

Privacy Preserving Data Publishing (PPDP)

From k -Anonymity to t -closeness



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Content

- **Motivation** of privacy preserving data publishing
 - Background
 - Privacy attack instances
- Existing **solutions**
 - k -Anonymity
 - L -Diversity
 - T -Closeness
- Challenges and Emerging Applications
- **Conclusion**

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Content

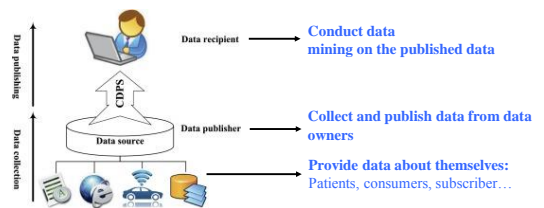
- **Lots of data is being collected and warehoused**
 - Web data, e-commerce
 - purchases at department/grocery stores
 - Bank/Credit Card transactions
 - Social Network
 - Hospital



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Motivation of PPDP

- Data collection and data publishing



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Motivation of PPDP

- There are two models of data holders:
 - In the **untrusted model**, the data holder is **not trusted** and may attempt to identify sensitive information from record owners.
 - In the **trusted model**, the data holder is **trustworthy** and record owners are willing to provide their personal information to the data holder;
 - however, the trust is not transitive to the data recipient.

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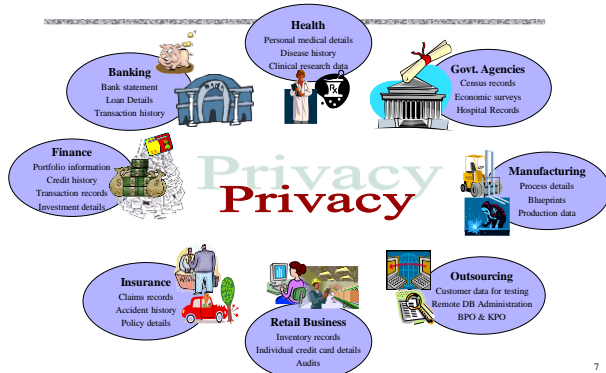
Application Data Publish for Business

- Uncovering findings from data, help enable companies to **make smarter business decisions**:
 - Netflix data mines movie viewing patterns to understand what drives user interest, and uses that to make decisions on which Netflix original series to produce.
 - Target identifies what are major customer segments within it's base and the unique shopping behaviors within those segments, which helps to guide messaging to different market audiences.
 - Proctor & Gamble utilizes time series models to more clearly understand future demand, which help plan for production levels more optimally.

NETFLIX



Motivation of PPDP



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Motivation of PPDP

- Objectives of PPDP
 - The privacy of the contributors are **protected**
 - The recipient gets **useful data**

Privacy



Data Utility

Prohibit the disclosure or misuse of sensitive information about private individuals:

- SSN
- Disease
- ...

Many types of research rely on the availability of private data:

- Demographic research
- Medical research
- Social network studies
- Web search studies

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Government Regulations of Privacy

| Country | Privacy Legislation |
|----------------|--|
| Australia | Privacy Amendment Act of 2000 |
| European Union | Personal Data Protection Directive 1998 |
| Hong Kong | Personal Data (Privacy) Ordinance of 1995 |
| United Kingdom | Data Protection Act of 1998 |
| United States | Security Breach Information Act (S.B. 1386) of 2002 Gramm-Leach-Bliley Act of 1999 Health Insurance Portability and Accountability Act of 1996 |

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What About Privacy?

- In PPDP, the following three components need to be defined.
 - **Sanitization mechanism:** Given an original data set, a sanitization mechanism sanitizes the data set by making the data less precise. We call such a snapshot a release candidate.
 - **Privacy criterion:** Given a release candidate, the privacy criterion defines whether the release candidate is safe for release or not.
 - **Utility metric:** Given a release candidate, the utility metric quantifies the utility of the release candidate.

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What About Privacy?

- **First thought:** anonymize the data
- **How?**
- Remove “personally identifying information” (PII)
 - Name, Social Security number, phone number, email, address... what else?
 - Anything that identifies the person directly

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Quasi-Identifiers

- Key attributes
 - Name, address, phone number - uniquely identifying!
 - Always removed before release
- Quasi-identifiers
 - (5-digit ZIP code, birth date, gender) uniquely identify 87% of the population in the U.S.
 - Can be used for linking anonymized dataset with other datasets

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Quasi-Identifiers

- Definition of Quasi-identifier:
 - A set of **non-sensitive** attributes $\{Q_1, Q_2, \dots, Q_w\}$ of a table is called a **quasi-identifier** if these attributes can be linked with external data to uniquely identify at least one individual in the general population Ω .

Classification of Attributes

Sensitive attributes

- Medical records, salaries, etc.
- These attributes is what the researchers need, so they are always released directly

| Key Attribute | Quasi-identifier | | | Sensitive attribute |
|---------------|------------------|--------|---------|---------------------|
| Name | DOB | Gender | Zipcode | Disease |
| Andre | 1/21/76 | Male | 53715 | Heart Disease |
| Beth | 4/13/86 | Female | 53715 | Hepatitis |
| Carol | 2/28/76 | Male | 53703 | Brochitis |
| Dan | 1/21/76 | Male | 53703 | Broken Arm |
| Ellen | 4/13/86 | Female | 53706 | Flu |
| Eric | 2/28/76 | Female | 53706 | Hang Nail |

What About Privacy?

- First thought:** anonymize the data
- How?**
- Remove “personally identifying information” (PII)
- Problem: Is this enough?**

Privacy Breach Example

Problem: Re-identification by Linking

Microdata: sensitive personal data held by an organization, e.g. medical records, transaction history. Often open to public access for reasons such as research.

| Microdata | | | | | Voter registration data | | | |
|-----------|---------|-----|-----|-----------------|-------------------------|---------|-----|-----|
| ID | QID | | | SA | Name | Zipcode | Age | Sex |
| Name | Zipcode | Age | Sex | Disease | | | | |
| Alice | 47677 | 29 | F | Ovarian Cancer | Alice | 47677 | 29 | F |
| Betty | 47602 | 22 | F | Ovarian Cancer | Bob | 47983 | 65 | M |
| Charles | 47678 | 27 | M | Prostate Cancer | Carol | 47677 | 22 | F |
| David | 47905 | 43 | M | Flu | Dan | 47532 | 23 | M |
| Emily | 47909 | 52 | F | Heart Disease | Ellen | 46789 | 43 | F |
| Fred | 47906 | 47 | M | Heart Disease | | | | |

Privacy Breach Example

Latanya Sweeney's Attack (1997):

Massachusetts hospital discharge dataset

| Medical Data Released as Anonymous | | | | | | | |
|------------------------------------|-------|----------|---------------|-------|----------|---------------------|---------|
| SSN | Name | Race | Date Of Birth | Sex | ZIP | Marital Status | Problem |
| | asian | 09/23/64 | female | 02139 | divorced | hypertension | |
| | asian | 09/30/64 | female | 02139 | divorced | obesity | |
| | asian | 04/19/64 | male | 02139 | married | chest pain | |
| | black | 03/13/63 | male | 02138 | married | hypertension | |
| | black | 03/19/63 | male | 02138 | married | shortness of breath | |
| | black | 09/13/64 | male | 02141 | married | shortness of breath | |
| | black | 09/07/64 | female | 02141 | married | obesity | |
| | white | 05/14/61 | male | 02138 | single | chest pain | |
| | white | 05/09/61 | male | 02138 | single | obesity | |
| | white | 09/13/61 | female | 02142 | widow | shortness of breath | |

Voter List

| Name | Address | City | ZIP | DOB | Sex | Party |
|----------------|--------------|-----------|-------|---------|--------|----------|
| Eue J. Carlson | 140 Main St. | Cambridge | 02148 | 9/19/61 | female | democrat |

Figure 1: Re-identifying anonymous data by linking to external data

Public voter dataset

Lessons Learned

- Any information released by the data curator can potentially be exploited by the adversary
- Solution?
 - Publish a **modified** version of the data, such that:
 - the contributors' privacy is "adequately" protected
 - the published data is useful for its intended purpose(at least to some degree)
- Two issues:
 - Privacy principle:** what do we mean by "adequately" protected privacy?
 - Modification method:** how should we modify the data to ensure privacy while maximizing utility?

Lessons Learned

- Any information released by the data curator can potentially be exploited by the adversary
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 - Publish a **modified** version of the data, such that:
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Existing solutions

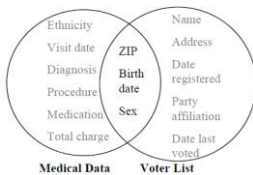
- Table 2.1 summarizes the attack models addressed by the privacy models.

Table 2.1: Privacy models

| Privacy Model | Attack Model | | | |
|---------------------------------------|----------------|-------------------|---------------|----------------------|
| | Record linkage | Attribute linkage | Table linkage | Probabilistic attack |
| k-Anonymity [201, 217] | ✓ | | | |
| MultiIR k-Anonymity [178] | ✓ | | | |
| ℓ -Diversity [162] | ✓ | ✓ | | |
| Confidence Bounding [237] | ✓ | ✓ | | |
| (α, k) -Anonymity [246] | ✓ | ✓ | | |
| (X, Y) -Privacy [236] | ✓ | ✓ | | |
| (k, e) -Anonymity [269] | ✓ | ✓ | | |
| (ϵ, m) -Anonymity [152] | ✓ | ✓ | | |
| Personalized Privacy [250] | ✓ | ✓ | | |
| ℓ -Closeness [153] | | ✓ | | ✓ |
| δ -Presence [176] | | | ✓ | |
| (c, t) -Isolation [46] | | | ✓ | ✓ |
| ϵ -Differential Privacy [74] | ✓ | | | ✓ |
| (d, γ) -Privacy [193] | | | ✓ | ✓ |
| Distributional Privacy [33] | | | ✓ | ✓ |

Existing attacks

- Record linkage:
 - adversaries collect auxiliary information about a certain individual from multiple data sources and then combine that data to form a whole picture about their target, which is often an individual's personally identifiable information



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Existing attacks

- Attribute linkage:
 - The adversary does not need to link an individual to a specific record, but can still determine the sensitive value associated with the individual.
 - For example: if Alice knows that Tom's record is: his zip code is 14852 and his age is 38, then without identifying which record is Tom's, Alice can still infer that Tom has Cancer.

| TID | Zip code | Age | Condition |
|-----|----------|---------|-----------------|
| 1 | 130*** | < 30 | Heart disease |
| 2 | 130*** | < 30 | Viral infection |
| 3 | 130*** | < 30 | Viral infection |
| 4 | 148*** | [30-40] | Cancer |
| 5 | 148*** | [30-40] | Cancer |
| 6 | 148*** | [30-40] | Cancer |

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Existing attacks

- Table linkage:
 - A table linkage occurs if an attacker can confidently infer the presence or the absence of the victim's record in the released table.
 - Suppose a hospital releases a data table with a particular type of disease.
 - Identifying the presence of the victim's record in the table is already damaging.

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Existing attacks

- Example table linkage:
 - Suppose the data publisher has released a 3-anonymous patient table (c)
 - The attacker is presumed to also have access to an external public table (d)
 - Table (c) is in Table (d)

| (c) 3-anonymous patient table | | | | (d) 4-anonymous external table | | | |
|-------------------------------|--------|---------|-----------|--------------------------------|--------------|--------|---------|
| Job | Sex | Age | Disease | Name | Job | Sex | Age |
| Professional | Male | [35-40] | Hepatitis | Alice | Artist | Female | [30-35] |
| Professional | Male | [35-40] | Hepatitis | Bob | Professional | Male | [35-40] |
| Professional | Male | [35-40] | HIV | Cathy | Artist | Female | [30-35] |
| Artist | Female | [30-35] | Flu | Doug | Professional | Male | [35-40] |
| Artist | Female | [30-35] | HIV | Emily | Artist | Female | [30-35] |
| Artist | Female | [30-35] | HIV | Fred | Professional | Male | [35-40] |
| Artist | Female | [30-35] | HIV | Gladys | Artist | Female | [30-35] |
| | | | | Henry | Professional | Male | [35-40] |
| | | | | Irene | Artist | Female | [30-35] |

- To launch a table linkage on a target victim, for Alice
 - The probability that Alice is present in (c) is $4/5=0.8$
 - because there are 4 records in (c) and 5 records in (d) containing <Artist,Female,[30-35]>.

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Existing attacks

- **Example:** Suppose the data publisher has released a 3-anonymous patient table (c)
- The attacker is presumed to also have access to an external public table (d)
- **Table (c) is in Table (d)**

| Job | Sex | Age | Disease |
|--------------|--------|---------|-----------|
| Professional | Male | (35-40) | Hepatitis |
| Professional | Male | (35-40) | HIV |
| Professional | Male | (35-40) | HIV |
| Artist | Female | (30-35) | Flu |
| Artist | Female | (30-35) | HIV |
| Artist | Female | (30-35) | HIV |
| Artist | Female | (30-35) | HIV |

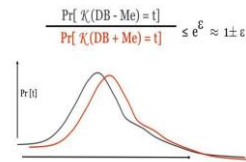
| Name | Job | Sex | Age |
|--------|--------------|--------|---------|
| Alice | Artist | Female | (30-35) |
| Bob | Professional | Male | (35-40) |
| Cathy | Artist | Female | (30-35) |
| Doug | Professional | Male | (35-40) |
| Emily | Artist | Female | (30-35) |
| Fred | Professional | Male | (35-40) |
| Gladys | Artist | Female | (30-35) |
| Henry | Professional | Male | (35-40) |
| Irene | Artist | Female | (30-35) |

Practice: what is the probability that Bob is present in (c)?

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Existing attacks

- **Probabilistic Attack:**
 - Probabilistic attack is not like linkage attack which precisely knows individual information, then gain sensitive information combined with existed background knowledge,
 - but it focuses on **changing adversary's probabilistic confidence of getting privacy information after acquiring published dataset.**
 - **Example:** differential privacy



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Next

- Existing representative **solutions**
 - **k-Anonymity**
 - L-Diversity
 - T-Closeness

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K-Anonymity: Intuition

- The information for each person contained in the released table **cannot be distinguished from at least k-1 individuals** whose information also appears in the release
 - **Example:** you try to identify a man in the released table, but the only information you have is his birth date and gender. There are k men in the table with the same birth date and gender.
- **Any quasi-identifier present in the released table must appear in at least k records**

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K-Anonymity Protection Model

- Private table: T
- Released table: RT
- Attributes: A_1, A_2, \dots, A_n
- Quasi-identifier subset: A_{i_1}, \dots, A_{i_j}

Let $RT(A_1, \dots, A_n)$ be a table, $QI_{RT} = (A_{i_1}, \dots, A_{i_j})$ be the quasi-identifier associated with RT, $A_{i_1}, \dots, A_{i_j} \subseteq A_1, \dots, A_n$, and RT satisfy k -anonymity. Then, each sequence of values in $RT[A_{i_1}, \dots, A_{i_j}]$ appears with at least k occurrences in $RT[QI_{RT}]$ for $x=i_1, \dots, j$.

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Example of a k-Anonymous Table

| | Race | Birth | Gender | ZIP | Problem |
|-----|-------|-------|--------|-------|--------------|
| t1 | Black | 1965 | m | 0214* | short breath |
| t2 | Black | 1965 | m | 0214* | chest pain |
| t3 | Black | 1965 | f | 0213* | hypertension |
| t4 | Black | 1965 | f | 0213* | hypertension |
| t5 | Black | 1964 | f | 0213* | obesity |
| t6 | Black | 1964 | f | 0213* | chest pain |
| t7 | White | 1964 | m | 0213* | chest pain |
| t8 | White | 1964 | m | 0213* | obesity |
| t9 | White | 1964 | m | 0213* | short breath |
| t10 | White | 1967 | m | 0213* | chest pain |
| t11 | White | 1967 | m | 0213* | chest pain |

Figure 2 Example of k -anonymity, where $k=2$ and $QI=\{Race, Birth, Gender, ZIP\}$

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Achieving k-Anonymity

- Suppression
- Generalization
- Swapping
- Randomization

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Achieving k-Anonymity

- Suppression
 - In this method, certain values of the attributes are replaced by an asterisk '*'. All or some values of a column may be replaced by '*'.

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Example of Suppression (1)

| Released table | | | | | External data | | | | |
|----------------|-------|--------|-----|---------|---------------|-------|--------|-----|------|
| Race | Birth | Gender | ZIP | Problem | Name | Birth | Gender | ZIP | Race |
| t1 | Black | 1965 | m | 0214* | about heart | | | | |
| t2 | Black | 1965 | m | 0214* | chest pain | | | | |
| t3 | Black | 1965 | f | 0213* | hypertension | | | | |
| t4 | Black | 1965 | f | 0213* | hypertension | | | | |
| t5 | Black | 1964 | f | 0213* | obesity | | | | |
| t6 | Black | 1964 | f | 0213* | chest pain | | | | |
| t7 | White | 1964 | m | 0213* | chest pain | | | | |
| t8 | White | 1964 | m | 0213* | obesity | | | | |
| t9 | White | 1964 | m | 0213* | about heart | | | | |
| t10 | White | 1967 | m | 0213* | chest pain | | | | |
| t11 | White | 1967 | m | 0213* | chest pain | | | | |

| Name | Birth | Gender | ZIP | Race |
|-------|-------|--------|-------|-------|
| Andre | 1964 | m | 02135 | White |
| Beth | 1964 | f | 55410 | Black |
| Carol | 1964 | f | 90210 | White |
| Dan | 1967 | m | 02174 | White |
| Ellen | 1968 | f | 02237 | White |

By linking these 2 tables, you still don't learn Andre's problem

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Example of Suppression (2)

| Microdata | | | | Suppressed table | | | |
|-----------|-----|-----|-----------------|------------------|----------|-----|-----------------|
| QID | | | SA | QID | | | SA |
| Zipcode | Age | Sex | Disease | Zipcode | Age | Sex | Disease |
| 47677 | 29 | F | Ovarian Cancer | 476** | 2* | * | Ovarian Cancer |
| 47602 | 22 | F | Ovarian Cancer | 476** | 2* | * | Ovarian Cancer |
| 47678 | 27 | M | Prostate Cancer | 476** | 2* | * | Prostate Cancer |
| 47905 | 43 | M | Flu | 4790* | [43, 52] | * | Flu |
| 47909 | 52 | F | Heart Disease | 4790* | [43, 52] | * | Heart Disease |
| 47906 | 47 | M | Heart Disease | 4790* | [43, 52] | * | Heart Disease |

- Released table is 3-anonymous
- If the adversary knows Alice's quasi-identifier (47677, 29, F), he still does not know which of the first 3 records corresponds to Alice's record

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Achieving k-Anonymity

- Generalization
 - In this method, individual values of attributes are replaced by with a broader category.
 - For example, the value '19' of the attribute 'Age' may be replaced by ' ≤ 20 ', the value '23' by ' $20 < \text{Age} \leq 30$ ', etc.

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Example of generalization

- Transform the QI values into less specific forms

| Age | Zipcode | Disease | Age | Zipcode | Disease |
|-----|---------|------------|----------|------------|------------|
| 21 | 12000 | dyspepsia | [21, 22] | [12k, 14k] | dyspepsia |
| 22 | 14000 | bronchitis | [21, 22] | [12k, 14k] | bronchitis |
| 24 | 18000 | flu | [23, 24] | [18k, 25k] | flu |
| 23 | 25000 | gastritis | [23, 24] | [18k, 25k] | gastritis |
| 41 | 20000 | flu | [36, 41] | [20k, 27k] | flu |
| 36 | 27000 | gastritis | [36, 41] | [20k, 27k] | gastritis |
| 37 | 33000 | dyspepsia | [37, 43] | [26k, 35k] | dyspepsia |
| 40 | 35000 | flu | [37, 43] | [26k, 35k] | flu |
| 43 | 26000 | gastritis | [37, 43] | [26k, 35k] | gastritis |
| 52 | 33000 | dyspepsia | [52, 56] | [33k, 34k] | dyspepsia |
| 56 | 34000 | gastritis | [52, 56] | [33k, 34k] | gastritis |

generalize

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Achieving k-Anonymity

- Swapping
 - produces a release candidate by swapping some attribute values.
 - For example, the data publisher may swap the age values of Ann and Eshwar, swap the gender values of Bruce and Cary, and so on.
 - remove the relationship between quasi identifiers and sensitive data

Example of Swapping

| Age | Zipcode | Disease |
|----------|------------|------------|
| [21, 22] | [12k, 14k] | dyspepsia |
| [21, 22] | [18k, 25k] | bronchitis |
| [23, 24] | [12k, 14k] | flu |
| [23, 24] | [18k, 25k] | gastritis |
| [36, 41] | [20k, 27k] | flu |
| [36, 41] | [20k, 27k] | gastritis |
| [37, 43] | [26k, 35k] | dyspepsia |
| [37, 43] | [26k, 35k] | flu |
| [37, 43] | [26k, 35k] | gastritis |
| [52, 56] | [33k, 34k] | dyspepsia |
| [52, 56] | [33k, 34k] | gastritis |

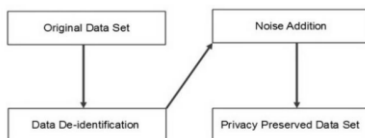
Swapping

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slide 38

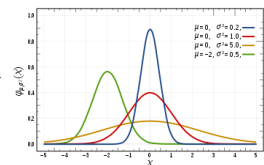
Achieving k-Anonymity

- Randomization
 - A release candidate of the randomization mechanism is generated by adding random noise to the data.
 - Gaussian noise



Example of Randomization

| Age | Zipcode | Disease |
|-----|---------|------------|
| 21 | 12000 | dyspepsia |
| 22 | 14000 | bronchitis |
| 24 | 18000 | flu |
| 23 | 25000 | gastritis |
| 41 | 20000 | flu |
| 36 | 27000 | gastritis |
| 37 | 33000 | dyspepsia |
| 40 | 35000 | flu |
| 43 | 26000 | gastritis |
| 52 | 33000 | dyspepsia |
| 56 | 34000 | gastritis |



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Example of Randomization

| Age | Zipcode | Disease |
|-----|---------|------------|
| 21 | 12000 | dyspepsia |
| 22 | 14000 | bronchitis |
| 24 | 18000 | flu |
| 23 | 25000 | gastritis |
| 41 | 20000 | flu |
| 36 | 27000 | gastritis |
| 37 | 33000 | dyspepsia |
| 40 | 35000 | flu |
| 43 | 26000 | gastritis |
| 52 | 33000 | dyspepsia |
| 56 | 34000 | gastritis |

→

| Age | Zipcode | Disease |
|-----|---------|------------|
| 22 | 13400 | dyspepsia |
| 23 | 13200 | bronchitis |
| 23 | 15650 | flu |
| 22 | 23200 | gastritis |
| 39 | 22300 | flu |
| 37 | 24400 | gastritis |
| 38 | 34400 | dyspepsia |
| 39 | 34500 | flu |
| 41 | 24500 | gastritis |
| 54 | 33500 | dyspepsia |
| 54 | 34600 | gastritis |

$\mu = 0, \sigma^2 = 2$ $\mu = 0, \sigma^2 = 2500$

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Achieving k-Anonymity

- Randomization
 - An example

| First Name | Last Name | SSN | Age | Major | GPA | Zip code | State | Scholarship Amount | Gender |
|------------|-----------|-------------|-----|------------------|------|----------|-------|--------------------|--------|
| John | Adel | 100-00-0000 | 20 | Computer Science | 4.00 | 210710A | MD | 5000.00M | |
| Peter | Chenel | 100-00-0100 | 18 | Biology | 3.15 | 210720D | MD | 5000.00M | |
| Erin | Brookel | 100-00-0110 | 21 | Chemistry | 2.19 | 210710A | MD | 2500.00F | |
| Wj | Ward | 100-00-0120 | 41 | History | 2.80 | 210710D | MD | 4700.00F | |
| Eva | Pikars | 100-00-0130 | 21 | Chemistry | 3.67 | 210709A | MD | 7800.00F | |
| Sandra | Hollywood | 100-00-0140 | 21 | Art | 3.65 | 210709D | MD | 9000.00F | |
| Orlando | Ockers | 100-00-0150 | 25 | Nurse | 4.00 | 210711A | MD | 8000.00M | |
| Melanie | Gravins | 100-00-0160 | 18 | Computer Science | 2.76 | 210709A | MD | 1000.00M | |
| Jacobi | Hobbs | 100-00-0170 | 18 | Biology | 3.00 | 210709A | MD | 700.00F | |
| Bruce | Adel | 100-00-0180 | 17 | Art | 2.88 | 210801D | MD | 1100.00M | |

Table 1: Original Data Set (All data for illustrative purposes).

| Scholarship Amount | Random Noise Between 1000 and 9000 | Random Noise | Perturbed Scholarship Amount |
|--------------------|------------------------------------|--------------|------------------------------|
| 5000.00 | | 7206.68 | 37296.68 |
| 6000.00 | | 2187.4 | 52087.4 |
| 25000.00 | | 4403.32 | 29403.32 |
| 67000.00 | | 5389.69 | 72389.69 |
| 78000.00 | | 6639.16 | 84639.16 |
| 90000.00 | | 6229.52 | 97119.52 |
| 90000.00 | | 1054.68 | 91554.68 |
| 10000.00 | | 6977.3 | 16977.3 |
| 7000.00 | | 3455.81 | 10455.81 |
| 11000.00 | | 6932.86 | 17932.86 |
| Mean | 20690 | | 27674.97 |
| Standard Deviation | 13435.028822444 | | 13892.428820319 |
| Variance | 180500000 | | 191482535.2802 |

Table 3: Random noise between 1000 and 9000 added to Scholarship attribute.

Attacks on k-Anonymity

- k-Anonymity does not provide privacy if
 - Sensitive values in an equivalence class lack diversity
 - The attacker has background knowledge

Homogeneity attack

| |
|-------------|
| Bob |
| Zipcode Age |
| 47678 27 |

Background knowledge attack

| |
|-------------|
| Carl |
| Zipcode Age |
| 47673 36 |

A 3-anonymous patient table

| Zipcode | Age | Disease |
|---------|-----|---------------|
| 476** | 2* | Heart Disease |
| 476** | 2* | Heart Disease |
| 476** | 2* | Heart Disease |
| 4790* | ≥40 | Flu |
| 4790* | ≥40 | Heart Disease |
| 4790* | ≥40 | Cancer |
| 476** | 3* | Heart Disease |
| 476** | 3* | Cancer |
| 476** | 3* | Cancer |

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Next

- Existing representative solutions
 - k-Anonymity
 - L-Diversity
 - T-Closeness

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I-Diversity

| | | |
|-------------|-------|----------|
| Caucas | 787XX | Flu |
| Caucas | 787XX | Shingles |
| Caucas | 787XX | Acne |
| Caucas | 787XX | Flu |
| Caucas | 787XX | Acne |
| Caucas | 787XX | Flu |
| Asian/AfrAm | 78XXX | Flu |
| Asian/AfrAm | 78XXX | Flu |
| Asian/AfrAm | 78XXX | Acne |
| Asian/AfrAm | 78XXX | Shingles |
| Asian/AfrAm | 78XXX | Acne |
| Asian/AfrAm | 78XXX | Flu |

Sensitive attributes must be
“diverse” within each
quasi-identifier equivalence class

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L-Diversity

- T^* : the Anonymized Table
- q^* : the generalized value of q in the published table T^*
- s : a possible value of the sensitive attribute
- $n(q^*, s')$: number of tuples with sensitive attribute s' and non-sensitive attribute q^*
- q^* -block: the set of tuples in T^* whose non-sensitive attribute values generalize to q^*

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L-Diversity

- Lack diversity: lack of diversity in the sensitive attribute manifests itself as follows:

$$\forall s' \neq s, \quad n_{(q^*, s')} \ll n_{(q^*, s)}$$

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L-Diversity

- Then, **L-Diversity Principle** can be defined as:
 - A q^* -block is L-diverse if contains at least L “well-represented” values for the sensitive attribute S .
 - A table is L-diverse if every q^* -block is L-diverse.

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An example

| | Non-Sensitive | | | Sensitive |
|----|---------------|------|-------------|-----------------|
| | Zip Code | Age | Nationality | Condition |
| 1 | 130** | < 30 | * | Heart Disease |
| 2 | 130** | < 30 | * | Heart Disease |
| 3 | 130** | < 30 | * | Viral Infection |
| 4 | 130** | < 30 | * | Viral Infection |
| 5 | 1485* | ≥ 40 | * | Cancer |
| 6 | 1485* | ≥ 40 | * | Heart Disease |
| 7 | 1485* | ≥ 40 | * | Viral Infection |
| 8 | 1485* | ≥ 40 | * | Viral Infection |
| 9 | 130** | 3+ | * | Cancer |
| 10 | 130** | 3+ | * | Cancer |
| 11 | 130** | 3+ | * | Cancer |
| 12 | 130** | 3+ | * | Cancer |

4-anonymous table

| | Non-Sensitive | | | Sensitive |
|----|---------------|------|-------------|-----------------|
| | Zip Code | Age | Nationality | Condition |
| 1 | 1305* | < 40 | * | Heart Disease |
| 4 | 1305* | < 40 | * | Viral Infection |
| 9 | 1305* | < 40 | * | Cancer |
| 10 | 1305* | < 40 | * | Cancer |
| 5 | 1485* | > 40 | * | Cancer |
| 6 | 1485* | > 40 | * | Heart Disease |
| 7 | 1485* | > 40 | * | Viral Infection |
| 8 | 1485* | > 40 | * | Viral Infection |
| 2 | 1306* | < 40 | * | Heart Disease |
| 3 | 1306* | < 40 | * | Viral Infection |
| 11 | 1306* | < 40 | * | Cancer |
| 12 | 1306* | < 40 | * | Cancer |

3 diverse table

- Using a 3-diverse table, we no longer are able to tell if Bob (a 31 year old American from zip code 13053) has cancer.
- We also cannot tell if Umeko (a 21 year old Japanese from zip code 13068) has a viral infection or cancer.

Probabilistic inference attacks over l-Diversity

- Each equivalence class has at least **l well-represented** sensitive values

| ... | Disease |
|-----|------------|
| ... | ... |
| ... | HIV |
| ... | HIV |
| ... | ... |
| ... | HIV |
| ... | pneumonia |
| ... | bronchitis |
| ... | ... |

10 records {

8 records have HIV

2 records have other values

- Doesn't prevent probabilistic inference attacks

- Infer: the patient has HIV with large possibility

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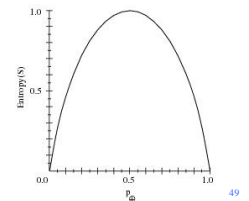
Other Versions of L-Diversity

- Probabilistic L-diversity
 - The frequency of the most frequent value in an equivalence class is bounded by $1/L$

Other Versions of l-Diversity

- ◆ Suppose S is a collection of 14 examples of some Boolean concept, including 9 positive and 5 negative examples. Then the entropy of S relative to this Boolean classification is

- Entropy([9+, 5-]) = $-(9/14)\log_2(9/14) - (5/14)\log_2(5/14) = 0.940$



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Other Versions of l-Diversity

- Entropy L-diversity
 - The entropy of the distribution of sensitive values in **each equivalence class** is at least $\log(L)$

$$-\sum_{s \in S} p(q^*, s) \log(p(q^*, s)) \geq \log(l)$$

- $\frac{r_{q^*,s}}{n_{q^*}}$ is the fraction of tuples in the q^* -block with sensitive attribute value equal to s
- Problem of Entropy L-diversity**
 - Here every q^* -block has at least L distinct values for the sensitive attribute
 - This implies that for a table to be entropy L-Diverse, the entropy of the entire table must be at least $\log(L)$.
 - Therefore, entropy L-Diversity may be **too restrictive to be practical**.

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Other Versions of L-Diversity

- Recursive (c,L)-diversity
 - $r_1 < c(r_1 + r_{i+1} + \dots + r_m)$ where r_i is the frequency of the i^{th} most frequent value
 - Intuition: the **most frequent value** does not appear too frequently

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Limitations of L-Diversity

- L-diversity may be **difficult and unnecessary** to achieve.
 - A single sensitive attribute
 - Two values: HIV positive (1%) and HIV negative (99%)
 - Very different degrees of sensitivity
- L-diversity is unnecessary to achieve
 - 2-diversity is unnecessary for an equivalence class that contains only negative records
- L-diversity is difficult to achieve
 - Suppose there are 10000 records in total
 - To have distinct 2-diversity, there can be at most $10000 * 1\% = 100$ equivalence classes

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Sensitive Attribute Disclosure

L-diversity is insufficient to prevent attribute disclosure.

Similarity attack

| | |
|------------|------------|
| Bob | |
| Zip | Age |
| 47678 | 27 |

A 3-diverse patient table

| Zipcode | Age | Salary | Disease |
|---------|-----|--------|-----------------------|
| 476** | 2* | 20K | Gastric Ulcer |
| 476** | 2* | 30K | Gastritis |
| 476** | 2* | 40K | Stomach Cancer |
| 4790* | ≥40 | 50K | Gastritis |
| 4790* | ≥40 | 100K | Flu |
| 4790* | ≥40 | 70K | Bronchitis |
| 476** | 3* | 60K | Bronchitis |
| 476** | 3* | 80K | Pneumonia |
| 476** | 3* | 90K | Stomach Cancer |

Conclusion

- Bob's salary is in [20k,40k], which is relatively low
- Bob has some stomach-related disease

L-diversity does not consider semantics of sensitive values!

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Next

- Existing representative **solutions**
 - k -Anonymity
 - L -Diversity
 - T -Closeness

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Why t-Closeness?

- Pre-existing privacy measures k -anonymity and L -diversity have flaws.
 - k -anonymity-each equivalence class has at least k records to protect against identity disclosure.
 - k -anonymity is vulnerable to homogeneity attacks and background knowledge attacks.
 - L -diversity: distribution of a sensitive attribute in each equivalence class has at least L “well represented” values to protect against attribute disclosure.
 - L -diversity is vulnerable to skewness attacks and similarity attacks.

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t-Closeness overview

- Privacy is measured by the information gain of an observer.
- We assume:
 - B0**: Alice believes that Bob has the virus because he has been acting sick.
 - B1**: Alice gets a summary report of the table and learns that only 1% of the population has the virus. This distribution is Q , the distribution of the sensitive attribute in the whole table. She believes that Bob is in that one percent.
 - B2**: Alice takes a look at the table, and finds that Bob is in equivalence class 3 because he is 32 and lives in zip code 47623. She learns P , the distribution of the sensitive attribute values in this class. Based on P she decides that it is actually quite likely that Bob has the virus.

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t-Closeness overview

- L -diversity limits the gain between $B0$ (belief before any knowledge of the table) and $B2$ (belief after examining the table and the relevant equivalence class) by requiring that P (distribution in the equivalence class) has diversity.
- Q (global distribution in the table) should be treated as public information.
- If the change from $B0$ to $B1$ is large, means that the Q contains lots of new information. But we can't control people's access to Q , so we shouldn't worry about it.
- Therefore should focusing on limiting the gain between $B1$ and $B2$. We can do so by limiting the difference between P and Q . The closer P and Q are, the closer $B1$ and $B2$ are.

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t-Closeness definition

- An equivalence class is said to have **t-closeness**
 - if the distance between the distribution of a sensitive attribute (P) in this class and the distribution of the attribute in the whole table(Q) is no more than a threshold t.
- A table is said to have t-closeness if all equivalence classes have t-closeness.

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t-Closeness

| | | |
|-------------|-------|----------|
| Caucas | 787XX | Flu |
| Caucas | 787XX | Shingles |
| Caucas | 787XX | Acne |
| Caucas | 787XX | Flu |
| Caucas | 787XX | Acne |
| Caucas | 787XX | Flu |
| Asian/AfrAm | 78XXX | Flu |
| Asian/AfrAm | 78XXX | Flu |
| Asian/AfrAm | 78XXX | Acne |
| Asian/AfrAm | 78XXX | Shingles |
| Asian/AfrAm | 78XXX | Acne |
| Asian/AfrAm | 78XXX | Flu |

Distribution of sensitive attributes within each quasi-identifier group should be “close” to their distribution in the entire original database

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Distance measurement

- Now that we’ve confirmed that limiting the difference between P and Q is the key to privacy, we need a way to measure the distance.
 - m: the number of sensitive values in an equivalence class
 - $P=(p_1, p_2, \dots, p_m)$, $Q=(q_1, q_2, \dots, q_m)$
- Here are some naive measurements:
 - Method 1: variational distance

$$D[P, Q] = \sum_{i=1}^m \frac{1}{2} |p_i - q_i|.$$

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Distance measurement

Example

| ZIP Code | Age | Salary | Disease |
|----------|-----|--------|----------------|
| 1 47677 | 29 | 3K | gastric ulcer |
| 2 47602 | 22 | 4K | gastritis |
| 3 47678 | 27 | 5K | stomach cancer |
| 4 47925 | 43 | 6K | gastritis |
| 5 47909 | 52 | 11K | flu |
| 6 47906 | 47 | 8K | bronchitis |
| 7 47605 | 30 | 7K | bronchitis |
| 8 47673 | 36 | 9K | pneumonia |
| 9 47607 | 32 | 10K | stomach cancer |

Table 3. Original Salary/Disease Table

| ZIP Code | Age | Salary | Disease |
|----------|------|--------|----------------|
| 1 476** | 2* | 3K | gastric ulcer |
| 2 476** | 2* | 4K | gastritis |
| 3 476** | 2* | 5K | stomach cancer |
| 4 4790* | ≥ 40 | 6K | gastritis |
| 5 4790* | ≥ 40 | 11K | flu |
| 6 4790* | ≥ 40 | 8K | bronchitis |
| 7 476** | 3* | 7K | bronchitis |
| 8 476** | 3* | 9K | pneumonia |
| 9 476** | 3* | 10K | stomach cancer |

Table 4. A 3-diverse version of Table 3

- Overall distribution of the Income attribute:
Q = {3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k}

- The first equivalence class in Table 4 has distribution:
P1 = {3k, 4k, 5k}

- The second equivalence class has distribution:
P2 = {6k, 8k, 11k}

$D(P1, Q) = 0.5 * (|1/3 - 1/9| + |1/3 - 1/9| + |1/3 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9|) = 1/2$
 $D(P2, Q) = 0.5 * (|1/3 - 1/9| + |1/3 - 1/9| + |1/3 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9|) = 1/2$

We have $D(P1, Q) = D(P2, Q)$

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Distance measurement

- Here are some naive measurements:

- Method 2: Kullback-Leibler (KL) distance

$$D[\mathbf{P}, \mathbf{Q}] = \sum_{i=1}^m p_i \log \frac{p_i}{q_i} = H(\mathbf{P}) - H(\mathbf{P}, \mathbf{Q})$$

- $H(\mathbf{P})$ is the entropy of \mathbf{P}

$$H(\mathbf{P}) = \sum_{i=1}^m p_i \log p_i$$

- $H(\mathbf{P}, \mathbf{Q})$ is the cross-entropy of \mathbf{P} and \mathbf{Q}

$$H(\mathbf{P}, \mathbf{Q}) = \sum_{i=1}^m p_i \log q_i$$

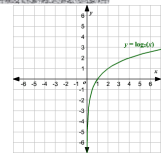
| | 0 | 1 |
|----|-----|-----|
| D1 | 0.1 | 0.9 |
| D2 | 0.2 | 0.8 |
| D3 | 0.9 | 0.1 |

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Kullback-Leibler (KL) distance

$$H(\mathbf{P}, \mathbf{Q}) = \sum_{i=1}^m p_i \log q_i$$

| | 0 | 1 |
|----|-----|-----|
| D1 | 0.1 | 0.9 |
| D2 | 0.2 | 0.8 |
| D3 | 0.9 | 0.1 |



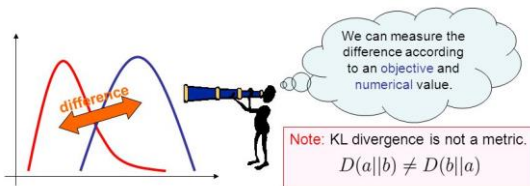
$$H(D1, D2) = 0.1 * \ln(0.2) + 0.9 * \ln(0.8) = -0.1609 - 0.2008 = -0.3617$$

$$H(D1, D3) = 0.1 * \ln(0.9) + 0.9 * \ln(0.1) = -0.0105 - 2.0723 = -2.0828$$

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Kullback-Leibler (KL) distance

In the context of machine learning, $D(\mathbf{P}, \mathbf{Q})$ is often called the information gain achieved if \mathbf{Q} is used instead of \mathbf{P} .



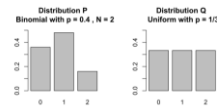
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Distance measurement

- Here are some naive measurements:

- Method 2: Kullback-Leibler (KL) distance

- Example: Let \mathbf{P} and \mathbf{Q} be the distributions shown in the table and figure



| | 0 | 1 | 2 |
|----------------|-------|-------|-------|
| Distribution P | 0.36 | 0.48 | 0.16 |
| Distribution Q | 0.333 | 0.333 | 0.333 |

The KL divergence is calculated as follows. This example uses the natural log with base e , designated \ln .

$$\begin{aligned} D_{KL}(\mathbf{Q}||\mathbf{P}) &= \sum_i Q(i) \ln \left(\frac{Q(i)}{P(i)} \right) \\ &= 0.333 \ln \left(\frac{0.333}{0.36} \right) + 0.333 \ln \left(\frac{0.333}{0.48} \right) + 0.333 \ln \left(\frac{0.333}{0.16} \right) \\ &= -0.02596 + (-0.12176) + 0.24408 \\ &= 0.09637 \end{aligned}$$

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Distance measurement

- ◆ However, these distance measures **do not reflect** the semantic distance among values.

- Let's see an example

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Distance measurement

See the example again

- Example

| | ZIP Code | Age | Salary | Disease |
|---|----------|-----|--------|----------------|
| 1 | 47677 | 29 | 3K | gastric ulcer |
| 2 | 47602 | 22 | 4K | gastritis |
| 3 | 47678 | 27 | 5K | stomach cancer |
| 4 | 47905 | 43 | 6K | gastritis |
| 5 | 47909 | 52 | 11K | flu |
| 6 | 47906 | 47 | 8K | bronchitis |
| 7 | 47605 | 30 | 7K | bronchitis |
| 8 | 47673 | 36 | 9K | pneumonia |
| 9 | 47607 | 32 | 10K | stomach cancer |

Table 3. Original Salary/Disease Table

| | ZIP Code | Age | Salary | Disease |
|---|----------|------|--------|----------------|
| 1 | 476** | 2* | 3K | gastric ulcer |
| 2 | 476** | 2* | 4K | gastritis |
| 3 | 476** | 2* | 5K | stomach cancer |
| 4 | 4790* | ≥ 40 | 6K | gastritis |
| 5 | 4790* | ≥ 40 | 11K | flu |
| 6 | 4790* | ≥ 40 | 8K | bronchitis |
| 7 | 476** | 3* | 7K | bronchitis |
| 8 | 476** | 3* | 9K | pneumonia |
| 9 | 476** | 3* | 10K | stomach cancer |

Table 4. A 3-diverse version of Table 3

- Overall distribution of the Income attribute:

$Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$

- The first equivalence class in Table 4 has distribution:

$P1 = \{3k, 4k, 5k\}$

- The second equivalence class has distribution:

$P2 = \{6k, 8k, 11k\}$

$D(P1, Q) = 0.5 * (|1/3 - 1/9| + |1/3 - 1/9| + |1/3 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9|) = 1/2$

$D(P2, Q) = 0.5 * (|1/3 - 1/9| + |1/3 - 1/9| + |1/3 - 1/9| + |1/3 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9| + |0 - 1/9|) = 1/2$

However, we would like to have

$D(P1, Q) > D(P2, Q)$

Since: Our intuition is that P1 results in more information leakage than P2, because the values in P1 are all in the lower end.

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Distance measurement

- However, these distance measures **do not reflect** the semantic distance among values.
- The distance measures mentioned above would not be able to do so, because from their point of view values such as 3k and 6k are just different points and have no other semantic meaning.
- How to avoid it?
 - Earth Mover's distance is good!

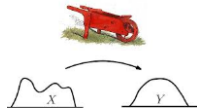
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Earth Mover's distance

- The EMD is based on the minimal amount of work needed to transform one distribution to another by moving distribution mass between each other.
 - Intuitively, one distribution is seen as a mass of earth spread in the space and the other as a collection of holes in the same space.
 - EMD measures the least amount of work needed to fill the holes with earth.
 - A unit of work corresponds to moving a unit of earth by a unit of ground distance.

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Earth Mover's distance



- Intuitively, one distribution is seen as a mass of earth spread in the space and the other as a collection of holes in the same space.
- EMD measures the least amount of work needed to fill the holes with earth.
- A unit of work corresponds to moving a unit of earth by a unit of ground distance.

slide 73

Earth Mover's distance

Definition of EMD:

- EMD can be formally defined using the well-studied transportation problem.
- $P=(p_1, p_2, \dots, p_m)$, $Q=(q_1, q_2, \dots, q_m)$

$$WORK(P, Q, F) = \sum_{i=1}^m \sum_{j=1}^m d_{ij} f_{ij}$$

subject to the following constraints:

$$f_{ij} \geq 0 \quad 1 \leq i \leq m, 1 \leq j \leq m \quad (c1)$$

$$p_i = \sum_{j=1}^m f_{ij} + \sum_{j=1}^m f_{ji} = q_i \quad 1 \leq i \leq m \quad (c2)$$

$$\sum_{i=1}^m \sum_{j=1}^m f_{ij} = \sum_{i=1}^m p_i = \sum_{i=1}^m q_i = 1 \quad (c3)$$

Properties of EMD:

- d_{ij} is the ground distance between i in P and j in Q , which is defined as $|p_i - q_j|/(m-1)$
- f_{ij} is the flow of mass to transform i in P into j in Q using the minimal amount of work.
- F is the mass flow to transform P into Q .
- $D[P, Q] = WORK(P, Q, F)$ is the work to transform P into Q
- $D[P, Q]$ is between 0 and 1.
- For any P_1 and P_2 , $D[P, Q] \leq \max(D[P_1, Q], D[P_2, Q])$.

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Earth Mover's distance

- EMD gives us a method for determining the distance between two distributions but doesn't tell us how to determine the distance between two elements in the distributions.
- The way to do that will differ depending on the type of data we're using...

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How to Calculate the EMD?

- To use t-closeness with EMD, we need to be able to calculate the EMD between two distributions.
 - EMD for Numerical Attributes
 - EMD for Categorical Attributes

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EMD for Numerical Attributes

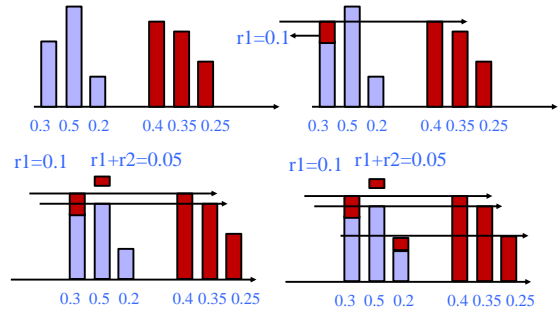
- Numerical attribute values are ordered.
 - Let the attribute domain be $\{v_1, v_2 \dots v_m\}$
 - Set $r_i = p_i - q_i$
 - The distance between P and Q can be calculated as:

$$D[P, Q] = \frac{1}{m-1} (|r_1| + |r_1 + r_2| + \dots + |r_1 + r_2 + \dots + r_{m-1}|)$$

$$= \frac{1}{m-1} \sum_{i=1}^{m-1} \left| \sum_{j=1}^i r_j \right|$$

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EMD for Numerical Attributes



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EMD for Categorical Attributes

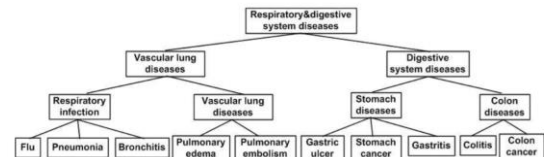
- For categorical attributes (i.e., diseases), a total order often does not exist.
- We consider two distance measures.
 - Method 1: Equal Distance:** The ground distance between any two values of a categorical attribute is defined to be 1.
 - As the distance between any two values is 1, for each point that $p_i - q_i > 0$, one just needs to move the extra to some other points.

$$D[P, Q] = \frac{1}{2} \sum_{i=1}^m |p_i - q_i| = \sum_{p_i \geq q_i} (p_i - q_i) = - \sum_{p_i < q_i} (p_i - q_i)$$

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EMD for Categorical Attributes

- Method 2: Hierarchical Distance:** The distance between two values of a categorical attribute is based on the **minimum level** to which these two values are generalized to the same value according to the domain hierarchy.
 - Example: **Hierarchy for categorical attributes Disease.**



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EMD for Categorical Attributes

Method 2: Hierarchical Distance

Several definitions:

- we define the *extra* of a leaf node that corresponds to element i , to be $p_i - q_i$, and the *extra* of an internal node N to be the sum of *extras* of leaf nodes below N .
- $Child(N)$ is the set of all leaf nodes below node N

$$extra(N) = \begin{cases} p_i - q_i & \text{if } N \text{ is a leaf} \\ \sum_{C \in Child(N)} extra(C) & \text{otherwise} \end{cases}$$

- We further define two other functions for *internal nodes*:

$$pos_extra(N) = \sum_{C \in Child(N) \wedge extra(C) > 0} |extra(C)|$$

$$neg_extra(N) = \sum_{C \in Child(N) \wedge extra(C) < 0} |extra(C)|$$

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EMD for Categorical Attributes

Method 2: Hierarchical Distance

Several definitions:

- The *extra* function has the property that the sum of *extra* values for nodes at the same level is 0.

$$cost(N) = \frac{height(N)}{H} \min(pos_extra(N), neg_extra(N))$$

- Thus, the earth mover's distance can be written as:

$$D[P, Q] = \sum_N cost(N)$$

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Example of EMD

Remember this slide? Now let's calculate the EMD and create a t -close table.

| ZIP Code | Age | Salary | Disease |
|----------|-----|--------|----------------|
| 1 47677 | 29 | 3K | gastric ulcer |
| 2 47602 | 22 | 4K | gastritis |
| 3 47678 | 27 | 5K | stomach cancer |
| 4 47905 | 43 | 6K | gastritis |
| 5 47909 | 52 | 11K | flu |
| 6 47906 | 47 | 8K | bronchitis |
| 7 47605 | 30 | 7K | bronchitis |
| 8 47673 | 36 | 9K | pneumonia |
| 9 47607 | 32 | 10K | stomach cancer |

Table 3. Original Salary/Disease Table

| ZIP Code | Age | Salary | Disease |
|----------|------|--------|----------------|
| 1 476** | 2* | 3K | gastric ulcer |
| 2 476** | 2* | 4K | gastritis |
| 3 476** | 2* | 5K | stomach cancer |
| 4 4790* | ≥ 40 | 6K | gastritis |
| 5 4790* | ≥ 40 | 11K | flu |
| 6 4790* | ≥ 40 | 8K | bronchitis |
| 7 476** | 3* | 7K | bronchitis |
| 8 476** | 3* | 9K | pneumonia |
| 9 476** | 3* | 10K | stomach cancer |

Table 4. A 3-diverse version of Table 3

$Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$

$P_1 = \{3k, 4k, 5k\}$

$P_2 = \{6k, 8k, 11k\}$

P_1 has more information leakage than P_2 because there are fewer people in that salary range and thus they are easier to identify, thus we should have $D[P_1, Q] > D[P_2, Q]$.

However, these algorithms just view 3k and 6k as different points and don't attach semantic meaning to them. They would calculate this wrong.

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Example of EMD

| ZIP Code | Age | Salary | Disease |
|----------|-----|--------|----------------|
| 1 47677 | 29 | 3K | gastric ulcer |
| 2 47602 | 22 | 4K | gastritis |
| 3 47678 | 27 | 5K | stomach cancer |
| 4 47905 | 43 | 6K | gastritis |
| 5 47909 | 52 | 11K | flu |
| 6 47906 | 47 | 8K | bronchitis |
| 7 47605 | 30 | 7K | bronchitis |
| 8 47673 | 36 | 9K | pneumonia |
| 9 47607 | 32 | 10K | stomach cancer |

Table 3. Original Salary/Disease Table

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| 1 476** | 2* | 3K | gastric ulcer |
| 2 476** | 2* | 4K | gastritis |
| 3 476** | 2* | 5K | stomach cancer |
| 4 4790* | ≥ 40 | 6K | gastritis |
| 5 4790* | ≥ 40 | 11K | flu |
| 6 4790* | ≥ 40 | 8K | bronchitis |
| 7 476** | 3* | 7K | bronchitis |
| 8 476** | 3* | 9K | pneumonia |
| 9 476** | 3* | 10K | stomach cancer |

Table 4. A 3-diverse version of Table 3

$Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$

$P_1 = \{3k, 4k, 5k\}$

One optimal mass flow that transforms P_1 to Q is to move 1/9 probability mass across the following pairs:

3k->3k, 3k->4k, 3k->5k
cost: $1/9 * ((3-3) + (4-3) + (5-3)) / 8$
4k->6k, 4k->7k, 4k->8k
cost: $1/9 * ((6-4) + (7-4) + (8-4)) / 8$
5k->9k, 5k->10k, 5k->11k
cost: $1/9 * ((9-5) + (10-5) + (11-5)) / 8$

Total cost: $1/9 * 27/8 = 0.375$

Remember: for numerical attributes, minimal work can be achieved by satisfying all elements of Q sequentially

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Example of EMD

| ZIP Code | Age | Salary | Disease |
|----------|-----|--------|----------------|
| 1 47677 | 29 | 3K | gastric ulcer |
| 2 47602 | 22 | 4K | gastritis |
| 3 47678 | 27 | 5K | stomach cancer |
| 4 47905 | 43 | 6K | gastritis |
| 5 47909 | 52 | 11K | flu |
| 6 47906 | 47 | 8K | bronchitis |
| 7 47605 | 30 | 7K | bronchitis |
| 8 47673 | 36 | 9K | pneumonia |
| 9 47607 | 32 | 10K | stomach cancer |

Table 3. Original Salary/Disease Table

| ZIP Code | Age | Salary | Disease |
|----------|------|--------|----------------|
| 1 476** | 2* | 3K | gastric ulcer |
| 2 476** | 2* | 4K | gastritis |
| 3 476** | 2* | 5K | stomach cancer |
| 4 4790* | ≥ 40 | 6K | gastritis |
| 5 4790* | ≥ 40 | 11K | flu |
| 6 4790* | ≥ 40 | 8K | bronchitis |
| 7 476** | 3* | 7K | bronchitis |
| 8 476** | 3* | 9K | pneumonia |
| 9 476** | 3* | 10K | stomach cancer |

Table 4. A 3-diverse version of Table 3

$Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$

$P_2 = \{6k, 8k, 11k\}$

One optimal mass flow that transforms P_2 to Q is to move $1/9$ probability mass across the following pairs:
 $6k \rightarrow 3k, 6k \rightarrow 4K, 6K \rightarrow 5k, \text{ cost} = 1/9 * (3+2+1)/8$
 $8k \rightarrow 6k, 8k \rightarrow 7k, 8k \rightarrow 8k \text{ cost} = 1/9 * (2+1+0)/8$
 $11k \rightarrow 9k, 11k \rightarrow 10k, 11K \rightarrow 11K \text{ cost} = 1/9 * (2+1)/8$

The cost of this is $1/9 \times (12)/8 = 12/72 = 3/18 = 0.167$.

Example of EMD

| ZIP Code | Age | Salary | Disease |
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Table 4. A 3-diverse version of Table 3

$Q = \{3k, 4k, 5k, 6k, 7k, 8k, 9k, 10k, 11k\}$

$P_1 = \{3k, 4k, 5k\}$

$P_2 = \{6k, 8k, 11k\}$

In conclusion,
 $D[P_1, Q]$ is 0.375 and $D[P_2, Q]$ has a distance of 0.167.
 Therefore, P_2 reveals less private data.

Content

- **Motivation** of privacy preserving data publishing
 - Background
 - Privacy attack instances
- Existing **solutions**
 - k -Anonymity
 - l -Diversity
 - T-Closeness
- **Challenges and Emerging Applications**
- **Conclusion**

Challenges and Emerging Applications

- The problems of privacy preservation, re-identification, and inference control **are not limited** to non-aggregate microdata and contingency tables.
- In many of these new applications, the privacy goal is generally de-identification,
 - that is, the removal of personally identifiable information.

Challenges and Emerging Applications

- Next, two representative emerging applications
 - Social Network Privacy
 - Search Log Privacy

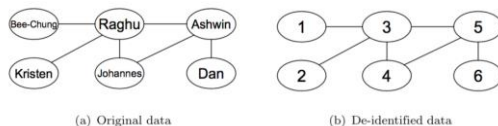
Social Network Privacy

◆ Social Network Privacy

- Social networks describe entities (often people) and the relationships between them.
- Social network analysis is often used to understand the nature of these relationships, such as patterns of influence in communities, or to detect collusion and fraud.
- the release of data is often prevented by concerns about the privacy of individuals.

Social Network Privacy

- Naive De-Identification and Attacks
 - We will model a social network as a simple, undirected graph $G = (V, E)$.
 - Nodes correspond to entities and edges represent connections between entities.
 - Each entity has an associated unique name (e.g., Raghu or Johannes).



Social Network Privacy

- Naive De-Identification and Attacks
- Unfortunately, there are various ways in which this naive solution can be compromised.
 - Active attack:
 - an attacker actively manipulates the structure of the graph before the data are released
 - Passive attack
 - these attacks can be launched based on background knowledge related to the graph's structure

Search Log Privacy

- On July 29, 2006, AOL(America Online INC.) published three-month Web search queries of around 600 thousand users.
- For a given user, this data set contained the queries submitted by the user to the AOL search engine.

Table 7.1. Example search log.

| User ID | Query | Time | Rank | URL |
|---------|-------------------------|------------------|------|---------------------------|
| 1 User1 | Tax ssn 111223333 | 2008-01-05 08:10 | | |
| 2 User2 | Restaurant arlington wi | 2008-01-03 10:20 | 1 | local.yahoo.com/... |
| 3 User2 | Restaurant arlington wi | 2008-01-03 10:22 | 4 | www.gorestaurants.net/... |
| 4 User2 | 70 single men | 2008-01-05 14:30 | | |
| 5 User2 | chen family tree | 2008-01-06 20:01 | 1 | chenfamilytree.com |
| 6 User2 | Nude pictures | 2008-01-10 21:42 | | |
| 7 User3 | www.some-church.com | 2008-01-08 10:35 | 1 | www.some-church.com |
| 8 User3 | Tax for pastor | 2008-01-13 22:50 | 8 | answers.yahoo.com/... |

^aRank and URL indicate the position and the URL on the search result page that the user clicked. Empty means no click.

Search Log Privacy

- To protect users' privacy, AOL **replaced** the AOL user names with randomly generated ID numbers.
- However**, soon after the data set was released, many users together with their private queries were identified.
- As an example**, the New York Times identified user No. 4417749 because this user searched for **her family name, her hometown, and something about her age**
 - By combining this information, it was not difficult to create a very short list of candidates that matched the information.

Search Log Privacy

- The AOL case signifies the need for appropriate search log anonymization. Existing privacy definitions do not apply directly to search logs.
- However, satisfactory solutions to search log publishing are still yet to be found.

Challenges in Emerging Applications

- The Curse of Dimensionality
 - With improving technology it is becoming easier to measure and record more information about each individual.
 - Thus, the number of attributes is growing, causing the size of the domain to increase exponentially.

Challenges in Emerging Applications

- Sequential Releases and Composability
 - The US Census Bureau publish data from the decennial census every 10 years
 - These sequential releases pose an **additional privacy threat** since user information can be linked across different releases.

Conclusion

- An overview of existing solutions for privacy preserving data publishing
 - k -Anonymity
 - l -Diversity
 - T-Closeness
- Challenges in Emerging Applications

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Q&A

