

Week 07 Problem Set

Graph Traversal, Digraphs

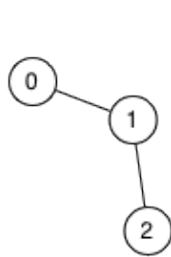
[\[Show with no answers\]](#) [\[Show with all answers\]](#)

Note:

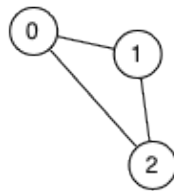
Sample solutions will be posted on Friday to help you prepare for the mid-term online test between Monday 12noon and Tuesday 12noon next week (10–11 September).

1. (Hamiltonian/Euler paths and circuits)

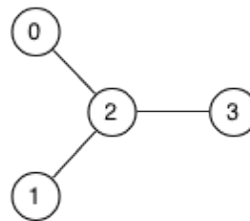
a. Identify any Hamiltonian/Euler paths/circuits in the following graphs:



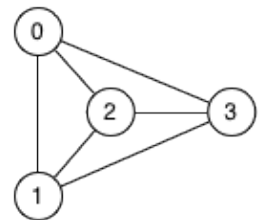
Graph 1



Graph 2

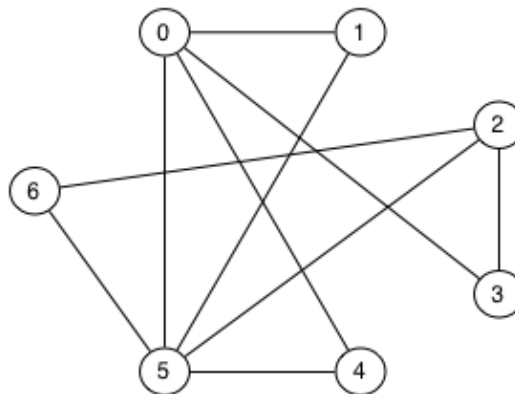


Graph 3



Graph 4

b. Find an Euler path and an Euler circuit (if they exist) in the following graph:



[\[show answer\]](#)

2. (Cycle check)

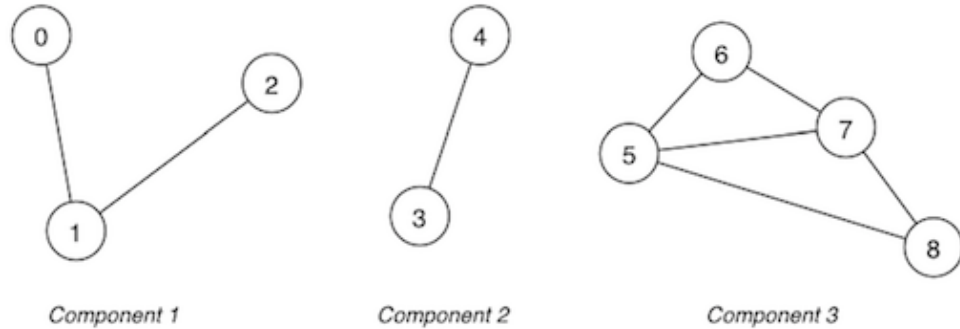
Take the "buggy" [cycle check](#) from the lecture and design a correct algorithm using depth-first search to determine if a graph has a cycle.

[\[show answer\]](#)

3. (Connected components)

a. Write a C program that computes the connected components in a graph. The graph should be built from user input in the same way as in exercise 2 last week (i.e., problem set week 6). Your program should use the Graph ADT ([Graph.h](#), [Graph.c](#)) from the lecture. These files should not be changed.

An example of the program executing is shown below for the following graph:



```

prompt$ ./components
Enter the number of vertices: 9
Enter an edge (from): 0
Enter an edge (to): 1
Enter an edge (from): 1
Enter an edge (to): 2
Enter an edge (from): 4
Enter an edge (to): 3
Enter an edge (from): 6
Enter an edge (to): 5
Enter an edge (from): 6
Enter an edge (to): 7
Enter an edge (from): 5
Enter an edge (to): 7
Enter an edge (from): 5
Enter an edge (to): 8
Enter an edge (from): 7
Enter an edge (to): 8
Enter an edge (from): done
Finished.
Number of components: 3
Component 1:
0
1
2
Component 2:
3
4
Component 3:
5
6
7
8

```

Note that:

- the vertices within a component are printed in ascending order
- the components themselves are output in ascending order of their smallest node.

You may assume that a graph has a maximum of 1000 nodes.

We have created a script that can automatically test your program. To run this test you can execute the `dryrun` program that corresponds to the problem set and week. It expects to find a program named `components.c` in the current directory. You can use `dryrun` as follows:

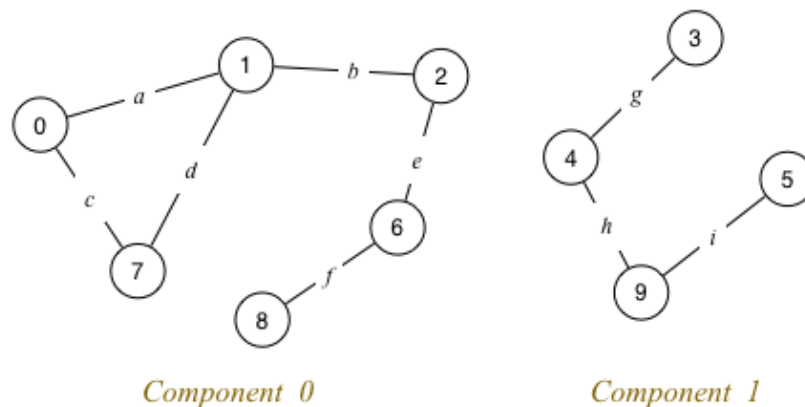
```
prompt$ -cs9024/bin/dryrun prob07
```

- b. Computing connected components can be avoided by maintaining a vertex-indexed connected components array as part of the Graph representation structure:

```
typedef struct GraphRep *Graph;

struct GraphRep {
    ...
    int nC; // # connected components
    int *cc; /* which component each vertex is contained in
              i.e. array [0..nV-1] of 0..nC-1 */
    ...
}
```

Consider the following graph with multiple components:



Assume a vertex-indexed connected components array $cc[0..nV-1]$ as introduced above:

```
nC    = 2
cc[ ] = {0,0,0,1,1,1,0,0,0,1}
```

Show how the $cc[]$ array would change if

1. edge d was removed
2. edge b was removed

- c. Consider an adjacency matrix graph representation augmented by the two fields

- nC (number of connected components)
- $cc[]$ (connected components array)

These fields are initialised as follows:

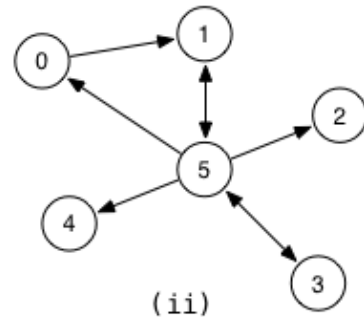
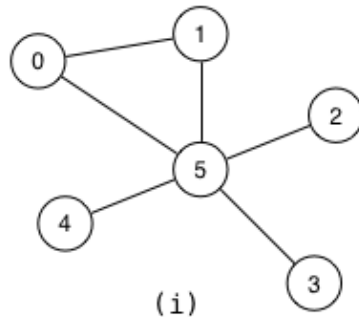
```
newGraph(V):
|   Input  number of nodes V
|   Output new empty graph
|
|   g.nV=V, g.nE=0, g.nC=V
|   allocate memory for g.edges[ ][ ]
|   for all i=0..V-1 do
|       g.cc[i]=i
|       for all j=0..V-1 do
|           g.edges[i][j]=0
|       end for
|   end for
|   return g
```

Modify the pseudo-code for edge insertion and edge removal from the lecture (week 6) to maintain the two new fields.

[\[show answer\]](#)

4. (Digraphs)

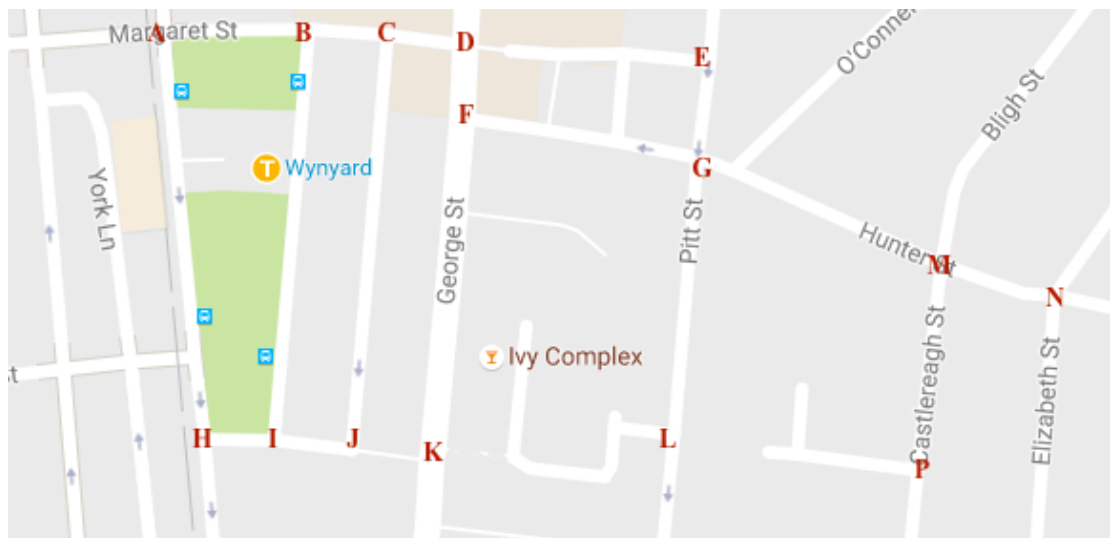
a. For each of the following graphs:



Show the concrete data structures if the graph was implemented via:

- adjacency matrix representation (assume full $V \times V$ matrix)
- adjacency list representation (if non-directional, include both (v, w) and (w, v))

b. Consider the following map of streets in the Sydney CBD:



Represent this as a directed graph, where intersections are vertices and the connecting streets are edges. Ensure that the directions on the edges correctly reflect any one-way streets (this is a driving map, not a walking map). You only need to make a graph which includes the intersections marked with red letters. Some things that don't show on the map: Castlereagh St is one-way heading south and Hunter St is one-way heading west.

For each of the following pairs of intersections, indicate whether there is a path from the first to the second. Show a path if there is one. If there is more than one path, show two different paths.

1. from intersection "D" on Margaret St to intersection "L" on Pitt St
2. from intersection "J" to the corner of Margaret St and York St (intersection "A")
3. from the intersection of Margaret St and York St ("A") to the intersection of Hunter St and

Castlereagh St ("M")

4. from intersection "M" on Castlereagh St to intersection "H" on York St

[\[show answer\]](#)

5. (Mock test)

Login to [COMP9024 on Moodle](#) between now and Sunday, 9 September, 12noon to do the "Mock Test" in preparation for the mid-term online test.

6. Challenge Exercise

None this week — review all the course contents so far & get ready for the mid-term online test.