

Formal Methods

Assignment 1

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February 27, 2018

1 Exercise 1

Problem : fix mutex to be live using eshmun

Objective : We must prevent deadlock (prevent a certain process to loop infinitely in the critical section).

Solution :

We will use eshmun to represent the processes and their states and try to achieve the goal. Moreover, we will use the initial diagram given in class for the states of the processes and add/delete states to make it live.

The property of liveness can be represented by the following CTL formula :

$AG(T1 \rightarrow AF(C1)) \text{ AND } AG(T2 \rightarrow AF(C2))$

The following steps are done :

1- Remove state (C1,C2) because of course we need to satisfy mutual exclusion.

2- Add Flags F1 and F2 for processes P1 and P2 to prevent deadlock.

3-In each transition we will make sure that we only change 1 state , for example if we are in state $S1 = (N1, N2)$ then we can only move to $(T1, N2)$ or $(N1, T2)$ this is because if we are working in a shared memory we have to prevent 2 processes from accessing the same file.

Now for the transitions : $S0(N1, N2)$ we have 2 transitions to $S1(T1, N1, F1)$ and $S2(N1, T2, F2)$ were in $S1$ process P1 will be requesting the critical section, and in $S2$ process P2 will be in requesting the critical section.

Then from $S1$, process P1 will enter the critical section in state $S3$, or both process P1 and P2 will be requesting the critical section but the mutex is with P1.

Now with P1 in the critical section in state $S3$, process p2 will be requesting the critical section in state $S6$ but it has no mutex F2, so in order to prevent deadlock and release the mutex F1 we move from $S6(C1, T2, F1)$ to $(C1, T2)$ then to $S2(N1, T2)$ and after that we give the mutex F2 to process P2 in state $S5(N1, T2, F2)$. Now, process S2 can enter the critical section $S7(N1, C2, F2)$.

Same thing is applied if we move from the initial state $S0$ to $S5$, were in this case process p2 will enter the critical section first and then P1 and so on. In the assumptions made we guarantee liveness since no process can enter a deadlock

and prevent the other process from entering the critical section. Hence, liveness property is satisfied in the built graph.

2 Exercise 2

Problem : let path formula $f = O_1 O_2 O_3 \dots O_N P$, for each O_i is either F or G, can we simplify f ?

Solution :

We try to produce different combinations of path f and see if this path can be reduced.

1- If $f = Fp$ (reduced)

2- If $f = Gp$ (reduced)

3- If $f = FFFF\dots Fp$. If we try to decompose this formula :

$F(F\dots Fp) =$ eventually $F\dots Fp$ will hold, $\#F = i$, then decomposing the internal formula we get :

eventually $FF\dots Fp$ will hold, $\#F = i-1$, and so on, until we reach $Fp =$ eventually p will hold.

Then we can reduce $FF\dots Fp$ to Fp which says that eventually p will hold.

4- If $f = GGG\dots Gp$, $\#G = i$, $G\dots Gp$ will always hold , $\#G = i-1$, if we follow the same steps as for part 3, we reach Gp which means that p will always be true at each state. Therefore $GG\dots Gp$ can be reduced to Gp .

5- If $f = FGFp$ this formula means that GFp will eventually holds, which in turns means that eventually and forever Fp will always hold, and hence p will eventually holds. From the semantics of the meaning of this formula we can see that it's equivalent to GFp which means that Fp will always hold, and hence p will eventually holds.

We can then deduce that $FGFp$ can be reduced to GFp .

6- Similarly, If $f = GFGp = FGp$ is always true \rightarrow eventually Gp will hold \rightarrow eventually p will always be true.

Then the formula $GFGp$ means that we will reach a state where p is true at this state and for all the states after it.

On the other hand, we have FGp means that eventually Gp will be true, and therefore, eventually we will reach a state where p is true at this state and for all states after it. So, $GFGp$ can be reduced to FGp .

By 5 and 6, we can deduce that for any alternating $FGFFGF\dots FGFp$ or $GFGFG\dots GFGp$, we can reduce this formula to the last 2 ... , for example, $FGFGFG\dots FGFGFGFp$ and $GFGFG\dots FGFGp$ can be reduced to GFp and can b FGp respectively.

In conclusion, if $f = O_1 O_2 O_3 \dots O_N p$, then we can combine all consecutive

F's and G's to single F and G, and for

$$f = O_1 O_2 O_3 \dots O_N p = \begin{cases} FGp & \text{if } O(N-1) = F \text{ and } G = O(N), \text{ for } N \geq 2 \\ GFp & \text{if } O(N-1) = G \text{ and } F = O(N), \text{ for } N \geq 2 \\ Fp & \text{if } O_1 = O_2 = \dots O_N = F, \text{ for } N \geq 1 \\ Gp & \text{if } O_1 = O_2 = \dots O_N = G, \text{ for } N \geq 1 \end{cases}$$