S-JT & TSVT SラT をファイラマS

(1) if x>0>0, then x2>02

Buof: x>a $xa>a^2$ sina x=a>0 $x^2>ax$

 $(X^2) x a > \alpha^2$.'. x2>a2 (xED) a mod n = b means that orin has a remainder a=nb means that a mod n=b mod n n divide (a-b): n (a-b)

> : Concepts : keys , quesams

2) Prove 52 is irrational

Contradictin: 52 is rational

Q=X:Xz:Xs·X4…Xn p=y1.y2.y5...yk

S= = = S=q=P

2q²=(x.xz.xs.x4...xn)(x.xz.xs.x4...xn).2

2q²=(y.yz.ys...yk)(y.yz.ys...yk)

P²=(y.yz.ys...yk)(y.yz.ys...yk)

2k

odd + evan

controdicen V DED.

3 prove injure prime number

Contradiation: Jimile prime number

P., Pz, Ps... Pa

Comarder X=(P1. P2. P3.....Pn)+1

none of our prime numbe disable . X has a unique prime factor : either X is prime or 3 other prime factor that nut in the list we listed Contradicus 1/

4) prace if 27-1 is prime than is prime Contrapositive: YnGN+, m nue prime ->2n-1 mul prime

LOE M=X-Y X22,922 27-1=2xy==(2x)y-1

 $(2^{x})^{\frac{1}{2}} + (2^{x})^{\frac{1}{2}} + (2^{x})^{\frac{1}{2}} + (2^{x})^{\frac{1}{2}} + (2^{x})^{\frac{1}{2}} + \cdots + 2^{x} + 1)$ $= 3^{2} = 4$

 $(2^{x})^{y}-|=(2^{x}-1)[(2^{x})^{y+1}+(2^{x})^{y+2}+2^{x}+1)$

n=x.4 メシュ

(2×)3-1 24 QED.

PHP: If n item are put into m containers, with nom, then at lease or contains must contain more than are item

1, 110 /

5 show that given a set of n positive integers, 3 a non-empty subset whose somes divibe by

Let the set be {a, az. as au... am, am}. we have si=ai Sz=aitaz S=aitaztas Si=artazt.-+ai Sn=aitart -- an coce 1: if any si is divisible by no ne done Que 2: no Si divsible by n SO Si=nq+ri | <n <n there are n-1 possible value for ri

we haven sum, cn-1) possible whefer in .. By PHP, two g the sun have the same reminder. Sm=artaztast...tam=nqn+r? y=r Sn=artazt...tam =nqn+r } Sm-Sn=n(9m-9n) which is distable by n. WED

(b) Chocolate (Stray Inducen)

S(n): n2/, beat n sque regue n-1

Base (ase: Sci), 1x1 regions 1x1-1=0 V

Induce Hypothesi: Let n ENI, supper the SG) hills with COSS that n.

YKGNI, OKK(N, SCK). (not a single K but for all K under the restriction)

Inducate Stop: pre YKENLCOCKENASCH) -> So) assume those is a single and we break it into a squaes and b squae, ocarn and orben (by IH)

641: (Q-1)+(b-1)+1= a+b-1 =n-1 b requies by in # g total beak n-1

Sum rule: P(E or F)=P(E)+P(F)-P(E and F)

overlap.

P(G|F): the probability of E dampand on previous F

product rule:

 $P(A \text{ and } B) = P(B) \cdot P(A|B) = P(A)P(B|A)$

efore: