

(\*This is for the subcase2 f2 +/-  $\sigma = -1$  \*)

$\alpha = 0.05$ ;  $\beta = 0.01$ ;  $\gamma = 0.05$ ;  $\epsilon = 0.01$ ;  $\xi = 0.01$ ;  $\theta = 1.0$ ;  $\psi = -0.1$ ;

$\text{In}[*]:= \text{FindRoot}\left[\left\{\alpha x - \beta y - \gamma z + \psi x^2, -\alpha x + \beta y + \gamma z + \theta y^2 - \epsilon x \text{Abs}[z], \xi - \alpha x + \beta y + \gamma z\right\}, \right. \\ \left. \{x, 100\}, \{y, 100\}, \{z, 100\}\right]$

$\text{Out}[*]=$

$\{x \rightarrow 0.316228, y \rightarrow 0.101505, z \rightarrow 0.0959267\}$

$\text{In}[*]:= \text{FindRoot}\left[\left\{\alpha x - \beta y - \gamma z + \psi x^2, -\alpha x + \beta y + \gamma z + \theta y^2 - \epsilon x \text{Abs}[z], \xi - \alpha x + \beta y + \gamma z\right\}, \right. \\ \left. \{x, -1\}, \{y, 100\}, \{z, 100\}\right]$

$\text{Out}[*]=$

$\{x \rightarrow -0.316228, y \rightarrow 0.0911586, z \rightarrow -0.534459\}$

$\text{In}[*]:= \text{f2}[y\_]= \theta y^2 - \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} y - \xi + \frac{\alpha \epsilon \xi}{\gamma \text{Abs}[\psi]} - \frac{\epsilon \xi}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}}$

$\text{Out}[*]=$

$-0.00963246 - 0.000632456 y + 1. y^2$

$\Delta = \frac{\epsilon^2 \beta^2 \xi}{\gamma^2 \text{Abs}[\psi]} - 4 \theta \left( -\xi + \frac{\alpha \epsilon \xi}{\gamma \text{Abs}[\psi]} - \frac{\epsilon \xi}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} \right)$

$\text{Out}[*]=$

0.0465302

$\text{In}[*]:= y1 = \left( \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} + \sqrt{\Delta} \right) / (2 \theta)$

$\text{Out}[*]=$

0.0984618

$\text{In}[*]:= y2 = \left( \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \sqrt{\Delta} \right) / (2 \theta)$

$\text{Out}[*]=$

-0.0978294

$\text{In}[*]:= z1 = \frac{\alpha}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \frac{\beta}{\gamma} y1 - \frac{\xi}{\gamma}$

$\text{Out}[*]=$

0.0965354

$$\text{In}[*]:= \text{z2} = \frac{\alpha}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \frac{\beta}{\gamma} y^2 - \frac{\xi}{\gamma}$$

Out[\*]=

0.135794

$$\text{In}[*]:= \text{x1} = \sqrt{\xi / \text{Abs}[\psi]}$$

Out[\*]=

0.316228


$$\text{In}[*]:= \text{x2} = -\sqrt{\xi / \text{Abs}[\psi]}$$

Out[\*]=

-0.316228

(\*This is for subcase2 f3: -/  $\sigma = +1$ \*)

In[\*]:= Clear[ $\alpha, \beta, \gamma, \epsilon, \xi, \theta, \psi, x, y, z$ ]

 FindRoot: 在  $\{x, y, z\} = \{-1., 100., 100.\}$  处, 函数值

$\{-1. \alpha - 100. \beta - 100. \gamma + 1. \psi, 1. \alpha + 100. \beta + 100. \gamma + 100. \epsilon + 10000. \theta, 1. \alpha + 100. \beta + 100. \gamma + \xi\}$   
不是由数字组成的维度为 {3} 的列表.

In[\*]:=  $\alpha = 0.05; \beta = 0.01; \gamma = 0.05; \epsilon = 0.01; \xi = 0.01; \theta = 1.0; \psi = -0.1;$

In[\*]:= FindRoot[ $\{\alpha x - \beta y - \gamma z + \psi x^2, -\alpha x + \beta y + \gamma z + \theta y^2 - \epsilon x \text{Abs}[z], \xi - \alpha x + \beta y + \gamma z\},$   
 $\{x, 100\}, \{y, 100\}, \{z, 100\}$ ]

Out[\*]=

$\{x \rightarrow 0.316228, y \rightarrow 0.101505, z \rightarrow 0.0959267\}$

In[\*]:= FindRoot[ $\{\alpha x - \beta y - \gamma z + \psi x^2, -\alpha x + \beta y + \gamma z + \theta y^2 - \epsilon x \text{Abs}[z], \xi - \alpha x + \beta y + \gamma z\},$   
 $\{x, -1\}, \{y, 100\}, \{z, 100\}$ ]

Out[\*]=

$\{x \rightarrow -0.316228, y \rightarrow 0.0911586, z \rightarrow -0.534459\}$

$$\text{In}[*]:= \text{f3} = \theta y^2 - \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} y - \xi - \frac{\alpha \epsilon \xi}{\gamma \text{Abs}[\psi]} - \frac{\epsilon \xi}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}}$$

Out[\*]=

$-0.0116325 - 0.000632456 y + 1. y^2$

$$\text{In}[*]:= \Delta = \frac{\epsilon^2 \beta^2 \xi}{\gamma^2 \text{Abs}[\psi]} - 4 \theta \left( -\xi - \frac{\alpha \epsilon \xi}{\gamma \text{Abs}[\psi]} - \frac{\epsilon \xi}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} \right)$$

Out[\*]=

0.0465302

$$\text{In}[*]:= y1 = \left( \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} + \sqrt{\Delta} \right) / (2 \theta)$$

Out[\*]=

0.108171

$$\text{In}[*]:= y2 = \left( \frac{\epsilon \beta}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \sqrt{\Delta} \right) / (2 \theta)$$

Out[\*]=

-0.107538

$$\text{In}[*]:= z1 = -\frac{\alpha}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \frac{\beta}{\gamma} y1 - \frac{\xi}{\gamma}$$

Out[\*]=

-0.537862

$$\text{In}[*]:= z2 = -\frac{\alpha}{\gamma} \sqrt{\frac{\xi}{\text{Abs}[\psi]}} - \frac{\beta}{\gamma} y2 - \frac{\xi}{\gamma}$$

Out[\*]=

-0.49472

$$\text{In}[*]:= x1 = \sqrt{\xi / \text{Abs}[\psi]}$$

Out[\*]=

0.316228

$$\text{In}[*]:= x2 = -\sqrt{\xi / \text{Abs}[\psi]}$$

Out[\*]=

-0.316228

**FindRoot:** "在 {x, y, z} = {-1., 100., 100.} 处, 函数值 {-1. \\\alpha - 100. \\\beta - 100. \\\gamma + 1. \\\psi, 1. \\\alpha + 100. \\\beta + 100. \\\gamma + 100. \\\epsilon + 10000. \\\theta, 1. \\\alpha + 100. \\\beta + 100. \\\gamma + \xi} 不是由数字组成的维度为 {3} 的列表."

**FindRoot:** 在 {x, y, z} = {-1., 100., 100.} 处, 函数值  
{-1. \alpha - 100. \beta - 100. \gamma + 1. \psi, 1. \alpha + 100. \beta + 100. \gamma + 100. \epsilon + 10000. \theta, 1. \alpha + 100. \beta + 100. \gamma + \xi}  
不是由数字组成的维度为 {3} 的列表.

```
In[ ]:= (*This is for the situation f4: -/-1*)
```

```
Clear[α, β, γ, ε, ζ, θ, ψ, x, y, z]
```

```
In[ ]:= α = 0.05; β = 0.01; γ = 0.05; ε = 0.01; ζ = 0.01; θ = 1.0; ψ = -0.1;
```

```
In[ ]:= FindRoot[{α x - β y - γ z + ψ x^2, -α x + β y + γ z + θ y^2 - ε x Abs[z], ζ - α x + β y + γ z},
  {x, 100}, {y, 100}, {z, 100}]
```

```
Out[ ]:=
```

```
{x → 0.316228, y → 0.101505, z → 0.0959267}
```

```
In[ ]:= f4[y_] = θ y^2 + \frac{ε β}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} y - ζ + \frac{α ε ζ}{γ Abs[ψ]} + \frac{ε ζ}{γ} \sqrt{\frac{ζ}{Abs[ψ]}}
```

```
Out[ ]:=
```

```
-0.00836754 + 0.000632456 y + 1. y^2
```

```
In[ ]:= Δ = \frac{ε^2 β^2 ζ}{γ^2 Abs[ψ]} - 4 θ \left( -ζ + \frac{α ε ζ}{γ Abs[ψ]} + \frac{ε ζ}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} \right)
```

```
Out[ ]:=
```

```
0.0334706
```

```
In[ ]:= y1 = \left( -\frac{ε β}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} + \sqrt{Δ} \right) / (2 θ)
```

```
Out[ ]:=
```

```
0.0911586
```

```
In[ ]:= y2 = \left( -\frac{ε β}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} - \sqrt{Δ} \right) / (2 θ)
```

```
Out[ ]:=
```

```
-0.0917911
```

```
In[ ]:= z1 = -\frac{α}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} - \frac{β}{γ} y1 - \frac{ζ}{γ}
```

```
Out[ ]:=
```

```
-0.534459
```

```
In[ ]:= z2 = -\frac{α}{γ} \sqrt{\frac{ζ}{Abs[ψ]}} - \frac{β}{γ} y2 - \frac{ζ}{γ}
```

```
Out[ ]:=
```

```
-0.49787
```

```
In[ ]:= x1 = -  $\sqrt{\xi / \text{Abs}[\psi]}$ 
```

```
Out[ ]:=  
-0.316228
```

```
In[ ]:=
```

```
FindRoot[{x^3 y + 2 x^2 + 9 x y, 4 y^4 - 5 x y^3 + 9 x y}, {x, 1}, {y, 4}]
```

```
Out[ ]:=  
{x → 1.68081 × 10-39, y → 2.7359 × 10-8}
```

```
In[ ]:= xyrule = FindRoot[{x^3 y + 2 x^2 + 9 x y, 4 y^4 - 5 x y^3 + 9 x y}, {x, 1}, {y, 1}]
```

```
Out[ ]:=  
{x → 6.1704 × 10-9, y → 1.68942 × 10-9}
```

```
In[ ]:= {x^3 y + 2 x^2 + 9 x y, 4 y^4 - 5 x y^3 + 9 x y} /. xyrule
```

```
Out[ ]:=  
{1.69967 × 10-16, 9.38196 × 10-17}
```

```
In[ ]:= For[i = -5, i < 5, i++;
```

```
    xyrule = FindRoot[{x^3 * y + 4 * y^2 - 3 x y, x y^4 - 8 y^3 + 7 x^2 y - 8}, {x, 3}, {y, i}];
```

```
    rasiduals = {x^3 y + 2 x^2 + 9 x y, 4 y^4 - 5 x y^3 + 9 x y} /. xyrule;
```

```
    Print[xyrule, "", rasiduals, "x = 3", ",", "y= ", i]
```


```
]
```

```
{x → 2.47105, y → -1.91881} {-59.4126, 98.8359} x = 3, y= -4
```

```
{x → 2.47105, y → -1.91881} {-59.4126, 98.8359} x = 3, y= -3
```

```
{x → 2.47105, y → -1.91881} {-59.4126, 98.8359} x = 3, y= -2
```

 **FindRoot:** 线搜索把步长降低到由 AccuracyGoal 和 PrecisionGoal

指定的容差范围内, 但是无法使优化目标函数的值减小得足够多. 您可能需要多于 MachinePrecision 位的工作精度以满足这些容差. 

```
{x → 1.57828, y → 0.4375} {12.9164, 5.70018} x = 3, y= -1
```

 **FindRoot:** 在点 {x, y} = {3., 0.} 碰到奇异雅克比. 尝试扰动初始点. 

```
{x → 3., y → 0.} {18., 0.} x = 3, y = 0
```

```
{x → -1.91648, y → 0.322392} {-0.484268, -5.19642} x = 3, y = 1
```

FindRoot: 线搜索把步长降低到由 AccuracyGoal 和 PrecisionGoal

指定的容差范围内, 但是无法使优化目标函数的值减小得足够多. 您可能需要多于 MachinePrecision 位的工作精度以满足这些容差. [i](#)

```
{x → 1.54823, y → 0.427009} {12.3287, 5.48024} x = 3, y = 2
```

FindRoot: 线搜索把步长降低到由 AccuracyGoal 和 PrecisionGoal

指定的容差范围内, 但是无法使优化目标函数的值减小得足够多. 您可能需要多于 MachinePrecision 位的工作精度以满足这些容差. [i](#)

General: 在本次计算中, FindRoot::lstol 的进一步输出将被抑制. [i](#)

```
{x → 1.53175, y → 0.421292} {12.0145, 5.36117} x = 3, y = 3
```

```
{x → 1.53126, y → 0.421123} {12.0052, 5.35764} x = 3, y = 4
```

```
{x → 1.55886, y → 0.430713} {12.5345, 5.55768} x = 3, y = 5
```

In[ ]:=

```
xyrule = FindRoot[{x^3 y + 2 x^2 + 9 x y, 4 y^4 - 5 x y^3 + 9 x y}, {x, 3}, {y, -4}]
```

Out[ ]:=

```
{x → 2.74443 × 10-39, y → -2.7002 × 10-8}
```

(\*April 2, this week we choose a general case and through change the staring point to watch the changes. Also we can see the equilibria, and try to restore the same diagram from the research paper\*)

(\*case 1b\*)

In[ ]:=

```
 $\alpha = 0.05;$ 
```

```
 $\beta = 0.01;$ 
```

```
 $\gamma = 0.05;$ 
```

```
 $\delta = 0.02;$ 
```

```
 $\epsilon = 0.03;$ 
```

```
 $\xi = 0.1;$ 
```



```
 $\eta = 0.04;$ 
```

```
 $\theta = 1.0;$ 
```

```
 $\psi = -0.01;$ 
```

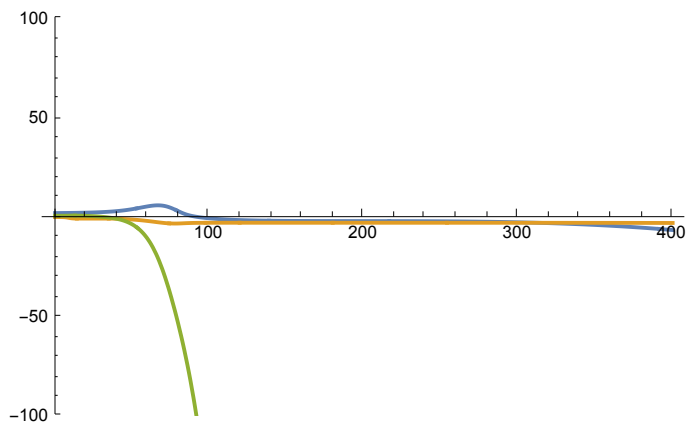
```
In[ ]:= s = NDSolve[{x'[t] ==  $\alpha$  x[t] +  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t]  $\times$  y[t],
  y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]]  $\times$  x[t],
  z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t]  $\times$  Abs[y[t]],
  x[0] == 2.3753, y[0] == 0.3699, z[0] == 1.0218}, {x, y, z}, {t, 180}]
```

Out[ ]:=

```
{ {x → InterpolatingFunction[ Domain: {{0., 180.}}
  Output: scalar ],
  y → InterpolatingFunction[ Domain: {{0., 180.}}
  Output: scalar ],
  z → InterpolatingFunction[ Domain: {{0., 180.}}
  Output: scalar ] ] }
```

```
In[ ]:= Plot[Evaluate[{x[t], y[t], z[t]} /. s], {t, 0, 400}, PlotRange → {100, -100}]
```

Out[ ]:=



In[ ]:=

```
Evaluate[{x[t], y[t], z[t]} /. s] /. t → 400
```

Out[ ]:=

```
{ {-1.66667, -2.5, -4.80485  $\times 10^8$  } }
```

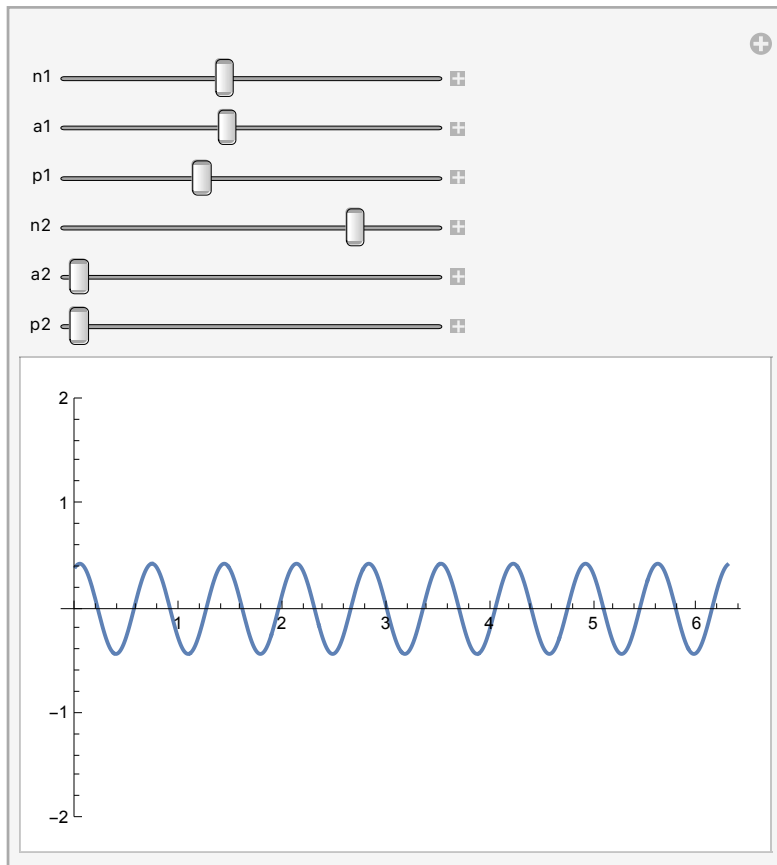
```
In[ ]:= Evaluate[{x[t], y[t], z[t]} /. s] /. t → 150
```

Out[ ]:=

```
{ {-1.55006, -2.49664, -1796.92 } }
```

```
In[ ]:= Manipulate[Plot[a1 Sin[n1 (x + p1)] + a2 Sin[n2 (x + p2)], {x, 0, 2 Pi}, PlotRange -> 2],
  {n1, 1, 20}, {a1, 0, 1}, {p1, 0, 2 Pi}, {n2, 1, 20}, {a2, 0, 1}, {p2, 0, 2 Pi}]
```

Out[ ]=



```
In[ ]:= (*New try*)
ClearAll
```

Out[ ]=




```
ClearAll
```

```
In[ ]:= α = 0.05;
β = 0.01;
γ = 0.05;
δ = 0.02;
ε = 0.03;
ξ = 0.1;
η = 0.04;
θ = 1.0;
ψ = -0.01;
```



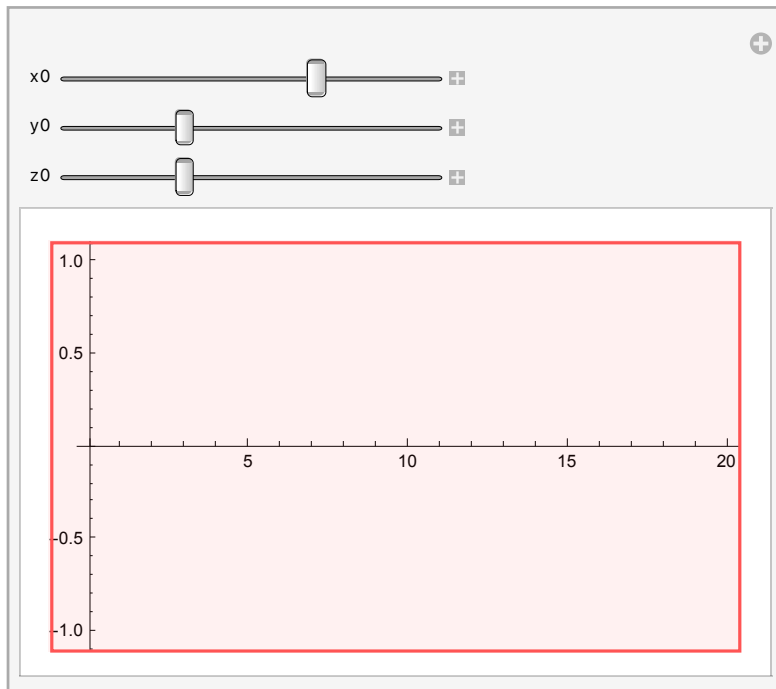
```
In[*]:= s = NDSolve[{x'[t] ==  $\alpha$  x[t] +  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t]  $\times$  y[t],
  y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]]  $\times$  x[t],
  z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t]  $\times$  Abs[y[t]],
  x[0] == 2.3753, y[0] == 0.3699, z[0] == 1.0218}, {x, y, z}, {t, 180}]
```

Out[\*]=

```
{ {x -> InterpolatingFunction[ Domain: {{0., 180.}} Output: scalar],
  y -> InterpolatingFunction[ Domain: {{0., 180.}} Output: scalar],
  z -> InterpolatingFunction[ Domain: {{0., 180.}} Output: scalar]} }
```

```
In[*]:= Manipulate[Plot[Evaluate[{x[t], y[t], z[t]} /.
  NDSolve[{x'[t] ==  $\alpha$  x[t] +  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t]  $\times$  y[t],
  y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]]  $\times$  x[t],
  z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t]  $\times$  Abs[y[t]],
  x[0] == x0, y[0] == y0, z[0] == z0}, {x, y, z}, {t, 500}]],
  {t, 0, 20}], {x0, 1.5, 2.5}, {y0, 0.1, 0.4}, {z0, 0.5, 1}]
```

Out[\*]=



**NDSolve:** 在  $t == 43.07390043755897$  处, 步长实际上为零; 可能存在奇点或者刚性系统. [i](#)

**NDSolve:** 在  $t == 428.2778915751553$  处误差测试失败; 无法继续. [i](#)

**NDSolve:** 在  $t == 475.9963471704903$  处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 490.36442365902656` 处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 494.5508003645437` 处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 451.03839494726344` 处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 462.36984853918614` 处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 462.36984853918614` 处误差测试失败; 无法继续. [i](#)

... **NDSolve**: 在 t == 42.051140676190315` 处, 步长实际上为零; 可能存在奇点或者刚性系统. [i](#)

... **NDSolve**: 在 t == 42.051140676190315` 处, 步长实际上为零; 可能存在奇点或者刚性系统. [i](#)

... **NDSolve**: 在 t == 42.051140676190315` 处, 步长实际上为零; 可能存在奇点或者刚性系统. [i](#)

... **NDSolve**: 在 t == 3.7371551234778977` 处, 步长实际上为零; 可能存在奇点或者刚性系统. [i](#)

... **NDSolve**: 在 t == 473.4893765211817` 处误差测试失败; 无法继续. [i](#)

**NDSolve::ndnum**: 在 t == 0. 处碰到一个导数的非数值量.

**ReplaceAll::reps**:

```
{NDSolve[{x'[t] ==  $\alpha$  x[t] +  $\psi$  x[t] +  $\beta$  y[t] -  $\gamma$  z[t] -  $\delta$  y[t] z[t],
          y'[t] == -( $\alpha$  x[t]) -  $\epsilon$  Abs[z[t]] x[t] +  $\beta$  y[t] +  $\theta$  y[t] +  $\gamma$  z[t],
          <<3>>, z[0] == 0.654}, {x, y, z}, {t, 500}]}
```

既不是替换规则列表, 也不是一个有效的分派表, 因此无法用来替换.

**NDSolve::dsvar**: 0.000408571 不能用作变量.

**ReplaceAll::reps**:

```
{NDSolve[{x'[0.000408571] ==
           $\alpha$  x[0.000408571] +  $\psi$  x[0.000408571] +  $\beta$  y[0.000408571] -
           $\gamma$  z[0.000408571] -  $\delta$  y[0.000408571] z[0.000408571], <<4>>,
          z[0] == 0.654}, {x, <<2>>}, {<<10>>1, 500}]}
```

既不是替换规则列表, 也不是一个有效的分派表, 因此无法用来替换.

**NDSolve::dsvar**: 0.000408571 不能用作变量.

**ReplaceAll::reps**:

```
{NDSolve[{x'[0.000408571] ==
           $\alpha$  x[0.000408571] +  $\psi$  x[0.000408571] +  $\beta$  y[0.000408571] -
          1.  $\gamma$  z[0.000408571] - 1.  $\delta$  y[0.000408571] z[0.000408571], <<4>>,
          z[0.] == 0.654}, {x, <<2>>}, {<<2>>}]}
```

既不是替换规则列表, 也不是一个有效的分派表, 因此无法用来替换.

**General::stop**: 在本次计算中, **ReplaceAll::reps** 的进一步输出将被抑制.

**NDSolve::dsvar**: 0.408572 不能用作变量.

**General::stop**: 在本次计算中, **NDSolve::dsvar** 的进一步输出将被抑制.

```
In[ ]:= (*This is for April 16th, try to change the diffierent value to detect
         the changes in the plot and look the different to see what happened*)
```

```
In[ ]:= ClearAll
```

```
Out[ ]:=
```

```
ClearAll
```




(\* This is case 1c\*)

```
In[ ]:=  $\alpha = 0.05;$ 
 $\beta = 0.01;$ 
 $\gamma = 0.05;$ 
 $\delta = 0.02;$ 
 $\epsilon = 0.01;$ 
 $\xi = 0.1;$ 
 $\eta = 0.05;$ 
 $\theta = 1.0;$ 
 $\psi = -0.01;$ 
```

```
In[ ]:= s = NDSolve[{x'[t] ==  $\alpha x[t] - \beta y[t] - \gamma z[t] + \psi x[t]^2 - \delta z[t] \times y[t]$ ,
y'[t] ==  $\beta y[t] - \alpha x[t] + \gamma z[t] + \theta y[t]^2 - \epsilon \text{Abs}[z[t]] \times x[t]$ ,
z'[t] ==  $\xi + \gamma z[t] - \alpha x[t] + \beta y[t] - \eta x[t] \times \text{Abs}[y[t]]$ ,
x[0] == 2.2821, y[0] == 0.2843, z[0] == 1.0082}, {x, y, z}, {t, 400}]
```

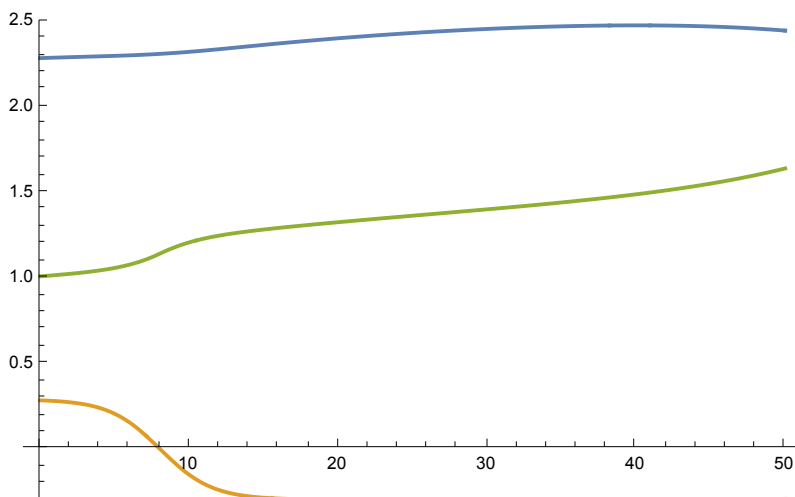
... **NDSolve:** 在  $t == 79.8975520898404$  处, 步长实际上为零; 可能存在奇点或者刚性系统. i

Out[ ]:=

```
{ {x → InterpolatingFunction[+  Domain: {{0., 79.9}} Output: scalar ] },
  y → InterpolatingFunction[+  Domain: {{0., 79.9}} Output: scalar ] },
  z → InterpolatingFunction[+  Domain: {{0., 79.9}} Output: scalar ] ] }
```

```
In[ ]:= Plot[Evaluate[{x[t], y[t], z[t]} /. s], {t, 0, 50}, PlotRange → {-0.3, 2.5}]
```

Out[ ]:=

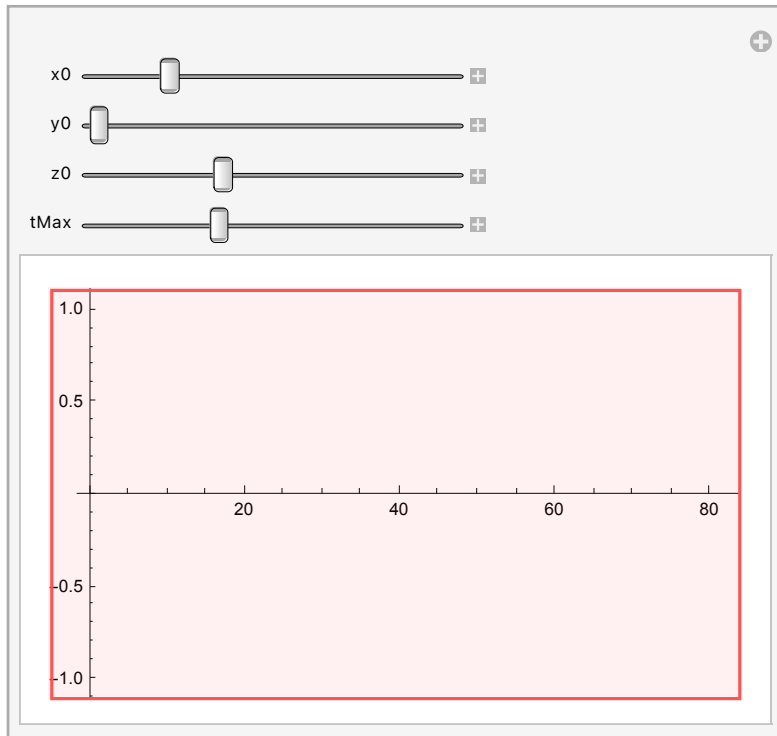


```

In[ ]:= Manipulate[Plot[Evaluate[{x[t], y[t], z[t]} /.
  NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t]  $\times$  y[t],
    y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]]  $\times$  x[t],
    z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t]  $\times$  Abs[y[t]],
    x[0] == x0, y[0] == y0, z[0] == z0}, {x, y, z}, {t, 500}]], {t, 0, tMax}],
  {x0, 2.2, 3}, {y0, 0.4, 1.0}, {z0, 0.9, 1.5}, {tMax, 20, 200}]

```

Out[ ]:=



... NDSolve: 在  $t == 3.1154616436382567$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 3.1593025611020686$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 445.6496069733122$  处误差测试失败; 无法继续. ⓘ

... NDSolve: 在  $t == 1.37365212132476$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 0.8774242262396175$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 50.9235640149503$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 50.9235640149503$  处, 步长实际上为零; 可能存在奇点或者刚性系统. ⓘ

... NDSolve: 在  $t == 485.1924821350333$  处误差测试失败; 无法继续. ⓘ

... NDSolve: 在  $t == 434.8056318328504$  处误差测试失败; 无法继续. ⓘ

... NDSolve: 在  $t == 460.76328096893275$  处误差测试失败; 无法继续. ⓘ

NDSolve::ndnum: 在  $t == 0$ . 处碰到一个导数的非数值量.

ReplaceAll::reps:

$$\begin{aligned} & \{ \text{NDSolve}[\{x'[t] == \alpha x[t] + \psi x[t] - \beta y[t] - \gamma z[t] - \delta y[t] z[t], \\ & y'[t] == -(\alpha x[t]) - \epsilon \text{Abs}[z[t]] x[t] + \beta y[t] + \theta y[t] + \gamma z[t], \\ & \{x, y, z\}, \{t, 500\}\} \} \end{aligned}$$

既不是替换规则列表，也不是一个有效的分派表，因此无法用来替换。

NDSolve::dsvar: 0.00167923 不能用作变量。

ReplaceAll::reps:

$$\begin{aligned} & \{ \text{NDSolve}[\{x'[0.00167923] == \alpha x[0.00167923] + \psi x[0.00167923] - \\ & \beta y[0.00167923] - \gamma z[0.00167923] - \delta y[0.00167923] z[0.00167923], \\ & \{x, y, z\}, \{0.00167923, 500\}\} \} \end{aligned}$$

既不是替换规则列表，也不是一个有效的分派表，因此无法用来替换。

NDSolve::dsvar: 0.00167923 不能用作变量。

ReplaceAll::reps:

$$\begin{aligned} & \{ \text{NDSolve}[\{x'[0.00167923] == \alpha x[0.00167923] + \psi x[0.00167923] - \\ & 1. \beta y[0.00167923] - 1. \gamma z[0.00167923] - \\ & 1. \delta y[0.00167923] z[0.00167923], \{x, y, z\}, \{0.00167923, 500\}\} \} \end{aligned}$$

既不是替换规则列表，也不是一个有效的分派表，因此无法用来替换。

General::stop: 在本次计算中，ReplaceAll::reps 的进一步输出将被抑制。

NDSolve::dsvar: 1.67923 不能用作变量。

General::stop: 在本次计算中，NDSolve::dsvar 的进一步输出将被抑制。

**NDSolve:** 在  $t == 22.889105268731754$  处，步长实际上为零；可能存在奇点或者刚性系统. [i](#)

**NDSolve:** 在  $t == 22.889105268731754$  处，步长实际上为零；可能存在奇点或者刚性系统. [i](#)

(\*For this case, before the initial condiction,  
when we close to initial condiction, the points are stable ,  
physical consistent.statble situation, if go infinitely,  
the module will break down. situation 2: when we close to the initial condition,  
when we change this module is still keep  
stable. if we get the different part with paper \*)




(\* Case 2\*)

```
In[ ]:= ClearAll
Out[ ]:=
ClearAll
```

```
In[ ]:=  $\alpha = 0.07;$ 
 $\beta = 0.01;$ 
 $\gamma = 0.01;$ 
 $\delta = 0.02;$ 
 $\epsilon = 0.04;$ 
 $\xi = 0.03;$ 
 $\eta = 0.03;$ 
 $\theta = 5.0;$ 
 $\psi = -0.1;$ 
```

```
s = NDSolve[{x'[t] ==  $\alpha x[t] + \beta y[t] - \gamma z[t] + \psi x[t]^2 - \delta z[t] \times y[t],$ 
  y'[t] ==  $\beta y[t] - \alpha x[t] + \gamma z[t] + \theta y[t]^2 - \epsilon \text{Abs}[z[t]] \times x[t],$ 
  z'[t] ==  $\xi + \gamma z[t] - \alpha x[t] + \beta y[t] - \eta x[t] \times \text{Abs}[y[t]],$ 
  x[0] == 0.4954, y[0] == 0.0898, z[0] == 0.6684}, {x, y, z}, {t, 400}]
```

```
Out[ ]:=
```

```
{ {x → InterpolatingFunction[ Domain: {{0., 400.}} Output: scalar],
  y → InterpolatingFunction[ Domain: {{0., 400.}} Output: scalar],
  z → InterpolatingFunction[ Domain: {{0., 400.}} Output: scalar]} ] }
```

```
Manipulate[Plot[Evaluate[{x[t], y[t], z[t]} /.
  NDSolve[{x'[t] ==  $\alpha x[t] + \beta y[t] - \gamma z[t] + \psi x[t]^2 - \delta z[t] \times y[t],$ 
    y'[t] ==  $\beta y[t] - \alpha x[t] + \gamma z[t] + \theta y[t]^2 - \epsilon \text{Abs}[z[t]] \times x[t],$ 
    z'[t] ==  $\xi + \gamma z[t] - \alpha x[t] + \beta y[t] - \eta x[t] \times \text{Abs}[y[t]],$ 
    x[0] == x0, y[0] == y0, z[0] == z0}, {x, y, z}, {t, 500} ]],
  {t, 0, 20}], {x0, 0.5, 1.5}, {y0, 0.1, 0.4}, {z0, 0.7, 1}]
```