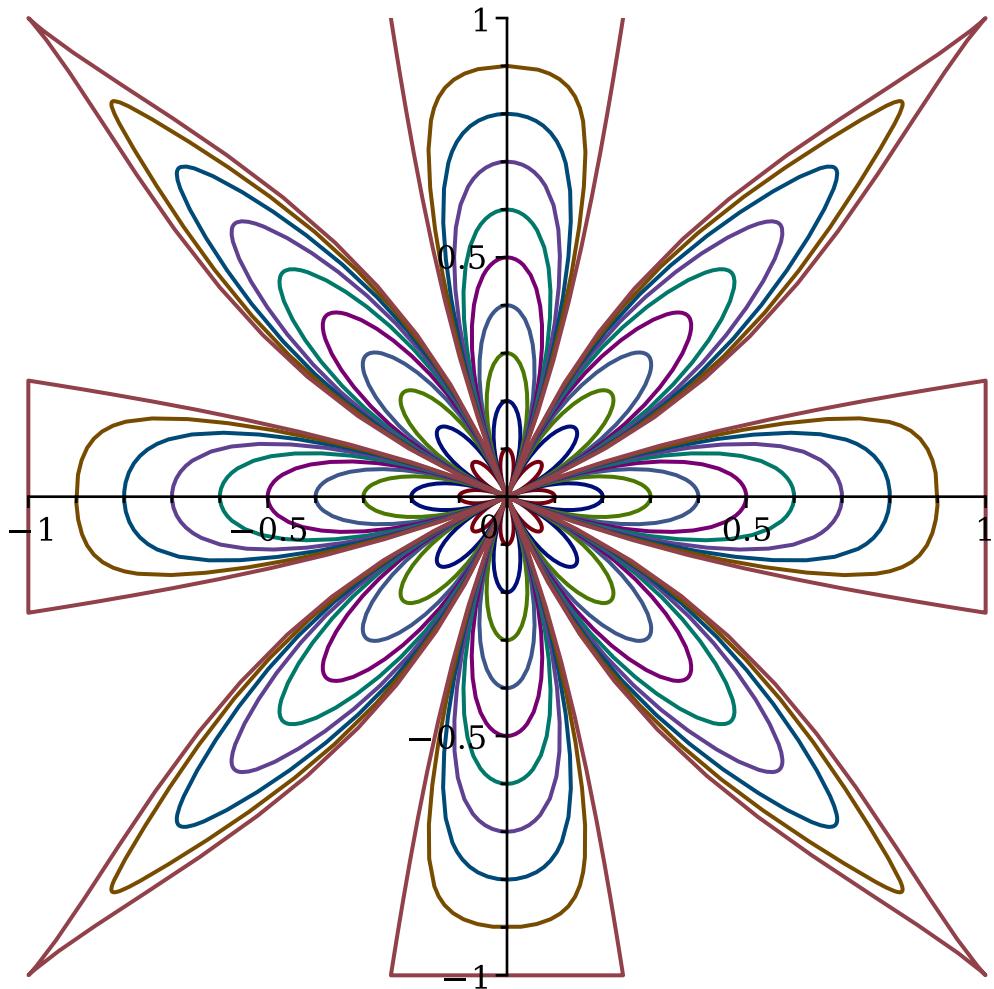
$$\begin{aligned}
 list\ f := & \left[\frac{\cos(4t)\sin(t)}{\sqrt{100-\cos(4t)^2\cos(t)^2}}, \frac{\cos(4t)\cos(t)}{\sqrt{100-\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \quad (34) \\
 & \left[\frac{2\cos(4t)\sin(t)}{\sqrt{100-4\cos(4t)^2\cos(t)^2}}, \frac{2\cos(4t)\cos(t)}{\sqrt{100-4\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \\
 & \left[\frac{3\cos(4t)\sin(t)}{\sqrt{100-9\cos(4t)^2\cos(t)^2}}, \frac{3\cos(4t)\cos(t)}{\sqrt{100-9\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \\
 & \left[\frac{4\cos(4t)\sin(t)}{\sqrt{100-16\cos(4t)^2\cos(t)^2}}, \frac{4\cos(4t)\cos(t)}{\sqrt{100-16\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \\
 & \left[\frac{5\cos(4t)\sin(t)}{\sqrt{100-25\cos(4t)^2\cos(t)^2}}, \frac{5\cos(4t)\cos(t)}{\sqrt{100-25\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \\
 & \left[\frac{6\cos(4t)\sin(t)}{\sqrt{100-36\cos(4t)^2\cos(t)^2}}, \frac{6\cos(4t)\cos(t)}{\sqrt{100-36\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right], \\
 & \left[\frac{7\cos(4t)\sin(t)}{\sqrt{100-49\cos(4t)^2\cos(t)^2}}, \frac{7\cos(4t)\cos(t)}{\sqrt{100-49\cos(4t)^2\sin(t)^2}}, t = 0..2\pi \right],
 \end{aligned}$$

$$\left[\frac{8 \cos(4t) \sin(t)}{\sqrt{100 - 64 \cos(4t)^2 \cos(t)^2}}, \frac{8 \cos(4t) \cos(t)}{\sqrt{100 - 64 \cos(4t)^2 \sin(t)^2}}, t = 0..2\pi \right],$$

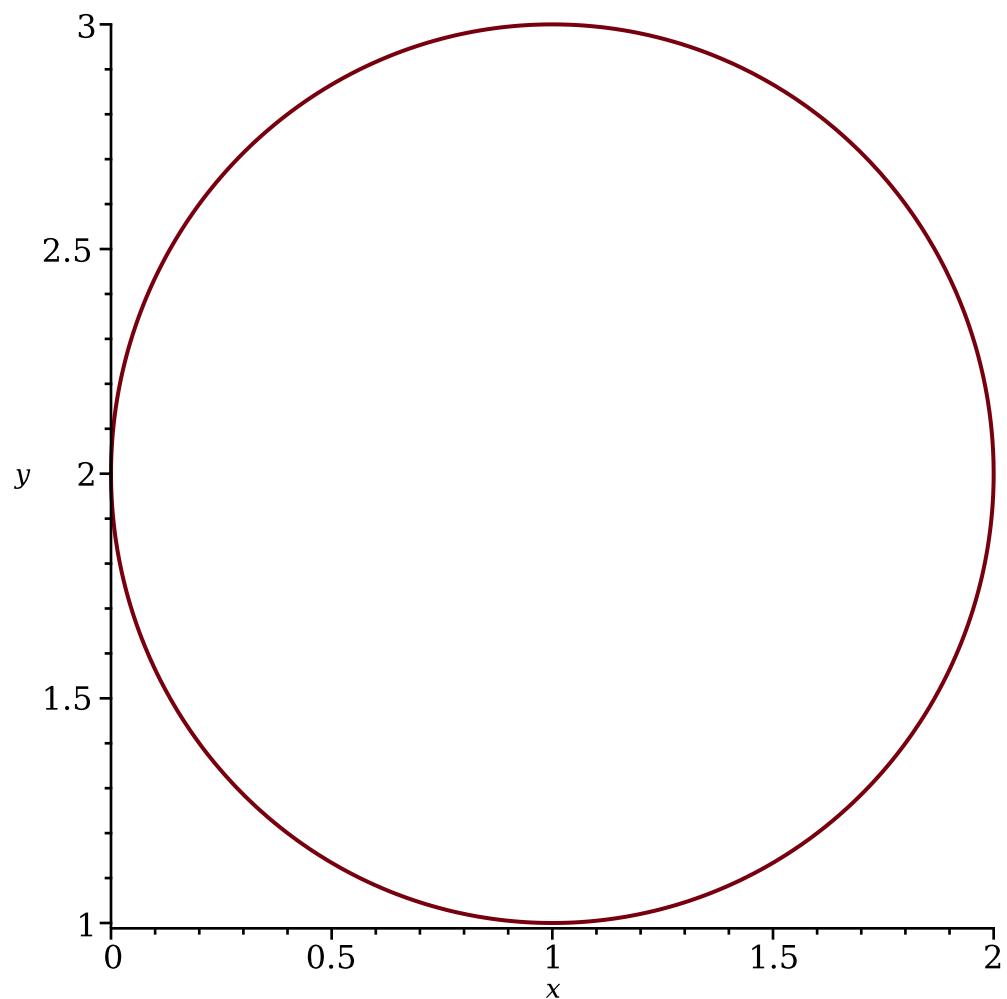
$$\left[\frac{9 \cos(4t) \sin(t)}{\sqrt{100 - 81 \cos(4t)^2 \cos(t)^2}}, \frac{9 \cos(4t) \cos(t)}{\sqrt{100 - 81 \cos(4t)^2 \sin(t)^2}}, t = 0..2\pi \right],$$

$$\left[\frac{10 \cos(4t) \sin(t)}{\sqrt{100 - 100 \cos(4t)^2 \cos(t)^2}}, \frac{10 \cos(4t) \cos(t)}{\sqrt{100 - 100 \cos(4t)^2 \sin(t)^2}}, t = 0..2\pi \right]$$

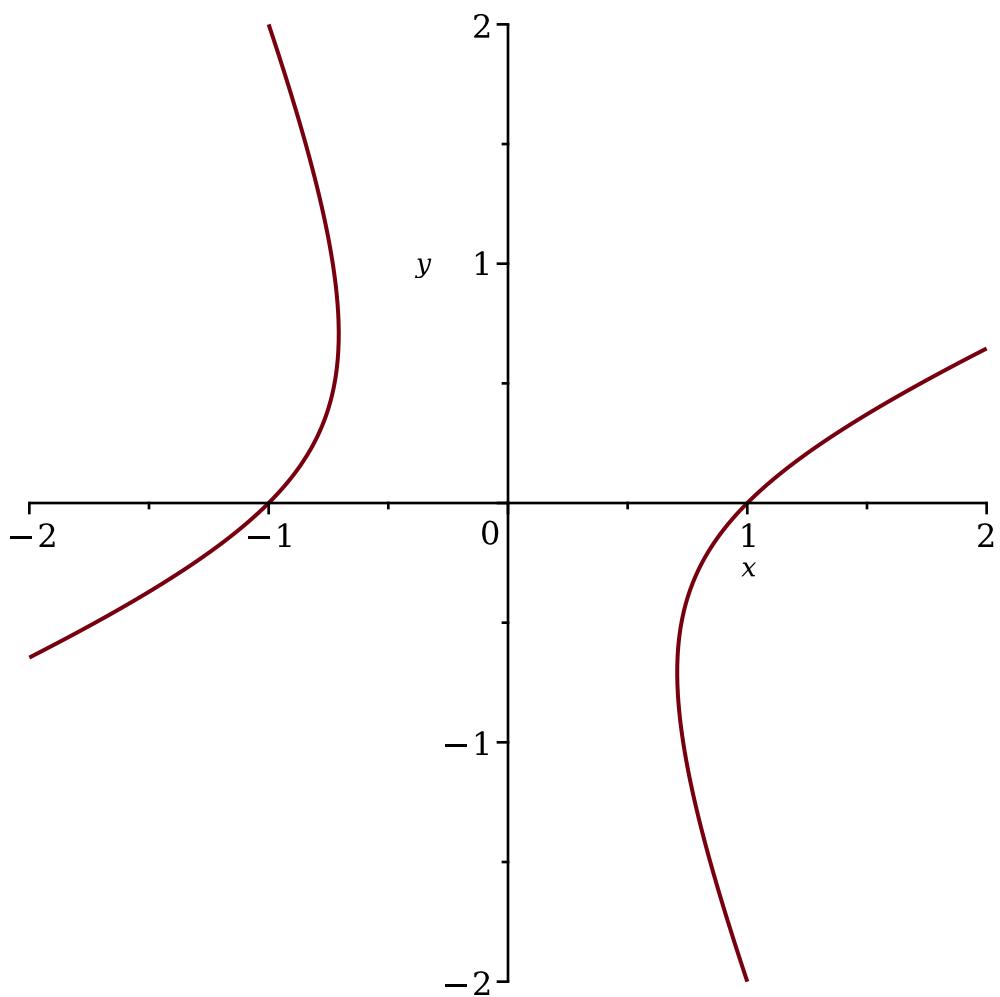
> `plot([list_f]);`



> `implicitplot(x^2+y^2-2*x-4*y+4=0)`



```
> implicitplot(x^2-2*x*y-y^2=1)
```

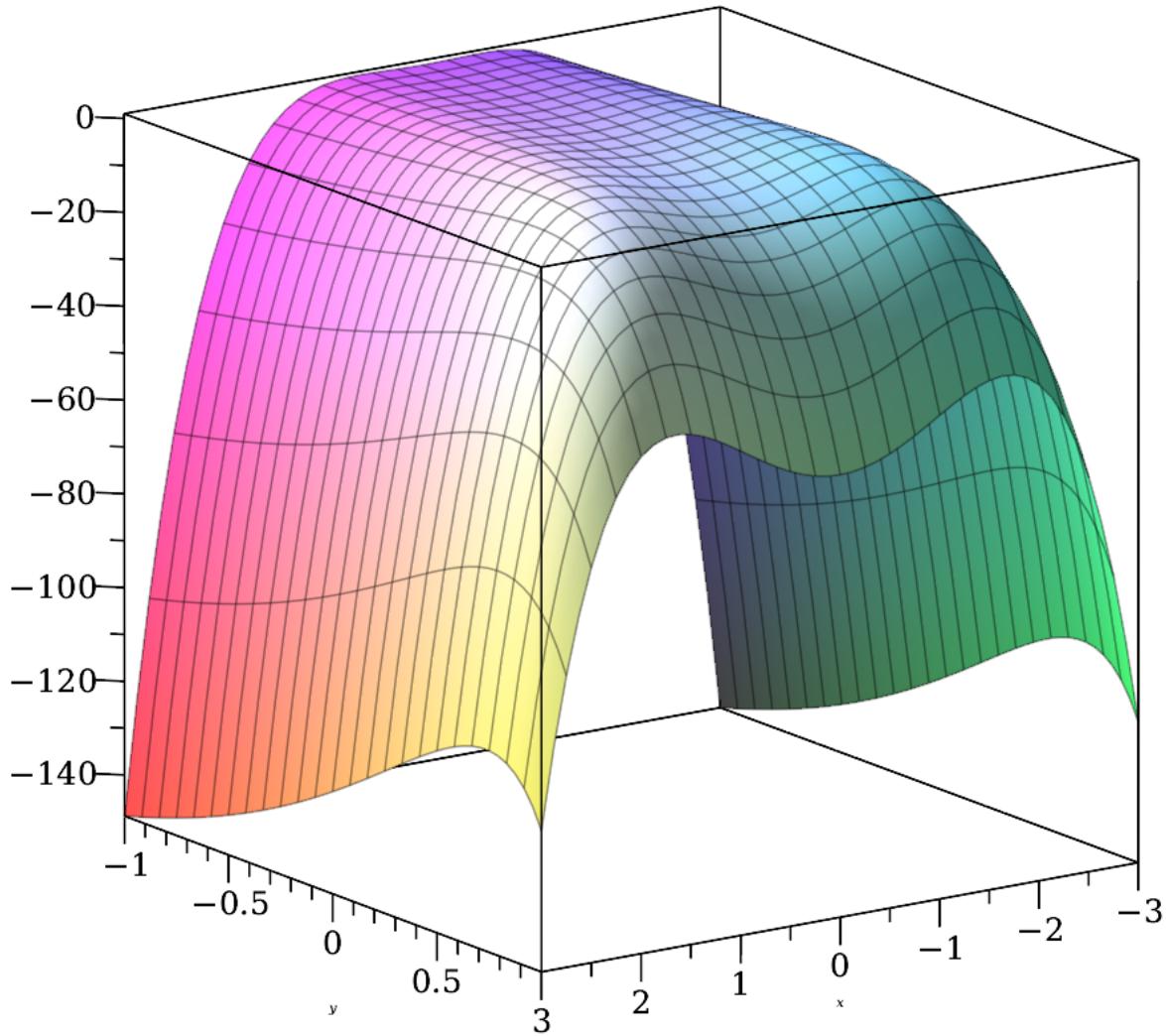


```
> z:=(x,y)->4*(x^2)*exp(y)-2*x^4-exp(4*y)
```

$$z := (x, y) \mapsto 4 \cdot x^2 \cdot e^y - 2 \cdot x^4 - e^{4 \cdot y}$$

(35)

```
> plot3d(z(x,y),x=-3..3,y=-1..1)
```

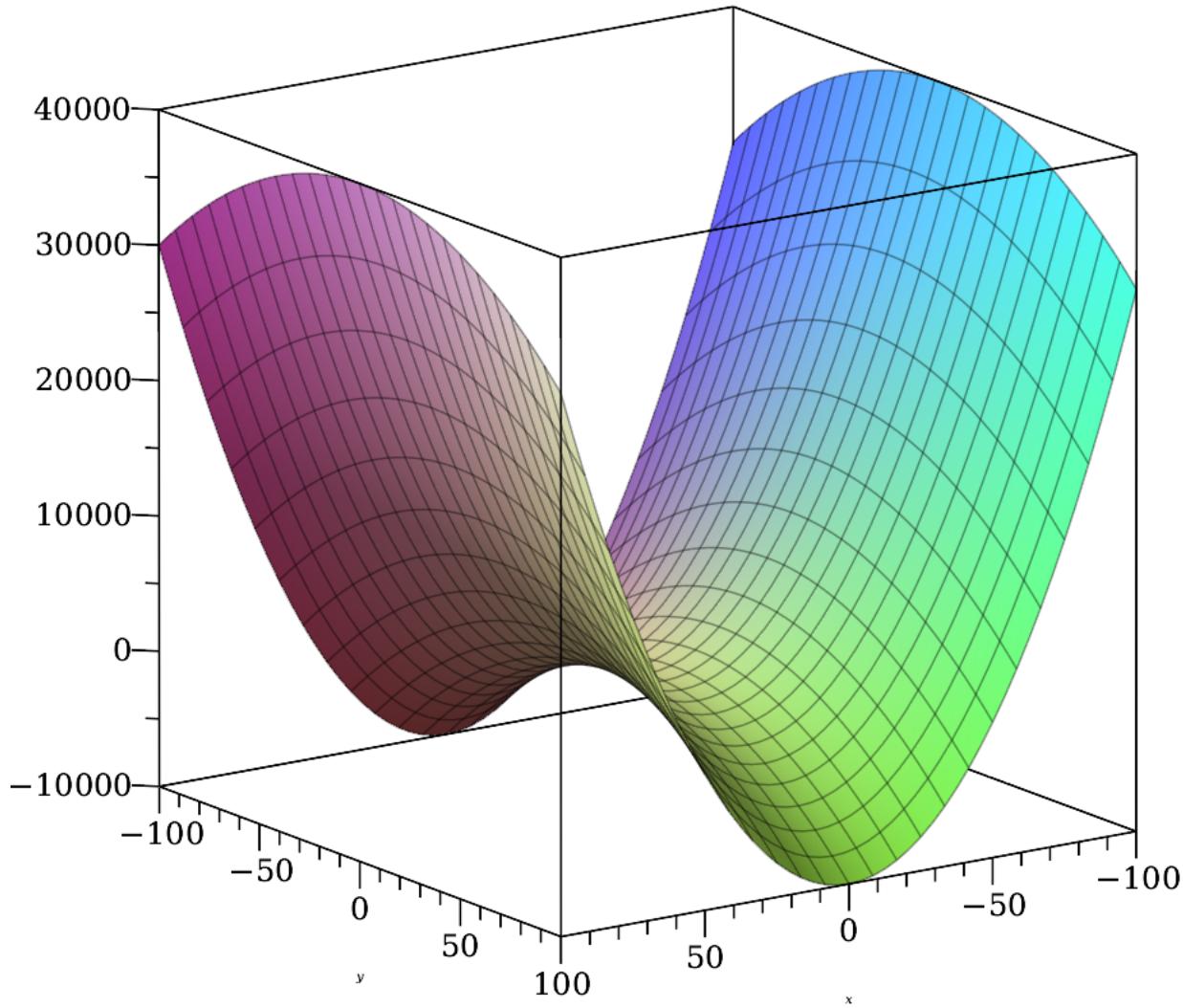


```
> z:=(x,y)->4*x^2-y^2  
z := (x, y)  $\mapsto$  4· $x^2 - y^2$ 
```



```
> plot3d(z(x,y),x=-100..100,y=-100..100)
```

(36)



> **with(linalg)**

[*BlockDiagonal, GramSchmidt, JordanBlock, LUdecomp, QRdecomp,*

(37)

Wronskian, addcol, addrow, adj, adjoint, angle, augment, backsub, band, basis, bezout, blockmatrix, charmat, charpoly, cholesky, col, coldim, colspace, colspan, companion, concat, cond, copyinto, crossprod, curl, definite, delcols, delrows, det, diag, diverge, dotprod, eigenvals, eigenvalues, eigenvectors, eigenvects, entermatrix, equal, exponential, extend, ffgausselim, fibonacci, forwardsub, frobenius, gausselim, gaussjord, geneqns, genmatrix, grad, hadamard, hermite, hessian,

*hilbert, htranspose, ihermite, indexfunc, innerprod, intbasis, inverse,
 ismith, issimilar, iszero, jacobian, jordan, kernel, laplacian, leastsqr,
 linsolve, matadd, matrix, minor, minpoly, mulcol, mulrow, multiply, norm,
 normalize, nullspace, orthog, permanent, pivot, potential, randmatrix,
 randvector, rank, ratform, row, rowdim, rowspace, rowspan, rref,
 scalarmul, singularvals, smith, stackmatrix, submatrix, subvector,
 sumbasis, swapcol, swaprow, sylvester, toeplitz, trace, transpose,
 vandermonde, vecpotent, vectdim, vector, wronskian*]

> **A:=matrix([[1,2,-1],[0,1,0],[3,-1,2]])**

$$A := \begin{bmatrix} 1 & 2 & -1 \\ 0 & 1 & 0 \\ 3 & -1 & 2 \end{bmatrix} \quad (38)$$

> **B:=matrix([[1,2,3],[1,1,2],[2,1,1]])**

$$B := \begin{bmatrix} 1 & 2 & 3 \\ 1 & 1 & 2 \\ 2 & 1 & 1 \end{bmatrix} \quad (39)$$

> **C:=matrix([[2,1,1],[0,1,-1],[4,2,2]])**

$$C := \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & -1 \\ 4 & 2 & 2 \end{bmatrix} \quad (40)$$

> **evalm(2*A-B*C)**

$$\begin{bmatrix} -12 & -5 & -7 \\ -10 & -4 & -4 \\ -2 & -7 & 1 \end{bmatrix} \quad (41)$$

```
> evalm(B^-1)
```

$$\begin{bmatrix} -\frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\ \frac{3}{2} & -\frac{5}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{3}{2} & -\frac{1}{2} \end{bmatrix} \quad (42)$$

```
=> eigenvals(C)
```

$$0, 3, 2$$

(43)

```
> eigenvecs(C)
```

$$\left[2, 1, \left\{ \begin{bmatrix} 1 & -2 & 2 \end{bmatrix} \right\} \right], \left[3, 1, \left\{ \begin{bmatrix} -1 & 1 & -2 \end{bmatrix} \right\} \right], \left[0, 1, \left\{ \begin{bmatrix} -1 & 1 & 1 \end{bmatrix} \right\} \right] \quad (44)$$