



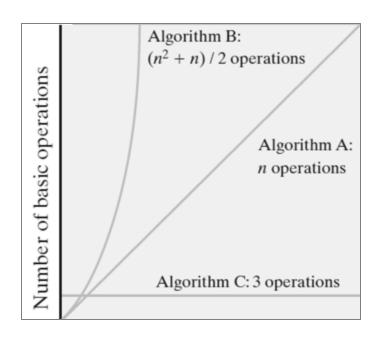
B1.3 The Big O Notation



Big O Notation



Computer scientists use a notation to represent an algorithm's complexity



- Algorithm A has a time requirement proportional to n
- Algorithm B has a time requirement proportional to n²
- Algorithm C has a constant time requirement

- We would instead say that Algorithm A is O(n), Algorithm B is $O(n^2)$, and Algorithm C is O(1)
- This is known as Big O Notation (read "Big Oh of n" or "order of n")

Big O Notation



- A means of expressing the runtime of an application
 - in terms of how quickly it grows,
 - relative to the input,
 - as the input get arbitrarily large

Constant time



```
public static void printFirstItem(int[] items) {
    System.out.println(items[0]);
}
```

- No matter what size the input array is, the execution time will always be the same
 - O(1) time

Linear time



```
public static void printAllItems(int[] items) {
   for (int item : items) {
     System.out.println(item);
   }
}
```

- Execution time is directly proportional to the size of the input array
 - O(n) time





```
public static void printAllorderedPairs(int[] items) {
   for (int first : items) {
      for (int second : items) {
        System.out.println(first + ", " + second);
      }
   }
}
```

- Execution time is directly proportional to the square of the size of the input array
 - $O(n^2)$ time





```
public static void printAllItemsTwice(int[] items) {
   for (int item : items) {
      System.out.println(item);
   }
   for (int item : items) {
      System.out.println(item);
   }
}
```

- Execution time is still directly proportional size of the input array
 - O(n) time even though there are 2n operations



Use the most significant term

```
public static void printPairsThenItems(int[] items) {
   for (int first : items) {
      for (int second : items) {
          System.out.println(first + ", " + second);
   for (int item : items) {
      System.out.println(item);
```

- Execution time is still directly proportional to the square of the size of the input array
 - $O(n^2)$ time even though there are $n^2 + n$ operations



Efficiency of Implementations of Bag ADT

Operation	Fixed-size Array	Linked Chain
add(newEntry)	O(1)	O(1)
remove()	O(1)	O(1)
remove (anEntry)	O(1), O(n), O(n)	O(1), O(n), O(n)
clear()	O(n)	O(n)
<pre>getFrequencyOf()</pre>	O(n)	O(n)
contains()	O(1), O(n), O(n)	O(1), O(n), O(n)
toString()	O(n)	O(n)
<pre>getCurrentSize()</pre>	O(1)	O(1)



Challenge

Prove the time complexity of the LinkedList add and remove operations

- Add a new class called ListComplexityTest to the Analysis project
- The main() method of ListComplexityTest should create a new LinkedList of Integer objects and generate N random integers < N*10, storing each in the LinkedList as it is generated.
- For each integer generated, measure the time taken in nanoseconds to store the element in the LinkedList and obtain the total time taken to add the elements.
- Now generate a further N random integers in the same range and attempt to remove an
 element of that value from the LinkedList, again calculating the total time to remove.
- Repeat for values of N of 10, 100, 1000, 10000 and 100000 elements and report for each value
 of N, the total time to add, the average time to add, the total time to remove and the average
 time to remove.