**COMP 4030/6030**: Assignment 03/02/2016

**Due date**: 03/02/2016

Email programming solutions to the TA (Quang Tran, qmtran@memphis.edu). Put "COMP 4030/6030 assignment 3" on the subject line.

- 1. (Programming assignment, 25 points) Write a Python function called Split, which takes a list of numbers A and returns a list of numbers B with the following properties:
  - The numbers in B are simply an rearrangement of the numbers in A.
  - In particular, A[0] appears somewhere in B, say at index i. (This means A[0] == B[i])
  - If  $j \le i$ , then  $B[j] \le B[i]$ .
  - If j > i, then B[j] > B[i].

Example: Split([ $\mathbf{10}$ ,7,20,3,0,9,15,7,18,50]) returns [7,3,0,9,7, $\mathbf{10}$ ,20,15,18,50]. Notice that numbers in the returned list are the same as those in the input list; they are simply rearranged. Further, the arrangement is such as in the returned list, (i) everything to the left of 10 (A[0]) is less than or equal to it and (ii) everything to the right of 10 is greater than it.

- 2. (Bonus Programming assignment, 20 points) Rewrite Python program in question 2 to take  $\Theta(1)$  of space. Notice that the space complexity does not account for the input list A.
- 3. (25 points) Analyze the running time complexity and space complexity of your own program in question 1.
- 4. (25 points) Explain why  $n^5 + 2n^2 \in \Theta(n^5)$ .
- 5. (25 points) Given the following function:

```
def find_cats(L, idx, output):
    if idx < len(L):
        if "cat" in L[idx]:
            output.append(L[idx])
            find_cats(L, idx+1, output)
        else:
            find_cats(L, idx+1, output)</pre>
```

Assuming L is a list of strings, explain why after executing the code below, A will be a list of all strings (in L) that contain "cat".

```
A = []
find_cats(L, 0, A)
```

Hint: this is an explanation of why a function is correct, not how it works. Clearly, in your explanation of why, you will probably refer to the logic of the function (i.e. how it works in some places). But explaining why something is correct and how it works are not the same thing.