7 Problems on Numbers

In this chapter, questions involving a set of numbers are put in the form of a puzzle. You have to analyse the given conditions, assume the unknown numbers and form equations accordingly, which on solving yield the unknown numbers.

SOLVED EXAMPLES

Ex. 1. ***A number is as much greater than 36 as is less than 86. Find the number.***

Sol. Let the number be x. Then, $x - 36 = 86 - x \Rightarrow 2x = 86 + 36 = 122 \Rightarrow x = 61$.

Hence, the required number is 61.

Ex. 2. ***Find a number such that when 15 is subtracted from 7 times the number, the result is 10 more than twice the number.*** **(Hotel Management, 2002)**

Sol. Let the number be x. Then, $7x - 15 = 2x + 10 \Rightarrow 5x = 25 \Rightarrow x = 5$.

Hence, the required number is 5.

Ex. 3. ***The sum of a rational number and its reciprocal is $\frac{13}{6}$. Find the number.***

Sol. Let the number be x. Then,

$$x + \frac{1}{x} = \frac{13}{6} \Rightarrow \frac{x^2+1}{x} = \frac{13}{6} \Rightarrow 6x^2 - 13x + 6 = 0 \Rightarrow 6x^2 - 9x - 4x + 6 = 0$$

$$\Rightarrow (3x - 2)(2x - 3) = 0 \Rightarrow x = \frac{2}{3} \text{ or } x = \frac{3}{2}.$$

Hence, the required number is $\frac{2}{3}$ or $\frac{3}{2}$.

Ex. 4. ***The sum of two numbers is 184. If one-third of the one exceeds one-seventh of the other by 8, find the smaller number.*** **(Bank Recruitment, 2011)**

Sol. Let the numbers be x and $(184 - x)$. Then,

$$\frac{x}{3} - \frac{(184-x)}{7} = 8 \Rightarrow 7x - 3(184 - x) = 168 \Rightarrow 10x = 720 \Rightarrow x = 72.$$

So, the numbers are 72 and 112. Hence, smaller number = 72.

Ex. 5. ***The difference of two numbers is 11 and one-fifth of their sum is 9. Find the numbers.***

Sol. Let the numbers be x and y. Then

$$x - y = 11 \quad \ldots(i)$$

and $\frac{1}{5}(x + y) = 9 \Rightarrow x + y = 45 \quad \ldots(ii)$

Adding (i) and (ii), we get : $2x = 56$ or $x = 28$.

Putting $x = 28$ in (i), we get : $y = 17$.

Hence, the numbers are 28 and 17.

Ex. 6. ***If the sum of two numbers is 42 and their product is 437, then find the absolute difference between the numbers.*** **(S.S.C., 2003; B.Ed., 2010)**

Sol. Let the numbers be x and y. Then, $x + y = 42$ and $xy = 437$.

$$x - y = \sqrt{(x+y)^2 - 4xy} = \sqrt{(42)^2 - 4 \quad 437} = \sqrt{1764 - 1748} = \sqrt{16} = 4.$$

$\therefore$ Required difference = 4.

Ex. 7. ***If the sum of two numbers is 10 and the sum of their reciprocals is $\frac{5}{12}$, find the numbers.*** **(P.C.S., 2006)**

Sol. Let the numbers be x and y.

Then, $x + y = 10$ ...(*i*)

And, $\frac{1}{x}+\frac{1}{y}=\frac{5}{12} \Rightarrow \frac{x+y}{xy} = \frac{5}{12} \Rightarrow xy = \frac{10 \ \ 12}{5} = 24$ ...(*ii*)

$\therefore \quad x - y = \sqrt{(x+y)^2 - 4xy} = \sqrt{(10)^2 - 4 \ \ 24} = \sqrt{100-96} = \sqrt{4} = 2 \Rightarrow x - y = 2$ ...(*iii*)

Adding (*i*) and (*iii*), we get: $2x = 12$ or $x = 6$.

Putting $x = 6$ in (*i*), we get: $y = 4$.

Hence, the required numbers are 6 and 4.

Ex. 8. ***Three numbers are in the ratio 3 : 2 : 5. The sum of their squares is 1862. Find the numbers.*** **(R.R.B., 2007)**

Sol. Let the numbers be $3x$, $2x$ and $5x$.

Then, $(3x)^2 + (2x)^2 + (5x)^2 = 1862 \Rightarrow 9x^2 + 4x^2 + 25x^2 = 1862$

$\Rightarrow 38x^2 = 1862 \Rightarrow x^2 = \frac{1862}{38} = 49 \Rightarrow x = \sqrt{49} = 7.$

Hence, the numbers are 21, 14 and 35.

Ex. 9. ***The sum of seven consecutive natural numbers is 1617. How many of these numbers are prime?*** **(S.S.C., 2006)**

Sol. Let the seven consecutive numbers be x, $(x + 1)$, $(x + 2)$, $(x + 3)$, $(x + 4)$, $(x + 5)$ and $(x + 6)$.

Then, $x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) = 1617$

$\Rightarrow 7x + 21 = 1617 \Rightarrow 7x = 1596 \Rightarrow x = 228.$

Thus, the numbers are 228, 229, 230, 231, 232, 233 and 234.

Of these numbers, only two numbers i.e. 229 and 233, are prime.

Ex. 10. ***The product of two consecutive numbers is 4032. Find the numbers.*** **(Bank P.O., 2008)**

Sol. Let the numbers be x and $(x + 1)$.

Then, $x(x + 1) = 4032 \Rightarrow x^2 + x - 4032 = 0 \Rightarrow x^2 + 64x - 63x - 4032 = 0$

$\Rightarrow x(x + 64) - 63(x + 64) = 0 \Rightarrow (x + 64)(x - 63) = 0$

$\Rightarrow x = 63.$ $[\because x \neq -64]$

Hence, the required numbers are 63 and 64.

Ex. 11. ***The sum of two numbers is 15 and the sum of their squares is 113. Find the numbers.*** **(R.R.B., 2006)**

Sol. Let the numbers be x and $(15 - x)$.

Then, $x^2 + (15 - x)^2 = 113 \Rightarrow x^2 + 225 + x^2 - 30x = 113$

$\Rightarrow 2x^2 - 30x + 112 = 0 \Rightarrow x^2 - 15x + 56 = 0$

$\Rightarrow (x - 7)(x - 8) = 0 \Rightarrow x = 7$ or $x = 8.$

So, the numbers are 7 and 8.

Ex. 12. ***The average of four consecutive even numbers is 27. Find the largest of these numbers.***

Sol. Let the four consecutive even numbers be x, $x + 2$, $x + 4$ and $x + 6$.

Then, sum of these numbers = $(27 \times 4) = 108$.

So, $x + (x + 2) + (x + 4) + (x + 6) = 108$ or $4x = 96$ or $x = 24$.

$\therefore$ Largest number = $(x + 6) = 30$.

Ex. 13. ***The sum of the squares of three consecutive odd numbers is 2531. Find the numbers.*** **(R.R.B., 2010)**

Sol. Let the numbers be x, $x + 2$ and $x + 4$.

Then, $x^2 + (x + 2)^2 + (x + 4)^2 = 2531 \Rightarrow 3x^2 + 12x - 2511 = 0 \Rightarrow x^2 + 4x - 837 = 0$

$\Rightarrow (x - 27)(x + 31) = 0 \Rightarrow x = 27.$

Hence, the required numbers are 27, 29 and 31.

Ex. 14. ***Of two numbers, 4 times the smaller one is less than 3 times the larger one by 5. If the sum of the numbers is larger than 6 times their difference by 6, find the two numbers.***

Sol. Let the numbers be x and y, such that $x > y$.

Then, $3x - 4y = 5$ ...(*i*)

and $(x + y) - 6(x - y) = 6 \Rightarrow -5x + 7y = 6$ ...(*ii*)

Solving (*i*) and (*ii*), we get : $x = 59$ and $y = 43$.

Hence, the required numbers are 59 and 43.

Ex. 15. ***The ratio between a two-digit number and the sum of the digits of that number is 4 : 1. If the digit in the unit's place is 3 more than the digit in the ten's place, what is the number?*** **(S.B.I.P.O., 2005)**

Sol. Let the ten's digit be x. Then, unit's digit = $(x + 3)$.

Sum of the digits = $x + (x + 3) = 2x + 3$. Number = $10x + (x + 3) = 11x + 3$.

$\therefore \dfrac{11x+3}{2x+3} = \dfrac{4}{1} \Leftrightarrow 11x + 3 = 4(2x + 3) \Leftrightarrow 3x = 9 \Leftrightarrow x = 3.$

Hence, required number = $11x + 3 = 36$.

Ex. 16. ***A number consists of two digits. The sum of the digits is 9. If 63 is subtracted from the number, its digits are interchanged. Find the number.***

Sol. Let the ten's digit be x. Then, unit's digit = $(9 - x)$.

Number = $10x + (9 - x) = 9x + 9$.

Number obtained by reversing the digits = $10(9 - x) + x = 90 - 9x$.

$\therefore (9x + 9) - 63 = 90 - 9x \Leftrightarrow 18x = 144 \Leftrightarrow x = 8.$

So, ten's digit = 8 and unit's digit = 1.

Hence, the required number is 81.

Ex. 17. ***In a three-digit number, the digit in the units place is four times the digit in the hundreds place. If the digits in the units place and the tens place are interchanged, the new number so formed is 18 more than the original number. If the digit in the hundreds place is one-third of the digit in the tens place, what is the original number?*** **(L.I.C., 2005)**

Sol. Let the digit in the hundreds place be x.

Then, digit in the units place = $4x$. And, digit in the tens place = $3x$.

Original number = $100x + 10 \times 3x + 4x = 100x + 30x + 4x = 134x$.

Number formed on interchanging the unit's and ten's digits

$= 100x + 10 \times 4x + 3x = 143x$.

$\therefore 143x - 134x = 18 \Leftrightarrow 9x = 18 \Leftrightarrow x = 2.$

Hence, original number = $134x = (134 \times 2) = 268$.

Ex. 18. ***If the digits of a two-digit number are interchanged, the number formed is greater than the original number by 45. If the difference between the digits is 5, what is the original number?*** **(Bank P.O., 2009)**

Sol. Since the number formed by interchanging the digits is greater so the ten's digit of the original number is smaller than the unit's digit.

Let the ten's digit be x. Then, unit's digit = $x + 5$.

Original number = $10x + (x + 5) = 11x + 5$.

Number formed on interchanging the digits = $10(x + 5) + x = 11x + 50$.

$\therefore (11x + 50) - (11x + 5) = 45 \Rightarrow 45 = 45$, which is independent of x.

Hence, the number cannot be determined from the given data.

Ex. 19. ***A fraction becomes*** $\dfrac{2}{3}$ ***when 1 is added to both its numerator and denominator. And, it becomes*** $\dfrac{1}{2}$ ***when 1 is subtracted from both the numerator and denominator. Find the fraction.***

Sol. Let the required fraction be $\dfrac{x}{y}$. Then,

$$\frac{x+1}{y+1} = \frac{2}{3} \Rightarrow 3x - 2y = -1 \quad ...(i) \text{ and } \frac{x-1}{y-1} = \frac{1}{2} \Rightarrow 2x - y = 1 \quad ... \text{ (i)}$$

Solving (*i*) and (*ii*), we get : $x = 3$, $y = 5$.

$\therefore$ Required fraction = $\dfrac{3}{5}$.

Ex. 20. ***50 is divided into two parts such that the sum of their reciprocals is $\frac{1}{12}$. Find the two parts.***

Sol. Let the two parts be x and $(50 - x)$.

Then, $\frac{1}{x} + \frac{1}{50-x} = \frac{1}{12} \Rightarrow \frac{50-x+x}{x(50-x)} = \frac{1}{12} \Rightarrow x^2 - 50x + 600 = 0$

$\Rightarrow (x - 30)(x - 20) = 0 \Rightarrow x = 30$ or $x = 20$.

So, the parts are 30 and 20.

Ex. 21. ***If three numbers are added in pairs, the sums equal 10, 19 and 21. Find the numbers.***

Sol. Let the numbers be x, y and z. Then,

$x + y = 10$ ...(*i*)

$y + z = 19$ ...(*ii*)

$x + z = 21$ ...(*iii*)

Adding (*i*), (*ii*) and (*iii*), we get : $2(x + y + z) = 50$ or $(x + y + z) = 25$.

Thus, $x = (25 - 19) = 6$; $y = (25 - 21) = 4$; $z = (25 - 10) = 15$.

Hence, the required numbers are 6, 4 and 15.

EXERCISE
(OBJECTIVE TYPE QUESTIONS)

Directions : ***Mark (✓) against the correct answer:***

1. By how much is $\frac{3}{4}$th of 568 lesser than $\frac{7}{8}$th of 1008? **(Bank P.O., 2008)**

(*a*) 444 (*b*) 448
(*c*) 452 (*d*) 456
(*e*) None of these

2. The difference between a number and its three-fifths is 50. What is the number?

(*a*) 75 (*b*) 100
(*c*) 125 (*d*) None of these

3. If a number is added to two-fifths of itself, the value so obtained is 455. What is the number? **(Bank Recruitment, 2010)**

(*a*) 325 (*b*) 350
(*c*) 400 (*d*) 420
(*e*) None of these

4. If a number is multiplied by two-thirds of itself the value so obtained is 864. What is the number? **(Bank Recruitment, 2010)**

(*a*) 34 (*b*) 36
(*c*) 38 (*d*) 44
(*e*) 46

5. If a number is decreased by 4 and divided by 6, the result is 8. What would be the result if 2 is subtracted from the number and then it is divided by 5?

(*a*) $9\frac{2}{3}$ (*b*) 10
(*c*) $10\frac{1}{5}$ (*d*) $11\frac{1}{5}$
(*e*) None of these

6. A number when multiplied by 13 is increased by 180. The number is **(P.C.S., 2004)**

(*a*) 5 (*b*) 12
(*c*) 15 (*d*) 45

7. The sum of twice a number and three times of 42 is 238. What is the sum of thrice the number and two times of 42? **(Bank P.O., 2010)**

(*a*) 245 (*b*) 250
(*c*) 252 (*d*) 264
(*e*) None of these

8. If one-third of one-fourth of a number is 15, then three-tenths of that number is

(*a*) 35 (*b*) 36
(*c*) 45 (*d*) 54

9. The difference between $\frac{3}{5}$th of $\frac{2}{3}$rd of a number and $\frac{2}{5}$th of $\frac{1}{4}$th of the same number is 288. What is the number? **(Bank P.O., 2006)**

(*a*) 850 (*b*) 895
(*c*) 955 (*d*) 960

10. A number is doubled and 9 is added. If the resultant is trebled, it becomes 75. What is that number?

(*a*) 3.5 (*b*) 6
(*c*) 8 (*d*) None of these

11. Three-fourth of a number is 60 more than its one-third. The number is

(*a*) 84 (*b*) 108
(*c*) 144 (*d*) None of these

12. A number whose fifth part increased by 4 is equal to its fourth part diminished by 10, is **(SNAP, 2010)**

(*a*) 240 (*b*) 260
(*c*) 270 (*d*) 280

13. When 24 is subtracted from a number, it reduces to its four-seventh. What is the sum of the digits of that number?

(*a*) 1 (*b*) 9
(*c*) 11 (*d*) Data inadequate
(*e*) None of these

14. Find the number which when multiplied by 15 is increased by 196. **(L.I.C., 2003)**

(*a*) 14 (*b*) 20
(*c*) 26 (*d*) 28

15. If a number, when divided by 4, is reduced by 21, the number is

(*a*) 18 (*b*) 20
(*c*) 28 (*d*) 38

16. A number whose fifth part increased by 4 is equal to its fourth part diminished by 10, is

(*a*) 240 (*b*) 260
(*c*) 270 (*d*) 280

17. The difference of two numbers is 20% of the larger number. If the smaller number is 12, the larger one is

(*a*) 15 (*b*) 16
(*c*) 18 (*d*) 20

18. If one-seventh of a number exceeds its eleventh part by 100, then the number is

(*a*) 770 (*b*) 1100
(*c*) 1825 (*d*) 1925

19. If the sum of one-half and one-fifth of a number exceeds one-third of that number by $7\frac{1}{3}$, the number is

(*a*) 15 (*b*) 18
(*c*) 20 (*d*) 30

20. If doubling a number and adding 20 to the result gives the same answer as multiplying the number by 8 and taking away 4 from the product, the number is

(*a*) 2 (*b*) 3
(*c*) 4 (*d*) 6

21. If 50 is subtracted from two-third of a number, the result is equal to sum of 40 and one-fourth of that number. What is the number? **(R.R.B., 2002)**

(*a*) 174 (*b*) 216
(*c*) 246 (*d*) 336

22. A student was asked to divide the half of a certain number by 6 and the other half by 4 and then to add the two quantities so obtained. Instead of doing so the student divided the number by 5 and the result fell short by 4. The given number was **(P.C.S., 2009)**

(*a*) 240 (*b*) 288
(*c*) 384 (*d*) 480

23. One-third of a two-digit number exceeds one-fourth of its successive number by 1. The number is

(*a*) 12 (*b*) 15
(*c*) 18 (*d*) 21

24. If the sum of a number and its square is 182, what is the number?

(*a*) 15 (*b*) 26
(*c*) 28 (*d*) 91
(*e*) None of these

25. If $(73)^2$ is subtracted from the square of a number, the answer so obtained is 5075. What is the number? **(L.I.C.A.D.O., 2007)**

(*a*) 96 (*b*) 98
(*c*) 102 (*d*) 106

26. Twenty times a positive integer is less than its square by 96. What is the integer?

(*a*) 20
(*b*) 24
(*c*) 30
(*d*) Cannot be determined
(*e*) None of these

27. Thrice the square of a natural number decreased by 4 times the number is equal to 50 more than the number. The number is **(S.S.C., 2003)**

(*a*) 4 (*b*) 5
(*c*) 6 (*d*) 10

28. The sum of a number and its reciprocal is one-eighth of 34. What is the product of the number and its square root?

(*a*) 8 (*b*) 27
(*c*) 32 (*d*) None of these

29. Two-third of a positive number and $\frac{25}{216}$ of its reciprocal are equal. The number is

(*a*) $\frac{5}{12}$ (*b*) $\frac{12}{5}$
(*c*) $\frac{25}{144}$ (*d*) $\frac{144}{25}$

30. Find the whole number which when increased by 20 is equal to 69 times the reciprocal of the number. **(M.A.T., 2007)**

(*a*) 2.5 (*b*) 3
(*c*) 5 (*d*) 7

31. A positive number when decreased by 4 is equal to 21 times the reciprocal of the number. The number is

(*a*) 3 (*b*) 5
(*c*) 7 (*d*) 9

32. The sum and product of two numbers are 12 and 35 respectively. The sum of their reciprocals will be **(S.S.C., 2007)**

(*a*) $\frac{12}{35}$ (*b*) $\frac{1}{35}$

(*c*) $\frac{35}{8}$ (*d*) $\frac{7}{32}$

33. The sum of a positive number and its reciprocal is thrice the difference of the number and its reciprocal. The number is

(*a*) $\sqrt{2}$ (*b*) $\frac{1}{\sqrt{2}}$

(*c*) $\sqrt{3}$ (*d*) $\frac{1}{\sqrt{3}}$

34. The product of two whole numbers is 37. The square root of the difference of the numbers is **(C.P.O., 2007)**

(*a*) 4.5 (*b*) 6

(*c*) 7.5 (*d*) 8

35. The product of two natural numbers is 17. Then, the sum of the reciprocals of their squares is

(*a*) $\frac{1}{289}$ (*b*) $\frac{289}{290}$

(*c*) $\frac{290}{289}$ (*d*) 289

36. If $2\frac{1}{2}$ is added to a number and the sum multiplied by $4\frac{1}{2}$ and 3 is added to the product and the sum is divided by $1\frac{1}{5}$, the quotient becomes 25. What is the number?

(*a*) $2\frac{1}{2}$ (*b*) $3\frac{1}{2}$

(*c*) $4\frac{1}{2}$ (*d*) $5\frac{1}{2}$

37. Three numbers are in the ratio 4 : 5 : 6 and their average is 25. The largest number is

(*a*) 30 (*b*) 32

(*c*) 36 (*d*) 42

38. Three numbers are in the ratio of 3 : 4 : 6 and their product is 1944. The largest of these numbers is **(M.B.A., 2006)**

(*a*) 6 (*b*) 12

(*c*) 18 (*d*) None of these

39. The ratio between a two-digit number and the sum of the digits of that number is 4 : 1. If the digit in the unit's place is 3 more than the digit in the ten's place, then the number is **(M.B.A., 2004)**

(*a*) 24 (*b*) 36

(*c*) 63 (*d*) 96

40. Two numbers are such that the square of one is 224 less than 8 times the square of the other. If the numbers be in the ratio of 3 : 4, the numbers are

(*a*) 6, 8 (*b*) 9, 12

(*c*) 12, 16 (*d*) None of these

41. Two numbers are such that the ratio between them is 4 : 7. If each is increased by 4, the ratio becomes 3 : 5. The larger number is

(*a*) 36 (*b*) 48

(*c*) 56 (*d*) 64

42. The sum of three numbers is 264. If the first number be twice the second and third number be one-third of the first, then the second number is: **(R.R.B., 2004)**

(*a*) 48 (*b*) 54

(*c*) 72 (*d*) 84

43. The sum of two numbers is 22. Five times one number is equal to 6 times the other. The bigger of the two numbers is

(*a*) 10 (*b*) 12

(*c*) 15 (*d*) 16

44. One-fifth of a number is equal to $\frac{5}{8}$ of another number. If 35 is added to the first number, it becomes four times of the second number. The second number is

(*a*) 25 (*b*) 40

(*c*) 70 (*d*) 125

45. The sum of two numbers is 25 and their difference is 13. Find their product.

(*a*) 104 (*b*) 114

(*c*) 315 (*d*) 325

46. If the sum of two numbers is 33 and their difference is 15, the smaller number is

(*a*) 9 (*b*) 12

(*c*) 15 (*d*) 18

47. The sum of two numbers is 40 and their difference is 4. The ratio of the numbers is

(*a*) 11 : 9 (*b*) 11 : 18

(*c*) 21 : 19 (*d*) 22 : 9

48. The product of two numbers is 192 and the sum of these two numbers is 28. What is the smaller of these two numbers?

(*a*) 12 (*b*) 14

(*c*) 16 (*d*) 18

(*e*) None of these

49. There are two numbers such that the sum of twice the first number and thrice the second number is 100 and the sum of thrice the first number and twice the second number is 120. Which is the larger number? **(Bank P.O., 2010)**

(*a*) 12 (*b*) 14
(*c*) 32 (*d*) 35
(*e*) None of these

50. What is the greater of the two numbers whose product is 1092 and the sum of the two numbers exceeds their difference by 42? **(S.B.I.P.O., 2008)**
(*a*) 44 (*b*) 48
(*c*) 52 (*d*) 54
(*e*) None of these

51. The difference between two integers is 5. Their product is 500. Find the numbers. **(Hotel Management, 2003)**
(*a*) 15, 20 (*b*) 20, 25
(*c*) 30, 25 (*d*) 21, 26

52. Two numbers differ by 5. If their product is 336, then the sum of the two numbers is
(*a*) 21 (*b*) 28
(*c*) 37 (*d*) 51

53. Two different natural numbers are such that their product is less than their sum. One of the numbers must be
(*a*) 1 (*b*) 2
(*c*) 3 (*d*) None of these

54. The product of two numbers is 9375 and the quotient, when the larger one is divided by the smaller, is 15. The sum of the numbers is **(S.S.C., 2004)**
(*a*) 380 (*b*) 395
(*c*) 400 (*d*) 425

55. The difference between two numbers is 1365. When the larger number is divided by the smaller one, the quotient is 6 and the remainder is 15. The smaller number is
(*a*) 240 (*b*) 270
(*c*) 295 (*d*) 360

56. The difference between two numbers is 16. If one-third of the smaller number is greater than one-seventh of the larger number by 4, then the two numbers are
(*a*) 9 and 25 (*b*) 12 and 28
(*c*) 33 and 49 (*d*) 56 and 72

57. The sum of two numbers is 40 and their product is 375. What will be the sum of their reciprocals?
(*a*) $\frac{1}{40}$ (*b*) $\frac{8}{75}$
(*c*) $\frac{75}{4}$ (*d*) $\frac{75}{8}$

58. The sum of two positive integers multiplied by the bigger number is 204, and their difference multiplied by the smaller number is 35. The numbers are
(*a*) 12, 5 (*b*) 13, 4
(*c*) 14, 3 (*d*) 24, 10

59. If the sum and difference of two numbers are 20 and 8 respectively, then the difference of their squares is
(*a*) 12 (*b*) 28
(*c*) 160 (*d*) 180

60. Two numbers are such that their difference, their sum and their product are to one another as 1 : 7 : 24. The product of the two numbers is **(M.B.A., 2010)**
(*a*) 6 (*b*) 12
(*c*) 24 (*d*) 48

61. The product of two numbers is 120 and the sum of their squares is 289. The sum of the numbers is **(R.R.B., 2004)**
(*a*) 20 (*b*) 23
(*c*) 169 (*d*) None of these

62. The product of two numbers is 45 and the sum of their squares is 106. The numbers are **(R.R.B., 2002)**
(*a*) 3 and 5 (*b*) 5 and 9
(*c*) 5 and 19 (*d*) 45 and 1

63. The sum of the squares of two numbers is 3341 and the difference of their squares is 891. The numbers are **(M.B.A., 2006)**
(*a*) 25, 36 (*b*) 25, 46
(*c*) 35, 46 (*d*) None of these

64. The difference between two positive integers is 3. If the sum of their squares is 369, then the sum of the numbers is **(S.S.C., 2003)**
(*a*) 25 (*b*) 27
(*c*) 33 (*d*) 81

65. If the sum of two numbers is 22 and the sum of their squares is 404, then the product of the numbers is
(*a*) 40 (*b*) 44
(*c*) 80 (*d*) 88

66. The difference between the squares of two numbers is 256000 and the sum of the numbers is 1000. The numbers are
(*a*) 600, 400 (*b*) 628, 372
(*c*) 640, 360 (*d*) None of these

67. The difference between two numbers is 3 and the difference between their squares is 63. Which is the larger number? **(Bank P.O., 2009)**
(*a*) 9
(*b*) 12
(*c*) 15
(*d*) Cannot be determined
(*e*) None of these

68. A, B, C, D and E are five consecutive odd numbers. The sum of A and C is 146. What is the value of E? **(Bank P.O., 2009)**

(*a*) 71 (*b*) 75
(*c*) 79 (*d*) 81
(*e*) None of these

69. Out of six consecutive natural numbers if the sum of first three is 27, what is the sum of the other three? **(S.S.C., 2010)**

(*a*) 24 (*b*) 25
(*c*) 35 (*d*) 36

70. The sum of seven consecutive numbers is 175. What is the difference between twice the largest number and thrice the smallest number? **(Bank Recruitment, 2010)**

(*a*) 7 (*b*) 8
(*c*) 10 (*d*) 12
(*e*) None of these

71. The sum of five consecutive odd numbers is 575. What is the sum of the next set of five consecutive odd numbers? **(NABARD, 2009)**

(*a*) 595
(*b*) 615
(*c*) 635
(*d*) Cannot be determined
(*e*) None of these

72. The sum of three consecutive odd numbers and three consecutive even numbers together is 231. Also, the smallest odd number is 11 less than the smallest even number. What is the sum of the largest odd number and the largest even number? **(Bank P.O., 2010)**

(*a*) 74
(*b*) 82
(*c*) 83
(*d*) Cannot be determined
(*e*) None of these

73. Three times the first of three consecutive odd integers is 3 more than twice the third. The third integer is **(M.B.A., 1998)**

(*a*) 9 (*b*) 11
(*c*) 13 (*d*) 15

74. The sum of four consecutive even integers is 1284. The greatest of them is

(*a*) 320 (*b*) 322
(*c*) 324 (*d*) 326

75. The sum of three consecutive odd numbers is 20 more than the first of these numbers. What is the middle number?

(*a*) 7 (*b*) 9
(*c*) 11 (*d*) Data inadequate
(*e*) None of these

76. The product of three consecutive even numbers when divided by 8 is 720. The product of their square roots is **(Hotel Management, 2006)**

(*a*) $12\sqrt{10}$ (*b*) $24\sqrt{10}$
(*c*) 120 (*d*) None of these

77. The sum of three consecutive multiples of 3 is 72. What is the largest number?

(*a*) 21 (*b*) 24
(*c*) 27 (*d*) 36

78. What is the sum of two consecutive even numbers, the difference of whose squares is 84? **(S.S.C., 2003)**

(*a*) 34 (*b*) 38
(*c*) 42 (*d*) 46

79. The sum of the squares of three consecutive natural numbers is 2030. What is the middle number?

(*a*) 25 (*b*) 26
(*c*) 27 (*d*) 28

80. If the product of three consecutive integers is 120, then the sum of the integers is **(M.B.A., 2006)**

(*a*) 9 (*b*) 12
(*c*) 14 (*d*) 15
(*e*) 18

81. There are two numbers such that the sum of twice the first and thrice the second is 39, while the sum of thrice the first and twice the second is 36. The larger of the two is

(*a*) 6 (*b*) 8
(*c*) 9 (*d*) 12

82. In a two-digit number, the digit in the unit's place is four times the digit in ten's place and sum of the digits is equal to 10. What is the number?

(*a*) 14 (*b*) 41
(*c*) 82 (*d*) Data inadequate
(*e*) None of these

83. A number of two digits has 3 for its unit's digit, and the sum of digits is $\frac{1}{7}$ of the number itself. The number is **(L.I.C., 2003)**

(*a*) 43 (*b*) 53
(*c*) 63 (*d*) 73

84. If a number of two digits is k times the sum of its digits, then the number formed by interchanging the digits is the sum of the digits multiplied by **(M.B.A., 2005)**

(*a*) $k - 1$ (*b*) $11 - k$
(*c*) $9 + k$ (*d*) $10 - k$

85. A two-digit number exceeds the sum of the digits of that number by 18. If the digit at the unit's place is double the digit in the ten's place, what is the number?

(*a*) 24 (*b*) 42
(*c*) 48 (*d*) Data inadequate

86. The sum of the digits of a two-digit number is 15 and the difference between the digits is 3. What is the two-digit number?

(*a*) 69
(*b*) 78
(*c*) 96
(*d*) Cannot be determined
(*e*) None of these

87. A two-digit number is 7 times the sum of its two digits. The number that is formed by reversing its digits is 18 less than the original number. What is the number? **(R.R.B., 2006)**

(*a*) 42 (*b*) 52
(*c*) 62 (*d*) 72

88. If the digit in the unit's place of a two-digit number is halved and the digit in the ten's place is doubled, the number thus obtained is equal to the number obtained by interchanging the digits. Which of the following is definitely true? **(NMAT, 2005)**

(*a*) Sum of the digits is a two-digit number.
(*b*) Digit in the unit's place is half of the digit in the ten's place.
(*c*) Digit in the unit's place and the ten's place are equal.
(*d*) Digit in the unit's place is twice the digit in the ten's place.

89. In a two-digit number, if it is known that its unit's digit exceeds its ten's digit by 2 and that the product of the given number and the sum of its digits is equal to 144, then the number is **(C.B.I., 2003)**

(*a*) 24 (*b*) 26
(*c*) 42 (*d*) 46

90. A number consists of two digits. If the digits interchange places and the new number is added to the original number, then the resulting number will be divisible by **(S.S.C., 2003)**

(*a*) 3 (*b*) 5
(*c*) 9 (*d*) 11

91. The sum of the digits of a two-digit number is 9 less than the number. Which of the following digits is at unit's place of the number?

(*a*) 1 (*b*) 2
(*c*) 4 (*d*) Data inadequate

92. The difference between a two-digit number and the number obtained by interchanging the positions of its digits is 36. What is the difference between the two digits of that number? **(Bank P.O., 2003)**

(*a*) 3 (*b*) 4
(*c*) 9 (*d*) Cannot be determined
(*e*) None of these

93. The difference between a two-digit number and the number obtained by interchanging the two digits is 63. Which is the smaller of the two numbers? **(Bank P.O., 2003)**

(*a*) 29
(*b*) 70
(*c*) 92
(*d*) Cannot be determined
(*e*) None of these

94. The sum of the digits of a two-digit number is $\frac{1}{5}$ of the difference between the number and the number obtained by interchanging the positions of the digits. What is definitely the difference between the digits of that number?

(*a*) 5 (*b*) 7
(*c*) 9 (*d*) Data inadequate
(*e*) None of these

95. The number obtained by interchanging the two digits of a two-digit number is lesser than the original number by 54. If the sum of the two digit of the number is 12, then what is the original number? **(Bank P.O., 2009)**

(*a*) 28
(*b*) 39
(*c*) 82
(*d*) Cannot be determined
(*e*) None of these

96. The difference between a two-digit number and the number obtained by interchanging the digits is 36. What is the difference between the sum and the difference of the digits of the number if the ratio between the digits of the number is 1 : 2?

(*a*) 4 (*b*) 8
(*c*) 16 (*d*) None of these

97. In a two-digit positive number, the digit in the unit's place is equal to the square of the digit in ten's place, and the difference between the number and the number obtained by interchanging the digits is 54. What is 40% of the original number? **(Bank P.O., 2008)**

(*a*) 15.6 (*b*) 24
(*c*) 37.2 (*d*) 39
(*e*) None of these

98. A number consists of 3 digits whose sum is 10. The middle digit is equal to the sum of the other two and the number will be increased by 99 if its digits are reversed. The number is **(Hotel Management, 2003)**

(*a*) 145 (*b*) 253

(*c*) 370 (*d*) 352

99. A two-digit number becomes five-sixth of itself when its digits are reversed. The two digits differ by one. The number is

(*a*) 45 (*b*) 54

(*c*) 56 (*d*) 65

100. If the square of a two-digit number is reduced by the square of the number formed by reversing the digits of the number, the final result is **(N.M.A.T., 2008)**

(*a*) divisible by 11 (*b*) divisible by 9

(*c*) necessarily irrational (*d*) Both (*a*) and (*b*)

101. A number consists of two digits such that the digit in the ten's place is less by 2 than the digit in the unit's place. Three times the number added to $\frac{6}{7}$ times the number obtained by reversing the digits equals 108. The sum of the digits in the number is **(S.S.C., 2003)**

(*a*) 6 (*b*) 7

(*c*) 8 (*d*) 9

102. The digit in the unit's place of a number is equal to the digit in the ten's place of half of that number and the digit in the ten's place of that number is less than the digit in unit's place of half of the number by 1. If the sum of the digits of the number is 7, then what is the number? **(S.B.I.P.O., 2001)**

(*a*) 34 (*b*) 52

(*c*) 162 (*d*) Data inadequate

(*e*) None of these

103. In a two-digit number, the digit in the unit's place is more than twice the digit in ten's place by 1. If the digits in the unit's place and the ten's place are interchanged, difference between the newly formed number and the original number is less than the original number by 1. What is the original number?

(*a*) 25 (*b*) 37

(*c*) 49 (*d*) 52

(*e*) 73

104. A certain number of two digits is three times the sum of its digits and if 45 be added to it, the digits are reversed. The number is **(N.M.A.T. 2006; L.I.C.A.A.O., 2003)**

(*a*) 23 (*b*) 27

(*c*) 32 (*d*) 72

105. A two-digit number is such that the product of the digits is 8. When 18 is added to the number, then the digits are reversed. The number is **(M.B.A., 2003)**

(*a*) 18 (*b*) 24

(*c*) 42 (*d*) 81

106. In a number of three digits, the digits in the unit's place and in the hundred's place are equal and the sum of all the digits is 8. The number of such numbers is

(*a*) 3 (*b*) 4

(*c*) 5 (*d*) 6

107. In a three-digit number, the digit in the unit's place is 75% of the digit in the ten's place. The digit in the ten's place is greater than the digit in the hundred's place by 1. If the sum of the digits in the ten's place and the hundred's place is 15, what is the number? **(Bank P.O., 2006)**

(*a*) 687

(*b*) 786

(*c*) 795

(*d*) Cannot be determined

(*e*) None of these

108. The product of two fractions is $\frac{14}{15}$ and their quotient is $\frac{35}{24}$. The greater fraction is **(S.S.C., 2005)**

(*a*) $\frac{4}{5}$ (*b*) $\frac{7}{6}$

(*c*) $\frac{7}{4}$ (*d*) $\frac{7}{3}$

109. In a pair of fractions, fraction A is twice the fraction B and the product of two fractions is $\frac{2}{25}$. What is the value of fraction A?

(*a*) $\frac{1}{5}$ (*b*) $\frac{1}{25}$

(*c*) $\frac{2}{5}$ (*d*) Data inadequate

110. If the difference between the reciprocal of a positive proper fraction and the fraction itself be $\frac{9}{20}$, then the fraction is **(C.P.O., 2006)**

(*a*) $\frac{3}{5}$ (*b*) $\frac{4}{5}$

(*c*) $\frac{5}{4}$ (*d*) $\frac{3}{10}$

111. The sum of the numerator and denominator of a fraction is 11. If 1 is added to the numerator and 2 is subtracted from the denominator, it becomes $\frac{2}{3}$. The fraction is

(*a*) $\frac{5}{6}$ (*b*) $\frac{6}{5}$

(*c*) $\frac{3}{8}$ (*d*) $\frac{8}{3}$

112. The denominator of a fraction is 3 more than the numerator. If the numerator as well as the denominator is increased by 4, the fraction becomes $\frac{4}{5}$. What was the original fraction?

(*a*) $\frac{8}{11}$ (*b*) $\frac{5}{8}$

(*c*) $\frac{10}{13}$ (*d*) $\frac{7}{10}$

113. The difference between the numerator and the denominator of a fraction is 5. If 5 is added to its denominator, the fraction is decreased by $1\frac{1}{4}$. Find the value of the fraction.

(*a*) $\frac{1}{6}$ (*b*) $2\frac{1}{4}$

(*c*) $3\frac{1}{4}$ (*d*) 6

114. The numerator and denominator of a fraction are in the ratio of 2 : 3. If 6 is subtracted from the numerator, the result is a fraction that has a value $\frac{2}{3}$ of the original fraction. The numerator of the original fraction is

(*a*) 6 (*b*) 18

(*c*) 27 (*d*) 36

115. If 1 is added to the denominator of a fraction, the fraction becomes $\frac{1}{2}$. If 1 is added to the numerator of the fraction, the fraction becomes 1. The fraction is

(*a*) $\frac{1}{3}$ (*b*) $\frac{2}{3}$

(*c*) $\frac{3}{4}$ (*d*) $\frac{3}{2}$

116. If the numerator of a fraction is increased by 2 and the denominator is increased by 3, the fraction becomes $\frac{7}{9}$ and if both the numerator as well as the denominator are decreased by 1, the fraction becomes $\frac{4}{5}$. What is the original fraction?

(*a*) $\frac{5}{6}$ (*b*) $\frac{9}{11}$

(*c*) $\frac{13}{16}$ (*d*) $\frac{17}{21}$

117. If the numerator of a fraction is increased by $\frac{1}{4}$ and the denominator is decreased by $\frac{1}{3}$, the new fraction obtained is $\frac{33}{64}$. What was the original fraction?

(Bank P.O., 2008)

(*a*) $\frac{3}{7}$ (*b*) $\frac{5}{7}$

(*c*) $\frac{7}{9}$ (*d*) Cannot be determined

(*e*) None of these

118. If the numerator of a fraction is increased by 200% and the denominator is increased by 300%, the resultant fraction is $\frac{15}{26}$. What was the original fraction? **(S.B.I.P.O., 2008)**

(*a*) $\frac{8}{11}$ (*b*) $\frac{10}{11}$

(*c*) $\frac{9}{13}$ (*d*) $\frac{10}{13}$

(*e*) None of these

119. When the numerator of a fraction increases by 4, the fraction increases by $\frac{2}{3}$. The denominator of the fraction is

(*a*) 2 (*b*) 3

(*c*) 4 (*d*) 6

120. A fraction is such that if the double of the numerator and the triple of the denominator is changed by + 10 percent and –30 percent respectively, then we get 11 percent of $\frac{16}{21}$. Find the fraction.

(A.T.M.A., 2004)

(*a*) $\frac{2}{25}$ (*b*) $\frac{3}{25}$

(*c*) $\frac{4}{25}$ (*d*) None of these

121. 54 is to be divided into two parts such that the sum of 10 times the first and 22 times the second is 780. The bigger part is

(*a*) 24 (*b*) 34

(*c*) 30 (*d*) 32

122. 243 has been divided into three parts such that half of the first part, one-third of the second part and one-fourth of the third part are equal. The largest part is

(*a*) 74 (*b*) 86

(*c*) 92 (*d*) 108

123. The sum of four numbers is 64. If you add 3 to the first number, 3 is subtracted from the second number, the third is multiplied by 3 and the fourth is divided by 3, then all the results are equal. What

is the difference between the largest and the smallest of the original numbers?

(*a*) 21 (*b*) 27

(*c*) 32 (*d*) Cannot be determined

(*e*) None of these

124. The sum of the squares of three numbers is 138, while the sum of their products taken two at a time is 131. Their sum is **(Hotel Management, 1999)**

(*a*) 20 (*b*) 30

(*c*) 40 (*d*) None of these

125. The sum of three numbers is 136. If the ratio between first and second be 2 : 3 and that between second and third is 5 : 3, then the second number is

(*a*) 40 (*b*) 48

(*c*) 60 (*d*) 72

126. Of the three numbers, the sum of the first two is 73; the sum of the second and the third is 77 and the sum of the third and thrice the first is 104. The third number is **(NABARD, 2008)**

(*a*) 25 (*b*) 39

(*c*) 48 (*d*) Cannot be determined

(*e*) None of these

127. If the product of two numbers is 5 and one of the number is $\frac{3}{2}$, then the sum of two numbers is **[Indian Railways—Gr. 'D' Exam, 2014]**

(a) $4\frac{1}{3}$ (b) $4\frac{2}{3}$

(c) $4\frac{5}{6}$ (d) $5\frac{1}{6}$

128. The sum of the squares of two positive integers is 100 and the difference of their squares is 28. The sum of the numbers is **[Indian Railways—Gr. 'D' Exam, 2014]**

(a) 12 (b) 13

(c) 14 (d) 15

129. The sum of two number is 37 and the difference of their squares is 185, then the difference between the two numbers is: **[SSC—CHSL (10 +2) Exam, 2015]**

(a) 10 (b) 4

(c) 5 (d) 3

130. A man bought some eggs of which 10% are rotten. He gives 80% of the remainder to his neighbors. Now he is left out with 36 eggs. How many eggs he bought? **[SSC—CHSL (10 +2) Exam, 2015]**

(a) 40 (b) 100

(c) 200 (d) 72

131. The sum of two numbers is 75 and their difference is 25. The product of the two numbers is: **[SSC—CHSL (10 +2) Exam, 2015]**

(a) 1350 (b) 1250

(c) 125 (d) 1000

132. In a Mathematics examination the number scored by 5 candidates are 5 successive odd integers. If their total marks are 185, the highest score is **[NICL—AAO Exam, 2015]**

(a) 39 (b) 43

(c) 41 (d) 47

133. The difference between two numbers is 10 and one-fifth of their sum is equal to 8. Find the smaller number **[ESIC—UDC Exam, 2016]**

(a) 28 (b) 45

(c) 35 (d) 15

ANSWERS

1. (*d*)	**2.** (*c*)	**3.** (*a*)	**4.** (*b*)	**5.** (*b*)	**6.** (*c*)	**7.** (*c*)	**8.** (*d*)	**9.** (*d*)	**10.** (*c*)
11. (*c*)	**12.** (*d*)	**13.** (*c*)	**14.** (*a*)	**15.** (*c*)	**16.** (*d*)	**17.** (*a*)	**18.** (*d*)	**19.** (*c*)	**20.** (*c*)
21. (*b*)	**22.** (*d*)	**23.** (*b*)	**24.** (*e*)	**25.** (*c*)	**26.** (*b*)	**27.** (*b*)	**28.** (*a*)	**29.** (*a*)	**30.** (*b*)
31. (*c*)	**32.** (*a*)	**33.** (*a*)	**34.** (*b*)	**35.** (*c*)	**36.** (*b*)	**37.** (*a*)	**38.** (*c*)	**39.** (*b*)	**40.** (*a*)
41. (*c*)	**42.** (*c*)	**43.** (*b*)	**44.** (*b*)	**45.** (*b*)	**46.** (*a*)	**47.** (*a*)	**48.** (*a*)	**49.** (*c*)	**50.** (*c*)
51. (*b*)	**52.** (*c*)	**53.** (*a*)	**54.** (*c*)	**55.** (*b*)	**56.** (*c*)	**57.** (*b*)	**58.** (*a*)	**59.** (*c*)	**60.** (*d*)
61. (*b*)	**62.** (*b*)	**63.** (*c*)	**64.** (*b*)	**65.** (*a*)	**66.** (*b*)	**67.** (*b*)	**68.** (*c*)	**69.** (*d*)	**70.** (*e*)
71. (*e*)	**72.** (*e*)	**73.** (*d*)	**74.** (*c*)	**75.** (*b*)	**76.** (*b*)	**77.** (*c*)	**78.** (*c*)	**79.** (*b*)	**80.** (*d*)
81. (*c*)	**82.** (*e*)	**83.** (*c*)	**84.** (*b*)	**85.** (*a*)	**86.** (*d*)	**87.** (*a*)	**88.** (*d*)	**89.** (*a*)	**90.** (*d*)
91. (*d*)	**92.** (*b*)	**93.** (*d*)	**94.** (*d*)	**95.** (*e*)	**96.** (*b*)	**97.** (*a*)	**98.** (*b*)	**99.** (*b*)	**100.** (*d*)
101. (*a*)	**102.** (*b*)	**103.** (*b*)	**104.** (*b*)	**105.** (*b*)	**106.** (*b*)	**107.** (*b*)	**108.** (*b*)	**109.** (*c*)	**110.** (*b*)
111. (*c*)	**112.** (*a*)	**113.** (*b*)	**114.** (*b*)	**115.** (*b*)	**116.** (*a*)	**117.** (*d*)	**118.** (*d*)	**119.** (*d*)	**120.** (*a*)
121. (*b*)	**122.** (*d*)	**123.** (*c*)	**124.** (*a*)	**125.** (*c*)	**126.** (*e*)	**127.** (*c*)	**128.** (*c*)	**129.** (*c*)	**130.** (*c*)
131. (*b*)	**132.** (*c*)	**133.** (*d*)							

SOLUTIONS

1. $\frac{7}{8}$ of 1008 − $\frac{3}{4}$ of 568 = $\left(1008 \quad \frac{7}{8}\right)-\left(568 \quad \frac{3}{4}\right)$

= 882 − 426 = 456.

2. Let the number be x.

Then, $x - \frac{3}{5}\ x = 50 \Leftrightarrow \frac{2}{5}\ x = 50$

$\Leftrightarrow x = \left(\frac{50 \quad 5}{2}\right) = 125.$

3. Let the number be x.

Then, $x + \frac{2}{5}\ x = 455 \Leftrightarrow \frac{7}{5}\ x = 455 \Leftrightarrow x = \left(\frac{455 \quad 5}{7}\right) = 325.$

4. Let the number be x. Then, $x \times \frac{2}{3}\ x = 864$

$\Leftrightarrow \frac{2}{3}\ x^2 = 864$

$\Leftrightarrow x^2 = \left(\frac{864 \quad 3}{2}\right) = 1296 \Leftrightarrow x = \sqrt{1296} = 36.$

5. Let the number be x. Then, $\frac{x-4}{6} = 8$

$\Leftrightarrow x - 4 = 48$

$\Leftrightarrow x = 52.$

$\therefore \quad \frac{x-2}{5} = \frac{52-2}{5} = \frac{50}{5} = 10.$

6. Let the number be x.

Then, $13x = x + 180 \Leftrightarrow 12x = 180$

$\Leftrightarrow x = \frac{180}{12} = 15.$

7. Let the number be x.

Then, $2x + 3 \times 42 = 238 \Leftrightarrow 2x + 126 = 238$

$\Leftrightarrow 2x = 112 \Leftrightarrow x = 56.$

$\therefore$ Required sum $= 3x + 2 \times 42 = 3 \times 56 + 2 \times 42$

$= 168 + 84 = 252.$

8. Let the number be x. Then, $\frac{1}{3}$ of $\frac{1}{4}$ of $x = 15$

$\Leftrightarrow x = 15 \times 12 = 180.$

So, required number $= \left(\frac{3}{10} \quad 180\right) = 54.$

9. Let the number be x.

Then, $\frac{3}{5}$ of $\frac{2}{3}$ of $x - \frac{2}{5}$ of $\frac{1}{4}$ of $x = 288$

$\Leftrightarrow \left(x \quad \frac{3}{5} \quad \frac{2}{3}\right)-\left(x \quad \frac{2}{5} \quad \frac{1}{4}\right) = 288$

$\Leftrightarrow \frac{2}{5}\ x - \frac{1}{10}\ x = 288$

$\Leftrightarrow \frac{3x}{10} = 288 \Leftrightarrow x = \left(\frac{288 \quad 10}{3}\right) = 960.$

10. Let the number be x.

Then, $3\ (2x + 9) = 75 \Leftrightarrow 2x + 9 = 25$

$\Leftrightarrow 2x = 16 \Leftrightarrow x = 8.$

11. Let the number be x.

Then, $\frac{3}{4}\ x - \frac{1}{3}\ x = 60$

$\Leftrightarrow \frac{5x}{12} = 60$

$\Leftrightarrow x = \left(\frac{60 \quad 12}{5}\right) = 144.$

12. Let the number be x.

Then, $\frac{x}{5} + 4 = \frac{x}{4} - 10 \Leftrightarrow \frac{x}{4} - \frac{x}{5} = 14$

$\Leftrightarrow \frac{x}{20} = 14 \Leftrightarrow x = 14 \times 20 = 280.$

13. Let the number be x.

Then, $x - 24 = \frac{4}{7}x \Leftrightarrow x - \frac{4}{7}x = 24$

$\Leftrightarrow \frac{3}{7}x = 24 \Leftrightarrow x = \left(\frac{24 \quad 7}{3}\right) = 56.$

$\therefore$ Sum of the digits = (5 + 6) = 11.

14. Let the number be x.

Then, $15x - x = 196$

$\Leftrightarrow 14x = 196$

$\Leftrightarrow x = 14.$

15. Let the number be x.

Then, $\frac{x}{4} = x - 21 \Leftrightarrow x = 4x - 84$

$\Leftrightarrow 3x = 84 \Leftrightarrow x = 28.$

16. Let the number be x.

Then, $\left(\frac{1}{5}x + 4\right) = \left(\frac{1}{4}x - 10\right)$

$\Leftrightarrow \frac{x}{20} = 14 \Leftrightarrow x = 14 \quad 20 = 280.$

17. Let the number be x.

Then, $x - 12 = 20\%$ of $x \Leftrightarrow x - \frac{x}{5} = 12$

$\Leftrightarrow \frac{4x}{5} = 12 \Leftrightarrow x = \left(\frac{12 \quad 5}{4}\right) = 15.$

18. Let the number be x.

Then, $\frac{1}{7}x - \frac{1}{11}x = 100 \Leftrightarrow \frac{4x}{77}$

$= 100 \Leftrightarrow x = \frac{7700}{4} = 1925.$

19. Let the number be x.

Then, $\left(\frac{1}{2}x + \frac{1}{5}x\right) - \frac{1}{3}x = \frac{22}{3} \Leftrightarrow \frac{11x}{30}$

$= \frac{22}{3} \Leftrightarrow x = \left(\frac{22 \quad 30}{3 \quad 11}\right) = 20.$

20. Let the number be x.

Then, $2x + 20 = 8x - 4 \Leftrightarrow 6x = 24$

$\Leftrightarrow x = 4.$

21. Let the number be x.

Then, $\frac{2}{3}x - 50 = \frac{1}{4}x + 40 \Leftrightarrow \frac{2}{3}x - \frac{1}{4}x = 90$

$\Leftrightarrow \frac{5x}{12} = 90 \Leftrightarrow x = \left(\frac{90 \quad 12}{5}\right) = 216.$

22. Let the number be x.

Then, $\left[\frac{(x/2)}{6} + \frac{(x/2)}{4}\right] - \frac{x}{5} = 4 \Leftrightarrow \frac{x}{12} + \frac{x}{8} - \frac{x}{5} = 4$

$\Leftrightarrow \frac{10x + 15x - 24x}{120} = 4$

$\Leftrightarrow x = 4 \times 120 = 480.$

23. Let the number be x.

Then, $\frac{x}{3} - \frac{(x+1)}{4} = 1 \Leftrightarrow 4x - 3(x + 1) = 12 \Leftrightarrow x = 15.$

24. Let the number be x.

Then, $x + x^2 = 182 \Leftrightarrow x^2 + x - 182 = 0$

$\Leftrightarrow (x + 14)(x - 13) = 0 \Leftrightarrow x = 13.$

25. Let the number be x.

Then, $x^2 - (73)^2 = 5075 \Leftrightarrow x^2 - 5329 = 5075$

$\Leftrightarrow x^2 = 5075 + 5329 = 10404$

$\Leftrightarrow x = \sqrt{10404} = 102.$

26. Let the integer be x.

Then, $x^2 - 20x = 96$

$\Leftrightarrow x^2 - 20x - 96 = 0$

$\Leftrightarrow (x + 4)(x - 24) = 0$

$\Leftrightarrow x = 24.$

27. Let the number be x.

Then, $3x^2 - 4x = x + 50$

$\Leftrightarrow 3x^2 - 5x - 50 = 0$

$\Leftrightarrow (3x + 10)(x - 5) = 0$

$\Leftrightarrow x = 5.$

28. Let the number be x.

Then, $x + \frac{1}{x} = \frac{34}{8} \Leftrightarrow \frac{x^2 + 1}{x} = \frac{34}{8}$

$\Leftrightarrow 8x^2 - 34x + 8 = 0$

$\Leftrightarrow 4x^2 - 17x + 4 = 0$

$\Leftrightarrow (4x - 1)(x - 4) = 0$

$\Leftrightarrow x = 4.$

$\left[\text{neglecting } x = \frac{1}{4}, \text{ as } x \text{ is a natural no.}\right]$

$\therefore$ Required number $= 4 \times \sqrt{4} = 4 \times 2 = 8.$

29. Let the number be x.

Then, $\frac{2}{3}x = \frac{25}{216} \quad \frac{1}{x} \Leftrightarrow x^2 = \frac{25}{216} \quad \frac{3}{2}$

$= \frac{25}{144} \Leftrightarrow x = \sqrt{\frac{25}{144}} = \frac{5}{12}.$

30. Let the required number be x.

Then, $x + 20 = \frac{69}{x} \Leftrightarrow x^2 + 20x - 69 = 0$

$\Leftrightarrow x^2 + 23x - 3x - 69 = 0$

$\Leftrightarrow x(x + 23) - 3(x + 23) = 0$

$\Leftrightarrow (x + 23)(x - 3) = 0$

$\Leftrightarrow x = 3 \qquad [\because x \neq -23]$

31. Let the number be x.

Then, $x - 4 = \frac{21}{x} \Leftrightarrow x^2 - 4x - 21 = 0$

$\Leftrightarrow (x - 7)(x + 3) = 0 \Leftrightarrow x = 7.$

32. Let the numbers be x and y.

Then, $x + y = 12$ and $xy = 35$.

$\therefore \quad \frac{1}{x} + \frac{1}{y} = \frac{x + y}{xy} = \frac{12}{35}.$

33. Let the number be x.

Then, $x + \frac{1}{x} = 3\left(x - \frac{1}{x}\right)$

$\Leftrightarrow \frac{x^2 + 1}{x} = 3\left(\frac{x^2 - 1}{x}\right)$

$\Leftrightarrow x^2 + 1 = 3x^2 - 3$

$\Leftrightarrow 2x^2 = 4$

$\Leftrightarrow x^2 = 2$

$\Leftrightarrow x = \sqrt{2}.$

34. Let the numbers be a and b.

Then, $ab = 37 \Rightarrow a = 1$ and $b = 37$.

So, $\sqrt{b - a} = \sqrt{37 - 1} = \sqrt{36} = 6.$

35. Let the numbers be a and b.

Then, $ab = 17 \Rightarrow a = 1$ and $b = 17$.

So, $\frac{1}{a^2} + \frac{1}{b^2} = \frac{a^2 + b^2}{a^2 b^2} = \frac{1^2 + (17)^2}{(1 \quad 17)^2} = \frac{290}{289}.$

36. Let the number be x. Then,

$\frac{4\frac{1}{2}\left(x + 2\frac{1}{2}\right) + 3}{1\frac{1}{5}} = 25 \Leftrightarrow \frac{\frac{9}{2}\left(x + \frac{5}{2}\right) + 3}{\frac{6}{5}} = 25$

$\Leftrightarrow \frac{9x}{2} + \frac{45}{4} + 3 = 25 \quad \frac{6}{5} = 30$

$\Leftrightarrow \frac{9x}{2} = 30 - \frac{57}{4} \Leftrightarrow \frac{9x}{2} = \frac{63}{4}$

$\Leftrightarrow x = \left(\frac{63}{4} \quad \frac{2}{9}\right) = \frac{7}{2} = 3\frac{1}{2}.$

37. Let the numbers be $4x$, $5x$ and $6x$.

Then, $\frac{4x + 5x + 6x}{3} = 25 \Leftrightarrow 5x = 25 \Leftrightarrow x = 5.$

$\therefore$ Largest number $= 6x = 30.$

38. Let the numbers be $3x$, $4x$ and $6x$.

Then, $3x \times 4x \times 6x = 1944$

$\Leftrightarrow 72x^3 = 1944 \Leftrightarrow x^3 = 27$

$\Leftrightarrow x = 3.$

$\therefore$ Largest number $= 6x = 18.$

39. Let the ten's digit be x. Then, unit's digit = $x + 3$.
Number = $10x + (x + 3) = 11x + 3$.
Sum of digits = $x + (x + 3) = 2x + 3$.

$$\therefore \quad \frac{11x+3}{2x+3} = \frac{4}{1} \Leftrightarrow 11x + 3 = 8x + 12$$
$$\Leftrightarrow 3x = 9 \Leftrightarrow x = 3.$$

Hence, required number = $11x + 3 = 11 \times 3 + 3 = 36$.

40. Let the numbers be $3x$ and $4x$.
Then, $(4x)^2 = 8 \times (3x)^2 - 224$
$\Leftrightarrow 16x^2 = 72x^2 - 224$
$\Leftrightarrow 56x^2 = 224 \Leftrightarrow x^2 = 4$
$\Leftrightarrow x = 2$.
So, the numbers are 6 and 8.

41. Let the numbers be $4x$ and $7x$.

$$\text{Then, } \frac{4x+4}{7x+4} = \frac{3}{5} \Leftrightarrow 5(4x+4) = 3(7x+4) \Leftrightarrow x = 8.$$

$\therefore$ Larger number = $7x = 56$.

42. Let the second number be x. Then, first number = $2x$ and third number = $\frac{2x}{3}$.

$$\therefore \quad 2x + x + \frac{2x}{3} = 264 \Leftrightarrow \frac{11x}{3} = 264$$
$$\Leftrightarrow x = \left(\frac{264}{11} \times 3\right) = 72.$$

43. Let the numbers be x and $(22 - x)$. Then, $5x = 6(22 - x)$
$\Leftrightarrow 11x = 132 \Leftrightarrow x = 12$.
So, the numbers are 12 and 10.

44. Let the numbers be x and y. Then, $\frac{1}{5}x = \frac{5}{8}y \Leftrightarrow y = \frac{8}{25}x$.

$$\text{Now, } x + 35 = 4y \Leftrightarrow x + 35 = \frac{32}{25}x$$
$$\Leftrightarrow \frac{7}{25}x = 35 \Leftrightarrow x = \left(\frac{35}{7} \times 25\right) = 125.$$
$$\therefore \quad \text{Second number} = y = \frac{8}{25}x = \left(\frac{8}{25} \times 125\right) = 40.$$

45. Let the numbers be x and y.
Then, $x + y = 25$ and $x - y = 13$.
$4xy = (x + y)^2 - (x - y)^2 = (25)^2 - (13)^2$
$= 625 - 169 = 456 \Rightarrow xy = 114$.

46. Let the numbers be x and y. Then,
$x + y = 33$ ...(*i*)
and $x - y = 15$ ...(*ii*)
Solving (*i*) and (*ii*), we get : $x = 24$, $y = 9$.
$\therefore$ Smaller number = 9.

47. Let the numbers be x and y.

$$\text{Then, } \frac{x+y}{x-y} = \frac{40}{4} = 10 \Leftrightarrow (x+y) = 10(x-y)$$
$$\Leftrightarrow 9x = 11y \Leftrightarrow \frac{x}{y} = \frac{11}{9}.$$

48. Let the numbers be x and $(28 - x)$.
Then, $x(28 - x) = 192 \Leftrightarrow x^2 - 28x + 192 = 0$
$\Leftrightarrow (x - 16)(x - 12) = 0$
$\Leftrightarrow x = 16$ or $x = 12$.
So, the numbers are 16 and 12.

49. Let the numbers be x and y. Then,
$2x + 3y = 100$ ...(*i*)
and $3x + 2y = 120$ ...(*ii*)
Adding (*i*) and (*ii*), we get : $5x + 5y = 220$
or $x + y = 44$ ...(*iii*)
Subtracting (*i*) from (*ii*); we get : $x - y = 20$ ...(*iv*)
Adding (*iii*) and (*iv*), we get: $2x = 64$ or $x = 32$.
Putting $x = 32$ in (*iii*), we get : $y = 12$.
Hence, larger number = 32.

50. Let the numbers be x and y. Then,
$xy = 1092$ ...(*i*)
And, $(x + y) - (x - y) = 42$
$\Leftrightarrow 2y = 42$
$\Leftrightarrow y = 21$.

$$\text{Putting } y = 21 \text{ in } (i), \text{ we get : } x = \frac{1092}{21} = 52.$$

Hence, greater number = 52.

51. Let the integers be x and $(x + 5)$. Then,
$x(x + 5) = 500 \Leftrightarrow x^2 + 5x - 500 = 0$
$\Leftrightarrow (x + 25)(x - 20) = 0$
$\Leftrightarrow x = 20$.
So, the numbers are 20 and 25.

52. Let the numbers be x and y.
Then, $x - y = 5$ and $xy = 336$.
$(x + y)^2 = (x - y)^2 + 4xy = 25 + 4 \times 336 = 1369$
$\Rightarrow x + y = \sqrt{1369} = 37$.

53. Since $1.\ x < 1 + x$, so one of the numbers is 1.

54. Let the numbers be x and y.

$$\text{Then, } xy = 9375 \text{ and } \frac{x}{y} = 15.$$
$$\frac{xy}{(x/y)} = \frac{9375}{15} \Leftrightarrow y^2 = 625 \Leftrightarrow y = 25$$
$\Rightarrow x = 15y = (15 \times 25) = 375$.
$\therefore$ Sum of the numbers = $375 + 25 = 400$.

55. Let the numbers be x and $(x + 1365)$.
Then, $x + 1365 = 6x + 15 \Leftrightarrow 5x = 1350 \Leftrightarrow x = 270$.

56. Let the numbers be x and $(x + 16)$.

$$\text{Then, } \frac{x}{3} - \frac{(x+16)}{7} = 4 \Leftrightarrow 7x - 3(x + 16)$$
$$= 84 \Leftrightarrow 4x = 84 + 48$$
$$= 132 \Leftrightarrow x = 33.$$

Hence, the numbers are 33 and 49.

57. Let the numbers be x and y.
Then, $x + y = 40$ and $xy = 375$.

$$\therefore \quad \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{40}{375} = \frac{8}{75}.$$

58. Let the numbers be x and y such that $x > y$.

Then, $x(x + y) = 204 \Rightarrow x^2 + xy = 204$ ...(*i*)

and $y(x - y) = 35 \Rightarrow xy - y^2 = 35$ ...(*ii*)

Subtracting (*ii*) from (*i*), we get : $x^2 + y^2 = 169$.

The only triplet satisfying this condition is (12, 5, 13). Thus, $x = 12$, $y = 5$.

59. Let the numbers be x and y.

Then, $x + y = 20$ and $x - y = 8$.

$\therefore \quad x^2 - y^2 = (x + y)(x - y) = 20 \times 8 = 160$.

60. Let the numbers be x and y.

Let $a - b = k$ ...(*i*)

$a + b = 7k$ ...(*ii*)

$ab = 24k$ ...(*iii*)

Adding (*i*) and (*ii*), we get : $2a = 8k$ or $a = 4k$.

Putting $a = 4k$ in (*i*), we get : $b = 3k$.

Putting $a = 4k$ and $b = 3k$ in (*iii*), we get : $4k \times 3k = 24k \Leftrightarrow 12k^2 = 24k \Leftrightarrow k = 2$.

Hence, product of numbers $= 24k = 24 \times 2 = 48$.

61. Let the numbers be x and y.

Then, $xy = 120$ and $x^2 + y^2 = 289$.

$\therefore \quad (x + y)^2 = x^2 + y^2 + 2xy = 289 + 240 = 529$.

$\therefore \quad x + y = \sqrt{529} = 23$.

62. Let the numbers be x and y.

Then, $xy = 45$ and $x^2 + y^2 = 106$.

$$(x + y) = \sqrt{(x^2 + y^2) + 2xy}$$

$$= \sqrt{106 + 90} = \sqrt{196} \Rightarrow x + y = 14 \quad ...(i)$$

$$(x - y) = \sqrt{(x^2 + y^2) - 2xy}$$

$$= \sqrt{106 - 90} = \sqrt{16} \Rightarrow x - y = 4 \quad ...(ii)$$

Solving (*i*) and (*ii*), we get : $x = 9$ and $y = 5$.

63. Let the numbers be x and y. Then,

$x^2 + y^2 = 3341$ ...(*i*)

and $x^2 - y^2 = 891$ ...(*ii*)

Adding (*i*) and (*ii*), we get :

$2x^2 = 4232$ or $x^2 = 2116$ or $x = 46$.

Subtracting (*ii*) from (*i*), we get :

$2y^2 = 2450$ or $y^2 = 1225$ or $y = 35$.

So, the numbers are 35 and 46.

64. Let the numbers be x and $(x + 3)$. Then,

$x^2 + (x + 3)^2 = 369$

$\Leftrightarrow \quad x^2 + x^2 + 9 + 6x = 369$

$\Leftrightarrow \quad 2x^2 + 6x - 360 = 0$

$\Leftrightarrow \quad x^2 + 3x - 180 = 0$

$\Leftrightarrow \quad (x + 15)(x - 12) = 0$

$\Leftrightarrow \quad x = 12$.

So, the numbers are 12 and 15.

$\therefore \quad$ Required sum $= (12 + 15) = 27$.

65. Let the numbers be x and y.

Then, $(x + y) = 22$ and $x^2 + y^2 = 404$.

Now, $2xy = (x + y)^2 - (x^2 + y^2) = (22)^2 - 404$

$= 484 - 404 = 80 \Rightarrow xy = 40$.

66. Let the numbers be x and y.

Then, $x^2 - y^2 = 256000$ and $x + y = 1000$.

On dividing, we get : $x - y = 256$.

Solving $x + y = 1000$ and $x - y = 256$,

we get : $x = 628$ and $y = 372$.

67. Let the numbers be x and y.

Then, $x^2 - y^2 = 63$ and $x - y = 3$.

On dividing, we get : $x + y = 21$.

Solving $x + y = 21$ and $x - y = 3$,

we get : $x = 12$ and $y = 9$.

$\therefore \quad$ Larger number $= 12$.

68. Let $A = x$, $B = x + 2$, $C = x + 4$,

$D = x + 6$ and $E = x + 8$.

Then, $A + C = 146 \Rightarrow x + (x + 4) = 146$

$\Rightarrow \quad 2x = 142 \Rightarrow x = 71$.

$\therefore \quad E = x + 8 = 71 + 8 = 79$.

69. Let the six numbers be x, $x + 1$, $x + 2$, $x + 3$, $x + 4$ and $x + 5$.

Then, $x + (x + 1) + (x + 2) = 27 \Rightarrow 3x + 3 = 27$.

Required sum $= (x + 3) + (x + 4) + (x + 5)$

$= 3x + 12 = (3x + 3) + 9 = 27 + 9 = 36$.

70. Let the seven numbers be x, $x + 1$, $x + 2$, $x + 3$, $x + 4$, $x + 5$ and $x + 6$.

Then, $x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) = 175$

$\Leftrightarrow \quad 7x + 21 = 175 \Leftrightarrow 7x = 154$

$\Leftrightarrow \quad x = 22$.

Required difference $= 2(x + 6) - 3x = 12 - x$

$= 12 - 22 = -10$.

71. Let the five numbers be x, $x + 2$, $x + 4$, $x + 6$ and $x + 8$.

Then, $x + (x + 2) + (x + 4) + (x + 6) + (x + 8) = 575$

$\Leftrightarrow \quad 5x + 20 = 575 \Leftrightarrow 5x = 555 \Leftrightarrow x = 111$.

$\therefore \quad$ Required sum $= (x + 10) + (x + 12) + (x + 14) + (x + 16) + (x + 18)$

$= 5x + 70 = 5 \times 111 + 70 = 555 + 70 = 625$.

72. Let the three odd numbers be x, $x + 2$, $x + 4$ and the three even numbers be $x + 11$, $x + 13$ and $x + 15$.

Then, $x + (x + 2) + (x + 4) + (x + 11) + (x + 13) + (x + 15) = 231$

$\Leftrightarrow \quad 6x + 45 = 231 \Leftrightarrow 6x = 186 \Leftrightarrow x = 31$.

$\therefore \quad$ Required sum $= (x + 4) + (x + 15) = 2x + 19 = 2 \times 31 + 19 = 62 + 19 = 81$.

73. Let the three integers be x, $x + 2$ and $x + 4$.

Then, $3x = 2(x + 4) + 3 \Leftrightarrow x = 11$.

$\therefore \quad$ Third integer $= x + 4 = 15$.

74. Let the four integers be x, $x + 2$, $x + 4$ and $x + 6$.

Then, $x + (x + 2) + (x + 4) + (x + 6) = 1284$

$\Leftrightarrow \quad 4x = 1272 \Leftrightarrow x = 318$.

$\therefore \quad$ Greatest integer $= x + 6 = 324$.

75. Let the numbers be x, $x + 2$ and $x + 4$.
Then, $x + (x + 2) + (x + 4) = x + 20$
$\Leftrightarrow \quad 2x = 14 \quad \Leftrightarrow \quad x = 7.$
$\therefore$ Middle number $= x + 2 = 9.$

76. Let the numbers be x, $x + 2$ and $x + 4$.
Then, $\dfrac{x(x+2)(x+4)}{8} = 720$
$\Rightarrow \quad x(x+2)(x+4) = 5760.$
$\therefore \quad \sqrt{x} \quad \sqrt{(x+2)} \quad \sqrt{(x+4)}$
$= \sqrt{x(x+2)(x+4)} = \sqrt{5760} = 24\sqrt{10}.$

77. Let the numbers be $3x$, $3x + 3$ and $3x + 6$.
Then, $3x + (3x + 3) + (3x + 6) = 72$
$\Leftrightarrow \quad 9x = 63$
$\Leftrightarrow \quad x = 7.$
$\therefore \quad$ Largest number $= 3x + 6 = 27.$

78. Let the numbers be x and $x + 2$.
Then, $(x + 2)^2 - x^2 = 84$
$\Leftrightarrow \quad 4x + 4 = 84$
$\Leftrightarrow \quad 4x = 80$
$\Leftrightarrow \quad x = 20.$
$\therefore \quad$ Required sum $= x + (x + 2) = 2x + 2 = 42.$

79. Let the numbers be x, $x + 1$ and $x + 2$.
Then, $x^2 + (x + 1)^2 + (x + 2)^2 = 2030$
$\Leftrightarrow 3x^2 + 6x - 2025 = 0$
$\Leftrightarrow x^2 + 2x - 675 = 0$
$\Leftrightarrow (x + 27)(x - 25) = 0$
$\Leftrightarrow x = 25.$
$\therefore \quad$ Middle number $= (x + 1) = 26.$

80. $120 = 2 \times 2 \times 2 \times 3 \times 5 = (2 \times 2) \times 5 \times (2 \times 3) = 4 \times 5 \times 6.$
Clearly, the three consecutive integers whose product is 120 are 4, 5 and 6.
Required sum $= 4 + 5 + 6 = 15.$

81. Let the numbers be x and y.
Then, $2x + 3y = 39$ ...(i)
and $3x + 2y = 36$ ...(ii)
On solving (i) and (ii), we get : $x = 6$ and $y = 9$.
$\therefore \quad$ Larger number $= 9.$

82. Let the ten's digit be x. Then, unit's digit $= 4x$.
$\therefore \quad x + 4x = 10 \quad \Leftrightarrow \quad 5x = 10 \quad \Leftrightarrow \quad x = 2.$
So, ten's digit $= 2$, unit's digit $= 8$.
Hence, the required number is 28.

83. Let the ten's digit be x.
Then, number $= 10x + 3$ and sum of digits $= (x + 3)$.
So, $(x+3) = \dfrac{1}{7}(10x+3) \quad \Leftrightarrow \quad 7x + 21$
$= 10x + 3 \quad \Leftrightarrow \quad 3x = 18 \quad \Leftrightarrow \quad x = 6.$
Hence, the number is 63.

84. Let the ten's digit be x and the unit's digit be y.
Then, number $= 10x + y$.
$\therefore \quad 10x + y = k(x + y) \quad \Rightarrow \quad k = \dfrac{10x+y}{x+y}.$
Number formed by interchanging the digits $= 10y + x$.
Let $10y + x = h(x + y)$.
Then, $h = \dfrac{10y+x}{x+y} = \dfrac{11(x+y)-(10x+y)}{x+y}$
$= 11 - \dfrac{10x+y}{x+y} = 11 - k.$

85. Let the ten's digit be x.
Then, unit's digit $= 2x$.
Number $= 10x + 2x = 12x$; Sum of digits $= x + 2x = 3x$.
$\therefore \quad 12x - 3x = 18 \quad \Leftrightarrow \quad 9x = 18 \quad \Leftrightarrow \quad x = 2.$
Hence, required number $= 12x = 24.$

86. Let the ten's digit be x and unit's digit be y.
Then, $x + y = 15$ and $x - y = 3$ or $y - x = 3$.
Solving $x + y = 15$ and $x - y = 3$, we get : $x = 9$, $y = 6$.
Solving $x + y = 15$ and $y - x = 3$, we get : $x = 6$, $y = 9$.
So, the number is either 96 or 69. Hence, the number cannot be determined.

87. Let the ten's digit be x and the unit's digit be y.
Then, number $= 10x + y$.
$\therefore \quad 10x + y = 7(x + y) \quad \Leftrightarrow \quad 3x = 6y \quad \Leftrightarrow \quad x = 2y.$
Number formed by reversing the digits $= 10y + x$.
$\therefore \quad (10x + y) - (10y + x) = 18 \Leftrightarrow 9x - 9y = 18 \Leftrightarrow x - y = 2 \Leftrightarrow 2y - y = 2 \Leftrightarrow y = 2.$
So, $x = 2y = 4$.
Hence, required number $= 10x + y = 40 + 2 = 42.$

88. Let the ten's digit be x and the unit's digit be y. Then, number $= 10x + y$.
New number $= 10 \times 2x + \dfrac{y}{2} = 20x + \dfrac{y}{2}.$
$\therefore \quad 20x + \dfrac{y}{2} = 10y + x \Rightarrow 40x + y = 20y + 2x$
$\Rightarrow \quad 38x = 19y \Rightarrow y = 2x.$
So, the unit's digit is twice the ten's digit.

89. Let the ten's digit be x. Then, unit's digit $= x + 2$.
Number $= 10x + (x + 2) = 11x + 2$; Sum of digits $= x + (x + 2) = 2x + 2$.
$\therefore \quad (11x + 2)(2x + 2) = 144$
$\Leftrightarrow \quad 22x^2 + 26x - 140 = 0$
$\Leftrightarrow \quad 11x^2 + 13x - 70 = 0$
$\Leftrightarrow \quad (x - 2)(11x + 35) = 0$
$\Leftrightarrow \quad x = 2.$
Hence, required number $= 11x + 2 = 24.$

90. Let the ten's digit be x and unit's digit be y.
Then, number $= 10x + y$.
Number obtained by interchanging the digits $= 10y + x$.
$\therefore \quad (10x + y) + (10y + x)$
$= 11(x + y)$, which is divisible by 11.

91. Let the ten's digit be x and unit's digit be y.
Then, $(10x + y) - (x + y) = 9$ or $x = 1$.
From this data, we cannot find y, the unit's digit.
So, the data is inadequate.

92. Let the ten's digit be x and unit's digit be y.
Then, $(10x + y) - (10y + x) = 36$
$\Leftrightarrow 9(x - y) = 36 \Leftrightarrow x - y = 4.$

93. Let the ten's digit be x and unit's digit be y.
Then, $(10x + y) - (10y + x) = 63$
$\Leftrightarrow 9(x - y) = 63 \Leftrightarrow x - y = 7.$
Thus, none of the numbers can be determined.

94. Let the ten's digit be x and unit's digit be y.
Then, $x + y = \frac{1}{5}[(10x + y) - (10y + x)]$
$\Leftrightarrow 5x + 5y = 9x - 9y \Leftrightarrow 4x = 14y.$
Thus, the value of $(x - y)$ cannot be determined from the given data.

95. Let ten's digit = x. Then, unit's digit = $(12 - x)$.
$\therefore$ $[10x + (12 - x)] - [10(12 - x) + x]$
$= 54 \Leftrightarrow 18x - 108 = 54 \Leftrightarrow 18x = 162 \Leftrightarrow x = 9.$
So, ten's digit = 9 and unit's digit = 3. Hence, original number = 93.

96. Since the number is greater than the number obtained on reversing the digits, so the ten's digit is greater than the unit's digit.
Let the ten's and unit's digits be $2x$ and x respectively.
Then, $(10 \times 2x + x) - (10x + 2x) = 36 \Leftrightarrow 9x = 36 \Leftrightarrow x = 4.$
$\therefore$ Required difference $= (2x + x) - (2x - x) = 2x = 8.$

97. Let ten's digit = x. Then, unit's digit = x^2. Then, number = $10x + x^2$.
Clearly, since $x^2 > x$, so the number formed by interchanging the digits is greater than the original number.
$\therefore$ $(10x^2 + x) - (10x + x^2)$
$= 54 \Leftrightarrow 9x^2 - 9x = 54 \Leftrightarrow x^2 - x$
$= 6 \Leftrightarrow x^2 - x - 6 = 0$
$\Leftrightarrow x^2 - 3x + 2x - 6 = 0$
$\Leftrightarrow x(x - 3) + 2(x - 3) = 0$
$\Leftrightarrow (x - 3)(x + 2) = 0$
$\Leftrightarrow x = 3.$
So, ten's digit = 3, unit's digit = $3^2 = 9$.
$\therefore$ Original number = 39.
Required result = 40% of 39 = 15.6.

98. Let the middle digit be x.
Then, $2x = 10$ or $x = 5$.
So, the number is either 253 or 352.
Since the number increases on reversing the digits, so the hundred's digit is smaller than the unit's digit. Hence, required number = 253.

99. Since the number reduces on reversing the digits, so ten's digit is greater than the unit's digit.
Let the unit's digit be x.
Then, ten's digit = $(x + 1)$.
$\therefore$ $10x + (x + 1) = \frac{5}{6}[10(x + 1) + x] \Leftrightarrow 66x + 6$
$= 55x + 50 \Leftrightarrow 11x = 44 \Leftrightarrow x = 4.$
Hence, required number = 54.

100. Let the two-digit number be $10x + y$.
Then, number formed by reversing the digits = $10y + x$.
Difference of squares of the numbers
$= (10x + y)^2 - (10y + x)^2$
$= (100x^2 + y^2 + 20xy) - (100y^2 + x^2 + 20xy)$
$= 99(x^2 - y^2)$, which is divisible by both 9 and 11

101. Let the unit's digit be x. Then, ten's digit = $(x - 2)$.
$\therefore$ $3[10(x - 2) + x] + \frac{6}{7}[10x + (x - 2)] = 108$
$\Leftrightarrow 231x - 420 + 66x - 12 = 756$
$\Leftrightarrow 297x = 1188$
$\Leftrightarrow x = 4.$
Hence, sum of the digits = $x + (x - 2) = 2x - 2 = 6$.

102. Let the ten's digit be x and unit's digit be y.
Then, $\frac{10x + y}{2} = 10y + (x + 1)$
$\Leftrightarrow$ $10x + y = 20y + 2x + 2$
$\Leftrightarrow$ $8x - 19y = 2$ ...(*i*)
and $x + y = 7$ ...(*ii*)
Solving (*i*) and (*ii*), we get : $x = 5$, $y = 2$. Hence, required number = 52.

103. Let the ten's digit be x.
Then, unit's digit = $2x + 1$.
$[10x + (2x + 1)] - [\{10(2x + 1) + x\} - \{10x + (2x + 1)\}] = 1$
$\Leftrightarrow$ $(12x + 1) - (9x + 9) = 1 \Leftrightarrow 3x = 9 \Leftrightarrow x = 3.$
So, ten's digit = 3 and unit's digit = 7. Hence, original number = 37.

104. Let the ten's digit be x and unit's digit be y.
Then, $10x + y = 3(x + y) \Rightarrow 7x - 2y = 0$ ...(*i*)
$10x + y + 45 = 10y + x \Rightarrow y - x = 5$ ...(*ii*)
Solving (*i*) and (*ii*), we get : $x = 2$ and $y = 7$.
$\therefore$ Required number = 27.

105. Let the ten's and unit's digits be x and $\frac{8}{x}$ respectively.
Then, $\left(10x + \frac{8}{x}\right) + 18 = 10\left(\frac{8}{x} + x\right)$
$\Leftrightarrow 10x^2 + 8 + 18x = 80 + x^2$
$\Leftrightarrow$ $9x^2 + 18x - 72 = 0$
$\Leftrightarrow$ $x^2 + 2x - 8 = 0$
$\Leftrightarrow$ $(x + 4)(x - 2) = 0$
$\Leftrightarrow$ $x = 2.$
So, ten's digit = 2 and unit's digit = 4. Hence, required number = 24.

106. Clearly, there are 4 such numbers: 161, 242, 323 and 404.

107. Let hundred's digit = x.
Then, ten's digit = $(x + 1)$.
Unit's digit = 75% of $(x + 1) = \frac{3}{4}(x + 1)$.
$\therefore$ $(x + 1) + x = 15 \Leftrightarrow 2x = 14 \Leftrightarrow x = 7.$
So, hundreds' digit = 7; ten's digit = 8; unit's digit = $\frac{3}{4}(7 + 1) = \frac{3}{4} \times 8 = 6.$
Hence, required number = 786.

108. Let the two fractions be a and b. Then, $ab = \frac{14}{15}$ and $\frac{a}{b} = \frac{35}{24}$.

$$\frac{ab}{(a/b)} = \left(\frac{14}{15} \quad \frac{24}{35}\right) \Leftrightarrow b^2 = \frac{16}{25} \Leftrightarrow b = \frac{4}{5};$$

$$ab = \frac{14}{15} \Rightarrow a = \left(\frac{14}{15} \quad \frac{5}{4}\right) = \frac{7}{6}.$$

Since $a > b$, so greater fraction is $\frac{7}{6}$.

109. $A = 2B \Rightarrow B = \frac{1}{2}A$. So, $AB = \frac{2}{25}$

$$\Rightarrow \frac{1}{2}A^2 = \frac{2}{25} \Rightarrow A^2 = \frac{4}{25} \Rightarrow A = \frac{2}{5}.$$

110. Let the fraction be $\frac{a}{1}$.

Then, $\frac{1}{a} - a = \frac{9}{20} \Leftrightarrow \frac{1-a^2}{a} = \frac{9}{20}$

$\Leftrightarrow 20 - 20a^2 = 9a$

$\Leftrightarrow 20a^2 + 9a - 20 = 0$

$\Leftrightarrow 20a^2 + 25a - 16a - 20 = 0$

$\Leftrightarrow 5a(4a + 5) - 4(4a + 5) = 0$

$\Leftrightarrow (4a + 5)(5a - 4) = 0 \Leftrightarrow a = \frac{4}{5}$. $\left[\because a \neq -\frac{5}{4}\right]$.

111. Let the fraction be $\frac{x}{y}$.

Then, $x + y = 11$ ...(*i*)

$$\frac{x+1}{y-2} = \frac{2}{3} \Rightarrow 3(x+1)$$

$= 2(y - 2) \Rightarrow 3x - 2y = -7$ ...(*ii*)

Solving (*i*) and (*ii*), we get: $x = 3$ and $y = 8$.

So, the fraction is $\frac{3}{8}$.

112. Let the numerator be x. Then, denominator $= x + 3$.

$$\text{Now, } \frac{x+4}{(x+3)+4} = \frac{4}{5} \Leftrightarrow 5(x+4)$$

$$= 4(x+7) \Leftrightarrow x = 8.$$

So, the fraction is $\frac{8}{11}$.

113. Let the denominator be x.

Then, numerator $= x + 5$.

$$\text{Now, } \frac{x+5}{x} - \frac{x+5}{x+5} = \frac{5}{4} \Leftrightarrow \frac{x+5}{x} = \frac{5}{4} + 1 = \frac{9}{4} = 2\frac{1}{4}.$$

So, the fraction is $2\frac{1}{4}$.

114. Let the fraction be $\frac{2x}{3x}$.

$$\text{Then, } \frac{2x-6}{3x} = \frac{2}{3} \quad \frac{2x}{3x} \Leftrightarrow \frac{2x-6}{3x}$$

$$= \frac{4x}{9x} \Leftrightarrow 18x^2 - 54x = 12x^2$$

$\Leftrightarrow 6x^2 = 54x \Leftrightarrow x = 9$.

Hence, numerator of the original fraction $= 2x = 18$.

115. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x}{y+1} = \frac{1}{2} \Leftrightarrow 2x - y = 1 \quad ...(i)$$

and, $\frac{x+1}{y} = 1 \Leftrightarrow x - y = -1$ ...(*ii*)

Solving (*i*) and (*ii*), we get : $x = 2$, $y = 3$.

Hence, the required fraction is $\frac{2}{3}$.

116. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x+2}{y+3} = \frac{7}{9} \Leftrightarrow 9x - 7y = 3 \quad ...(i)$$

and $\frac{x-1}{y-1} = \frac{4}{5} \Leftrightarrow 5x - 4y = 1$ ...(*ii*)

Solving (*i*) and (*ii*), we get : $x = 5$, $y = 6$.

Hence, the original fraction is $\frac{5}{6}$.

117. Let the fraction be $\frac{x}{y}$. Then,

$$\frac{x+\frac{1}{4}}{y-\frac{1}{3}} = \frac{33}{64} \Leftrightarrow \frac{3(4x+1)}{4(3y-1)} = \frac{33}{64} \Leftrightarrow \frac{4x+1}{3y-1} = \frac{33}{64} \quad \frac{4}{3} = \frac{11}{16}$$

$\Leftrightarrow 16(4x + 1) = 11(3y - 1)$

$\Leftrightarrow 64x + 16 = 33y - 11$

$\Leftrightarrow 64x - 33y = -27$, which cannot be solved to find $\frac{x}{y}$.

Hence, the original fraction cannot be determined from the given data.

118. Let the fraction be $\frac{x}{y}$.

$$\text{Then, } \frac{x + 200\% \text{ of } x}{y + 300\% \text{ of } y} = \frac{15}{26} \Leftrightarrow \frac{3x}{4y} = \frac{15}{26} \Leftrightarrow \frac{x}{y} = \frac{15}{26} \quad \frac{4}{3} = \frac{10}{13}.$$

119. Let the fraction be $\frac{x}{y}$.

$$\text{Then, } \frac{x+4}{y} - \frac{x}{y} = \frac{2}{3} \Leftrightarrow \frac{4}{y} = \frac{2}{3} \Leftrightarrow y = \left(\frac{4}{2} \quad 3\right) = 6.$$

$\therefore$ Denominator $= 6$.

120. Let the fraction be $\frac{x}{y}$.

$$\text{Then, } \frac{110\% \text{ of } 2x}{70\% \text{ of } 3y} = 11\% \text{ of } \frac{16}{21} \Leftrightarrow \frac{22x}{21y} = \frac{11}{100} \quad \frac{16}{21}$$

$$\Leftrightarrow \frac{x}{y} = \left(\frac{11}{100} \quad \frac{16}{21} \quad \frac{21}{22}\right) = \frac{2}{25}.$$

121. Let the two parts be $(54 - x)$ and x.

Then, $10(54 - x) + 22x = 780 \Leftrightarrow 12x = 240 \Leftrightarrow x = 20$.

$\therefore$ Bigger part $= (54 - x) = 34$.

122. Let the three parts be A, B and C.

Let $\frac{A}{2} = \frac{B}{3} = \frac{C}{4} = x$.

Then, $A = 2x$, $B = 3x$ and $C = 4x$.

So, $A : B : C = 2 : 3 : 4$.

$\therefore$ Largest part $= \left(243 \quad \frac{4}{9}\right) = 108$.

123. Let the four numbers be A, B, C and D.

Let $A + 3 = B - 3 = 3C = \frac{D}{3} = x$.

Then, $A = x - 3$, $B = x + 3$, $C = \frac{x}{3}$ and $D = 3x$.

$$A + B + C + D = 64 \Rightarrow (x-3) + (x+3) + \frac{x}{3} + 3x = 64$$

$$\Rightarrow 5x + \frac{x}{3} = 64 \Rightarrow 16x = 192 \Rightarrow x = 12.$$

Thus, the numbers are 9, 15, 4 and 36.

$\therefore$ Required difference $= (36 - 4) = 32$.

124. Let the numbers be a, b and c. Then, $a^2 + b^2 + c^2 = 138$ and $(ab + bc + ca) = 131$.

$(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca) = 138 + 2 \times 131 = 400$

$\Rightarrow (a + b + c) = \sqrt{400} = 20$.

125. $A : B = 2 : 3$ and $B : C = 5 : 3 = \frac{3}{5} \quad 5 : \frac{3}{5} \quad 3 = 3 : \frac{9}{5}$.

So, $A : B : C = 2 : 3 : \frac{9}{5} = 10 : 15 : 9$.

$\therefore$ Second number $= \left(136 \quad \frac{15}{34}\right) = 60$.

126. Let the numbers be x, y and z.

Then, $x + y = 73$, $y + z = 77$ and $3x + z = 104$.

$\therefore$ $y = 73 - x$, $z = 77 - y = 77 - (73 - x) = 4 + x$.

$\therefore$ $3x + 4 + x = 104 \Leftrightarrow 4x = 100 \Leftrightarrow x = 25$.

$y = (73 - 25) = 48$ and $z = (4 + 25) = 29$.

$\therefore$ Third number $= 29$.

127. Let two numbers be a and b

Given $ab = 5$ and $a = \frac{3}{2}$

$\Rightarrow b = \frac{5}{a}$

$b = \frac{5}{\frac{3}{2}} = \frac{5 \quad 2}{3} = \frac{10}{3}$

$\therefore$ Required sum of $a + b = \frac{3}{2} + \frac{10}{3}$

LCM of 2 and 3 $= 6$

$$= \frac{9+20}{6} = \frac{29}{6} = 4\frac{5}{6}$$

128. Let the positive integers be a and b where $a > b$.

According to the question,

$a^2 + b^2 = 100$ ....(i)

$a^2 - b^2 = 28$ ....(ii)

By adding (i) and (ii), we get

$\therefore a^2 + b^2 + a^2 - b^2 = 100 + 28$

$\Rightarrow 2a^2 = 128$

$\Rightarrow a^2 = \frac{128}{2} = 64$

$\therefore a = \sqrt{64} = 8$

From equation (i).

$8^2 + b^2 = 100$

$\Rightarrow b^2 = 100 - 64 = 36$

$\Rightarrow b = \sqrt{36} = 6$

$\therefore a + b = 8 + 6 = 14$

129. Let the numbers be a and b where $a > b$.

According to the question,

$a + b = 37$ and $a^2 - b^2 = 185$

$\Rightarrow (a+b)(a-b) = 185$

$\Rightarrow 37(a-b) = 185$

$\Rightarrow a - b = \frac{185}{37} = 5$

130. Let the total number of eggs bought be a.

10% of eggs are rotten.

$\therefore$ Remaining eggs

$$= a - 10\% \text{ of } a = a - \frac{10a}{100} = \frac{100a - 10a}{100} = \frac{90a}{100} = \frac{9a}{10}$$

Man gives 80% of $\frac{9a}{100}$ eggs to his neighbour

$$= \frac{80}{100} \quad \frac{9a}{10} = \frac{72a}{100}$$

Remaining eggs $= \frac{9a}{10} - \frac{72a}{100} = \frac{90a - 72a}{100} = \frac{18a}{100} = \frac{9a}{50}$

According to the question.

$\frac{9a}{50} = 36 \Rightarrow 9a = 36 \quad 50$

$\Rightarrow a = \frac{36 \quad 50}{9} = 200$

Hence the total number of eggs. bought be 200.

131. Let the numbers be a and b.

According to the question.

$a + b = 75$

$a - b = 25$

$\because (a+b)^2 - (a-b)^2 = 4ab$

$\Rightarrow 75^2 - 25^2 = 4ab$

$4ab = (75 + 25)(75 - 25)$

$\left[\because a^2 - b^2 = (a+b)(a-b)\right]$

$\Rightarrow 4ab = 100 \quad 50$

$\Rightarrow ab = \frac{100 \quad 50}{4} = 1250$

132. Let the five successive odd number be,

$x, x + 2, x + 4, x + 6, x + 8$

Then, according to given information

$185 = x + x + 2 + x + 4 + x + 6 + x + 8$

$\Rightarrow 185 = 5x + 20$

$\Rightarrow 5x = 185 - 20 = 165$

$\Rightarrow x = 33$

Highest number = 33 + 8 = 41

133. Let the numbers be a and b where $a > b$.

According to the questions,

$a - b = 10$ .....(i)

And $\frac{a+b}{5} = 8$

By cross multiplying, we get

$\Rightarrow a + b = 40$ ...(ii)

By subtracting equation (ii) from (i) we get

$2b = 40 - 10 = 30$

$\Rightarrow b = \frac{30}{2} = 15$

And from (i)

$a = 10 + 15 = 25$

$\Rightarrow a = 23$

EXERCISE

(DATA SUFFICIENCY TYPE QUESTIONS)

Directions (Questions 1 to 15): Each of the questions given below consists of a statement and/or a question and two statements numbered I and II given below it. You have to decide whether the data provided in the statement(s) is/are sufficient to answer the question. Read both the statements and

Give answer (a) if the data in Statement I alone are sufficient to answer the question, while the data in Statement II alone are not sufficient to answer the question;

Give answer (b) if the data in Statement II alone are sufficient to answer the question, while the data in Statement I alone are not sufficient to answer the question;

Give answer (c) if the data either in Statement I or in Statement II alone are sufficient to answer the question;

Give answer (d) if the data even in both Statements I and II together are not sufficient to answer the question;

Give answer (e) if the data in both Statements I and II together are necessary to answer the question.

1. What is the two-digit number? **(Bank P.O., 2008)**

I. The difference between the two digits is 9.

II. The sum of the digits is equal to the difference between the two digits.

2. What is the value of the two-digit number ab?

I. The difference between its digits is 2.

II. The sum of its digits is 4. **(M.A.T., 2005)**

3. What is the two-digit number where the digit at the unit's place is smaller?

I. The difference between the two digits is 5. **(Bank P.O., 2006)**

II. The sum of the two digits is 7.

4. How much is four-fifths of the number? **(Bank P.O., 2009)**

I. Three-fourths of the number is 2.5 less than its four-fifths.

II. Half of the number added to it is 75.

5. What is the smaller of the two numbers?

I. The difference between these two numbers is one-third of the greater number.

II. The sum of these two numbers is 30.

6. What is the two-digit number? **(Bank P.O., 2009)**

I. Sum of the digits is 6.

II. Digit in the ten's place is double the digit in the unit's place.

7. What is the difference between the digits of a two-digit number? **(M.A.T., 2007)**

I. The sum of the digits of that number is 8.

II. One-fifth of that number is 15 less than half of 44.

8. What is the three-digit number? **(Bank P.O., 2008)**

I. Two-fifth of that number is less than half of that number by 20.

II. One-fourth of that number is 25% of that number.

9. What is the difference between two two-digit numbers? **(Bank. P.O., 2010)**

I. The square of the first number is 9 times the second number.

II. The ratio of the first number to the second number is 3 : 4.

10. What is the third number of 8 consecutive real numbers? **(M.A.T., 2001)**

I. Product of the numbers is 34,459,425.

II. Sum of numbers is 84.

11. What is the ratio between the two numbers?

I. The sum of two numbers is twice their difference.

II. The smaller number is 6.

12. What is the two-digit number whose first digit is a and the second digit is b? The number is greater than 9. **(M.A.T., 2000)**

I. The number is a multiple of 51.

II. The sum of the digits a and b is 6.

13. What is the two-digit number? **(SIDBI, 2006)**

I. The sum of the two digits of the number is 13.

II. The number obtained by interchanging the two digits of the number is smaller than the original number by 45.

14. What is the original number? **(M.B.A., 2007)**

I. Sum of the two digits of a number is 10. The ratio between the two digits is 1 : 4.

II. Product of two digits of a number is 16 and quotient of two digits is 4.

15. What is the value of the two-digit number? **(Bank P.O., 2009)**

I. The product of the digits is 72 and the difference between the digits is 1.

II. The digit at the unit place is greater than the other.

Directions (Questions 16 to 22): ***Each of the questions given below consists of a question followed by three statements. You have to study the question and the statements and decide which of the statement(s) is/are necessary to answer the given question.***

16. What is the two-digit number? **(M.B.A., 2002)**

I. Sum of the digits is 7.

II. Difference between the number and the number obtained by interchanging the digits is 9.

III. Digit in the ten's place is bigger than the digit in the unit's place by 1.

(*a*) I and II only (*b*) II and III only

(*c*) I and III only (*d*) All I, II and III

(*e*) None of these

17. What is the sum of the digits of the two-digit number?

I. The ratio between the ten's digit and unit's digit of the number is 3 : 2.

II. The number obtained on revering the order of its digits is 18 less than the original number.

III. The product of the digits is 24.

(*a*) Any two of the three (*b*) I only or II and III only

(*c*) All I, II and III (*d*) I and II only

(*e*) None of these

18. What will be the sum of two numbers?

I. Among the two numbers, the bigger number is greater than the smaller number by 6.

II. 40% of the smaller number is equal to 30% of the bigger number.

III. The ratio between half of the bigger number and one-third of the smaller number is 2 : 1.

(*a*) I and II only (*b*) II and III only

(*c*) All I, II and III (*d*)Any two of the three

(*e*) None of these

19. What is the two-digit number? **(M.A.T., 2005)**

I. The difference between the two-digit number and the number formed by interchanging the digits is 27.

II. The difference between the two digits is 3.

III. The digit at unit's place is less than that at ten's place by 3.

(*a*) I and II only (*b*) I and III only

(*c*) All I, II and III (*d*) I, and either II or III

(*e*) Even with all I, II and III, answer cannot be given.

20. What is the two-digit number? **(Bank P.O., 2004)**

I. Digit in the ten's place is cube of the digit in unit's place.

II. Digit in the ten's place is four times the digit in the unit's place.

III. The two digits are not equal.

(*a*) I and II only (*b*) I and III only

(*c*) Any two of the three (*d*) I and either II or III only

(*e*) None of these

21. Find three positive consecutive even numbers. **(M.A.T., 2006)**

I. The average of four consecutive even numbers starting from the last of the given numbers is 17.

II. The difference of the highest and the lowest numbers is 4.

III. The sum of the squares of the three numbers is 440.

(*a*) I only (*b*) I and II only

(*c*) III only (*d*) Either I or III

22. What is the two-digit number? **(Bank P.O., 2006)**

I. The number obtained by interchanging the digits of the number is greater than the original number by 18.

II. Sum of the digits of the number is 14.

III. Difference between the two digits of the number is 2.

(*a*) Any two of the three (*b*) Only I and III

(*c*) II and either I or III (*d*) III and either I or II

(*e*) All of these

ANSWERS

1. (*a*)	**2.** (*d*)	**3.** (*e*)	**4.** (*c*)	**5.** (*e*)	**6.** (*e*)	**7.** (*b*)	**8.** (*a*)	**9.** (*e*)	**10.** (*b*)
11. (*a*)	**12.** (*a*)	**13.** (*e*)	**14.** (*b*)	**15.** (*e*)	**16.** (*e*)	**17.** (*a*)	**18.** (*e*)	**19.** (*e*)	**20.** (*a*)
21. (*d*)	**22.** (*c*)								

SOLUTIONS

1. I. Two digits with difference 9 are 9 and 0. And, the two-digit number formed using 9 and 0 is 90.

II. Let the ten's and unit's digits be x and y respectively.
Then, $x - y = x + y \Leftrightarrow 2y = 0 \Leftrightarrow y = 0$.
So, the ten's digit cannot be determined.
Thus, I only gives the answer, while II does not.
$\therefore$ The correct answer is (*a*).

2. I. gives, $a - b = 2$ …(*i*)
or $b - a = 2$ …(*ii*)

II. gives, $a + b = 4$ …(*iii*)
Solving (*i*) and (*iii*), we get : $a = 3$ and $b = 1$.
Solving (*ii*) and (*iii*), we get : $a = 1$ and $b = 3$.
So, the required number is either 13 or 31.
Thus, even both I and II together do not give the answer.
$\therefore$ The correct answer is (*d*).

3. Let the ten's and unit's digits be x and y respectively, where $x > y$.

I. gives, $x - y = 5$ ...(*i*)

II. gives, $x + y = 7$ ...(*ii*)

Solving (*i*) and (*ii*), we get : $x = 6$ and $y = 1$. So, the required number is 61.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

4. Let the required number be x.

I. $\frac{4}{5}x - \frac{3}{4}x = 2.5 \Leftrightarrow \frac{x}{20} = 2.5 \Leftrightarrow x = 50.$

So, $\frac{4}{5}x = \left(\frac{4}{5} \text{ of } 50\right) = 40.$

II. $x + \frac{x}{2} = 75 \Leftrightarrow \frac{3x}{2} = 75 \Leftrightarrow x = \left(\frac{75}{3} \text{ of } 2\right) = 50.$

So, $\frac{4}{5}x = \left(\frac{4}{5} \text{ of } 50\right) = 40.$

Thus, either I or II alone gives the answer.

$\therefore$ The correct answer is (*c*).

5. **II.** Let the greater number be x. Then, smaller number $= (30 - x)$.

I. $x - (30 - x) = \frac{x}{3} \Leftrightarrow 2x - 30 = \frac{x}{3} \Leftrightarrow 6x - 90 = x$

$\Leftrightarrow 5x = 90 \Leftrightarrow x = 18.$

So, smaller number $= 30 - 18 = 12$.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

6. Let the ten's and unit's digits be x and y respectively.

I. $x + y = 6$ ...(*i*)

II. $x = 2y$ ...(*ii*)

Solving (*i*) and (*ii*), we get : $x = 4$, $y = 2$. So, the required number is 42.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

7. **I.** Let the ten's and unit's digits of the number be a and b respectively.

Then, $a + b = 8$.

II. Let the required number be x.

Then, $\frac{x}{5} = \left(\frac{1}{2} \text{ of } 44\right) - 15 = 7 \Leftrightarrow x = 35.$

So, the required number is 35.

Thus, II alone gives the answer.

$\therefore$ The correct answer is (*b*).

8. Let the required number be x.

I. $\frac{x}{2} - \frac{2x}{5} = 20 \Leftrightarrow \frac{5x - 4x}{10} = 20 \Leftrightarrow \frac{x}{10} = 20 \Leftrightarrow x = 200.$

II. $\frac{x}{4} = 25\% \text{ of } x \Leftrightarrow \frac{x}{4} = \frac{x}{4}.$

Thus, I alone gives the answer.

$\therefore$ The correct answer is (*a*).

9. **II.** Let the two numbers be $3x$ and $4x$.

I. $(3x)^2 = 9 \times 4x \Leftrightarrow 9x^2 = 36x \Leftrightarrow x = 4.$

So, the numbers are 12 and 16.

$\therefore$ Required difference $= 16 - 12 = 4$.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

10. Let the 8 consecutive real numbers be x, $(x + 1)$, $(x + 2)$, $(x + 3)$, $(x + 4)$, $(x + 5)$, $(x + 6)$ and $(x + 7)$.

I. gives, $x(x + 1)(x + 2)(x + 3)(x + 4)(x + 5)(x + 6)(x + 7) = 34459425$.

This equation cannot be solved for x.

II. gives, $x + (x + 1) + (x + 2) + (x + 3) + (x + 4) + (x + 5) + (x + 6) + (x + 7) = 84$

$\Leftrightarrow 8x + 28 = 84 \Leftrightarrow 8x = 56 \Leftrightarrow x = 7.$

$\therefore$ Third number $= x + 2 = 7 + 2 = 9$.

Thus, II alone gives the answer.

$\therefore$ The correct answer is (*b*).

11. Let the two numbers be x and y.

I. gives, $x + y = 2(x - y) \Leftrightarrow x = 3y$

$\Leftrightarrow \frac{x}{y} = \frac{3}{1} \Leftrightarrow x : y = 3 : 1.$

Thus, I only gives the answer.

II. does not give the answer.

$\therefore$ Correct answer is (*a*).

12. The only two-digit number which is a multiple of 51, is 51. So, I alone gives the answer while II alone does not.

$\therefore$ The correct answer is (*a*).

13. Let the ten's digit be x and the unit's digit be y.

Then, number $= 10x + y$.

I. $x + y = 13 \Leftrightarrow y = (13 - x)$.

So, number $= 10x + (13 - x)$.

II. $[10x + (13 - x)] - [10(13 - x) + x] = 45$

$\Leftrightarrow (9x + 13) - (130 - 9x) = 45$

$\Leftrightarrow 18x = 162 \Leftrightarrow x = 9.$

$y = 13 - x = 13 - 9 = 4$.

So, required number $= 94$.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

14. Let the ten's and unit's digits be x and y respectively. Then,

I. $x + y = 10$ and $\frac{x}{y} = \frac{1}{4}.$

II. $xy = 16$ and $\frac{x}{y} = \frac{4}{1}.$

$\therefore$ II gives, $x^2 = 64 \Leftrightarrow x = 8$.

So, $4y = 8 \Leftrightarrow y = 2$.

Thus, II alone gives the answer while I alone does not.

$\therefore$ The correct answer is (*b*).

15. Let the ten's digit be x and the unit's digit be y.

II. $y > x$.

I. $xy = 72$ and $y - x = 1$ or $y = x + 1$

$\Leftrightarrow x(x + 1) = 72 \Leftrightarrow x^2 + x - 72 = 0$

$\Leftrightarrow x^2 + 9x - 8x - 72 = 0$

$\Leftrightarrow x(x + 9) - 8(x + 9) = 0$

$\Leftrightarrow (x + 9)(x - 8) = 0 \Leftrightarrow x = 8.$

So, $y = x + 1 = 9$

$\therefore$ Required number $= 89$.

Thus, both I and II together give the answer.

$\therefore$ The correct answer is (*e*).

16. Let the ten's and unit's digit be x and y respectively.

I. $x + y = 7$.

II. $(10x + y) - (10y + x) = 9 \Rightarrow x - y = 1.$

III. $x - y = 1.$

Thus, I and II as well as I and III give the answer.

$\therefore$ Correct answer is (*e*).

17. **I.** Let the ten's and unit's digit be $3x$ and $2x$ respectively.

II. $(30x + 2x) - (20x + 3x) = 18 \Leftrightarrow x = 2.$

III. $3x \times 2x = 24 \Leftrightarrow x^2 = 4 \Leftrightarrow x = 2.$

Thus, any two of the three will give the answer.

$\therefore$ Correct answer is (*a*).

18. Let the required numbers be x and y, where $x > y$.

I. $x - y = 6$ ...(*i*)

II. $\frac{30}{100}x = \frac{40}{100}y \Leftrightarrow 3x - 4y = 0$ ...(*ii*)

III. $\frac{\frac{1}{2}x}{\frac{1}{3}y} = \frac{2}{1} \Leftrightarrow \frac{3x}{2y} = \frac{2}{1} \Leftrightarrow \frac{x}{y} = \frac{4}{3} \Leftrightarrow 3x - 4y = 0$ ...(*iii*)

So, we may solve (*i*) and (*ii*) or (*i*) and (*iii*) together to find x and y.

Thus, I, and either II or III together give the answer.

$\therefore$ Correct answer is (*e*).

19. Let the ten's and unit's digit be x and y respectively.

I. $(10x + y) - (10y + x) = 27 \Leftrightarrow x - y = 3.$

II. $x - y = 3.$

III. $x - y = 3.$

Thus, even all the given three statements together do not give the answer.

$\therefore$ Correct answer is (*e*).

20. Let the ten's digit be x and the unit's digit be y.

I. $x = y^3$ ...(*i*)

II. $x = 4y$ ...(*ii*)

III. $x \neq y$ ...(*iii*)

From (*i*) and (*ii*), we have : $y^3 = 4y \Leftrightarrow y^3 - 4y = 0$

$\Leftrightarrow y(y^2 - 4) = 0$

$\Leftrightarrow y^2 - 4 = 0$ [$\because y \neq 0$]

$\Leftrightarrow y^2 = 4 \Leftrightarrow y = 2.$

So, $x = y^3 = 2^3 = 8.$

$\therefore$ The required number is 82.

Thus, I and II together give the answer.

$\therefore$ Correct answer is (*a*).

21. Let the three consecutive even numbers be x, $(x + 2)$ and $(x + 4)$.

I. $\frac{(x+4)+(x+6)+(x+8)+(x+10)}{4} = 17$

$\Leftrightarrow 4x + 28 = 68 \Leftrightarrow 4x = 40 \Leftrightarrow x = 10.$

So, the required numbers are 10, 12 and 14.

II. $(x + 4) - x = 4 \Leftrightarrow 4 = 4.$

So, the value of x cannot be determined.

III. $x^2 + (x + 2)^2 + (x + 4)^2 = 440$

$\Leftrightarrow x^2 + x^2 + 4 + 4x + x^2 + 16 + 8x = 440$

$\Leftrightarrow 3x^2 + 12x - 420 = 0$

$\Leftrightarrow x^2 + 4x - 140 = 0$

$\Leftrightarrow x^2 + 14x - 10x - 140$

$\Leftrightarrow x(x + 14) - 10(x + 14) = 0$

$\Leftrightarrow (x + 14)(x - 10) = 0$

$\Leftrightarrow x = 10.$

So, the required numbers are 10, 12 and 14.

Thus, I alone or III alone gives the answer.

$\therefore$ Correct answer is (*d*).

22. Let the ten's digit be x and unit's digit be y.

(I and II). $x + y = 14$ or $y = (14 - x)$ ...(*i*)

And, $[10(14 - x) + x] - [10x + (14 - x)]$

$= 18 \Leftrightarrow (140 - 9x) - (9x + 14) = 18$

$\Leftrightarrow 18x = 108 \Leftrightarrow x = 6.$

So, $y = 14 - 6 = 8.$

$\therefore$ Required number = 68.

(II and III). $x + y = 14$ ...(*ii*)

and $x - y = \pm 2$ ...(*iii*)

Solving (*ii*) and (*iii*), we get : $x = 6$ or 8.

If $x = 6$, $y = 8$ & If $x = 8$, $y = 6$.

$\therefore$ Required number is either 68 or 86.

(I and III). Since the number obtained by interchanging the digits is greater, the ten's digit is smaller than the unit's digit.

$x + y = 14$ ...(*iv*)

And, $y - x = 2$ ...(*v*)

Solving (*iv*) and (*v*), we get : $y = 8.$

So, $x = 14 - y = 6.$

$\therefore$ Required number = 68.

Thus, II and either I or III gives the answer.

$\therefore$ Correct answer is (*c*).