$$\beta \equiv 1 - \alpha$$

$$H[z] = \frac{\alpha}{1 - \beta \cdot z^{-1}}$$