(1) Cxy Wy = L Cxx Wx (2) Cyx Wx = L Cyy wy mith Cxx = 1/N XXT Cxx = 1/N YYT Cxy = 1/N XYT Cxx = 1/N XXT Wx = Xdx Wy = Ydyand XERdixN YERDEXN Lx, dy ERM (1) (3) 1/XYTYZY - L 1/XXXTX XX (3) Kydy = L Kxdx with Kx = XTX ER and Ky = YTY ERNXN (2) (3) XXXXXX = LAYYTYLY Kx Xx = L Kydy (4) 1, (3) Ky Ky Kx Xx = L Kx Xx IXX = LXX => KM (VXX L=1 You can pick any dx and compute the corresponding dy from dx: Ky Kx dx = dy

(2b) (1) on worksheet with
$$w_x = X_{dx}$$
 $w_y Y_{dy}$

Find $d_x \in \mathbb{R}^N$ $d_y \in \mathbb{R}^N$ maximizing $d_x \times X^T \times Y^T Y_{dy} = d_x^T A \cdot B d_y$

subject to $d_x \times X^T \times X^T \times d_x = d_x^T A^2 d_x$
 $d_y \times Y^T Y Y^T Y d_y = d_y \times B^2 d_y$

$$\mathcal{L} = d_x \times A \cdot B d_y - h_1 \left(d_x \times A^2 d_x \right) - h_2 \left(d_y \times B^2 d_y \right)$$

(2) $\frac{\partial L}{\partial dx} = A \cdot B d_y - h_1 A^2 d_x = 0$

(2)
$$\frac{JL}{Jax} = ABdy - L_1 A^2 L_x = 0$$

(3)
$$\frac{JL}{Jdy} = \alpha_{x}^{T}ABA = L_{z}B^{2}dy = BAdx - L_{z}B^{2}dy = Olsince}$$

$$d_{x}^{T}(3) - d_{x}^{T}(2): d_{y}^{T}BAdx - h_{z}d_{y}^{T}B^{2}dy - d_{x}^{T}ABdy - h_{z}d_{x}^{T}A^{2}dx = 0$$

$$(4) - L_{z} - h_{z} = 0 \Rightarrow L_{z} = h_{z} = L = P$$

(4) in (3): AB
$$dy = PA^3 dx$$

(4) in (3): BA $dx = PB^2 dy$

$$= \begin{bmatrix} O & AB \\ BA & O \end{bmatrix} \begin{bmatrix} dx \\ dy \end{bmatrix} = P\begin{bmatrix} A^2 & O \\ O & B^2 \end{bmatrix} \begin{bmatrix} dx \\ dy \end{bmatrix}$$

()
$$A \cdot B d_y = \rho A^2 d_x$$

 $X^T X Y^T Y d_y = \rho X^T X X^T X d_x$
 $d_X^T X^T X Y^T Y d_y = \rho d_X^T X^T X X^T X d_x$
 $w_X^T C_{XY} w_Y = \rho w_X^T C_{XX} w_X$
 $= \rho w_X^T C_{XY} w_Y$

Since we want to max find max (wx (xywy) we need to find the solution with largest P.

For XER and YER winth ob = 1 from restraint wy Tyy wy = 1 it follows (=) $\frac{\omega_{y^{2}} \|y\|_{2}^{2}}{\|y\|} = 1$ (=) $\omega_{y} = \frac{\sqrt{N}}{\|y\|} > 0$ Simply fy (1) from worksheet Find wx Eld maximizing wx Cxy = wx X xT subject to wXXXXWX = 1 = WXXXXTWX L= UxTXYT - L WXXXXTWX $\frac{\partial L}{\partial w_{x}} = XY^{T} - L XX^{T}w_{x} = 0$ (2) $XY^{T} = L XX^{T}w_{x}$ $\angle = 2$ $Y^T = \lambda X^T \omega_X = \lambda^2 Y^T = \lambda^T \omega_X$ (a) The LSR Objective can be rewritten: $\|x^{T}v-y\|^{2}=v^{T}XX^{T}v-2v^{T}Xy^{T}+hyu^{2}$ min (VTXXTU - ZVTXY) 10 = 88TV - 2XYT = 0 (=> XTV = 2YT (b) so with 6 1/2 Wx=00