Introduction to Digital Image Processing

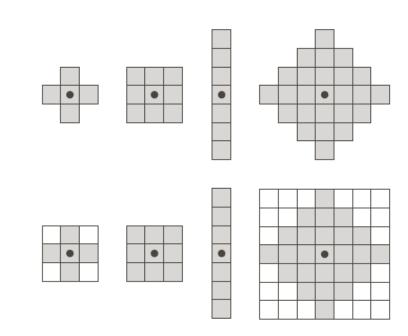
— MORPHOLOGICAL OPERATIONS

Xiaohui Yuan

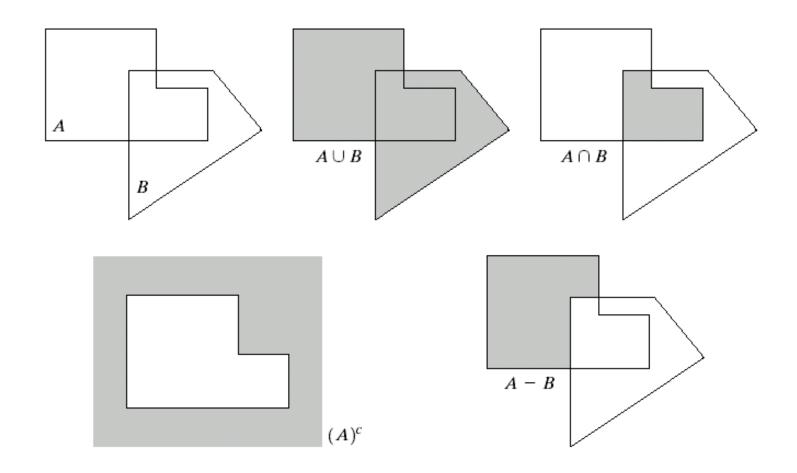
Department of Computer Science and Engineering University of North Texas xiaohui.yuan@unt.edu

Morphological operations and Structuring Element

- Morphological operations are used to extract image components for the representation and description of image regions, such as boundaries and skeletons.
 - Typical operations include Erosion, Dilation, Opening, Closing, Hit-or-miss transformation, and Thinning, Thickening
- Structuring Elements (SE) contain 0, 1 and (or) Not-a-Number (NaN)
 - NaNs in an SE that does not involve computing
- Every Structuring Element has an "origin"
 - The computing result is applied to the origin
- Shape and size can be adapted to geometric properties of the objects
- Examples of Structuring Elements



Basic Set Operations

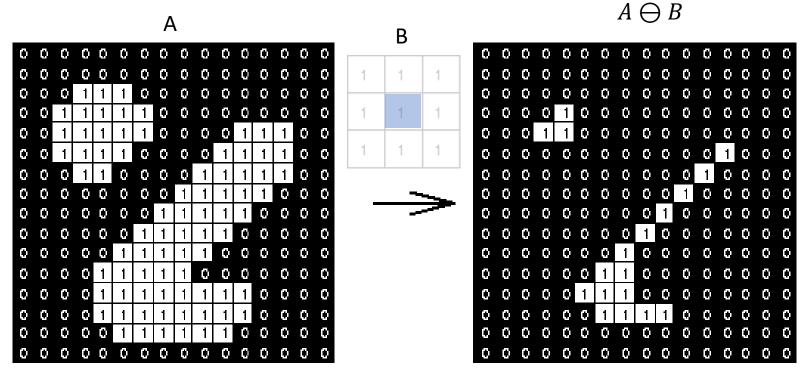


Erosion

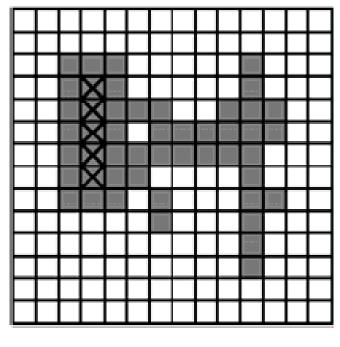
• With an image A and an SE B, the erosion of A by B, denoted by $A \ominus B$, is defined as

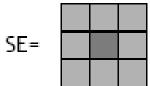
$$A \ominus B = \{z | (B)_z \subseteq A\}$$

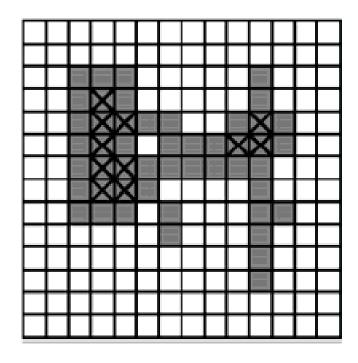
z is an element of A

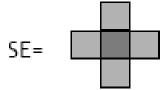


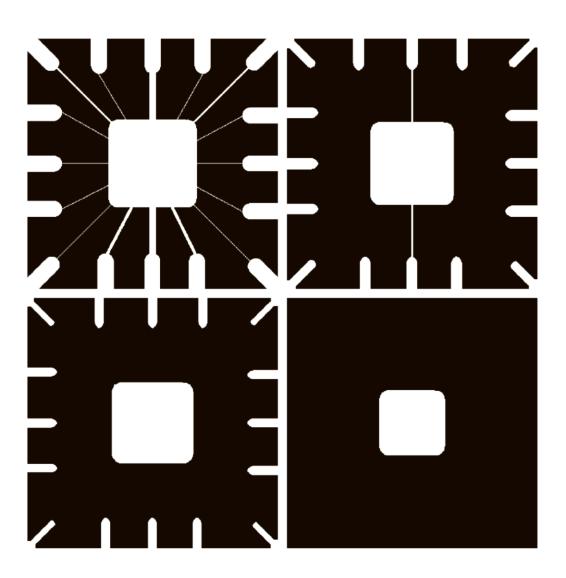
Examples of Erosion







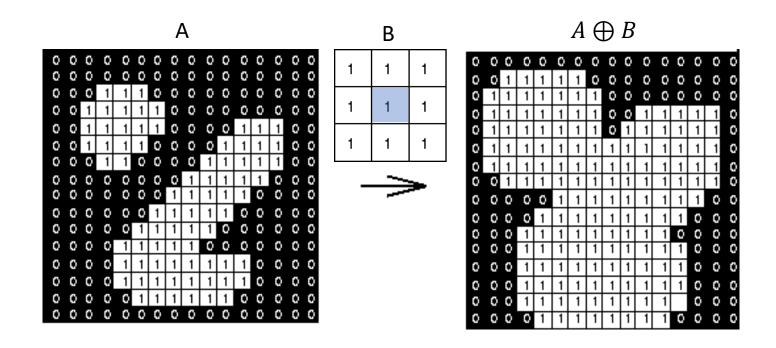




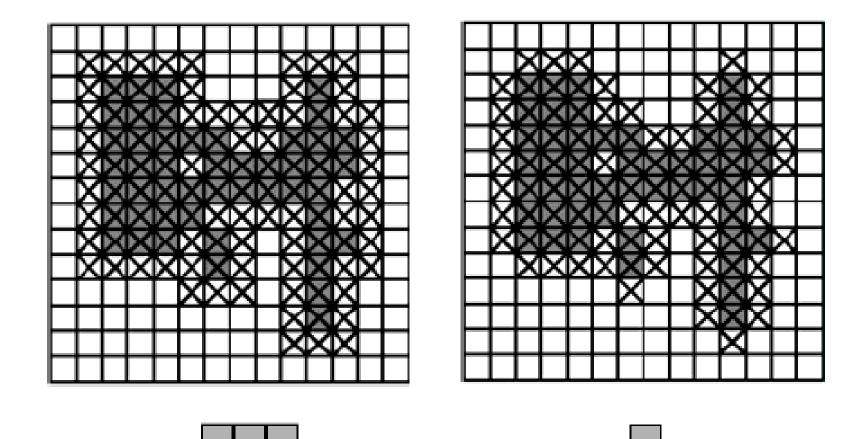
Dilation

• With an image A and a structuring element B, the dilation of A by B, denoted by $A \oplus B$, is defined as

$$A \oplus B = \{z | (B)_z \cap A \neq \emptyset\}$$



Dilation



SE=

SE=

Using Dilation to Bridging Gaps

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.

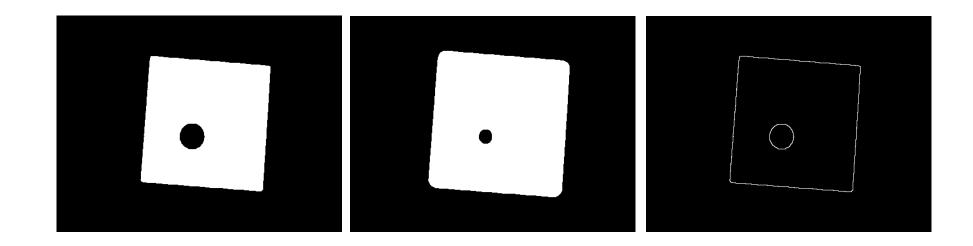
Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.

0	1	0
1	1	1
0	1	0

Edge Detection

Using dilation and image subtraction

- 1. Dilate the original image
- 2. Subtract the original image from the dilated version



Opening

Opening is achieved by erosion followed by dilation

$$A \circ B = (A \ominus B) \oplus B$$

• Opening is idempotent, i.e., repeated application has no further effects: $(A \circ B) \circ B = A \circ B$

It is used to eliminate protrusions and break connections.

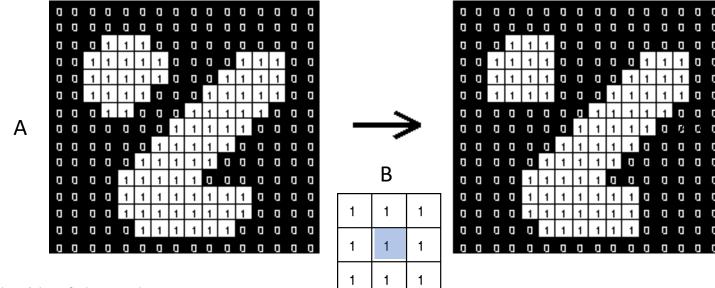


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Opening

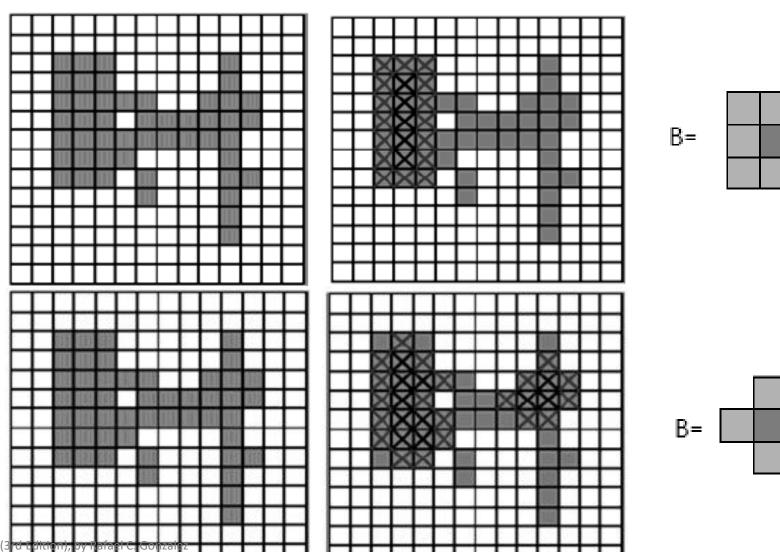
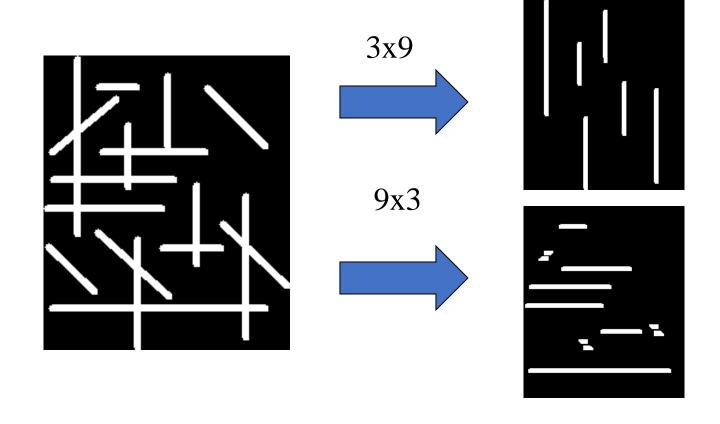


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Opening Example

• 3x9 and 9x3 Structuring Element



Closing

- Take the structuring element (SE) and slide it around *outside* each foreground region.
 - All background pixels that can be covered by the SE with the SE being entirely within the background region will be preserved.
 - All background pixels that cannot be reached by the structuring element without lapping over the edge of the foreground object will be turned into a foreground.
- Closing is idempotent: Repeated application has no further effects!

Closing

Closing is achieved by dilation followed by erosion

$$A \bullet B = (A \oplus B) \ominus B$$

- It is also idempotent: $(A \bullet B) \bullet B = A \bullet B$
- It is used to fuse narrow gaps and eliminate small holes

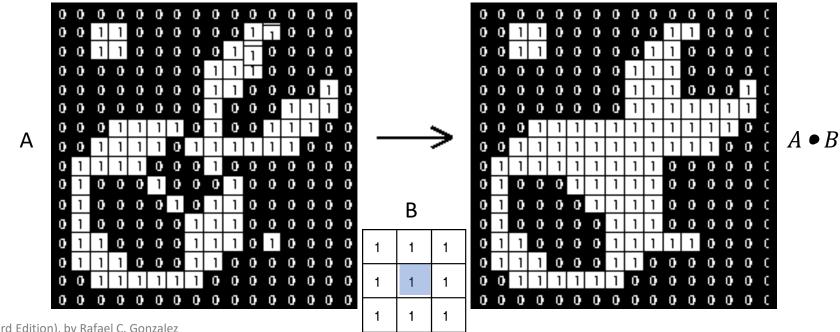


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Closing Examples

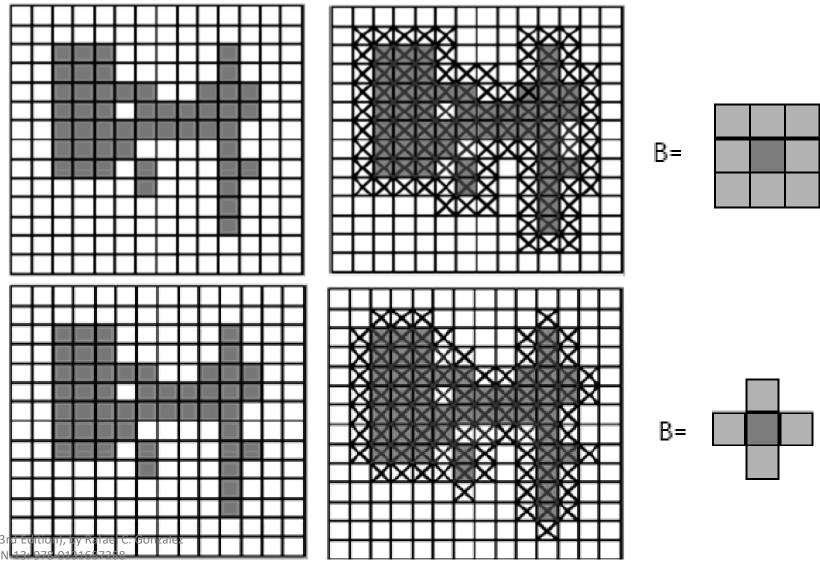
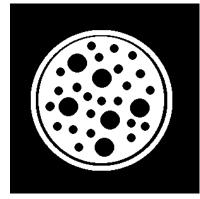
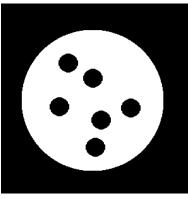


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Closing Examples

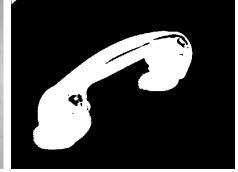
SE: disc of size 22





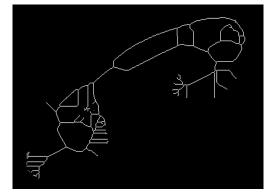
SE: disc of size 20

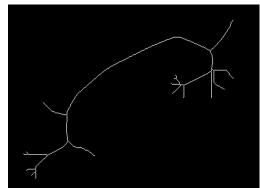






Skeleton operation looks better for closed image





Hit-and-miss Transform

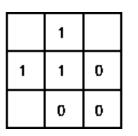
- Hit-and-miss transform looks for particular patterns within the image.
- If the foreground and background pixels in the SE *exactly match* the foreground and background pixels in the image, then the pixel underneath the origin of the structuring element is set to the foreground color.
- Example for a Hit-and-miss Structuring Element

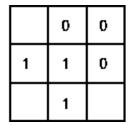
	1	
0	1	1
0	0	

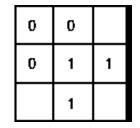
Corner Detection

Structuring Elements representing four corners

	1	
0	1	1
0	0	







- Apply each Structuring Element
- Use OR operation to combine the four results

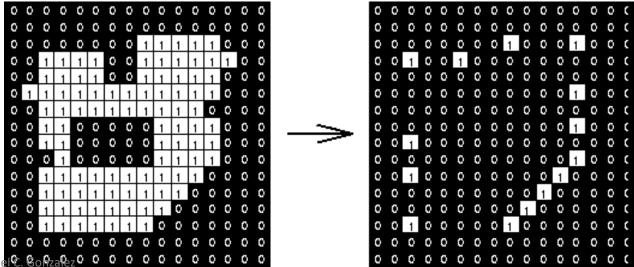


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Thinning

Thinning of an image A with B is defined as

$$A - HaM(A, B)$$

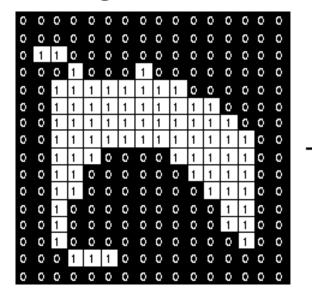
where HaM is the Hit-and-Miss operator and 0-1=0!!

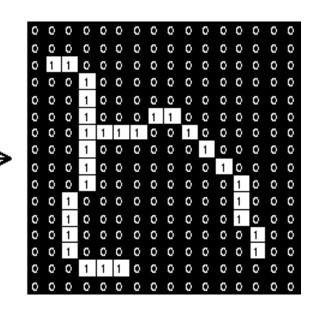
- If foreground and background fit the structuring element exactly, then the pixel at the origin of the SE is set to 0.
- Note that the value of the SE at the origin is 1 or NaN.

Two Hitand-miss SE are used

0	0	0
	1	
1	1	1

	0	0
1	1	0
	1	



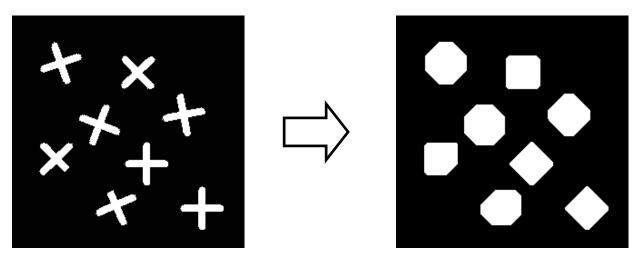


Thickening

• Thickening of an image A with B is defined as A + HaM(A, B)

where HaM is the Hit-and-Miss operator and 1 + 1 = 1!

- If foreground and background match exactly the SE, then set the pixel at its origin to 1.
- Note that the value of the SE at the origin is 0 or NaN.



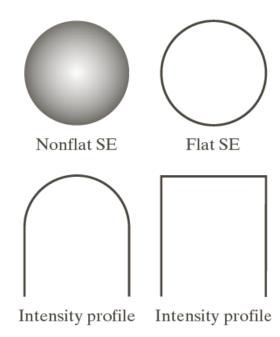
What about Grayscale Images?

Using flat SE

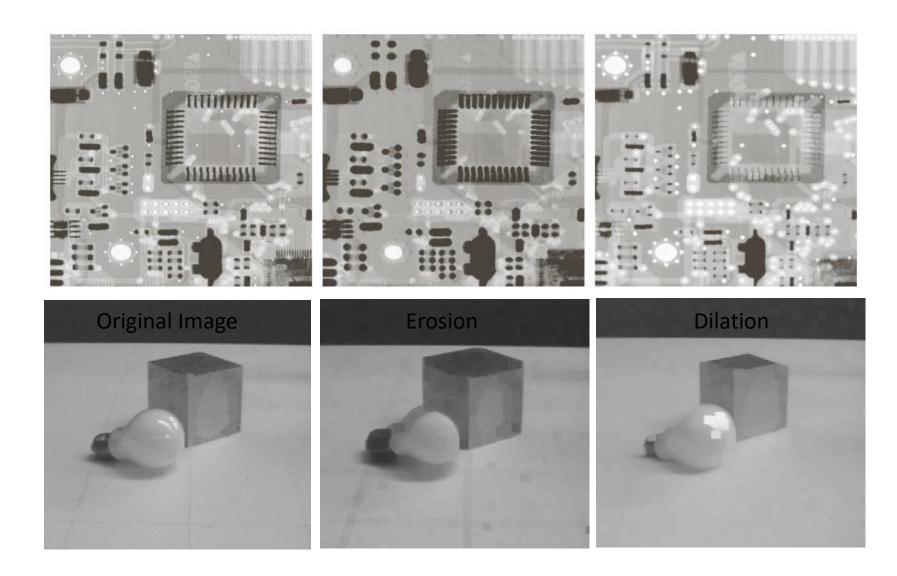
- Erosion: $[A \ominus B](x,y) = \min_{(s,t) \in b} \{A(x+s,y+t)\}$
- Dilation: $[A \oplus B](x,y) = \max_{(s,t) \in b} \{A(x-s,y-t)\}$

Using non-flat SE

- Erosion: $[A \ominus B](x,y) = \min_{(s,t) \in b} \{A(x+s,y+t) B(s,t)\}$ Dilation: $[A \oplus B](x,y) = \max_{(s,t) \in b} \{A(x-s,y-t) + B(s,t)\}$



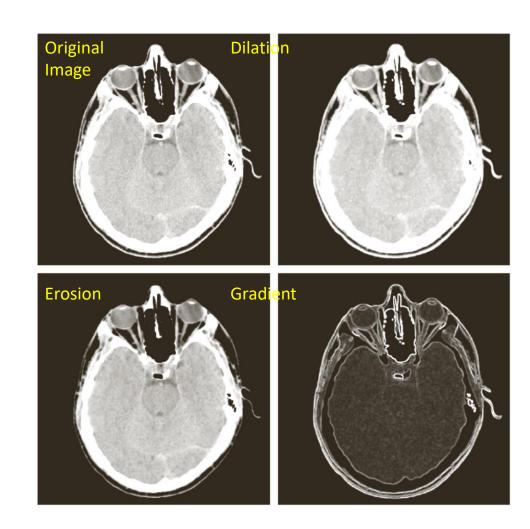
Erosion and Dilation Example



Morphological Gradient

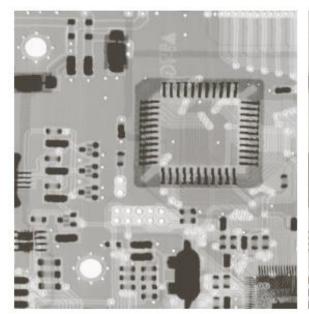
• Dilation and erosion can be used to obtain the morphological gradient of an image $g = (A \oplus B) - (A \ominus B)$

 The edges are enhanced, and the contribution of the homogeneous areas are suppressed, thus producing a "derivativelike" (gradient) effect.

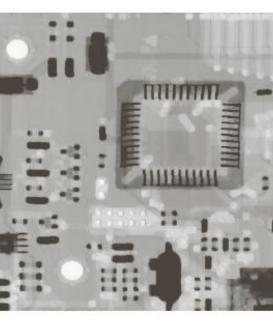


Opening and Closing

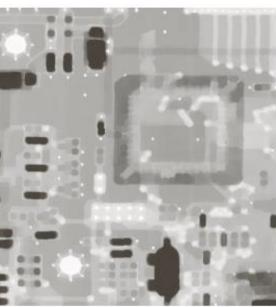
- Opening $A \circ B = (A \ominus B) \oplus B$
 - It suppresses bright details smaller than the specified SE
- Closing $A \cdot B = (A \oplus B) \ominus B$
 - It suppresses dark details
- Opening and closing are used often in combination for image smoothing and noise removal



Original image



Opening disk SE, radius=3



Closing disk SE, radius=5

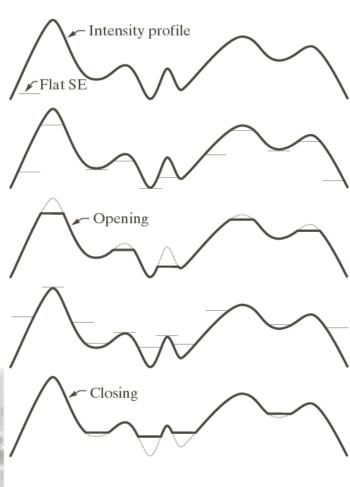


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