Data Structures and Algorithms

Week 04 Problem Set **Dynamic Data Structures**

1. (Memory management)

Consider the following function:

```
/* Makes an array of 10 integers and returns a pointer to it */
int *makeArrayOfInts(void) {
  int arr[10];
   int i;
   for (i=0; i<10; i++) {
     arr[i] = i;
   return arr;
}
```

Explain what is wrong with this function. Rewrite the function so that it correctly achieves the intended result using malloc().

Answer:

The function is erroneous because the array arr will cease to exist after the line return arr, since arr is local to this function and gets destroyed once the function returns. So the caller will get a pointer to something that doesn't exist anymore, and you will start to see garbage, segmentation faults, and other errors.

Arrays created with malloc() are stored in a separate place in memory, the heap, which ensures they live on indefinitely until you free them yourself.

The correctly implemented function is as follows:

```
int *makeArrayOfInts() {
  int *arr = malloc(sizeof(int) * 10);
  assert(arr != NULL);
  int i;
   for (i=0; i<10; i++) {
     arr[i] = i;
   return arr; // this is fine because the array itself will live on
}
```

2. (Memory management)

Consider the following program:

```
#include <stdio.h>
#include <stdlib.h>
Void func(int *a) {
   a = malloc(sizeof(int));
int main(void) {
   int *p;
   func(p);
   *p = 6;
   printf("%d\n",*p);
   free(p);
   return 0;
}
```

Explain what is wrong with this program.

Answer:

The program is not valid because func() makes a *copy* of the pointer p. So when malloc() is called, the result is assigned to the copied pointer rather than to p. Pointer p itself is pointing to random memory (e.g., 0x0000) before and after the function call. Hence, when you dereference it, the program will (likely) crash.

If you want to use a function to add memory to a pointer, then you need to pass the *address* of the pointer (i.e. a pointer to a pointer, or "double pointer"):

```
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
void func(int **a) {
   *a = malloc(sizeof(int));
                             // always check that memory allocation was successful
   assert(*a != NULL);
}
int main(void) {
  int *p;
   func(&p);
   *p = 6;
   printf("%d\n",*p);
   free(p);
  return 0:
}
```

Note also that you should always ensure that malloc() did not return NULL before you proceed.

3. (Dynamic arrays)

Write a C program that uses a dynamic array of unsigned long long int numbers (8 bytes, only positive numbers) to compute the *n*'th Fibonacci number, where *n* is given as command line argument. For example, **./fib 60** should result in 1548008755920.

Hint: The placeholder 11u (instead of d) can be used to print an unsigned long long int. Recall that the Fibonacci numbers are defined as Fib(1) = 1, Fib(2) = 1 and Fib(n) = Fib(n-1) + Fib(n-2) for $n \ge 3$.

Answer:

```
#include <stdio.h>
#include <stdlib.h>
int main(int argc, char *argv[]) {
   if (argc != 2) {
      fprintf(stderr, "Usage: %s number\n", argv[0]);
      return 1;
   }
   int n = atoi(argv[1]);
   if (n > 0) {
      unsigned long long int *arr = malloc(n * sizeof(unsigned long long int));
      arr[0] = 1;
      arr[1] = 1;
      int i;
      for (i = 2; i < n; i++) {
         arr[i] = arr[i-1] + arr[i-2];
      printf("%llu\n", arr[n-1]);
                                    // don't forget to free the array
      free(arr);
   return 0;
}
```

4. (Dynamic stacks and queues)

- a. Describe in words how you would implement a *queue* ADT using a dynamic linked list. Which of the functions for the linked list implementation of a stack from the lecture need to be changed, and how?
- b. Suppose that you have a stack *S* containing *n* elements and a queue *Q* that is initially empty. Describe in words how you can use *Q* to scan *S* in order to check if it contains a certain element *x*, with the additional

constraint that your algorithm must return the elements back to *S* in their original order. You should **not** use an additional array or linked list — only use *S* and *Q*.

Answer

- a. In the stack ADT, elements are added to ("push") and removed from ("pop") the beginning of the linked list. For a queue, we have two options: either we add ("enqueue") new elements at the end and continue to take elements off ("dequeue") from the beginning. Or we continue to add elements at the beginning and dequeue from the end. Operating on both ends will be more efficient if we use a datastructure with two pointers: one pointing to the *first* and one pointing to the *last* element of a list.
- b. The solution is to use the queue Q to process the elements in two phases. In the first phase, we iteratively pop all the elements from S and enqueue them in Q, then dequeue the elements from Q and push them back onto S. As a result, all the elements are now in reversed order on S. In the second phase, we again pop all the elements from S, but this time we also look for the element x. By again passing the elements through Q and back onto S, we reverse the reversal, thereby restoring the original order of the elements on S.

5. (Dynamic linked lists)

Write a C-program called **Ilbuild.c** that builds a linked list of integers from user input. Your program should use the following functions:

- NodeT *makeNode(int value): taken from the lecture
- void freeLL(NodeT *head): taken from the lecture
- void showLL(NodeT *head): taken from the lecture but needs modification
- NodeT *joinLL(NodeT *head1, NodeT *head2): appends linked list head2 to list head1. Needs to be implemented.

The program:

- starts with an empty linked list called all (say), initialised to NULL
- prompts the user with the message "Enter a number: "
- makes a linked list node called *new* from user's response
- o appends new to all
- asks for more user input and repeats the cycle
- the cycle is terminated when the user enters any non-numeric character
- on termination, the program generates the message "Finished. List is " followed by the contents of the linked list in the format shown below.

A sample interaction is:

```
prompt$ ./llbuild
Enter an integer: 12
Enter an integer: 34
Enter an integer: 56
Enter an integer: quit
Finished. List is 12->34->56
```

Note that any non-numeric data 'finishes' the interaction. If the user provides no data, then no list should be output:

```
prompt$ ./llbuild
Enter an integer: #
Finished.
```

We have created a script that can automatically test your program. To run this test you can execute the dryrun program that corresponds to the problem set and week. It expects to find a program named llbuild.c in the current directory. You can use dryrun as follows:

```
prompt$ -cs9024/bin/dryrun prob04
```

Answer:

```
// llbuild.c: create a linked list from user input, and print
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>

typedef struct node {
```

```
int data;
   struct node *next;
} NodeT;
NodeT *joinLL(NodeT *head1, NodeT *head2) {
// either or both head1 and head2 may be NULL
   if (head1 == NULL) {
      head1 = head2;
   } else {
      NodeT *p = head1;
      while (p->next != NULL) {
         p = p->next;
      p->next = head2; // this does nothing if head2 == NULL
   return head1;
}
NodeT *makeNode(int v) {
   NodeT *new = malloc(sizeof(NodeT));
   assert(new != NULL);
   new->data = v;
   new->next = NULL;
   return new;
}
void showLL(NodeT *list) {
   NodeT *p;
   for (p = list; p != NULL; p = p->next) {
      printf("%d", p->data);
      if (p->next != NULL)
         printf("->");
   putchar('\n');
void freeLL(NodeT *list) {
    NodeT *p = list;
    while (p != NULL) {
        NodeT *temp = p->next;
        free(p);
        p = temp;
    }
}
int main(void) {
   NodeT *all = NULL;
   int data;
   printf("Enter an integer: ");
   while (scanf("%d", &data) == 1) {
      NodeT *new = makeNode(data);
      all = joinLL(all, new);
      printf("Enter an integer: ");
   if (all != NULL) {
      printf("Finished. List is ");
      showLL(all);
      freeLL(all);
   } else {
      printf("Finished.\n");
   return 0;
}
```

6. Challenge Exercise

Extend the C-program from the previous exercise to split the linked list in two halves and output the result. If the list has an odd number of elements, then the first list should contain one more element than the second.

Note that:

- your algorithm should be 'in-place' (so you are not permitted to create a second linked list or use some other data structure such as an array);
- you should not traverse the list more than once (e.g. to count the number of elements and then restart from the beginning).

An example of the program executing could be

```
prompt$ ./llsplit
Enter an integer: 421
Enter an integer: 456732
Enter an integer: 321
Enter an integer: 4
Enter an integer: 86
Enter an integer: 89342
Enter an integer: 9
Enter an integer: 9
Enter an integer: #
Finished. List is 421->456732->321->4->86->89342->9
First half is 421->456732->321->4
Second half is 86->89342->9
```

Answer:

The following solution uses a "slow" and a "fast" pointer to traverse the list. The fast pointer always jumps 2 elements ahead. At any time, if slow points to the i^{th} element, then fast points to the $2 \cdot i^{th}$ element. Hence, when the fast pointer reaches the end of the list, the slow pointer points to the last element of the first half.

```
NodeT *splitList(NodeT *head) { // returns pointer to second half
   assert(head != NULL);

NodeT *slow, *fast;

slow = head;
fast = head->next;
while (fast != NULL && fast->next != NULL) {
    slow = slow->next;
   fast = fast->next->next;
}
fast = slow->next;
// this becomes head of second half
slow->next = NULL;
// cut off at end of first half
return fast;
}
```