

1.  $x = \text{none}$ ,  $y = a^m$ ,  $z = b^m$

We should be able to pump  $y$  as much as we want, and the string should still be accepted.

Assume  $m = 8$ , then  $xyz = a^8b^8$ , this is an accepted string. Therefore  $xy^2z$  should also be accepted, however,  $xy^2z = a^{16}b^8$ , this is not an accepted string. Therefore this language is not regular.

2.  $x = \text{none}$ ,  $y = (a + b)^*$ ,  $z = \text{none}$

We should be able to pump  $y$  as much as we want, and the string should still be accepted.

Assume  $n_a = 1$ , and  $n_b = 2$  then  $xyz = abb \mid bab \mid bba$ , this is an accepted string. Therefore  $xy^2z$  should also be accepted, however,  $xy^2z = abbabb \mid babbab \mid bbabba$ , this is not an accepted string because the  $n_a = 1$ , and  $n_b = 2$  no longer holds true. Therefore this language is not regular.

3.  $x = \text{none}$ ,  $y = a^m$ ,  $z = b^n$

We should be able to pump  $y$  as much as we want, and the string should still be accepted.

Assume  $m = 2$ ,  $n = 1$  then  $xyz = aab$ , this is an accepted string. Therefore pumping  $y$  down should also be accepted, however,  $xz = b$ , this is not an accepted string because  $0 / 1$  is not a positive integer. Therefore this language is not regular.

4.  $x = \text{none}$ ,  $y = a^{2^n}$ ,  $z = \text{none}$

We should be able to pump  $y$  as much as we want, and the string should still be accepted.

Assume  $n = 1$  then  $xyz = aa$ , this is an accepted string. Therefore  $xy^3z$  should also be accepted, however,  $xy^3z = aaaaaa$ , this is not an accepted string. Therefore this language is not regular.