




(*This is for special cases and to
look what will happend. Stable or Unstable.*)
(*This is for page 29 figure 9*)


```
In[ ]:=  $\alpha = .01;$   
 $\beta = .07;$   
 $\gamma = .07;$   
 $\delta = .07;$   
 $\epsilon = .03;$   
 $\xi = .07;$   
 $\eta = .0;$   
 $\theta = 0.1;$   
 $\psi = -0.01;$ 
```


```
In[ ]:= s = NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t] x y[t],  
y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]] x[t],  
z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t] Abs[y[t]],  
x[0] == 6.4828, y[0] == 2.2467, z[0] == -2.2706}, {x, y, z}, {t, 400}]
```


 **NDSolve:** 在点 $t == 143.4123054174886$ 处达到了最大步数 103453. 

Out[]:=

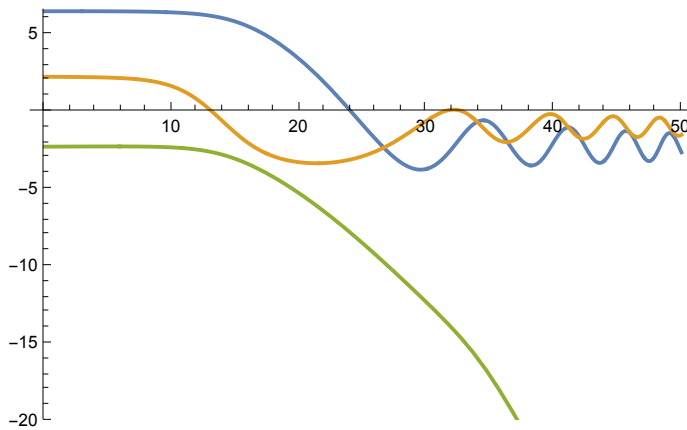
```
{ {x → InterpolatingFunction[ Domain: {{0., 143.}}  
Output: scalar ] ,  
y → InterpolatingFunction[ Domain: {{0., 143.}}  
Output: scalar ] ,  
z → InterpolatingFunction[ Domain: {{0., 143.}}  
Output: scalar ] ] }
```

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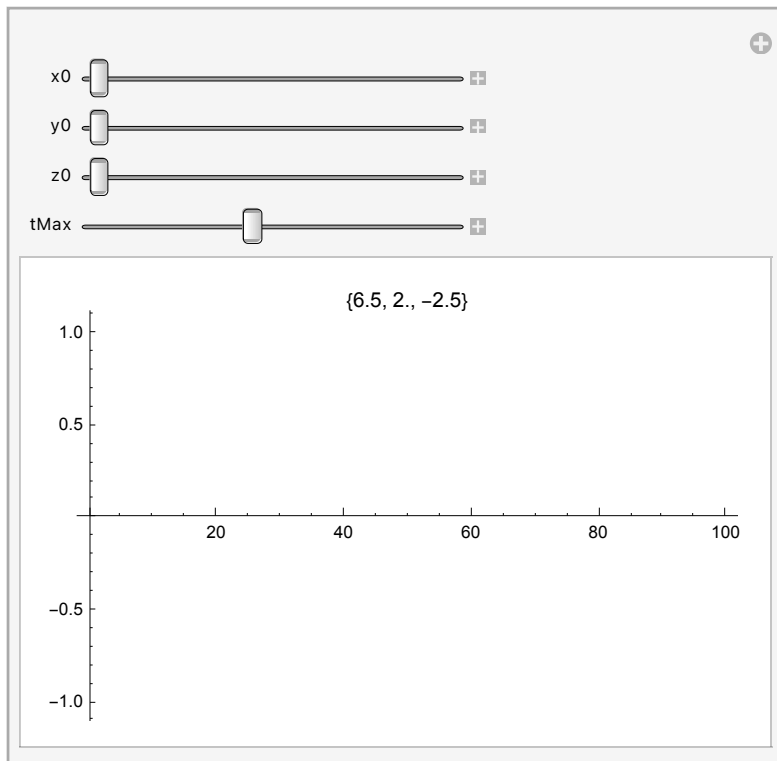
```
In[ ]:= Plot[Evaluate[{x[t], y[t], z[t]} /. s], {t, 0, 50}, PlotRange -> {-20, 6.5}]
```



```
In[ ]:= Manipulate[Plot[Evaluate[{x[t], y[t], z[t]} /.
  NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t] y[t],
    y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]] x[t],
    z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t] Abs[y[t]], x[0] == x0, y[0] == y0,
    z[0] == z0}, {x, y, z}, {t, 500}]], {t, 0, tMax}, PlotLabel -> {x0, y0, z0}],
  {x0, 6.5, 10}, {y0, 2.0, 2.5}, {z0, -2.5, -3}, {tMax, 20, 200}]

(*Evaluate[
  {x[t], y[t], z[t]} /. NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t] y[t],
    y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]] x[t],
    z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t] Abs[y[t]], x[0] == x0, y[0] == y0, z[0] == z0},
  {x, y, z}, {t, 500}]] /. t -> 100*)
```

Out[]=



NDSolve::ndnum: Encountered non-numerical value for a derivative at t == 0..

ReplaceAll::reps:

```

      2
{NDSolve[{x'[t] ==  $\alpha$  x[t] +  $\psi$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] -  $\delta$  y[t] z[t],
      y'[t] == -( $\alpha$  x[t]) -  $\epsilon$  Abs[z[t]] x[t] +  $\beta$  y[t] +  $\theta$  y[t] +  $\gamma$  z[t],
      <<3>>, z[0] == -2.5}, {x, y, z}, {t, 500}]} is neither a list of
replacement rules nor a valid dispatch table, and so cannot be used for
replacing.

```

NDSolve::dsvar: 0.00204286 cannot be used as a variable.

ReplaceAll::reps:

```

      2
{NDSolve[{x'[0.00204286] ==  $\alpha$  x[0.00204286] +  $\psi$  x[0.00204286] -
       $\beta$  y[0.00204286] -  $\gamma$  z[0.00204286] -  $\delta$  y[0.00204286] z[0.00204286],
      <<4>>, z[0] == -2.5}, {x, y, z}, {0.00204286, 500}]} is neither a list
of replacement rules nor a valid dispatch table, and so cannot be used
for replacing.

```

NDSolve::dsvar: 0.00204286 cannot be used as a variable.

ReplaceAll::reps:

```

      2
{NDSolve[{x'[0.00204286] ==  $\alpha$  x[0.00204286] +  $\psi$  x[0.00204286] -
      1.  $\beta$  y[0.00204286] - 1.  $\gamma$  z[0.00204286] -
      1.  $\delta$  y[0.00204286] z[0.00204286], <<4>>, z[0.] == -2.5}, {<<3>>},
{<<10>>, 500.}] is neither a list of replacement rules nor a valid
dispatch table, and so cannot be used for replacing.

```

General::stop: Further output of ReplaceAll::reps
will be suppressed during this calculation.

NDSolve::dsvar: 2.04286 cannot be used as a variable.

General::stop: Further output of NDSolve::dsvar
will be suppressed during this calculation.

```

In[ ]:= x[20]
Out[ ]:=
x[20]

(* For this case,
we can change the range to know it became more and more stable*)

In[ ]:=
ClearAll
Out[ ]:=
ClearAll

In[ ]:=  $\alpha = .01;$ 
 $\beta = .07;$ 
 $\gamma = .07;$ 
 $\delta = .07;$ 
 $\epsilon = .03;$ 
 $\xi = .07;$ 
 $\eta = .0;$ 
 $\theta = 0.1;$ 
 $\psi = -0.01;$ 




In[ ]:= s = NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t] x y[t],
y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]] x[t],
z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t] Abs[y[t]],
x[0] == 3.9544, y[0] == -1.3335, z[0] == 0.8484}, {x, y, z}, {t, 400}]

```


 **NDSolve:** 在点 $t == 220.81572730801324$ 处达到了最大步数 113314. 


Out[]:=


```

{ {x → InterpolatingFunction[ Domain: {{0., 221.}}
Output: scalar],
y → InterpolatingFunction[ Domain: {{0., 221.}}
Output: scalar],
z → InterpolatingFunction[ Domain: {{0., 221.}}
Output: scalar]} }

```

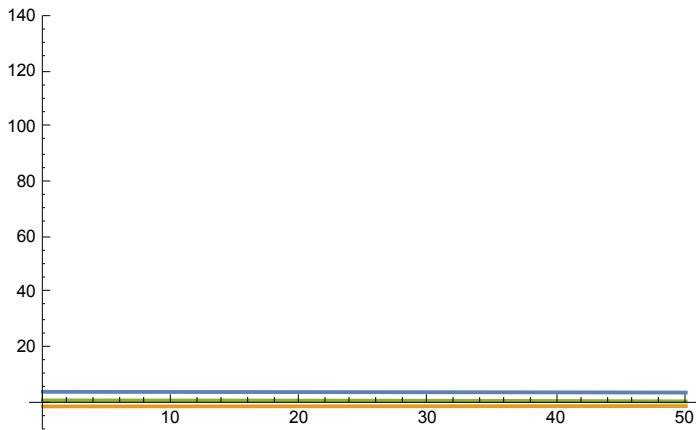
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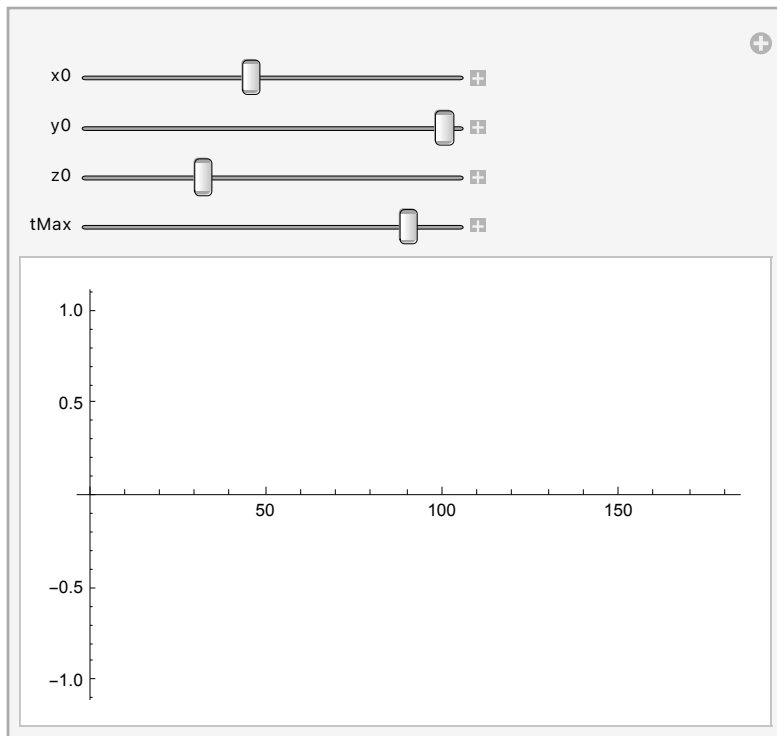
```
In[ ]:= Plot[Evaluate[{x[t], y[t], z[t]} /. s], {t, 0, 50}, PlotRange -> {140, -10}]
```

```
Out[ ]:=
```



```
In[ ]:= Manipulate[Plot[Evaluate[{x[t], y[t], z[t]} /.  
NDSolve[{x'[t] ==  $\alpha$  x[t] -  $\beta$  y[t] -  $\gamma$  z[t] +  $\psi$  x[t]^2 -  $\delta$  z[t] x y[t],  
y'[t] ==  $\beta$  y[t] -  $\alpha$  x[t] +  $\gamma$  z[t] +  $\theta$  y[t]^2 -  $\epsilon$  Abs[z[t]] x x[t],  
z'[t] ==  $\xi$  +  $\gamma$  z[t] -  $\alpha$  x[t] +  $\beta$  y[t] -  $\eta$  x[t] Abs[y[t]],  
x[0] == x0, y[0] == y0, z[0] == z0}, {x, y, z}, {t, 500}]], {t, 0, tMax}],  
{x0, 3.5, 6}, {y0, -2.0, -1.0}, {z0, 0.5, 1.5}, {tMax, 20, 200}]
```

```
Out[ ]:=
```



... **NDSolve**: 在点 $t == 207.15413655874616$ 处达到了最大步数 2411328. i

... **NDSolve**: 在点 $t == 207.15413655874616$ 处达到了最大步数 2411328. i

... NDSolve: 在点 t == 204.86164730459691` 处达到了最大步数 2335046. [i](#)

... NDSolve: 在点 t == 190.92946341531982` 处达到了最大步数 590866. [i](#)

... NDSolve: 在点 t == 221.83183461662347` 处达到了最大步数 121343. [i](#)

... NDSolve: 在点 t == 221.83183461662347` 处达到了最大步数 121343. [i](#)

... NDSolve: 在点 t == 221.83183461662347` 处达到了最大步数 121343. [i](#)

... NDSolve: 在点 t == 221.83183461662347` 处达到了最大步数 121343. [i](#)

... NDSolve: 在点 t == 221.83183461662347` 处达到了最大步数 121343. [i](#)

... NDSolve: 在点 t == 205.32813396648237` 处达到了最大步数 285530. [i](#)

... NDSolve: 在点 t == 204.76793269160464` 处达到了最大步数 394256. [i](#)

... NDSolve: 在点 t == 263.21616759511073` 处达到了最大步数 1164120. [i](#)

... NDSolve: 在点 t == 236.93587181764377` 处达到了最大步数 1115495. [i](#)

NDSolve::ndnum: Encountered non-numerical value for a derivative at t == 0..

ReplaceAll::reps:

$$\{ \text{NDSolve}[\{x'[t] == \alpha x[t] + \psi x[t] - \beta y[t] - \gamma z[t] - \delta y[t] z[t],$$

$$y'[t] == -(\alpha x[t]) - \epsilon \text{Abs}[z[t]] x[t] + \beta y[t] + \theta y[t] + \gamma z[t],$$

$$\langle\langle 3 \rangle\rangle, z[0] == 0.8\}, \{x, y, z\}, \{t, 500\}\} \text{ is neither a list of}$$

replacement rules nor a valid dispatch table, and so cannot be used for replacing.

NDSolve::dsvar: 0.0036894 cannot be used as a variable.

ReplaceAll::reps:

$$\{ \text{NDSolve}[\{x'[0.0036894] == \alpha x[0.0036894] + \psi x[0.0036894] -$$

$$\beta y[0.0036894] - \gamma z[0.0036894] - \delta y[0.0036894] z[0.0036894],$$

$$y'[0.0036894] == -\langle\langle 1 \rangle\rangle + \langle\langle 4 \rangle\rangle, \langle\langle 3 \rangle\rangle, z[0] == 0.8\}, \langle\langle 2 \rangle\rangle\} \text{ is}$$

neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

NDSolve::dsvar: 0.0036894 cannot be used as a variable.

ReplaceAll::reps:

$$\{ \text{NDSolve}[\{x'[0.0036894] == \alpha x[0.0036894] + \psi x[0.0036894] -$$

$$1. \beta y[0.0036894] - 1. \gamma z[0.0036894] -$$

$$1. \delta y[0.0036894] z[0.0036894], \langle\langle 4 \rangle\rangle, z[0.] == 0.8\}, \{x, y, z\},$$

$$\{0.0036894, 500.\}\} \text{ is neither a list of replacement rules nor a valid}$$

dispatch table, and so cannot be used for replacing.

General::stop: Further output of ReplaceAll::reps
will be suppressed during this calculation.

NDSolve::dsvar: 3.6894 cannot be used as a variable.

General::stop: Further output of NDSolve::dsvar
will be suppressed during this calculation.

(* This case is still unstable *)