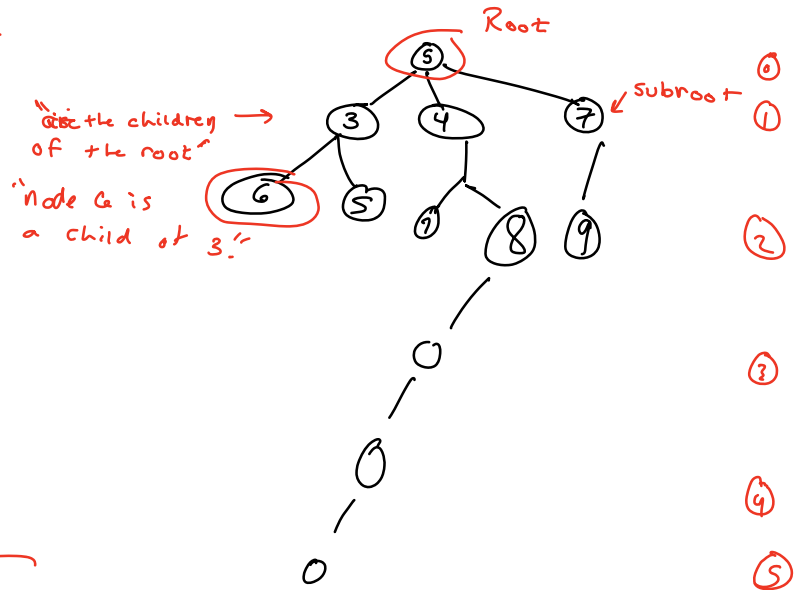
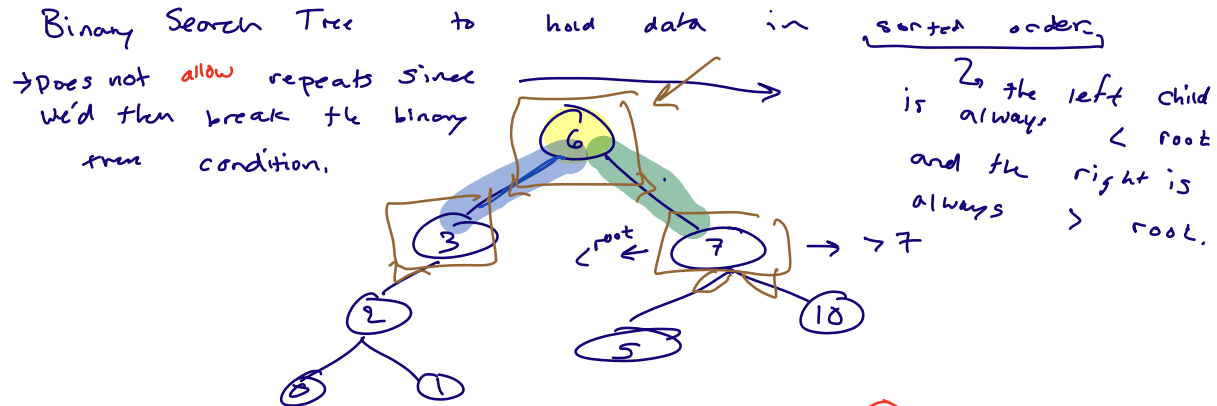


Tree

height of a tree is 6.



example non-binary tree since the root of the tree has more than 2 children.
~~Def~~ A binary is such that every node has at most 2 children.



how do we represent btrees?

```
typedef struct binary_tree_node bstnode;
struct binary_tree_node {
    void *item;
    bstnode * lsub;
    bstnode * rsub;
};
```

```
3;
typedef struct {
    bstnode * root;
    3 bst;
} → typedef (bstnode*) bst;
```

- 1 create/Destroy
- 2 Iterate
- 3 Insert/Remove
- 4 how many elements
- 5 height of tree.

```

typedef struct list_node {
    struct list_node *next;
};

```

```

typedef struct {
    list_node *head;
} list;

```

Encapsulation → linked List

list → head
↑

list → head = NULL;

list_node *myList = NULL;

list *myList = malloc(sizeof(list));
myList → head = NULL;

```

btree_node* btree_node_insert(btree_node *node,
    void *item,
    Comparator comp) {
    if (node == NULL) {
        btree_node *newnode = btree_node_create();
        newnode->item = item;
        return newnode; // if this first thing is NOT the case
    } else if (comp(item, node->item) < 0) {
        node->lsub = btree_node_insert(node->lsub, item, comp);
    } else if (comp(item, node->item) > 0) {
        node->rsb = btree_node_insert(node->rsb, item, comp);
    }
    return node;
}

```

```

btree_node* btree_node_insert(btree_node *node,
                               void *item,
                               Comparator comp) {
    if (node == NULL) {
        btree_node *newnode = btree_node_create();
        newnode->item = item;
        return newnode; // if this first thing is NOT the case
    } else if (comp(item, node->item) < 0) { 6 < 7?
        node->lsub = btree_node_insert(node->lsub, item, comp);
    } else if (comp(item, node->item) > 0) {
        node->rsub = btree_node_insert(node->rsub, item, comp);
    }

    return node;
}

```

base case {

2 {

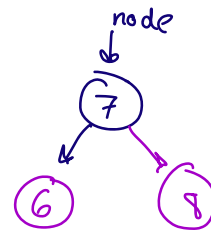
3 {

① Tree empty

tree → root = new node

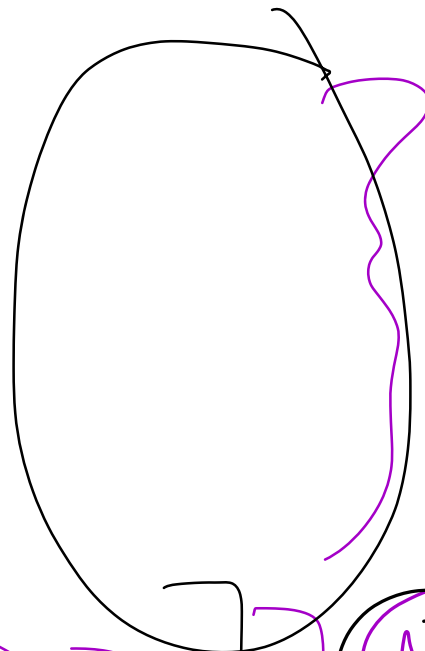
② insert 6

③ Insert 8



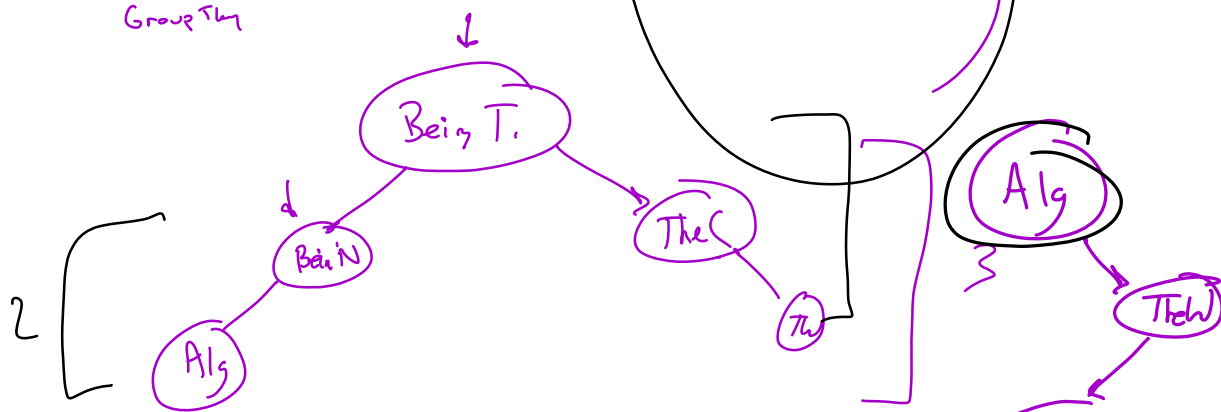
Alg
The W
The C
Being Time
Being N

height
=
size



Not
Optimal

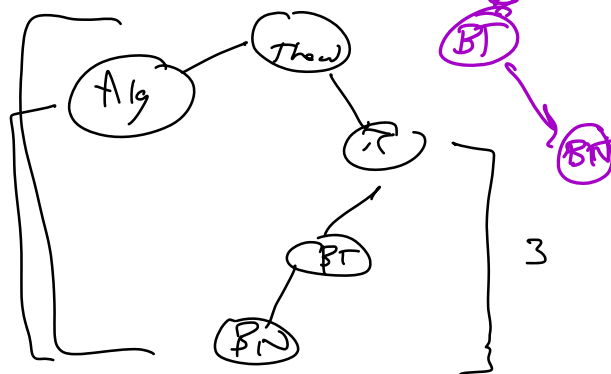
"Grouping"



Find $\Theta(\log n)$.

Find List
 $\Theta(n)$

height
1
6
4



Balance it?

We write a balanced insert function.

We check if when inserting we cause the tree to become unbalanced.

```
factor = height(node->lsub) - height(node->rsub);
```

```
if ( factor == 0 ) { // our tree
```

```
3 else if ( factor > 0 ) {
```

```
    // rotate right
```

```
3 else {
```

```
    // rotate left
```

```
3
```

```
btree_node * rsubRotate ( btree_node * old_root ) {
```

```
    btree_node * newRoot = oldRoot->lsub;
```

```
    btree_node * newGuy1 = newRoot->rsub;
```

```
    newRoot->rsub = old_root
```

```
    old_root->lsub = newGuy1;
```

```
    return newRoot;
```

➤

```
// to do other rotations
```

```
// return the newRoot in insert.
```

