

# The impact of internet stock message boards on cross-sectional returns of small-capitalization stocks

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# Contents

- Introduction
  - Background
  - Literatures
  - Motivation
  - Contribution
- Data
- Method
- Results
- Conclusions

# 1. Background

- Messages posted on internet stock message boards have become one of the many sources of information for investors and traders alike.
- Whether the activity of internet stock message boards quickly reflects itself into prices?
  - Tumarkin and Whitelaw (2001) show that message boards improve the speed of information being reflected in stock prices.
  - The Securities and Exchange Commission in the US has prosecuted people for the manipulation of stock prices via the misuse of internet messages.

# 1.Literatures

- Aggarwal and Wu (2006): study 142 manipulation cases prosecuted by the SEC from 1990 to 2001—  
—these cases are associated with higher stock prices, volatility and liquidity and occur more often in markets characterized by low levels of regulation and disclosure requirements.
- Message board-related study: Wysocki (1999) finds that short-sellers are highly active on message boards with preferences for stocks with the largest information asymmetry, weak fundamentals, and high risks.

# 1.Literatures

- The prices of small and large stocks reflect public information quickly:
- Tumarkin and Whitelaw (2001): message board activity is linked to contemporaneous stock returns but not to future stock returns.
- Das and Chen (2007): a rapid reflection of market activity in board messages, but no predictive power for subsequent returns.
- Antweiler and Frank (2004): negative significant returns on the following day after higher message posting volume, but of small economic impact.
- Das and Chen (2007): the aggregated high-tech sector sentiment predicts high-tech sector index returns, but not for individual stocks.

# 1.Motivations

- Q1: Whether the activity of message boards can quickly reflect itself into prices in highly regulated market places, especially for small growth stocks with low media coverage and analyst followings?
  - Yes
- Q2: Whether the effect of message board activity on small stocks is different to the effect on large stocks?
  - Yes

# 1.Contributions

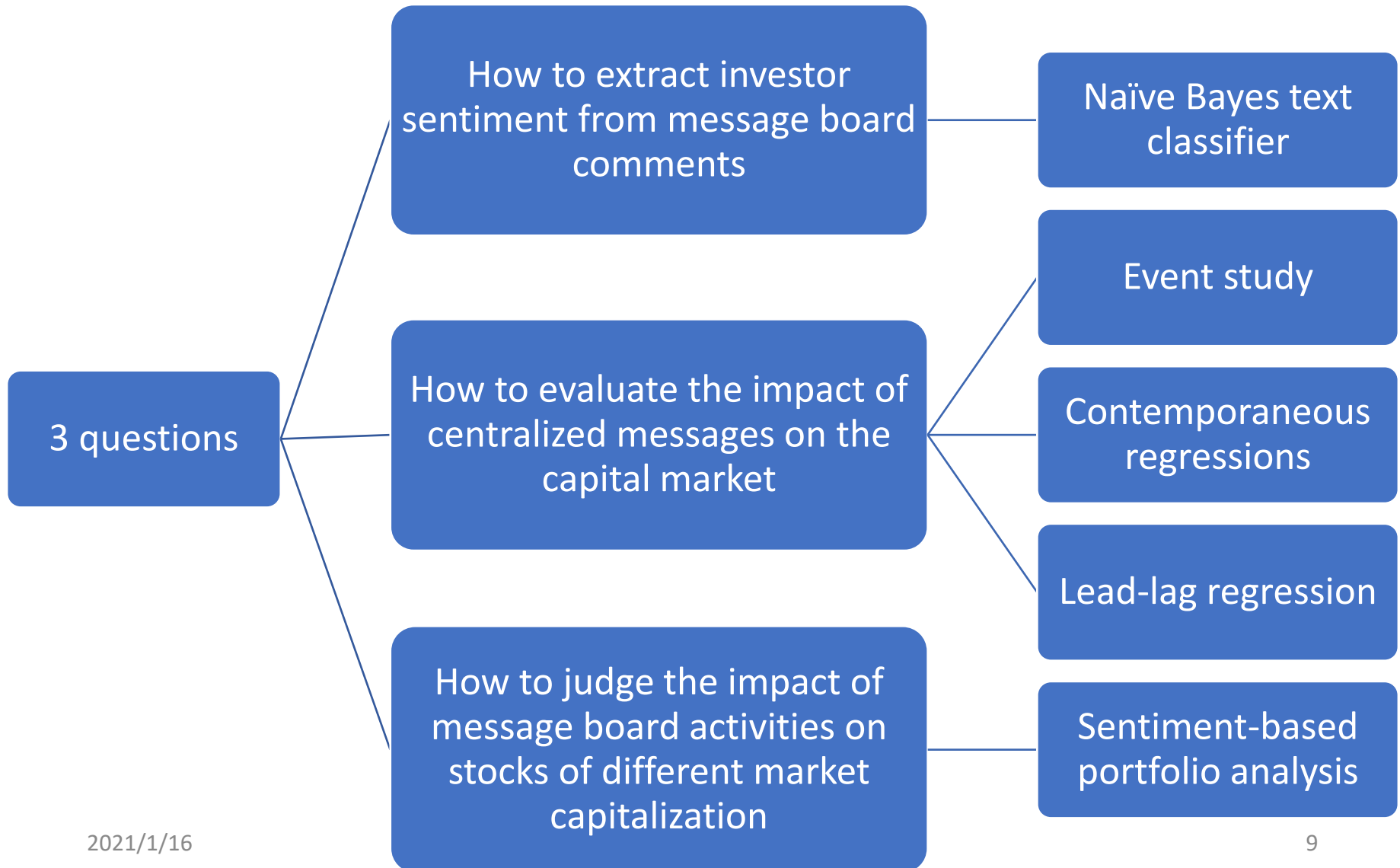
- The author conducts a comprehensive test of the Australian stock market
- The author analyzes the impact of message boards on stocks with different market capitalization for the first time

## 2.Data

- Time: January 2003 to December 2008
- Stock: 2,608,343 messages and 2142 firms listed on the ASX(discussed in HotCopper)
- Database: Securities Industry Research Centre of Asia–Pacific (SIRCA)
  - transaction: timestamp, ticker, price, and bid and ask quotes just prior to each transaction.
  - daily and monthly closing prices
- Market performance: the S&P All Ordinaries index(it includes almost all Australian ASX listed companies)



# 3.Method



### 3.Method\_Naïve Bayes text classifier

- $\{W_k\}(k=1,\dots,K)$ : a sequence of words where each word  $W_k$  is indexed by  $k$
- class  $C$  ; counter class  $\tilde{C}$
- $m_k; \widetilde{m}_k$ : the number of occurrences of word  $W_k$  in all messages of class  $C$  and  $\tilde{C}$
- $n; \tilde{n}$ : the total number of words in all messages of class  $C$  and  $\tilde{C}$

# 3.Method\_Naïve Bayes text classifier

- the conditional probabilities of words found in messages from the training set:

- $P(W_k|C) = (1 + m_k)/(1 + n)$

- $P(W_k|\tilde{C}) = (1 + \tilde{m}_k)/(1 + \tilde{n})$

- posterior probability:

- $$P(C|W_k) = \frac{P(W_k|C)P(C)}{P(W_k)} = \frac{P(W_k|C)P(C)}{P(W_k|C)P(C) + P(W_k|\tilde{C})P(\tilde{C})}$$

- Log: 
$$\frac{P(C|W_k)}{P(\tilde{C}|W_k)} = \frac{P(C)}{P(\tilde{C})} \times \frac{P(W_k|C)}{P(W_k|\tilde{C})}$$

- $$P(C|W_K) = P(C) \exp[\sum_{k=1}^K \ln(\frac{P(W_k|C)}{P(W_k|\tilde{C})})]$$

|          | Message | Words                          | Class             |
|----------|---------|--------------------------------|-------------------|
| Training | 1       | Buy BHP. Looks like a buy      | Buy ( <i>B</i> )  |
|          | 2       | Buy ANZ. Hot stock             | Buy ( <i>B</i> )  |
|          | 3       | Sell XYZ now. Certainly a sell | Sell ( <i>S</i> ) |
| Test     | 4       | Buy buy buy CBA                | ?                 |

Priors of the probability:

$$P(B) = 2/3$$

$$P(C) = 1/3$$

Conditional probability:

$$P(\text{Buy}|B) = (1 + 3)/(1 + 10) = 4/11$$

$$P(\text{Buy}|B) = P(\text{Looks}|B) = P(\text{like}|B) = P(a|B) = P(\text{ANZ}|B) = P(\text{Hot}|B) \\ = P(\text{stock}|B) = (1 + 1)/(1 + 10) = 2/11$$

$$P(\text{CBA}|B) = (1 + 0)/(1 + 10) = 1/11$$

$$P(\text{Sell}|S) = (1 + 2)/(1 + 6) = 3/7$$

$$P(\text{XYZ}|S) = P(\text{now}|S) = P(\text{Certainly}|S) = P(a|S) = (1 + 1)/(1 + 6) = 2/7$$

$$P(\text{Buy}|S) = P(\text{CBA}|S) = (1 + 0)/(1 + 6) = 1/7$$

|          | Message | Words                          | Class             |
|----------|---------|--------------------------------|-------------------|
| Training | 1       | Buy BHP. Looks like a buy      | Buy ( <i>B</i> )  |
|          | 2       | Buy ANZ. Hot stock             | Buy ( <i>B</i> )  |
|          | 3       | Sell XYZ now. Certainly a sell | Sell ( <i>S</i> ) |
| Test     | 4       | Buy buy buy CBA                | ?                 |

$P(B|message4)$

$$\begin{aligned}
 &= P(B) \cdot \exp\left\{3 \cdot \ln\left[\frac{P(\text{Buy}|B)}{P(\text{Buy}|S)}\right] + \ln\left[\frac{P(\text{CBA}|B)}{P(\text{CBA}|S)}\right]\right\} \\
 &= \frac{2}{3} \cdot \exp\left\{3 \cdot \ln\left[\frac{(4/11)}{(1/7)}\right] + \ln\left[\frac{(1/11)}{(1/7)}\right]\right\} \\
 &= 7.00
 \end{aligned}$$

$P(S|message4)$

$$\begin{aligned}
 &= P(S) \cdot \exp\left\{3 \cdot \ln\left[\frac{P(\text{Buy}|S)}{P(\text{Buy}|B)}\right] + \ln\left[\frac{P(\text{CBA}|S)}{P(\text{CBA}|B)}\right]\right\} \\
 &= \frac{1}{3} \cdot \exp\left\{3 \cdot \ln\left[\frac{(1/7)}{(4/11)}\right] + \ln\left[\frac{(1/7)}{(1/11)}\right]\right\} \\
 &= 0.03
 \end{aligned}$$

Result: Buy

### 3.Method\_Naïve Bayes text classifier

- Investors attitude: {buy, hold, sell}
- $M_{i,t}^C = \sum_{j \rightarrow D(T)} x_{i,j}^C$  : the sum of messages of class C for stock  $i$  in time interval  $D(t)$
- $x_{i,j}^C$ : a dummy variable which is one when message  $j$  for stock  $i$  is of type C, and zero otherwise
- $M_{i,t} = M_{i,t}^{BUY} + M_{i,t}^{SELL}$
- The degree of investor optimism:
- $Bullishness_{i,t} = \frac{M_{i,t}^{BUY} - M_{i,t}^{SELL}}{M_{i,t}} \cdot \ln(1 + M_{i,t})$

### 3.Method\_Naïve Bayes text classifier

- The disagreement index:

- $$A_{i,t} = 1 - \sqrt{1 - \left( \frac{M_{i,t}^{BUY} - M_{i,t}^{SELL}}{M_{i,t}} \right)^2}$$

- Rank stocks into: rank 1– 100 (Large cap), rank 101– 299(Mid cap), and rank 300–2000 (Small cap)

|              | <i>Bullishness</i> |
|--------------|--------------------|
| Small stocks | 0.03               |
| Large stocks | -0.02              |

# 3.Method\_Event Study

- **Event day:** comparing the standard deviation of the previous five days' numbers of messages with the actual number of messages posted on the event day. When the message number exceeded two times the standard deviation of the previous five days, with a minimum of ten message postings, an event took place.

——Tumarkin and Whitelaw (2001)



# 3.Method\_Event Study

- Controlling for public information
- Clean only ASX company announcements: All observations within a range of three days of ASX price-sensitive company announcements were removed in order to focus on private information disseminated via *HotCopper*.
- Signal G, also called the Australian Company Announcements (ACA) database, flags whether ASX company announcements are price sensitive.

# 3.Method\_Event Study

- Heavily discussed large stocks in the event study sample show strong financial performances (e.g. positive ROE, EBIT margin, or EPS).
- Target small stocks of online investors exhibit weak financial performances.

Financial aspects of event study sample.

| Financial aspect | Stock capitalization | Mean     | Median | Std. dev. | Min.        | Max.    | N   |
|------------------|----------------------|----------|--------|-----------|-------------|---------|-----|
| Market-to-book   | Large                | 4.85     | 1.11   | 16.12     | 0.21        | 93.69   | 33  |
|                  | Small                | 2.93     | 0.57   | 21.58     | 0.00        | 319.23  | 308 |
| ROE              | Large                | 0.15     | 0.15   | 0.12      | -0.27       | 0.44    | 38  |
|                  | Small                | -0.27    | -0.11  | 1.03      | -11.35      | 9.18    | 411 |
| EBIT margin      | Large                | 11.58    | 0.17   | 60.39     | -0.67       | 319.74  | 28  |
|                  | Small                | -1565.44 | -1.78  | 16,749.74 | -269,433.27 | 1435.71 | 286 |
| P/E ratio        | Large                | 22.07    | 16.54  | 35.22     | -7.47       | 202.82  | 33  |
|                  | Small                | -13.76   | -6.49  | 60.91     | -801.89     | 200.00  | 308 |
| EPS              | Large                | 0.55     | 0.49   | 1.16      | -4.00       | 2.79    | 38  |
|                  | Small                | -0.03    | -0.01  | 0.23      | -3.38       | 0.60    | 405 |

# 3.Method\_Event Study

- MacKinlay (1997):
- Abnormal returns and volumes were computed in order to examine the impact of message board activity on financial market reactions
- Event period:  $t-5 \sim t+5$
- For small & large stocks

| <i>Day t</i>                    |               | t-5   | t-4  | t-3   | t-2   | t-1   | t0   | t+1  | t+2   | t+3  | t+4   | t+5   |
|---------------------------------|---------------|-------|------|-------|-------|-------|------|------|-------|------|-------|-------|
| <i>Abnormal Average Returns</i> | <i>Small</i>  | 0.4%  | 0.1% | 0.0%  | 0.3%  | 0.5%  | 3.6% | 0.2% | -0.2% | 0.2% | 0.1%  | 0.2%  |
|                                 |               | ***   |      |       | **    | ***   | ***  |      |       |      |       |       |
|                                 | <i>Mid</i>    | -0.2% | 0.1% | -0.1% | -0.2% | -0.3% | 0.8% | 0.3% | 0.1%  | 0.2% | -0.2% | 0.0%  |
|                                 |               |       |      |       |       | *     | **   |      |       |      |       |       |
|                                 | <i>Large</i>  | -0.1% | 0.0% | 0.1%  | 0.3%  | 0.0%  | 0.1% | 0.2% | 0.1%  | 0.1% | 0.2%  | -0.1% |
|                                 |               |       |      |       |       |       |      | *    |       |      | *     |       |
|                                 | $\Delta S, L$ | 0.5%  | 0.1% | 0.0%  | -0.1% | 0.5%  | 3.4% | 0.0% | -0.3% | 0.1% | -0.2% | 0.2%  |
|                                 |               |       |      |       |       |       | ***  |      |       |      |       |       |

- Average Abnormal Returns (AARs) are only significantly high for small stocks
- The AARs are significant two days prior the event day and on day  $t + 1$
- Future returns are not predicted by high posting activity
- Price sensitive information quickly reflects itself in the prices of Australian large capitalization stocks

| Day $t$                        |              | t-5  | t-4 | t-3 | t-2 | t-1 | t0   | t+1  | t+2  | t+3 | t+4 | t+5 |
|--------------------------------|--------------|------|-----|-----|-----|-----|------|------|------|-----|-----|-----|
| <b>Abnormal Average Volume</b> | <i>Small</i> | 122% | 80% | 50% | 46% | 56% | 275% | 158% | 103% | 81% | 76% | 70% |
|                                |              | ***  | *** | *** | *** | *** | ***  | ***  | ***  | *** | *** | *** |
|                                | <i>Mid</i>   | 2%   | 3%  | -8% | -3% | 13% | 89%  | 42%  | 18%  | 9%  | 16% | 11% |
|                                |              |      |     |     |     |     | ***  | ***  | **   |     |     |     |
|                                | <i>Large</i> | 1%   | 12% | 5%  | 0%  | 0%  | 35%  | 17%  | 7%   | 5%  | 1%  | 2%  |
|                                |              |      |     |     |     |     | ***  | **   |      |     |     |     |
| $\Delta S, L$                  |              | 120% | 67% | 44% | 46% | 56% | 240% | 141% | 95%  | 75% | 75% | 68% |
|                                |              |      |     | *   | *   | **  | ***  | ***  | ***  | *** | **  | *** |

- High posting activity particularly impacts on AAVs for small stocks compared to large stocks on the event day
- For small stocks, trading volume is significantly higher during the whole event period
- Message board activity might sustainably increase trading volume, especially for small stocks.

# 3.Method\_Contemporaneous regressions

- Former studies did not assess the interdependence between message board postings or sentiment and size-dependent stock portfolios.
- Antweiler and Frank (2004)
- $R_{i,t} = \alpha + \beta_1 \text{LogMessages}_{i,t} + \beta_2 \text{Bullishness}_t + \beta_3 \text{Agreement}_{i,t} + \beta_4 \text{MarketRet}_t + \beta_5 R_{i,t-1}$
- $\text{Volatility}_{i,t} = \alpha + \beta_1 \text{LogMessages}_{i,t} + \beta_2 \text{AbsSentiment}_{i,t} + \beta_3 \text{Agreement}_{i,t} + \beta_4 \text{Market}_t + \beta_5 \text{TradeVolume}_{i,t} + \beta_6 \text{Volatility}_{i,t-1}$

### 3.Method\_Contemporaneous regressions

- $BAS_{i,t} = \alpha + \beta_1 LogMessages_{i,t} + \beta_2 AbsSentiment_{i,t} + \beta_3 Agreement_{i,t} + \beta_4 Market_t + \beta_5 BAS_{i,t-1}$
- $TradeSize_{i,t} = \alpha + \beta_1 LogMessages_{i,t} + \beta_2 AbsSentiment_{i,t} + \beta_3 Agreement_{i,t} + \beta_4 Market_t + \beta_5 TradeSize_{i,t-1}$
- $TradeVolume_{i,t} = \alpha + \beta_1 LogMessages_{i,t} + \beta_2 AbsSentiment_{i,t} + \beta_3 Agreement_{i,t} + \beta_4 Market_t + \beta_5 TradeVolume_{i,t-1}$

| Dependent variable                | Return <sub>t</sub> |        |           |        |           |        | Volatility <sub>t</sub> |        |          |        |          |        | BAS <sub>t</sub> |        |          |        |          |        |
|-----------------------------------|---------------------|--------|-----------|--------|-----------|--------|-------------------------|--------|----------|--------|----------|--------|------------------|--------|----------|--------|----------|--------|
|                                   | Small               |        | Medium    |        | Large     |        | Small                   |        | Medium   |        | Large    |        | Small            |        | Medium   |        | Large    |        |
|                                   | Est.                | t-Stat | Est.      | t-Stat | Est.      | t-Stat | Est.                    | t-Stat | Est.     | t-Stat | Est.     | t-Stat | Est.             | t-Stat | Est.     | t-Stat | Est.     | t-Stat |
| <i>Msg. board variables</i>       |                     |        |           |        |           |        |                         |        |          |        |          |        |                  |        |          |        |          |        |
| LogMessages <sub>t</sub>          | 0.011***            | 23.64  | 0.004***  | 8.26   | 0.001***  | 3.73   | 0.101***                | 7.58   | 0.109*** | 6.79   | 0.024**  | 2.85   | 0.000            | 0.13   | 0.000    | -1.11  | 0.000    | 0.23   |
| Bullishness <sub>t</sub>          | 0.008***            | 22.26  | 0.005***  | 10.99  | 0.002***  | 6.33   |                         |        |          |        |          |        |                  |        |          |        |          |        |
| AbsSentiment <sub>t</sub>         |                     |        |           |        |           |        | 0.003**                 | 2.68   | 0.006*   | 2.53   | 0.003*** | 3.81   | 0.000            | -0.37  | 0.000    | 1.18   | 0.000    | 0.81   |
| Agreement <sub>t</sub>            | 0.001               | 1.29   | 0.001     | 1.63   | 0.001**   | 2.96   | 0.039***                | 4.03   | -0.012   | -1.15  | 0.013*   | 2.04   | 0.000*           | -1.97  | 0.000*** | -3.51  | -0.001   | -1.45  |
| <i>Control variables</i>          |                     |        |           |        |           |        |                         |        |          |        |          |        |                  |        |          |        |          |        |
| Market return <sub>t</sub>        | 0.766***            | 10.80  | 0.795***  | 25.03  | 0.909***  | 32.98  |                         |        |          |        |          |        |                  |        |          |        |          |        |
| Market <sub>t</sub>               |                     |        |           |        |           |        | -0.138***               | -4.77  | -0.062** | -3.07  | -0.001   | -0.1   | 0.004***         | 3.89   | 0.003    | 1.47   | 0.025    | 1.37   |
| Log trade volume <sub>t</sub>     |                     |        |           |        |           |        | 0.273***                | 54.11  | 0.068*** | 19.22  | 0.074*** | 14.99  |                  |        |          |        |          |        |
| <i>Lagged dependent variables</i> |                     |        |           |        |           |        |                         |        |          |        |          |        |                  |        |          |        |          |        |
| Return <sub>t-1</sub>             | -0.135***           | -28.24 | -0.037*** | -5.26  | -0.043*** | -4.72  |                         |        |          |        |          |        |                  |        |          |        |          |        |
| Volatility <sub>t-1</sub>         |                     |        |           |        |           |        | 0.129***                | 27.15  | 0.244*** | 22.80  | 0.223*** | 12.57  |                  |        |          |        |          |        |
| BAS <sub>t-1</sub>                |                     |        |           |        |           |        |                         |        |          |        |          |        | 0.469***         | 9.42   | 0.569*** | 9.64   | 0.545*** | 6.97   |
| R-square                          | 0.05                |        | 0.10      |        | 0.19      |        | 0.19                    |        | 0.26     |        | 0.24     |        | 0.47             |        | 0.61     |        | 0.63     |        |
| Number of observations            | 849,675             |        | 209,692   |        | 103,158   |        | 849,675                 |        | 209,692  |        | 103,158  |        | 849,675          |        | 209,692  |        | 103,158  |        |

## • Returns:

- Contemporaneous raw returns are, in particular, higher for small stocks with more message postings and higher sentiment relative to large stocks.
- Small stocks are more affected by message board activity

## • Volatility:

- the volatility is particularly high for small stocks with higher posting activity and high trading volumes relative to large stocks.

## • BAS:

- internet stock message boards help to quicken the speed of information being reflected in the prices of small stocks.



| Dependent variable<br>Market capitalization | Log trade small <sub>t</sub> |        |          |        |          |        | Log trade large <sub>t</sub> |        |          |        |          |        | Log trade volume <sub>t</sub> |        |          |        |          |        |
|---|------------------------------|--------|----------|--------|----------|--------|------------------------------|--------|----------|--------|----------|--------|-------------------------------|--------|----------|--------|----------|--------|
|   | Small                        |        | Medium   |        | Large    |        | Small                        |        | Medium   |        | Large    |        | Small                         |        | Medium   |        | Large    |        |
|   | Est.                         | t-Stat | Est.     | t-Stat | Est.     | t-Stat | Est.                         | t-Stat | Est.     | t-Stat | Est.     | t-Stat | Est.                          | t-Stat | Est.     | t-Stat | Est.     | t-Stat |
| <i>Msg. board variables</i>                 |                              |        |          |        |          |        |                              |        |          |        |          |        |                               |        |          |        |          |        |
| LogMessages <sub>t</sub>                    | 0.302***                     | 35.18  | 0.150*** | 12.69  | 0.058*** | 5.70   | 0.000                        | 0.95   | 0.006**  | 2.56   | 0.047*** | 3.27   | 0.459***                      | 32.98  | 0.255*** | 13.62  | 0.122*** | 8.64   |
| Bullishness <sub>t</sub>                    |                              |        |          |        |          |        |                              |        |          |        |          |        |                               |        |          |        |          |        |
| AbsSentiment <sub>t</sub>                   | 0.003***                     | 4.95   | 0.002*   | 2.01   | 0.001    | 1.70   | 0.000                        | -0.25  | 0.000    | -1.68  | 0.001    | 0.44   | 0.002**                       | 2.17   | 0.002    | 1.20   | 0.001    | 1.34   |
| Agreement <sub>t</sub>                      | 0.021***                     | 4.09   | 0.019*   | 2.18   | 0.009    | 1.14   | 0.000                        | 0.31   | 0.001    | 0.48   | -0.014   | -1.08  | 0.083***                      | 9.12   | 0.059*** | 4.58   | 0.035**  | 2.66   |
| <i>Control variables</i>                    |                              |        |          |        |          |        |                              |        |          |        |          |        |                               |        |          |        |          |        |
| Market <sub>t</sub>                         | 0.265***                     | 10.53  | 1.068*** | 16.78  | 0.832*** | 12.11  | 0.002***                     | 9.43   | 0.071*** | 9.85   | 0.459*** | 12.60  | 0.343***                      | 7.37   | 0.947*** | 11.18  | 0.685*** | 11.55  |
| <i>Lagged dependent variables</i>           |                              |        |          |        |          |        |                              |        |          |        |          |        |                               |        |          |        |          |        |
| Log trade small <sub>t-1</sub>              | 0.541***                     | 98.96  | 0.646*** | 51.18  | 0.672*** | 27.31  |                              |        |          |        |          |        |                               |        |          |        |          |        |
| Log trade large <sub>t-1</sub>              |                              |        |          |        |          |        | 0.101***                     | 6.52   | 0.219*** | 11.43  | 0.356*** | 15.93  |                               |        |          |        |          |        |
| Log trade volume <sub>t-1</sub>             |                              |        |          |        |          |        |                              |        |          |        |          |        | 0.373***                      | 53.89  | 0.464*** | 29.15  | 0.492*** | 22.17  |
| R-square                                    | 0.64                         |        | 0.85     |        | 0.92     |        | 0.03                         |        | 0.14     |        | 0.43     |        | 0.56                          |        | 0.78     |        | 0.90     |        |
| Number of observations                      | 849,675                      |        | 209,692  |        | 103,158  |        | 849,675                      |        | 209,692  |        | 103,158  |        | 849,675                       |        | 209,692  |        | 103,158  |        |

- Trade small/large:
  - message board activity particularly influences individual investor trades with low volumes. Messages that refer to large stocks strongly correlate with the number of large trades, suggesting institutional investor activity on message boards.
- Trade Volume:
  - the trading volume is especially sensitive to the number of messages for small stocks.

# 3.Method\_Lead-Lag regressions

1 day lead-lag regression: return, volatility and bid-ask spread by market capitalization.

| Dependent variable                | Return <sub>t+1</sub> |        |           |        |           |        | Volatility <sub>t+1</sub> |        |           |        |           |        | BAS <sub>t+1</sub> |        |          |        |          |        |
|-----------------------------------|-----------------------|--------|-----------|--------|-----------|--------|---------------------------|--------|-----------|--------|-----------|--------|--------------------|--------|----------|--------|----------|--------|
|                                   | Small                 |        | Medium    |        | Large     |        | Small                     |        | Medium    |        | Large     |        | Small              |        | Medium   |        | Large    |        |
|                                   | Est.                  | t-Stat | Est.      | t-Stat | Est.      | t-Stat | Est.                      | t-Stat | Est.      | t-Stat | Est.      | t-Stat | Est.               | t-Stat | Est.     | t-Stat | Est.     | t-Stat |
| <i>Msg. board variables</i>       |                       |        |           |        |           |        |                           |        |           |        |           |        |                    |        |          |        |          |        |
| LogMessages <sub>t</sub>          | 0.002***              | 7.87   | 0.001***  | 3.50   | 0.000     | 0.96   | -0.026*                   | -2.42  | 0.017     | 1.37   | -0.018*** | -3.62  | -0.000**           | -3.04  | 0.000*** | -3.18  | 0.000    | 0.15   |
| Bullishness <sub>t</sub>          | 0.001***              | 5.71   | 0.000     | 1.01   | 0.000     | -0.63  |                           |        |           |        |           |        |                    |        |          |        |          |        |
| AbsSentiment <sub>t</sub>         |                       |        |           |        |           |        | 0.000                     | 0.09   | 0.001     | 0.55   | 0.002**   | 3.15   | 0.000*             | 2.09   | 0.000**  | 2.50   | 0.000    | 0.55   |
| Agreement <sub>t</sub>            | 0.000                 | 1.44   | 0.000     | 1.01   | 0.000*    | 1.95   | 0.010                     | 1.27   | -0.011    | -1.50  | 0.004     | 0.95   | 0.000***           | -3.36  | 0.000**  | -2.75  | -0.001   | -0.92  |
| <i>Control variables</i>          |                       |        |           |        |           |        |                           |        |           |        |           |        |                    |        |          |        |          |        |
| Market return <sub>t+1</sub>      | 0.790***              | 11.04  | 0.799***  | 24.99  | 0.912***  | 32.92  |                           |        |           |        |           |        |                    |        |          |        |          |        |
| Market <sub>t+1</sub>             |                       |        |           |        |           |        | -0.106***                 | -3.7   | -0.066*** | -3.24  | -0.005    | -0.34  | 0.004***           | 3.87   | 0.003    | 1.41   | 0.022    | 1.40   |
| Log trade volume <sub>t</sub>     |                       |        |           |        |           |        | 0.280***                  | 56.72  | 0.073***  | 19.33  | 0.077***  | 14.93  |                    |        |          |        |          |        |
| <i>Lagged dependent variables</i> |                       |        |           |        |           |        |                           |        |           |        |           |        |                    |        |          |        |          |        |
| Return <sub>t</sub>               | -0.133***             | -26.27 | -0.037*** | -5.09  | -0.043*** | -4.64  |                           |        |           |        |           |        |                    |        |          |        |          |        |
| Volatility <sub>t</sub>           |                       |        |           |        |           |        | 0.134***                  | 27.33  | 0.255***  | 23.24  | 0.223***  | 11.69  |                    |        |          |        |          |        |
| BAS <sub>t</sub>                  |                       |        |           |        |           |        |                           |        |           |        |           |        | 0.486***           | 9.07   | 0.522*** | 16.32  | 0.579*** | 7.76   |
| R-square                          | 0.04                  |        | 0.09      |        | 0.19      |        | 0.19                      |        | 0.25      |        | 0.23      |        | 0.44               |        | 0.60     |        | 0.63     |        |
| Number of observations            | 817,213               |        | 207,648   |        | 102,292   |        | 817,213                   |        | 207,648   |        | 102,292   |        | 817,213            |        | 207,648  |        | 102,292  |        |

1 day lead-lag regression: small and large trades and trade volume by market capitalization.

| Dependent variable                | Log trade small <sub>t+1</sub> |        |          |        |          |        | Log trade large <sub>t+1</sub> |        |          |        |          |        | Log trade volume <sub>t+1</sub> |        |          |        |          |        |
|-----------------------------------|--------------------------------|--------|----------|--------|----------|--------|--------------------------------|--------|----------|--------|----------|--------|---------------------------------|--------|----------|--------|----------|--------|
|                                   | Small                          |        | Medium   |        | Large    |        | Small                          |        | Medium   |        | Large    |        | Small                           |        | Medium   |        | Large    |        |
|                                   | Est.                           | t-Stat | Est.     | t-Stat | Est.     | t-Stat | Est.                           | t-Stat | Est.     | t-Stat | Est.     | t-Stat | Est.                            | t-Stat | Est.     | t-Stat | Est.     | t-Stat |
| <i>Msg. board variables</i>       |                                |        |          |        |          |        |                                |        |          |        |          |        |                                 |        |          |        |          |        |
| LogMessages <sub>t</sub>          | 0.139***                       | 20.87  | 0.038*** | 4.06   | -0.007   | -0.91  | 0.000                          | -0.80  | 0.002    | 1.26   | 0.023    | 1.90   | 0.255***                        | 22.73  | 0.113*** | 6.99   | 0.035*** | 3.66   |
| Bullishness <sub>t</sub>          |                                |        |          |        |          |        |                                |        |          |        |          |        |                                 |        |          |        |          |        |
| AbsSentiment <sub>t</sub>         | 0.003***                       | 4.80   | 0.000    | -0.64  | 0.001*   | 2.31   | 0.000                          | -0.31  | 0.000    | -0.2   | 0.000    | 0.40   | 0.004***                        | 4.37   | 0.000    | 0.02   | 0.001    | 1.35   |
| Agreement <sub>t</sub>            | 0.000                          | 0.00   | -0.003   | -0.38  | 0.003    | 0.42   | 0.000                          | -0.38  | 0.004*   | 2.30   | -0.011   | -1.01  | 0.026***                        | 3.51   | 0.032**  | 2.85   | 0.008    | 0.92   |
| <i>Control variables</i>          |                                |        |          |        |          |        |                                |        |          |        |          |        |                                 |        |          |        |          |        |
| Market <sub>t+1</sub>             | 0.297***                       | 11.63  | 1.065*** | 16.82  | 0.817*** | 11.80  | 0.003***                       | 9.42   | 0.071*** | 9.85   | 0.462*** | 12.68  | 0.391***                        | 8.29   | 0.952*** | 11.25  | 0.676*** | 11.18  |
| <i>Lagged dependent variables</i> |                                |        |          |        |          |        |                                |        |          |        |          |        |                                 |        |          |        |          |        |
| Log trade small <sub>t</sub>      | 0.560***                       | 99.60  | 0.651*** | 51.73  | 0.678*** | 27.31  |                                |        |          |        |          |        |                                 |        |          |        |          |        |
| Log trade large <sub>t</sub>      |                                |        |          |        |          |        | 0.100***                       | 6.40   | 0.220*** | 11.26  | 0.355*** | 15.73  |                                 |        |          |        |          |        |
| Log trade volume <sub>t</sub>     |                                |        |          |        |          |        |                                |        |          |        |          |        | 0.382***                        | 53.84  | 0.468*** | 28.96  | 0.499*** | 21.77  |
| R-square                          | 0.63                           |        | 0.85     |        | 0.92     |        | 0.03                           |        | 0.14     |        | 0.43     |        | 0.56                            |        | 0.78     |        | 0.90     |        |
| Number of observations            | 817,213                        |        | 207,648  |        | 102,292  |        | 817,213                        |        | 207,648  |        | 102,292  |        | 817,213                         |        | 207,648  |        | 102,292  |        |

### 3.Method\_Lead-Lag regressions

- Returns cannot be predicted in subsequent days after message posting activity.
- However, financial trading variables, such as the trade volume and trade sizes, significantly correlate with the corresponding number of messages.

# 3.Method\_Sentiment-based portfolio analysis

## **Short-term sentiment-based portfolio returns**

- All stocks belongs to different quartiles based on the average daily bullishness expressed in corresponding board messages.
- The first quartile represents the ‘Bullish’ portfolio
- The fourth quartile describes the ‘Bearish’ portfolio.
- Stocks are held for one and two days with reported cumulative returns (CRs)

| Portfolio   | Bullishness               | $t = 0$            | $t + 1$            | $t + 2$            |
|---|---------------------------|--------------------|--------------------|--------------------|
| <i>Panel B: cumulative returns for large cap stocks</i> |                           |                    |                    |                    |
| Bullish   | 0.803                     | 0.30%***<br>(8.48) | 0.34%***<br>(7.17) | 0.33%***<br>(4.42) |
| 2. Quartile   | 0.070                     | 0.30%***<br>(7.11) | 0.36%***<br>(6.78) | 0.40%***<br>(4.77) |
| 3. Quartile   | -0.519                    | 0.13%***<br>(3.59) | 0.21%***<br>(4.53) | 0.26%***<br>(3.77) |
| Bearish   | -1.162                    | 0.01%<br>(0.18)    | 0.06%<br>(0.82)    | 0.08%<br>(0.80)    |
|   | $\Delta$ Bullish, Bearish | 0.29%***<br>(4.83) | 0.29%***<br>(3.55) | 0.25%*<br>(2.01)   |

- The “Bullish” gets higher returns
- The spread is smaller than that of “small cap stocks”

| Portfolio   | Bullishness               | $t = 0$             | $t + 1$             | $t + 2$             |
|---|---------------------------|---------------------|---------------------|---------------------|
| <i>Panel D: cumulative returns for small cap stocks</i> |                           |                     |                     |                     |
| Bullish   | 0.976                     | 1.56%***<br>(48.24) | 1.75%***<br>(38.86) | 1.64%***<br>(24.63) |
| 2. Quartile   | 0.448                     | 1.38%***<br>(25.42) | 1.52%***<br>(21.31) | 1.38%***<br>(13.21) |
| 3. Quartile   | −0.279                    | 1.11%***<br>(26.92) | 1.20%***<br>(22.26) | 1.08%***<br>(13.48) |
| Bearish   | −0.985                    | 0.39%***<br>(7.49)  | 0.46%***<br>(6.88)  | 0.34%***<br>(3.48)  |
|   | $\Delta$ Bullish, Bearish | 1.17%***<br>(19.97) | 1.29%***<br>(16.24) | 1.30%***<br>(11.24) |

- We do not find negative CRs for bearish small stocks—— individual investors hold relatively few stocks in their portfolio and only sell stocks they own, due to resource constraints.
- Buy-trades are easier to realize for individual investors, who cannot devote as much time and resources to search for buy and sell opportunities as institutional investors.

# 3.Method\_Sentiment-based portfolio analysis

## **Long-term sentiment-based portfolio returns**

- Whether message boards contain value-relevant information?
  - constructed small and large stock portfolios
  - assigned each stock into quartiles based on the monthly average bullishness for the formation period  $J = 0$  (same month)
  - the holding periods  $K = 0, 1-3$ , and  $4-6$  months
  - CAPM\FF3\C4

| Holding period $K = 0$ |                    |                    |                     |                     |             | Holding period $K = 1-3$ |                     |                     |                     |                     |             | Holding period $K = 4-6$ |                    |                     |                     |                     |             |
|------------------------|--------------------|--------------------|---------------------|---------------------|-------------|--------------------------|---------------------|---------------------|---------------------|---------------------|-------------|--------------------------|--------------------|---------------------|---------------------|---------------------|-------------|
|                        | Bullish            | 2Q                 | 3Q                  | Bearish             | $\Delta BB$ |                          | Bullish             | 2Q                  | 3Q                  | Bearish             | $\Delta BB$ |                          | Bullish            | 2Q                  | 3Q                  | Bearish             | $\Delta BB$ |
| Carhart four factor    |                    |                    |                     |                     |             | Carhart four factor      |                     |                     |                     |                     |             | Carhart four factor      |                    |                     |                     |                     |             |
| $\alpha$               | 0.008<br>(1.72)    | 0.004<br>(1.03)    | -0.004<br>(-1.64)   | 0.001<br>(0.43)     | 0.007       | $\alpha$                 | -0.001<br>(-0.48)   | -0.001<br>(-0.29)   | 0.000<br>(-0.12)    | 0.002<br>(0.82)     | -0.003      | $\alpha$                 | -0.007<br>(-1.48)  | 0.000<br>(-0.00)    | 0.000<br>(0.07)     | 0.003<br>(0.93)     | -0.009      |
| $\beta_{rm}$           | 1.329***<br>(8.20) | 1.066***<br>(7.95) | 1.181***<br>(14.49) | 1.112***<br>(11.10) | 0.217       | $\beta_{rm}$             | 1.419***<br>(12.63) | 1.153***<br>(11.78) | 1.182***<br>(13.16) | 1.133***<br>(20.09) | 0.286       | $\beta_{rm}$             | 1.742***<br>(9.96) | 1.297***<br>(14.47) | 1.029***<br>(12.43) | 1.096***<br>(18.85) | 0.646       |
| $\beta_{HML}$          | -0.111<br>(-0.53)  | 0.191<br>(1.25)    | 0.206<br>(1.67)     | -0.209<br>(-1.52)   | 0.098       | $\beta_{HML}$            | 0.227<br>(1.77)     | -0.072<br>(-0.61)   | 0.011<br>(0.12)     | -0.043<br>(-0.53)   | 0.270       | $\beta_{HML}$            | 0.113<br>(0.65)    | -0.076<br>(-0.52)   | 0.070<br>(0.82)     | -0.110<br>(-1.21)   | 0.223       |
| $\beta_{SMB}$          | -0.029<br>(-0.21)  | 0.091<br>(0.74)    | 0.033<br>(0.50)     | -0.039<br>(-0.54)   | 0.010       | $\beta_{SMB}$            | 0.092<br>(1.26)     | -0.079<br>(-1.13)   | -0.038<br>(-0.73)   | 0.030<br>(0.65)     | 0.062       | $\beta_{SMB}$            | 0.047<br>(0.59)    | -0.262**<br>(-3.18) | -0.052<br>(-1.00)   | -0.098<br>(-1.19)   | 0.145       |
| $\beta_{MOM}$          | 0.262<br>(1.52)    | 0.150<br>(0.93)    | -0.145<br>(-1.79)   | -0.145<br>(-1.52)   | 0.407       | $\beta_{MOM}$            | 0.038<br>(0.36)     | 0.071<br>(0.72)     | 0.058<br>(0.81)     | -0.106<br>(-1.87)   | 0.145       | $\beta_{MOM}$            | -0.160<br>(-1.14)  | -0.243*<br>(-2.10)  | 0.069<br>(1.00)     | 0.015<br>(0.16)     | -0.176      |
| $R^2$                  | 0.17               | 0.15               | 0.20                | 0.16                |             | $R^2$                    | 0.20                | 0.15                | 0.17                | 0.17                |             | $R^2$                    | 0.26               | 0.19                | 0.14                | 0.17                |             |

## Large cap stocks

- Longer-term returns of this time regression suggest that large stocks with bullish message board sentiment do not significantly and economically meaningfully outperform bearish stocks.
- Message boards do not contain value-relevant information for large stocks.
- Large stocks experience higher media attention and analyst coverage, and are therefore expected to be embedded in an efficient market environment



| Holding period $K = 0$ |                     |                     |                     |                     |             | Holding period $K = 1-3$ |                     |                     |                     |                     |             | Holding period $K = 4-6$ |                     |                     |                     |                     |             |
|------------------------|---------------------|---------------------|---------------------|---------------------|-------------|--------------------------|---------------------|---------------------|---------------------|---------------------|-------------|--------------------------|---------------------|---------------------|---------------------|---------------------|-------------|
|                        | Bullish             | 2Q                  | 3Q                  | Bearish             | $\Delta BB$ |                          | Bullish             | 2Q                  | 3Q                  | Bearish             | $\Delta BB$ |                          | Bullish             | 2Q                  | 3Q                  | Bearish             | $\Delta BB$ |
| Carhart four factor    |                     |                     |                     |                     |             | Carhart four factor      |                     |                     |                     |                     |             | Carhart four factor      |                     |                     |                     |                     |             |
| $\alpha$               | 0.065***<br>(17.07) | 0.017***<br>(5.80)  | 0.007<br>(1.88)     | -0.007*<br>(-1.99)  | 0.072       | $\alpha$                 | 0.017***<br>(6.59)  | 0.021***<br>(7.34)  | 0.011***<br>(3.84)  | 0.002<br>(0.74)     | 0.015       | $\alpha$                 | 0.012***<br>(5.08)  | 0.024***<br>(7.12)  | 0.016***<br>(5.22)  | 0.006*<br>(2.17)    | 0.005       |
| $\beta_{rm}$           | 1.435***<br>(11.41) | 1.277***<br>(13.73) | 1.283***<br>(12.17) | 1.585***<br>(14.59) | -0.150      | $\beta_{rm}$             | 1.777***<br>(27.67) | 1.758***<br>(23.22) | 1.801***<br>(26.26) | 1.805***<br>(26.03) | -0.028      | $\beta_{rm}$             | 1.835***<br>(30.05) | 1.643***<br>(22.28) | 1.601***<br>(20.85) | 1.524***<br>(19.04) | 0.311       |
| $\beta_{HML}$          | 0.100<br>(0.53)     | 0.363**<br>(2.74)   | 0.215<br>(1.33)     | 0.824***<br>(4.84)  | -0.725      | $\beta_{HML}$            | 0.098<br>(0.92)     | 0.165<br>(1.42)     | -0.145<br>(-1.24)   | -0.212<br>(-1.96)   | 0.310       | $\beta_{HML}$            | 0.399***<br>(4.08)  | 0.180<br>(1.40)     | 0.217<br>(1.81)     | 0.164<br>(1.28)     | 0.235       |
| $\beta_{SMB}$          | 1.652***<br>(18.55) | 1.336***<br>(18.75) | 1.213***<br>(13.50) | 1.440***<br>(15.69) | 0.211       | $\beta_{SMB}$            | -0.039<br>(-0.64)   | 0.091<br>(1.34)     | -0.052<br>(-0.67)   | -0.050<br>(-0.71)   | 0.011       | $\beta_{SMB}$            | 0.108<br>(1.86)     | -0.004<br>(-0.05)   | 0.024<br>(0.32)     | -0.002<br>(-0.02)   | 0.110       |
| $\beta_{MOM}$          | 0.505***<br>(4.16)  | 0.301**<br>(3.16)   | -0.234*<br>(-2.00)  | -0.088<br>(-0.72)   | 0.593       | $\beta_{MOM}$            | 0.084<br>(1.04)     | 0.156<br>(1.78)     | 0.119<br>(1.26)     | -0.003<br>(-0.04)   | 0.087       | $\beta_{MOM}$            | -0.059<br>(-0.80)   | -0.179<br>(-1.69)   | -0.202*<br>(-2.14)  | -0.111<br>(-1.09)   | 0.053       |
| $R^2$                  | 0.10                | 0.11                | 0.10                | 0.09                |             | $R^2$                    | 0.05                | 0.05                | 0.06                | 0.05                |             | $R^2$                    | 0.06                | 0.04                | 0.05                | 0.04                |             |

## Small cap stocks

- Bullish stocks significantly and economically outperform bearish stocks with the impact decreasing in subsequent holding periods
- $\beta_{HML}$  estimates found for bullish and bearish small stocks (0.100 and 0.824, respectively), but with only significance for bearish stocks—bearish stocks are associated with value stocks whereas bullish stocks are considered as growth stocks with higher market perceived growth potential

# 5.Conclusion

- Higher message board activity reflects itself quickly in the prices of small stocks.
- Message board sentiment is incorporated into the stock price in the same month.
- Bullish stocks significantly and economically outperform bearish stocks in the short term, especially for small stocks.