

For geometric series $= 1 + r + r^2 + \dots \infty$

① Convergent if $|r| \leq 1$

② Divergent if $|r| > 1$

③ Oscillatory if $r \leq -1$

Eg: ① G.P. $= 1 + \frac{1}{2} + \frac{1}{4} + \dots \infty$

Sol: Here, $r = \frac{1/2}{1} = \frac{1}{2}$

$\therefore r \leq 1 \Rightarrow$ G.P is convergent

② G.P: $1 - \frac{1}{3} + \frac{1}{3^2} + \dots \infty$

Sol: Here, $r = \frac{-1/3}{1} = -\frac{1}{3}$

$\therefore r \leq 1 \Rightarrow$ G.P is convergent

③ G.P: $2 + 4 + 8 + \dots \infty$

Sol: Here, $r = 2$

$\therefore r > 1 \Rightarrow$ G.P is divergent

④ G.P: $-2 + (-2)^2 + (-2)^3 + \dots \infty$

Sol: Here, $r = -2$

$\therefore r \leq -1 \Rightarrow$ G.P is oscillatory