

Lagrange interpolation is a method of finding a polynomial that passes through a given set of points. Given a set of points  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ , the Lagrange interpolation polynomial is defined as:

$$L(x) = y_1 * L_1(x) + y_2 * L_2(x) + \dots + y_n * L_n(x)$$

where  $L_i(x)$  is defined as:

$$L_i(x) = \prod_{j \neq i} (x - x_j) / (x_i - x_j)$$

In other words,  $L_i(x)$  is the product of all  $(x - x_j)$  terms, where  $j$  ranges from 1 to  $n$ , except for  $j = i$ , divided by  $(x_i - x_j)$ .

The steps for finding the Lagrange interpolation polynomial are as follows:

1. Given a set of  $n$  points  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ , determine the value of  $x$  for which you want to find the corresponding value of  $y$ .
2. For each  $i = 1, 2, \dots, n$ , compute  $L_i(x)$  using the formula above.
3. Compute  $L(x)$  using the formula above.
4. The value of  $y$  corresponding to  $x$  is given by  $L(x)$ .

Here's an example:

Suppose we have the following set of points:  $(1, 3), (2, 5), (3, 9)$ , and we want to find the value of  $y$  corresponding to  $x = 4$ .

1. We want to find  $L(4)$ .

2. We compute  $L_1(4)$ ,  $L_2(4)$ , and  $L_3(4)$  using the formula above:

$$L_1(4) = (4 - 2) * (4 - 3) / ((1 - 2) * (1 - 3)) = -2$$

$$L_2(4) = (4 - 1) * (4 - 3) / ((2 - 1) * (2 - 3)) = 3$$

$$L_3(4) = (4 - 1) * (4 - 2) / ((3 - 1) * (3 - 2)) = -2$$

3. We compute  $L(4)$  using the formula above:

$$L(4) = 3 * (-2) + 5 * 3 + 9 * (-2) = -3$$

4. Therefore, the value of  $y$  corresponding to  $x = 4$  is  $-3$ .